

Exclusive meson production at NLO

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Motivation

Hard exclusive processes

- ▶ constrain generalized parton distributions
- ▶ t dependence $\rightsquigarrow$ distribution of partons in transverse plane correlated with momentum fraction x
- ▶ proton helicity flip distribution E $\rightsquigarrow$
 - orbital angular momentum
 - transverse polarization $\leftrightarrow$ spatial distribution of partons

Exclusive meson production (vs. DVCS)

- ▶ vector mesons $\rightsquigarrow$ enhanced sensitivity to gluons
- ▶ quantitative description more difficult

Factorization theorem

Collins, Frankfurt, Strikman '96

- ▶ light meson production $\gamma^* + p \rightarrow (\rho, \phi, \pi, \dots) + p$
- ▶ limit of large Q^2
- ▶ valid from low to high x_B

collinear factorization: amplitude $\propto$ convolutions $\mathcal{F}(\xi, t, Q^2)$

$$\mathcal{F} = \sum_{a=q,g} \int dx F^a(x, \xi, t; \mu_F) K^a(x, \xi, z, \log \frac{\mu_F^2}{Q^2}, \log \frac{\mu_R^2}{Q^2}) \phi(z; \mu_F)$$

$$\xi = x_B / (2 - x_B)$$

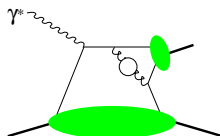
F^a = generalized parton distribution $H^a, E^q, \tilde{H}^a, \tilde{E}^a$

ϕ = meson light-cone distribution amplitude

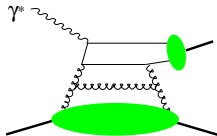
K^a = hard scattering kernel: known to NLO

D. Ivanov, L. Szymanowski, G. Krasnikov '04

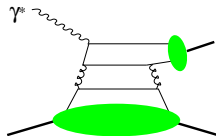
NLO graphs (vector mesons)



flavor singlet and nonsinglet
 $u + d + s$ $u - d, d - s$



gluons



flavor singlet

$\gamma_L^* p$ cross section

unpol. target

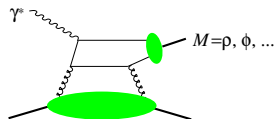
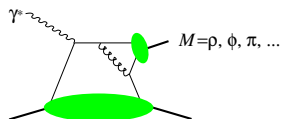
$$\sigma_L \propto (1 - \xi^2) |\mathcal{H}|^2 - \left(\xi^2 + \frac{t}{4M_p^2} \right) |\mathcal{E}|^2 - 2\xi^2 \operatorname{Re}(\mathcal{E}^* \mathcal{H})$$

transverse target polarization

$$\sigma_L^\uparrow - \sigma_L^\downarrow \propto \frac{1}{M_p} \sqrt{t_0 - t} \sqrt{1 - \xi^2} \operatorname{Im}(\mathcal{E}^* \mathcal{H})$$

Warning

- ▶ factorization theorem valid for large Q^2
- ▶ at $Q^2 \sim \text{few GeV}^2$ significant power corrections
M. Vanderhaeghen et al. '98, S. Goloskokov and P. Kroll '05, '06
- ▶ in particular: parton k_T in hard propagators $\sim 1/(zQ^2 + k_T^2)$



- ▶ can take into account but then no NLO calculation
same remark holds for color dipole models
- ▶ $\rightsquigarrow$ strategy: identify kinematics where NLO corr's moderate
there may use LO calculation including power corrections

Results

Details of calculation (focus on H^g , H^q in this talk)

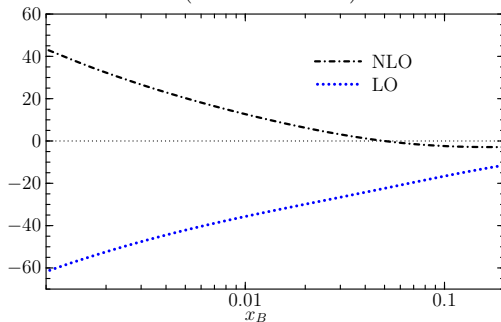
- ▶ double distribution model Musatov, Radyushkin '99
- ▶ input distributions: CTEQ6M at $\mu_F = 1.3 \text{ GeV}$
- ▶ LO evolution of GPDs numerical code A. Vinnikov '06
- ▶ meson distribution amplitude: asymptotic form $\phi \propto z(1-z)$
- ▶ two-loop $\alpha_s(\mu_R)$ with $n_f = 3$
 - $\alpha_s(m_c) = 0.395$
 - $\alpha_s(m_Z) = 0.118$

Small x_B

numerically:

quark singlet + gluon, $\mu_F = \mu_R = Q = 4 \text{ GeV}$

$$\text{Im} \left(\mathcal{H}^g + \mathcal{H}^{S(a)} + \mathcal{H}^{S(b)} \right)$$

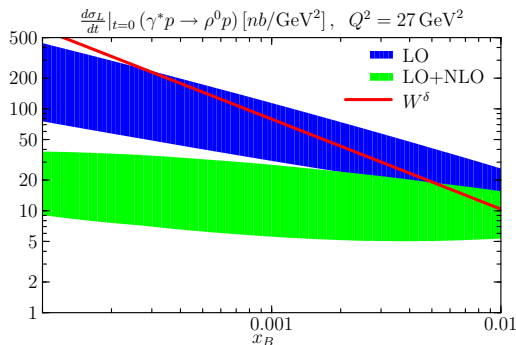


- ▶ large NLO term
- ▶ sign opposite to LO

Small x_B

numerically:

ρ cross section



- ▶ retain large scale uncertainty at NLO
- ▶ see **no** perturbative stability

W^δ with $\delta = 0.88$ (normalization arbitrary):
fit to prel. ZEUS data (EPS 2001) for $0.001 \lesssim x_B \lesssim 0.005$

analytically:

D. Ivanov et al. '04

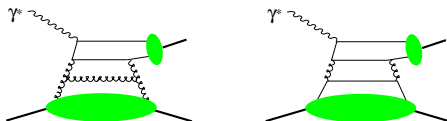
$$\xi \mathcal{H}^g \sim H^g(\xi, \xi, t) - \frac{3\alpha_s}{\pi} \left[\log \frac{\mu_F^2}{Q^2} + 2 \right] \int_{1/2}^{1/(2\xi)} \frac{dy}{1+y} H^g((1+2y)\xi, \xi, t)$$

$$\mathcal{H}^q \sim H^q(\xi, \xi, t) - \frac{6\alpha_s}{\pi} \left[\log \frac{\mu_F^2}{Q^2} + 3 \right] \int_{1/2}^{1/(2\xi)} dy H^q((1+2y)\xi, \xi, t)$$

for flavor singlet

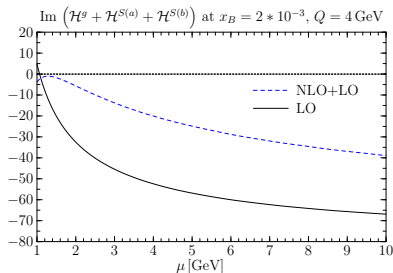
approx. numerically excellent for $\xi \lesssim 10^{-2}$

- with $H^g(x, \dots) \sim \text{flat}$ and $H^q(x, \dots) \sim 1/x^*$ build up $\log 1/\xi$ terms = BFKL type logarithms



* remember that $H^g(x, 0, 0) = xg(x)$ and $H^q(x, 0, 0) = q(x)$

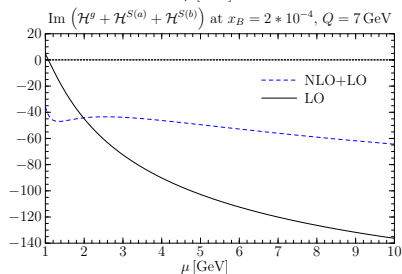
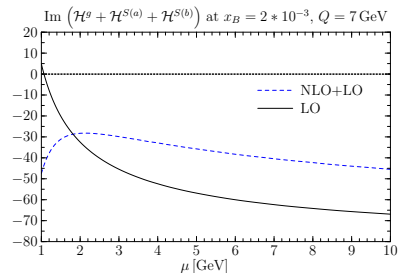
When do corrections become moderate?



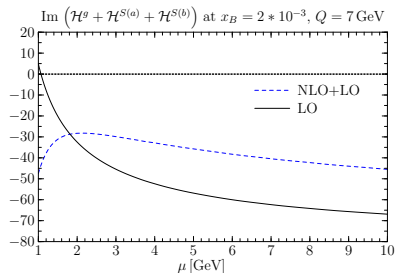
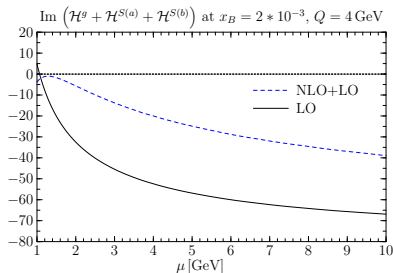
$x_B = 2 \times 10^{-3}$: corr's still large at $Q = 4 \text{ GeV}$

$x_B = 2 \times 10^{-4}$: no stability even at $Q = 7 \text{ GeV}$

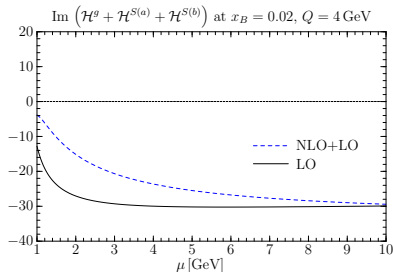
have set $\mu_F = \mu_R = \mu$



When do corrections become moderate?



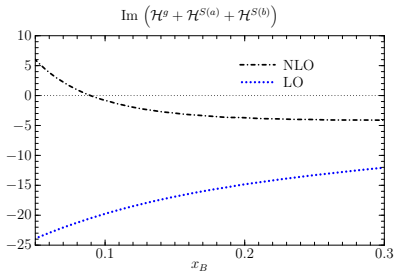
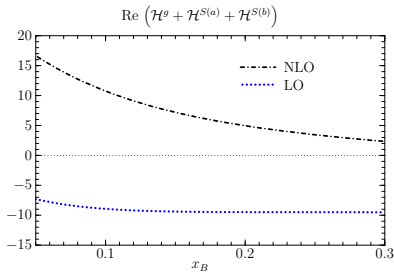
$x_B = 2 \times 10^{-2}$: corr's
moderate at $Q = 4 \text{ GeV}$



Fixed target kinematics

example $\mu_F = \mu_R = Q = 2 \text{ GeV}$

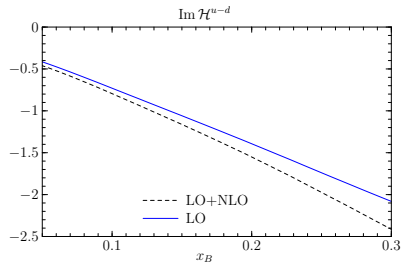
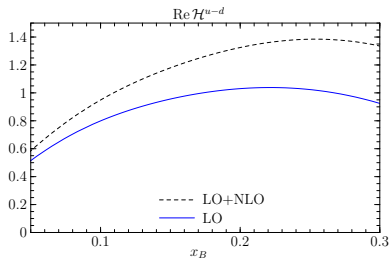
- ▶ gluons + quark singlet: corr's moderate for **Im**
- ▶ but still important for **Re** and smaller x_B
no problem for $|\mathcal{H}|^2$ but possibly for $\text{Im}(\mathcal{E}^*\mathcal{H})$
becomes better for $Q = 3 \text{ GeV}$



Fixed target kinematics

example $\mu_F = \mu_R = Q = 2 \text{ GeV}$

- ▶ quark flavor non-singlet: moderate corr's
very similar for polarized quark terms $\tilde{\mathcal{H}}$

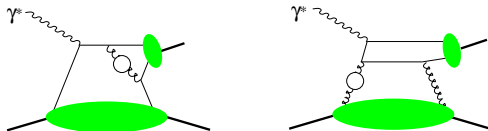


Choice of renormalization scale μ_R

- ▶ often discussed in literature: **BLM** scale setting
choose μ_R so that β_0 terms vanish at NLO
- ▶ gluons: only term $\propto \beta_0 \log(\mu_R/\mu_F) \rightsquigarrow \mu_R = \mu_F$
does not help with small- x logarithms
- ▶ quarks: structure of NLO corrections is

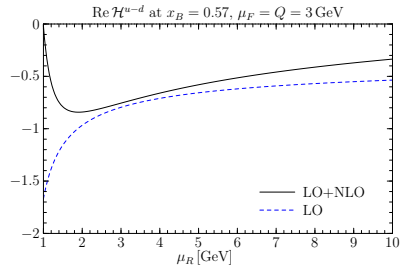
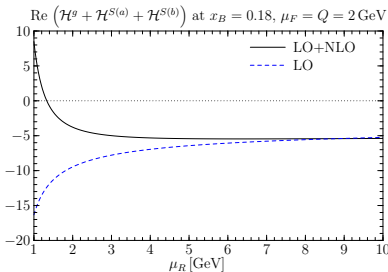
$$\text{large} - \beta_0 \left[\text{large} - \text{small} \times \log \frac{Q^2}{\mu_R^2} \right] - \text{tiny} \times \log \frac{Q^2}{\mu_F^2}$$

- $\rightsquigarrow$ BLM requires $\mu_R \ll Q$... **typically** $\mu_R \lesssim 0.2 Q$
only in perturbative region for **very** large Q^2
leaves **large** correction from β_0 independ't terms



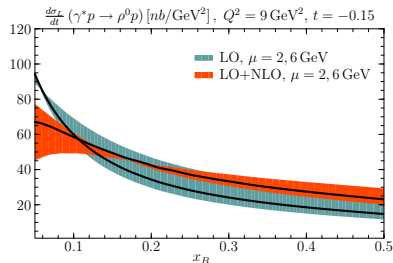
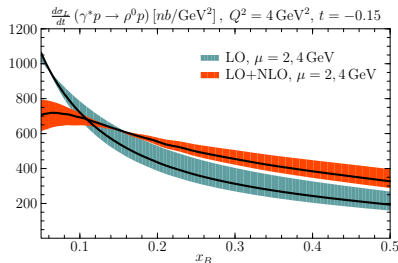
Choice of renormalization scale μ_R

- for $\mu_R \lesssim 2 \text{ GeV}$ typically find unstable behavior



$$\alpha_s(1.4 \text{ GeV}) \approx 0.4$$

Unpolarized cross section σ_L in typical kinematics of COMPASS, HERMES, JLAB@12



central lines: $\mu_F = \mu_R = \mu = 3 GeV$

$\mu_F = \mu_R = \mu = 4 GeV$

↪ perturbative stability except if both x_B and Q^2 small

Polarized cross section $\sigma_L^\uparrow - \sigma_L^\downarrow$

in typical kinematics of Compass, HERMES, JLAB@12

Work in progress

Summary

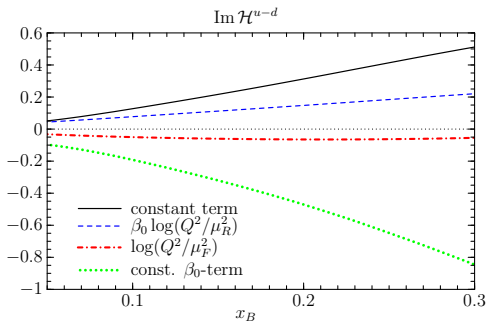
in detailed numerical studies find

- ▶ small $x_B \lesssim 10^{-3}$: huge NLO corrections
even for $Q^2 \sim \text{several GeV}^2$
 $\rightsquigarrow$ must resum high-energy logarithms for reliable expressions
- ▶ moderate to large x_B :
 - gluon/singlet sector becomes gradually stable
 - quark non-singlet sector looks stableas long as Q not too small (want at least $Q^2 = 4 \text{ GeV}^2$)
scales μ_F and μ_R not chosen too small

Choice of scale

NLO correction for quarks:

$$\text{large} - \beta_0 \left[\text{large} - \text{small} \times \log \frac{Q^2}{\mu_R^2} \right] - \text{tiny} \times \log \frac{Q^2}{\mu_F^2}$$

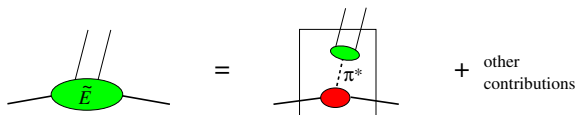


$$\mu_F = \mu_R = 2 \text{ GeV}$$

Pseudoscalar mesons

see also: Belitsky and Müller '01

- ▶ quark GPDs most important
- ▶ convolutions with
 - $\tilde{H}^u - \tilde{H}^d$: similar to $H^u - H^d$
 - $\tilde{E}^u - \tilde{E}^d$: dominated by pion exchange



with asymptotic pion distribution amplitude:

$$\tilde{\mathcal{E}} \propto 1 + \frac{\alpha_s}{\pi} 1.1 \times \left[3 + \log \frac{\mu_R^2}{Q^2} \right]$$

$\rightsquigarrow$ corrections moderate but not small

$$\text{BLM scale } \mu_R^2 = e^{-14/3} Q^2 \approx 0.01 Q^2 \rightsquigarrow \tilde{\mathcal{E}} \propto 1 - \frac{\alpha_s}{\pi} 1.8$$