



# Challenges and opportunities of gravitational-wave searches above 10 kHz

Nancy Aggarwal · Odylio D. Aguiar · Diego Blas · Andreas Bauswein · Giancarlo Cella · Sebastian Clesse et al. *[full author details at the end of the article]*

Received: 11 February 2025 / Accepted: 25 July 2025 / Published online: 3 November 2025  
© The Author(s) 2025

## Abstract

The first direct measurement of gravitational waves by the LIGO and Virgo collaborations has opened up new avenues to explore our Universe. This White Paper outlines the challenges and gains expected in gravitational-wave searches at frequencies above the LIGO/Virgo band. The scarcity of possible astrophysical sources in most of this frequency range provides a unique opportunity to discover physics beyond the Standard Model operating both in the early and late Universe, and we highlight some of the most promising of these sources. We review several detector concepts that have been proposed to take up this challenge, and compare their expected sensitivity with the signal strength predicted in various models. This report is the summary of a series of workshops on the topic of high-frequency gravitational

---

This article is a revised version of <https://doi.org/10.1007/s41114-021-00032-5>.

**Change summary** Major revision, updated and expanded.

**Change details** Title: Challenges and Opportunities of Gravitational Wave searches above 10 kHz (previously: at MHz to GHz frequencies), to emphasize inclusion of frequencies below a MHz and above the GHz range. Authors: Inclusion of new authors who played a key role in coordinating this update: Diego Blas, Sebastian Ellis, Gabriele Franciolini, Camilo García-Cely, Asuka Ito, Joachim Kopp, Sung Mook Lee, Killian Martineau, Jamie McDonald, Krisztian Peters, Andreas Ringwald, Carlos Tamarit. Introduction: Minor changes. Section 2: Significant rewriting to emphasize the different data analysis methods for different GW signals and detectors. Introduction of noise-equivalent strain as key quantity for detector comparison. Section 3: Extended version of previous Sect. 3.1, comparing detector sensitivities for different type of gravitational wave sources. Section 4 (previously Sect. 3.2 and 3.3): Discussion on astrophysical sources has been extended, in particular Sects. 4.1.1 and 4.1.3. Section 5 (previously Sect. 4): Significantly extended and restructured, reflecting many new developments in the field. Sensitivities of the different detector concepts are now displayed in figures (overview figures in Sect. 3 and grouped by detector class in Sect. 5), the summary tables in Sect. 5.9 instead focus on listing the different proposals with references, frequency range and key technologies. Appendix A has been added, the previous Appendix A has been integrated into Sect. 4. All figures and tables have been redone. The number of references has increased from 352 to 594.

---

Extended author information available on the last page of the article

wave detection, held in 2019 (ICTP, Trieste, Italy), 2021 (online) and 2023 (CERN, Geneva, Switzerland).

**Keywords** Gravitational waves · Early universe · Compact objects · Quantum sensing · Axion searches · Microwave cavities

## Contents

|       |                                                                               |    |
|-------|-------------------------------------------------------------------------------|----|
| 1     | Introduction.....                                                             | 3  |
| 2     | Basic concepts and notation.....                                              | 6  |
| 2.1   | Acronyms and conventions .....                                                | 6  |
| 2.2   | Characterizing sources.....                                                   | 8  |
| 2.2.1 | Stochastic gravitational waves.....                                           | 8  |
| 2.2.2 | Transient gravitational wave sources .....                                    | 9  |
| 2.2.3 | Persistent coherent gravitational wave sources.....                           | 10 |
| 2.3   | Characterizing detectors .....                                                | 10 |
| 2.3.1 | Detector sensitivity to stochastic GWs .....                                  | 13 |
| 2.3.2 | Detector sensitivity to transient GWs .....                                   | 13 |
| 2.3.3 | Detector sensitivity to persistent coherent GWs.....                          | 14 |
| 2.4   | Note on characteristic strain for HFGWs.....                                  | 15 |
| 3     | Overview of detector sensitivities and possible signals .....                 | 15 |
| 4     | Sources of gravitational waves at high frequencies.....                       | 21 |
| 4.1   | Late universe.....                                                            | 21 |
| 4.1.1 | Known astrophysical systems .....                                             | 21 |
| 4.1.2 | Light primordial black holes .....                                            | 27 |
| 4.1.3 | Memory effects .....                                                          | 36 |
| 4.1.4 | Exotic compact objects .....                                                  | 38 |
| 4.1.5 | Black hole superradiance.....                                                 | 39 |
| 4.2   | Early universe .....                                                          | 41 |
| 4.2.1 | Inflation.....                                                                | 44 |
| 4.2.2 | (P)reheating .....                                                            | 47 |
| 4.2.3 | The cosmic gravitational microwave background .....                           | 50 |
| 4.2.4 | Phase transitions.....                                                        | 52 |
| 4.2.5 | Topological defects .....                                                     | 54 |
| 4.2.6 | Evaporating primordial black holes.....                                       | 57 |
| 4.2.7 | Miscellaneous .....                                                           | 58 |
| 4.3   | Gravitational wave generation in laboratory setups.....                       | 59 |
| 4.4   | Summary of sources .....                                                      | 60 |
| 5     | Detection of gravitational waves at high frequencies.....                     | 62 |
| 5.1   | Laser interferometers and resonant mass detectors and their limitations ..... | 64 |
| 5.1.1 | Neutron star extreme matter observatory (NEMO) .....                          | 65 |
| 5.1.2 | Interferometers up to 100 MHz .....                                           | 65 |
| 5.1.3 | Spherical resonant masses.....                                                | 66 |
| 5.1.4 | Summary: sensitivities of interferometers and resonant mass detectors.....    | 68 |
| 5.2   | Modern resonant mass detectors.....                                           | 69 |
| 5.2.1 | Optically levitated sensors .....                                             | 69 |
| 5.2.2 | Bulk acoustic wave devices.....                                               | 70 |
| 5.2.3 | Deformation of microwave cavities .....                                       | 72 |
| 5.2.4 | Magnetic Weber bars .....                                                     | 73 |

|       |                                                                          |     |
|-------|--------------------------------------------------------------------------|-----|
| 5.2.5 | Summary: strain sensitivities of modern resonant mass detectors.....     | 74  |
| 5.3   | Electromagnetic oscillators.....                                         | 75  |
| 5.3.1 | Microwave cavities .....                                                 | 76  |
| 5.3.2 | Low-mass axion haloscopes .....                                          | 79  |
| 5.3.3 | Summary: strain sensitivities of electromagnetic oscillators.....        | 80  |
| 5.4   | Photon (re-)generation experiments.....                                  | 80  |
| 5.4.1 | Light-shining-through-a-wall experiments and axion helioscopes.....      | 80  |
| 5.4.2 | Dielectric axion haloscopes .....                                        | 83  |
| 5.4.3 | Summary: strain sensitivities of photon (re-)generation experiments..... | 85  |
| 5.5   | Other electromagnetic gravitational wave detectors .....                 | 85  |
| 5.5.1 | High energy pulsed lasers .....                                          | 85  |
| 5.5.2 | GW to electromagnetic-wave conversion in a static electric field .....   | 86  |
| 5.5.3 | Resonant polarization rotation .....                                     | 86  |
| 5.5.4 | Heterodyne enhancement of magnetic conversion .....                      | 87  |
| 5.6   | Astrophysical and cosmological detection concepts .....                  | 87  |
| 5.7   | Other concepts .....                                                     | 89  |
| 5.7.1 | Superconductors as GW detectors.....                                     | 89  |
| 5.7.2 | Graviton–magnon resonance.....                                           | 90  |
| 5.7.3 | Atomic precision measurements.....                                       | 91  |
| 5.7.4 | One-electron quantum cyclotron .....                                     | 91  |
| 5.7.5 | Rydberg atoms.....                                                       | 92  |
| 5.8   | Cross-correlating multiple detectors .....                               | 93  |
| 5.8.1 | The overlap reduction function .....                                     | 93  |
| 5.8.2 | Signal switching .....                                                   | 94  |
| 5.8.3 | Issues related to data acquisition and long term storage.....            | 95  |
| 5.8.4 | Coincidence counting experiments .....                                   | 96  |
| 5.9   | Summary of detector sensitivities .....                                  | 96  |
| 6     | Discussion and conclusions.....                                          | 98  |
|       | Appendix: Electromagnetic Signals Generated by GWs .....                 | 101 |
|       | References.....                                                          | 105 |

## 1 Introduction

Over centuries, the main tool for observing the Universe has been electromagnetic waves, covering more than 20 orders of magnitude in frequency, from radio waves to gamma rays. The recent onset of gravitational wave astronomy has opened up a totally new window to observe our Universe (Abbott et al. 2016b). As for electromagnetic observations, we may expect that at every scale in gravitational wave frequency, there should be interesting and unique physics to be discovered. Current and planned projects such as pulsar timing arrays and ground- or space-based interferometers will explore gravitational waves in the well-motivated frequency range between nHz and kHz. However, both from the experimental and from the theoretical point of view it is worth considering also gravitational waves at much higher frequencies, such as the MHz and GHz bands.

A strong theoretical motivation for exploring frequencies above kHz is that there are hardly any known astrophysical objects small and dense enough to potentially emit at frequencies beyond 10 kHz with a sizeable amplitude. Any discovery of gravitational waves at higher frequencies would thus indicate new physics beyond the Standard Model of particle physics, linked for instance to exotic astrophysical

objects (such as primordial black holes or boson stars) or to cosmological events in the early Universe such as phase transitions, preheating after inflation, oscillons, cosmic strings, thermal fluctuations after reheating, etc., see Caprini and Figueroa (2018) for a review. This should be seen in contrast to GW astronomy at lower frequencies, where, as detector sensitivities increase, astrophysical gravitational wave foregrounds are posing an increasing challenge to searches for fainter signals from new physics. In cosmology, gravitational waves may be the only way to observe certain epochs. In particular, before the recombination of electrons and nuclei into neutral atoms and the associated emission of the cosmic microwave background radiation, electromagnetic waves cannot propagate freely, so no electromagnetic signal can reach us from these early epochs. Gravitational waves, on the other hand, decouple essentially immediately after being produced thanks to the weakness of gravity. They travel undisturbed through the Universe, forming a stochastic background that could eventually be detected. Even though it may not be easy to unambiguously determine the specific cosmological source of a gravitational-wave signal, indications of its cosmological nature can be gained from properties such as isotropy and stationarity, in analogy to the original discovery of the cosmic microwave background.

The frequency of a cosmological gravitational wave signal is related to the epoch at which it is emitted: causality restricts the wavelength to be smaller than the cosmological horizon size at the time of gravitational wave production. This roughly implies that signals at frequencies above the range of the existing laser interferometers LIGO (Aasi et al. 2015; Abbott et al. 2016a; Buikema et al. 2020; Tse et al. 2019), Virgo (Acernese et al. 2015, 2019), and KAGRA (Akutsu et al. 2019; Aso et al. 2013) correspond to gravitational waves produced at temperatures  $\gtrsim 10^{10}$  GeV.<sup>1</sup> (Here, we have assumed radiation domination all the way to matter–radiation equality, as is the case in standard cosmology.) In particular, GHz frequencies correspond to the horizon size at the highest energies conceivable in particle physics (such as the Grand Unification or string scale) and phenomena like phase transitions and preheating after inflation would naturally produce gravitational waves with frequencies in the range from around 10 kHz (the upper end of the LIGO detection band) to GHz. Astrophysical sources such as mergers of compact binaries can generate gravitational waves at even higher frequencies. We moreover stress that essentially all detector concepts discussed in this review are probing uncharted territory. Even in regions of parameter space where no signals are expected or even envisaged, one may find unexpected surprises once one starts experimentally probing these regions for the first time.

Several proposals have been put forward for pushing the high-frequency end of interferometric detectors into the high-frequency region. Detectors for the MHz, GHz and THz frequency bands, however, require radically different experimental approaches. Over the years, there have been isolated attempts to search for such gravitational waves of very high frequencies, but interest in the field has increased significantly in recent years, with many new proposals and numerous emerging R&D efforts. The current status of many of these ideas must be regarded as highly preliminary, driven by theoretical work

<sup>1</sup> Cosmological events occurring at lower temperatures can also source such high-frequencies gravitational waves if the typical scale of the source is hierarchically smaller than the horizon scale.

rather than serious discussion of experimental noise sources, while others are already at the prototyping stage or setting first limits. The published concepts span a wide range of technologies with no real consensus yet as to where the community effort should be concentrated. Concrete R&D efforts are crucial to evaluate the suitability and potential of different technologies and are thus key to progress even when the sensitivity of prototypes falls short of the expected signals by several orders of magnitude. In addition to the selection of suitable technological pathways towards a serious attempt at a detection at high frequencies, there needs to be an identification of the most realistic sources and thereby the waveforms and spectra for which such detectors should be optimised. This process demands a close collaboration of theorists and experimentalists.

The goal of this report is to summarise and start a dialogue among the various communities involved regarding the importance and feasibility of searches for high-frequency gravitational waves. We are aware that this may be a long-term goal but, keeping in mind that the strain sensitivity of the first historical gravitational wave detectors was eight orders of magnitude less than achieved in the current generation, we are convinced that the physics motivation is strong enough to start a systematic study of the different sources of high-frequency gravitational waves and their potential detectability already now. The origin of this initiative was a workshop organised at ICTP in October 2019 called “Challenges and Opportunities of High-Frequency Gravitational Wave Detection”, where members of the theoretical and experimental communities interested on high-frequency gravitational waves got together to explore the motivations and challenges towards this search. Follow up workshops were held hosted by CERN in October 2021 and December 2023, and a 4th edition is planned for July 2025 in Mainz.<sup>2</sup> This series of workshops and the present White Paper set the stage for the launch of the Ultra-High-Frequency Gravitational Wave (UHF-GW) initiative,<sup>3</sup> whose goals include supporting the R&D and prototyping phase of experimental projects, stimulating technological advancements that may lead to new detection schemes, and fostering a vibrant theoretical community.

The remainder of this report is organized as follows: Sect. 2 introduces basic concepts and notation for the subsequent discussion of high-frequency gravitational-wave sources and detectors. Section 3 provides an executive summary of the sensitivities of different detector concepts discussed in this report and illustrates their reach to some exemplary categories of gravitational wave signals. A more detailed discussion of sources then follows in Sect. 4, while detectors are discussed in detail in Sect. 5. We conclude in Sect. 6. For a summary of the various detector concepts as well as the corresponding frequency ranges and sensitivities see Figs. 1,

<sup>2</sup> Slides and recordings of the contributions to these workshops can be found at: <http://indico.ictp.it/event/9006/> (2019), <https://indico.cern.ch/event/1074510/> (2021) and <https://indico.cern.ch/event/1257532/> (2023).

<sup>3</sup> <http://www.ctc.cam.ac.uk/activities/UHF-GW.php>.

2, 3 and 4 in Sect. 3, as well as Tables 6 and 7 in Sect. 5.9. For a summary of sources see Tables 1 and 2 in Sect. 4.4.

## 2 Basic concepts and notation

We introduce here the main concepts, and set out the notation, that will be used in this report in order to appropriately characterise GW sources and the ability of detectors to measure them. We start by discussing sources in a general way, and follow up with a similarly general discussion of detectors.

### 2.1 Acronyms and conventions

We will frequently use the following acronyms

|         |                                                   |
|---------|---------------------------------------------------|
| BBN     | Big Bang Nucleosynthesis                          |
| BH      | Black hole                                        |
| CMB     | Cosmic microwave background                       |
| FOPT    | First-order phase transition                      |
| GW      | Gravitational wave                                |
| ISCO    | Innermost stable circular orbit (of a black hole) |
| LVK     | LIGO–Virgo–KAGRA                                  |
| QCD     | Quantum chromodynamics                            |
| SGWB    | Stochastic gravitational wave background          |
| SMBH    | Supermassive black hole                           |
| SNR     | Signal-to-noise ratio                             |
| UHF-GWs | Ultra-high frequency gravitational waves          |

We will frequently encounter Fourier transforms, which, for a time-dependent quantity  $q(t)$ , we write as

$$q(t) = \int_{-\infty}^{\infty} df e^{2\pi i f t} q(f), \quad q(f) = \int_{-\infty}^{\infty} dt e^{-2\pi i f t} q(t), \quad (1)$$

where  $f$  is the frequency. Even though  $q(t)$  are typically real-valued data,  $q(f)$  will in general be complex. A related quantity we will frequently encounter is the two-sided power spectral density (PSD), which we denote  $S_q(f)$ .<sup>4</sup> It is defined as

<sup>4</sup> The GW literature often uses the *one-sided* PSD,  $S_q(f)^{(1)}$ , which is related to the two-sided PSD according to  $S_q(f)^{(1)} = 2S_q(f)$ . We admit to adding to this confusion by switching from one-sided PSDs (used in the first version of this review) to two-sided PSDs here. This minimal change allows us to improve consistency in our notation while keeping key conversion formulas between  $\Omega_{\text{GW}}$  (normalized energy density),  $S_h$  (strain-equivalent noise PSD) and  $h_c$  (characteristic strain) formally identical.

$$\langle q(f) q^*(f') \rangle \equiv S_q(f) \delta(f - f'), \quad (2)$$

and is related to the auto-correlation function  $R_q(\tau) = \langle q^*(t) q(t - \tau) \rangle$  by

$$R_q(\tau) = \int_{-\infty}^{\infty} df e^{i2\pi\tau} S_q(f). \quad (3)$$

Gravitational waves can be conveniently described in either the “transverse-traceless” (TT) gauge, or in the local inertial frame (LIF) of the detector, usually called the “proper detector frame” (PDF) (Rakhmanov 2005, 2014; Maggiore 2007). The PDF is typically constructed with respect to the center of mass of the detector.

It is important to keep in mind that the choice of gauge, while often having a big impact on the complexity of calculations, does not affect the physics. When characterizing GW sources, one often works in TT gauge. Meanwhile when discussing detectors, the choice of gauge often depends on whether the detector components can be considered as freely falling or not. If they are freely falling, then the TT gauge description is often most useful. If they are not, the PDF is usually favored, especially if the GW wavelength is much larger than the size of the detector,  $\omega_g L \ll 1$ . Of course, general relativity requires that the final result be gauge/frame-independent, so that calculations in both approaches must agree. In practice, verifying this frame-independence for a given experimental setup can be cumbersome, although significant efforts have been made to show the equivalence for HFGW detectors (see, e.g., Ratzinger et al. 2024). The metric perturbation for a gravitational wave in TT gauge can be written as

$$h_{ij}^{\text{TT}}(\mathbf{x}, t) = \sum_{a=+, \times} \int_{-\infty}^{+\infty} h_a(f, \hat{\mathbf{k}}) e_{ij}^a(\hat{\mathbf{k}}) \exp(-2\pi i(ft - \hat{\mathbf{k}} \cdot \mathbf{x})), \quad (4)$$

where the polarization tensors  $e_{ij}^a(\hat{\mathbf{k}})$  are defined as

$$e_{ij}^+(\hat{\mathbf{k}}) = \frac{1}{\sqrt{2}} (\hat{\mathbf{u}}_i \hat{\mathbf{u}}_j - \hat{\mathbf{v}}_i \hat{\mathbf{v}}_j), \quad e_{ij}^\times(\hat{\mathbf{k}}) = \frac{1}{\sqrt{2}} (\hat{\mathbf{u}}_i \hat{\mathbf{v}}_j + \hat{\mathbf{v}}_i \hat{\mathbf{u}}_j). \quad (5)$$

Here, the unit vectors  $\hat{\mathbf{u}}, \hat{\mathbf{v}}$  are orthogonal to the direction of propagation of the GW  $\hat{\mathbf{k}} = \mathbf{k}/|\mathbf{k}|$  and to each other. When traced over spatial and polarization indices, the polarization tensors satisfy the completeness relation  $e_{ij}^a e_{ij}^a = 2$ .<sup>5</sup>

We will work in natural units,  $c = \hbar = G = 1$ , though we will occasionally reintroduce when displaying explicit dimensions helps clarify the physical meaning of the expressions.

<sup>5</sup> Note that the literature is split between this convention and  $e_{ij}^a e_{ij}^a = 4$ . The latter convention is obtained by removing the factor  $1/\sqrt{2}$  in our definition of the polarization tensors.

## 2.2 Characterizing sources

Sources of HFGWs can be classified into three broad categories: stochastic, transient, and persistent. In the case of the two latter categories, we assume that the signal is resolvable, either through its spatial origin, time-dependence, or both. A precise discussion of the physical origin of these three categories will follow in subsequent sections. Nevertheless, it is useful to recall that cosmological mechanisms will typically generate stochastic GWs; inspirals and mergers of compact objects can lead to resolvable transient GWs; processes such as decays or annihilation of axions in superradiant clouds can lead to resolvable persistent and coherent GWs. Below we introduce these categories in turn, introducing the notation required to quantify the GW strength at each stage.

### 2.2.1 Stochastic gravitational waves

Stochastic gravitational waves can be produced by various processes, including for instance phase transitions in the early Universe, the dynamics of inflation, subsequent (p)reheating, or fluctuations in the thermal plasma. They are often characterized by their spectral energy density,

$$\Omega_{\text{GW}}(f) = \frac{1}{\rho_c} \frac{d\rho_g}{d \ln f}, \quad (6)$$

which normalizes the GW energy density per log-frequency interval,  $\frac{d\rho_g}{d \ln f}$ , to the critical energy density of the Universe,  $\rho_c = 3H_0^2/(8\pi G)$ , where  $H_0$  is the Hubble parameter today, and  $G$  is Newton's constant. The total energy density in GWs,  $\rho_g$ , is related to the metric perturbation according to

$$\rho_g = \frac{1}{32\pi G} \langle \dot{h}_{\mu\nu} \dot{h}^{\mu\nu} \rangle = \frac{1}{32\pi G} \langle \dot{h}_+^2 + \dot{h}_\times^2 \rangle, \quad (7)$$

where the first equality is exact and can be computed in the transverse-traceless (TT) gauge, resulting in the second equality. Since  $\rho_g$  is a Lorentz scalar, it is frame-invariant. The averaging  $\langle \dots \rangle$  is over time.

This definition of the GW energy density lends itself to being related to the two-sided power spectral density  $S_h(f)$  [cf. Eq. (2)] (Allen and Romano 1999; Maggiore 2007; Thrane and Romano 2013; Moore et al. 2015)<sup>6</sup>:

$$\langle h_a(f, \phi, \theta) h_{a'}^*(f', \phi', \theta') \rangle \equiv \frac{1}{4\pi} S_h^a(f) \delta(f - f') \delta(\phi - \phi') \delta(\cos \theta - \cos \theta') \delta_{aa'}, \quad (8)$$

where  $\phi, \theta$  are angles on the celestial sphere and  $a = +, \times$  is the polarization. This expression is only valid for an isotropic stochastic background. If the background is anisotropic,  $S_h^a(f)$  retains a dependence on  $\phi$  and  $\theta$ , i.e.,  $S_h^a(f) \rightarrow S_h^a(f, \phi, \theta)$ . The

<sup>6</sup> Note the different conventions in the literature, which we discuss below.



total power spectral density  $S_h(f) = \frac{1}{2} \sum_a S_h^a(f)$  is related to the relative energy density in GWs by

$$\Omega_{\text{GW}}(f) = \frac{4\pi^2}{3H_0^2} |f|^3 S_h(|f|). \quad (9)$$

The GW power spectral density is therefore a useful proxy for the relative energy density in stochastic GWs. As already emphasized above in Footnote 4, conventions for  $S_h(f)$  differ in the literature. We follow Allen and Romano (1999) in using two-sided PSDs, but follow Maggiore (2007) in normalizing by a factor  $4\pi$  so that the integration over solid angle yields 1, such that Eqs. (4) and (8) yield

$$\langle h_a(t, \mathbf{x})^2 \rangle = \int_{-\infty}^{+\infty} df S_h^a. \quad (10)$$

Taking into account also the different choices for the normalization of the polarization tensors (with our convention being  $e_{ij}^a e_{ij}^a = 2$ ), we obtain

$$S_h(f) = 4\pi S_h^{\text{Allen-Romano}}(f) = \frac{1}{2} S_h^{\text{Maggiore}}(f) = S_h^{\text{Thrane-Romano, Moore}}(f). \quad (11)$$

Another useful quantity that is often used in the literature to characterize the amplitude of stochastic GWs is the ‘characteristic strain’  $h_{\text{c,sto}}$ . It is defined with respect to the GW power spectral density according to

$$h_{\text{c,sto}} \equiv \sqrt{f S_h(f)}, \quad (12)$$

and is therefore dimensionless. Using Eq. (9), we can also relate the characteristic strain to the relative GW energy density,

$$h_{\text{c,sto}} = \frac{H_0}{2\pi f} (3\Omega_{\text{GW}}(|f|))^{1/2}. \quad (13)$$

## 2.2.2 Transient gravitational wave sources

Transient sources such as primordial black hole mergers (see Sect. 4.1.2 or GW bursts (e.g. from hyperbolic encounters of compact objects or from cosmic string cusps) lead to signals with a short duration compared with the experimental measurement time. Nevertheless, such signals can still be characterized in terms of their PSD

$$\langle h(f) h^*(f') \rangle \equiv S_h(f) \delta(f - f'), \quad (14)$$

with  $h(f)$  being the Fourier transform of the GW strain amplitude,  $h(t)$ , as defined in Eq. (1). The frequency dependence of  $h(f)$  is dictated by the source properties, while the overall amplitude is inversely proportional to the source distance. The latter allows one to express detector capabilities in terms of a “distance reach” (see e.g. Sect. 4.1.2). Of importance for data analysis is that for given assumptions on the properties of the source, the frequency of the GW signal and its phase are known.

Depending on the specifics of the detector, this can allow for a matched filtering analysis that improves the sensitivity to such sources. As a result, rather than using the strain PSD to characterise the signal-to-noise ratio for BH mergers, it is best to use  $h(f)$ , as we discuss below.

### 2.2.3 Persistent coherent gravitational wave sources

Various sources can lead to GWs that are monochromatic or at least coherent over a long timescale. An example is black hole superradiance, discussed in Sect. 4.1.5. Such sources can also be treated in Fourier space, where their PSD takes on a particularly simple form, namely

$$S_h(f) = \frac{1}{2} h_0^2 [\delta(f - f_g) + \delta(f + f_g)]. \quad (15)$$

The second Delta function, which accounts for negative frequencies, appears due to our choice of working with two-sided PSDs. In a scenario where the signal is very coherent, but not perfectly monochromatic, it can be useful to instead assume that the signal has a fixed bandwidth  $\Delta f_g \ll f_g$ , whereupon we can write the PSD in a simple form by replacing the delta functions with a broader peaked distribution with a width  $\Delta f_g = f_g/Q_g$ , where we have defined  $Q_g$  as the quality factor of the signal.

## 2.3 Characterizing detectors

It is inherently difficult to compare detection technologies and approaches, as they each have very different noise sources and amplitudes, bandwidths, antenna patterns, analysis strategy, etc. Nevertheless, certain quantities lend themselves to comparing detectors. In particular, the noise-equivalent strain power spectral density,  $S_h^{\text{noise}}(f)$  gives a measure of the noise in the detector as well as its response to a signal of generic spectral density  $S_h(f)$ . In simple terms,  $S_h^{\text{noise}}(f)$  can be viewed as the detector noise folded with the inverse of the detector response function.

In more detail, let us consider what a detector measures in its data stream. A detector taking data in the frequency domain can be viewed as recording a quantity  $d(f) = n(f) + s(f)$ , where  $n(f)$  is the noise in the detector and  $s(f)$  is the signal (if present).<sup>7</sup> The quantity  $s(f)$  is itself a convolution of the GW signal  $h(f)$  and the detector response, often characterized by its “transfer function”  $T_h(f)$ , such that  $s(f) \equiv T_h(f) h(f)$ .<sup>8</sup> We add a subscript  $h$  to this transfer function to distinguish it from the possibly different detector transfer function for noise,  $T_n(f)$ , defined such that  $n(f) = T_n(f) \bar{n}(f)$ , with  $\bar{n}(f)$  the raw noise in the detector. The quantities  $s(f)$

<sup>7</sup> In the interferometer literature,  $d(f)$  is often normalized such that  $s(f) = h(f)$ , meaning that  $n(f)$  carries information about how the strain is imprinted on the data measured by the detector.

<sup>8</sup> For example, an experiment whose observable is a voltage has a dimensionful transfer function that encodes how the dimensionless strain signal is converted into a pure-signal voltage measurable at the output.

and  $n(f)$  can each be characterized by two-sided PSDs,  $S_{\text{sig}}(f) \equiv |T_h(f)|^2 S_h(f)$  and  $S_{\text{noise}}(f) \equiv |T_n(f)|^2 S_{\bar{n}}(f)$ , respectively. If a detector has multiple noise sources, as most of them do, each noise source must be calibrated separately to the readout channel and added in quadrature. These quantities allow us to finally define the noise-equivalent strain PSD as

$$S_h^{\text{noise}}(f) \equiv S_h(f) \frac{S_{\text{noise}}(f)}{S_{\text{sig}}(f)} = S_{\bar{n}}(f) \frac{|T_n(f)|^2}{|T_h(f)|^2}. \quad (16)$$

The interpretation of this quantity is that the detector is sensitive to a given signal power spectral density  $S_{\text{sig}}(f)$ , which is a combination of the intrinsic properties of the GW,  $S_h(f)$ , and the response of the detector to this input. Evaluating a detector's sensitivity to an unknown GW input therefore reduces to computing the quantities  $S_{\bar{n}}(f)$ ,  $T_n(f)$ , and  $T_h(f)$ .

Numerically, the sensitivity of a detector is quantified by the signal-to-noise ratio (SNR). The data output is typically fed through a filter  $F(t)$ , which is usually implemented in software. The recorded data is therefore the convolution  $d'(f) \sim F^*(f) d(f)$ . The SNR is maximized by finding the optimal filter. The variance  $\sigma_d^2$  of  $d(f)$  in the absence of signal ( $s(f) = 0$ ) sets the noise level in the detector. We must now distinguish between recorded data that depends linearly on  $s(f)$ ,  $n(f)$ , and data that depends quadratically on these quantities. In the case of linear data,  $d'(f)_{s=0} \sim F^*(f) n(f)$  implies

$$\begin{aligned} (\sigma_d^2)^{\text{lin}} &= \langle (d'_{s=0})^2 \rangle - \langle d'_{s=0} \rangle^2 \\ &\simeq \int df |F(f)|^2 S_{\text{noise}}(f). \end{aligned} \quad (17)$$

Meanwhile, if the data is quadratic in  $s(f)$  and  $n(f)$ , we have  $d'(t)_{s=0} \sim F^2(t) n^2(t)$ , which in turn implies

$$\begin{aligned} (\sigma_d^2)^{\text{quad}} &= \langle (d'_{s=0})^2 \rangle - \langle d'_{s=0} \rangle^2 \\ &\simeq \frac{1}{\Delta t} \int df |F(f)|^4 S_{\text{noise}}^2(f). \end{aligned} \quad (18)$$

Here,  $\Delta t = \min[t_{\text{int}}, \tau]$  is the smaller of the experimental integration time  $t_{\text{int}}$  or the signal duration  $\tau$ . We are implicitly assuming here that the integration time is the longest timescale in the experiment. This is true for stochastic backgrounds, for example, but not for short transient sources.

For the signal in the absence of noise, we can define the signal power as

$$P_{\text{sig}} \simeq \begin{cases} \int df F^*(f) s(f) & \text{linear,} \\ \int df |F(f)|^2 S_{\text{sig}}(f) & \text{quadratic.} \end{cases} \quad (19)$$

For a linear signal,  $P_{\text{sig}}$  can be interpreted as being equivalent to the time-average of the data stream  $d'(t)$ , since  $\langle n(t) \rangle = 0$ , so the only possible contribution comes from

$s(t)$ . This further implies that if  $\langle s(t) \rangle = 0$  as well, the signal must be auto-correlated with itself to be observable, rendering the measurement quadratic. For a quadratic signal,  $P_{\text{sig}}$  should be thought of as the power in excess of the mean noise power.

The SNR is then straightforwardly given by

$$\text{SNR} = \frac{P_{\text{sig}}}{\sqrt{\sigma_d^2(f)}} \quad (20)$$

$$= \begin{cases} \frac{\int df F^*(f) s(f)}{(\int df |F(f)|^2 S_{\text{noise}}(f))^{1/2}} & \text{linear,} \\ \frac{\int df |F(f)|^2 S_{\text{sig}}(f)}{(\frac{1}{\Delta t} \int df |F(f)|^4 S_{\text{noise}}^2(f))^{1/2}} & \text{quadratic.} \end{cases} \quad (21)$$

In the linear case, the optimal filter is  $F(f) = Ks(f)/S_{\text{noise}}(f)$ , where  $K$  is an arbitrary constant. Meanwhile in the quadratic case, the optimal filter is  $|F(f)|^2 = K'S_{\text{sig}}(f)/S_{\text{noise}}^2(f)$ , with  $K'$  another arbitrary constant.

The end result is that the optimal SNR for a generic signal is (Maggiore 2007)

$$\text{SNR}^{\text{lin}} = \left[ 2 \Delta t \int_0^\infty df \frac{S_h(f)}{S_h^{\text{noise}}(f)} \right]^{1/2}, \quad (22)$$

$$\text{SNR}^{\text{quad}} = \left[ 2 \Delta t \int_0^\infty df \left( \frac{S_h(f)}{S_h^{\text{noise}}(f)} \right)^2 \right]^{1/2}, \quad (23)$$

for a detector sensitive to an observable linear in the GW strain  $h$  in the first line, and for a detector sensitive to an observable that is quadratic in  $h$  in the second line.<sup>9</sup> To obtain an expression in terms of  $S_h(f)$  and  $S_h^{\text{noise}}(f)$ , we have used Eq. (16). We see that the difference between a linearly sensitive detector and a quadratically sensitive detector is the relative scaling with  $S_h(f)$  and the integration time  $\Delta t$ , that is, the degree to which a longer integration time can compensate for a smaller signal while keeping the SNR fixed. In order to compare the ability of a given detector to establish an exclusion limit or make a discovery, care must be taken in establishing what the appropriate threshold value is for the SNR. For this purpose, it is often useful to relate the SNR to the test statistic given a likelihood function (Cowan et al. 2011). Below, we consider the resulting sensitivity of detectors to various types of GW sources in terms of SNR.

In practice, one often works with binned data, in which case the integral over frequencies in Eqs. (22) and (23) reduces to a sum over bins in frequency-space, where each bin has a size  $\delta f = 1/t_{\text{FFT}}$  that comes from the ability to resolve a signal in the frequency domain. The quantity  $t_{\text{FFT}}$  is the timescale of the fast Fourier transform used in the data analysis. The frequency integral or sum should be limited

<sup>9</sup> Note that the linear SNR is often written in the literature without the factor  $t_{\text{int}}$ , and in terms of  $|h(f)|^2$  instead of  $S_h(f)$ . To recover the form above, we can use that  $|h(f)|^2 \sim S_h(f)\delta(f-f)$ , and that  $\delta(0)$  can only be resolved at the level of  $t_{\text{int}}$ .

to the frequency range over which the detector or signal has support,  $\Delta f = \min[\Delta f_{\text{det}}, \Delta f_g]$  which effectively limits the bandwidth.

### 2.3.1 Detector sensitivity to stochastic GWs

Stochastic GWs are by nature signals for which we lack phase information. Searching for them therefore requires a different strategy from that used to search for, e.g., inspirals where a waveform can be matched to the signal. For  $N$  detectors sensitive to an observable linear in the GW strain, the signal can be cross-correlated between detectors, leading to an SNR which is similar to that of an observable quadratic in the strain. In particular (Maggiore 2007)

$$\text{SNR} \simeq \left[ N(N-1) t_{\text{int}} \int_0^\infty df \Gamma(f)^2 \left( \frac{S_h(f)}{S_h^{\text{noise}}(f)} \right)^2 \right]^{1/2}, \quad (24)$$

where the function  $\Gamma(f)$  is the “overlap reduction function”, which captures the fact that the pairs of detectors may exhibit different responses to GW signals due to, e.g., different orientations, locations, etc. (Maggiore 2007). Here, we have assumed for simplicity that  $\Gamma(f)$  is the same for all detector pairings.

For observables quadratic in the strain, a single detector searching for a stochastic background will have an SNR given by Eq. (23). This is identical to Eq. (24) without the combinatorial prefactor  $N(N-1)$  and without the overlap reduction function. Combining multiple quadratic-in-strain detectors assuming the signal (but not the noise) to be correlated across detectors and taking the signal and noise to be independent so that they can be added in quadrature, the SNR scales as  $\sqrt{N}$ .

For both types of detector, we observe that the SNR can be improved by increasing the integration time. If we approximate  $S_h \sim h^2/\Delta f$ , the sensitivity scales as

$$\text{SNR} \propto t_{\text{int}}^{1/2}. \quad (25)$$

For cosmological GW backgrounds, we can express  $S_h(f)$  in Eq. (24) in terms of  $\Omega_{\text{GW}}(f)$  using Eq. (9), which leads to

$$\text{SNR} \simeq \frac{3H_0^2}{4\pi^2} \left[ N(N-1) t_{\text{int}} \int_0^\infty df \left( \frac{\Gamma(f) \Omega_{\text{GW}}(f)}{f^3 S_h^{\text{noise}}(f)} \right)^2 \right]^{1/2}. \quad (26)$$

Given that typical cosmological sources emit over a fairly broad frequency range, the frequency integral is likely to yield a factor  $\sim \min(\Delta f, f)$ , such that the scaling is often  $\text{SNR} \propto (t_{\text{int}} \Delta f)^{1/2}$  (see, e.g., Chapt. 7 of Maggiore 2007).

### 2.3.2 Detector sensitivity to transient GWs

In Sect. 2.2.2 above, we have argued that transient GWs can be characterized by the PSD of the GW signal, given by Eq. (14). If the signal PSD and noise-equivalent strain PSD can be treated as being approximately flat in a band of width  $\Delta f$  around the central frequency  $f$ , we can write the sensitivity as

$$S_h^{\text{lin}}(f) \gtrsim \text{SNR}^2 \times S_h^{\text{noise}}(f) \left( \frac{1}{\Delta f \Delta t} \right), \quad (27)$$

$$S_h^{\text{quad}}(f) \gtrsim \text{SNR}^2 \times S_h^{\text{noise}}(f) \left( \frac{1}{\Delta f \Delta t} \right)^{1/2}. \quad (28)$$

The time scale relevant in the denominator is either the signal duration,  $\tau$ , or the data taking time,  $t_{\text{int}}$ , whichever is shorter. In the second line we observe that a quadratic-in-strain detector is necessarily limited to be less sensitive than a linear-in-strain detector unless the bandwidth saturates the maximum possible resolution, i.e.  $\Delta f = 1/\Delta t$ .

From the signal PSD, the dimensionless strain sensitivity can be obtained, though the exact relation depends on the type of source. For example, for a monochromatic burst of duration  $\tau$ , the strain is

$$h \sim \sqrt{S_h/\tau}. \quad (29)$$

This allows us to estimate the dimensionless strain sensitivity based on Eqs. (27) and (28).

In addition, also the frequency-evolution of the signal must also be taken into account. For high-frequency GW sources, this can often be very fast, for instance  $\dot{f} \propto f^{11/3}$  for inspiralling primordial black hole binaries. In the frequency domain, this can be accounted for by determining the total number of cycles  $\mathcal{N}$  the signal spends inside a detector bandwidth.

A further convenient way of parameterizing the sensitivity to transient sources is the so-called distance reach  $d$  for a fixed SNR. If we schematically write  $S_h(f) = S_h^0(f)/d^2$  and assume optimal filtering,  $d$  is given by (Maggiore 2007)

$$d^k = \frac{2}{\text{SNR}} \left[ \Delta t \int_{f_{\min}}^{f_{\max}} df \left( \frac{S_h^0(f)}{S_h^{\text{noise}}(f)} \right)^k \right]^{1/2}, \quad (30)$$

with  $k = 1, 2$  for linear and quadratic detectors, respectively.

### 2.3.3 Detector sensitivity to persistent coherent GWs

For sufficiently persistent coherent GWs, we have argued previously that the signal PSD could be approximated by a Dirac delta-function in frequency space, or by a window function over some narrow width  $\Delta f_g$ . If the signal PSD is approximated as a delta-function and the detector response has a width  $\Delta f_{\text{det}} \leq 1/t_{\text{int}}$ , then the frequency resolution is given by  $\delta f = 1/t_{\text{int}}$ . We can then write the sensitivity to the GW strain as

$$h \gtrsim \text{SNR} \times \left( \frac{S_h^{\text{noise}}(f_g)}{t_{\text{int}}} \right)^{1/2} \quad (\text{linear}), \quad (31)$$

$$h \gtrsim \text{SNR}^{1/2} \times \left( \frac{S_h^{\text{noise}}(f_g)}{t_{\text{int}}} \right)^{1/2} \quad (\text{quadratic}). \quad (32)$$

If the detector response is broad,  $\Delta f_{\text{det}} \geq 1/t_{\text{int}}$ , the sensitivity for linear-in-strain detectors is still given by Eq. (31), but for quadratic-in-strain detectors it is modified to

$$h \gtrsim \text{SNR}^{1/2} \times (S_h^{\text{noise}}(f_g))^{1/2} \left( \frac{\Delta f_{\text{det}}}{t_{\text{int}}} \right)^{1/4} \quad (\text{quadratic}, \Delta f_{\text{det}} \geq 1/t_{\text{int}}). \quad (33)$$

owing to the fact that the integral  $\int df S_h(f)^2 \sim h^4 \delta(0)$ , and the ability to resolve  $\delta(0)$  is limited by the detector response, i.e.,  $\delta(0) \sim 1/\Delta f_{\text{det}}$ .

## 2.4 Note on characteristic strain for HFGWs

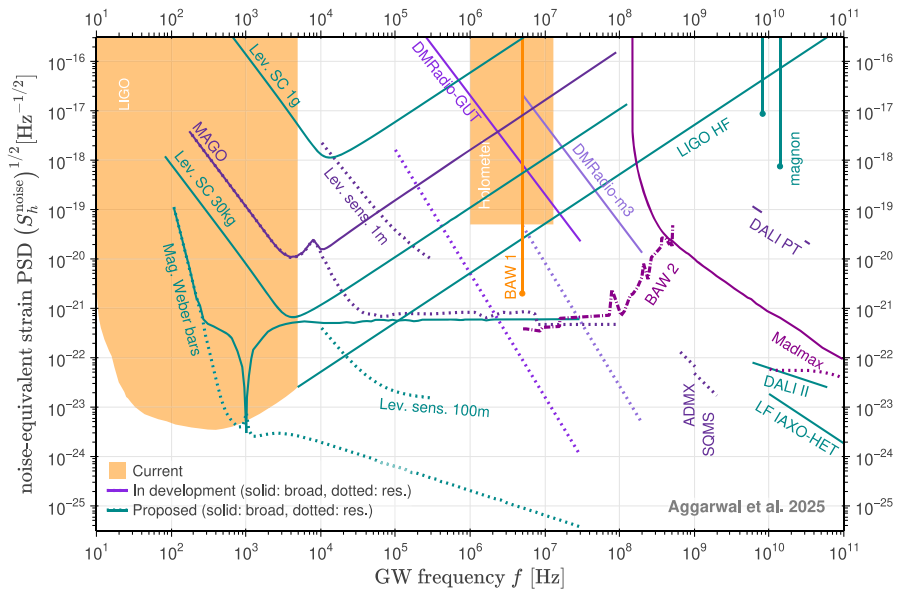
The quantity “characteristic strain” is often used in the literature (see, e.g., Moore et al. 2015). It is particularly useful for inspiralling sources, since it is designed to include the effect of the frequency evolution of the signal, keeping track of how many cycles of a given signal can be seen within some detector bandwidth.

However, most definitions of  $h_c$  in the literature start from the assumption of a matched filtering search for a signal of known frequency and phase, and a broadband detector such as an interferometer. As such, the definitions often seen in the literature on interferometers should not be directly applied to other signals/detectors. In this review, many detectors and signals are considered that do not have the same properties as the combination of BH inspirals at interferometers. Therefore, great care must be taken when considering the characteristic strain of the source, and mapping it onto a formula for the signal-to-noise ratio in a given detector.

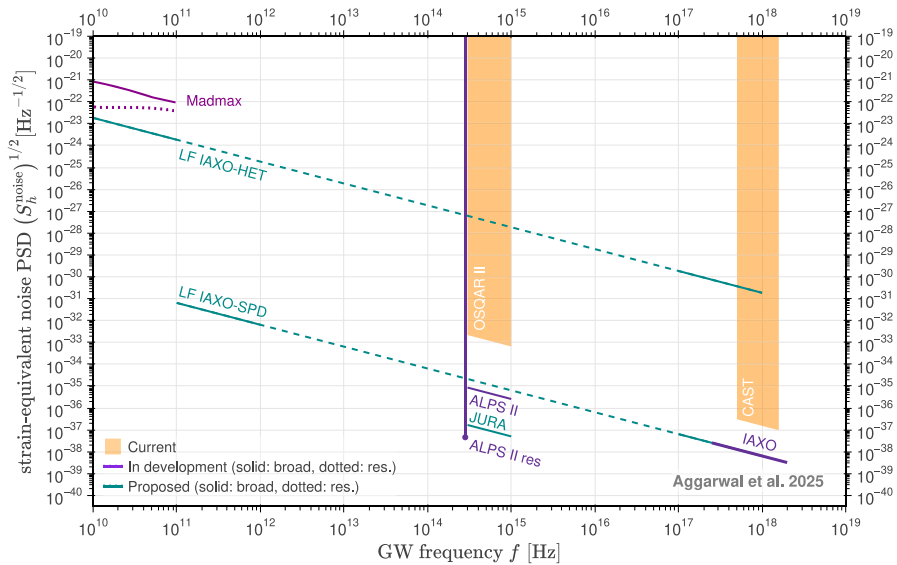
## 3 Overview of detector sensitivities and possible signals

The goal of this section is to provide a brief overview of the different detector concepts discussed in this review together with their sensitivity to some exemplary GW signals. The latter will be discussed in more detail in Sect. 4.1 (astrophysical sources) and Sect. 4.2 (cosmological source), while the detector concepts are the topic of Sect. 5. All details and references are given there. We caution that the figures below are indicative only and subject to a range of caveats.<sup>10</sup> The sensitivity

<sup>10</sup> In the first version of this review, we attempted to show different detector sensitivities together with the strengths of different types of signals in a single plot, using characteristic strain as a measure. We caution that a plot of that type contains many hidden variables (such as time scales associated with the signal, the detector integration time, and the detector bandwidth), which may lead to misleading conclusions. In this updated version of the review, we therefore choose a different approach and compare different detector concepts only in terms of noise-equivalent strain (which contains no information on the GW source) or for specific source classes.



**Fig. 1** Overview of achieved and projected strain sensitivities of high-frequency gravitational wave detectors up to 100 GHz. Solid (dashed) lines indicate broadband (resonant) detectors. The color coding (see text for details) indicates the development stage ranging from published GW results (orange) to active R&D efforts (purple) and proposed concepts (cyan). Details on the different proposals are given in Sect. 5



**Fig. 2** Overview of projected strain sensitivities of gravitational wave detectors above 100 GHz. The color coding is the same as in Fig. 1, with orange, purple and cyan curves indicating published GW results, active R&D efforts, and proposed concepts, respectively. Details on the different proposals are given in Sect. 5



curves shown in these figures are available at the HFGWPlotter webpage (Muia et al. 2025a, b).

Figures 1 and 2 provide an overview of the noise-equivalent strain sensitivities [see Eq. (16)] of a range of ultra-high frequency gravitational wave detectors discussed in more detail in Sect. 5. Here and throughout this review, we show sensitivities of resonant detectors ( $\Delta f_{\text{det}} \ll f$ ) as dashed curves and those of broadband detectors as solid curves. The color coding indicates the development stage of different experiments: orange curves correspond to detectors for which results on GW searches have been published. Purple indicates detector concepts under active research and development, which can either mean that a detector or detector prototype exists, or that there is a detailed technical proposal, funding is available for R&D, and/or a collaborative effort is underway in the community supporting the proposal. This category includes concepts whose development is driven by physics goals other than GWs, for instance light dark matter searches. Finally, cyan curves indicate detector concepts which have been proposed but are, to our knowledge, not yet under active R&D. This classification is necessarily somewhat subjective and will evolve over time; it should therefore be taken as indicative only. For better visibility, we have split these summary plots into two frequency regimes, namely below 100 GHz (Fig. 1) and above (Fig. 2).

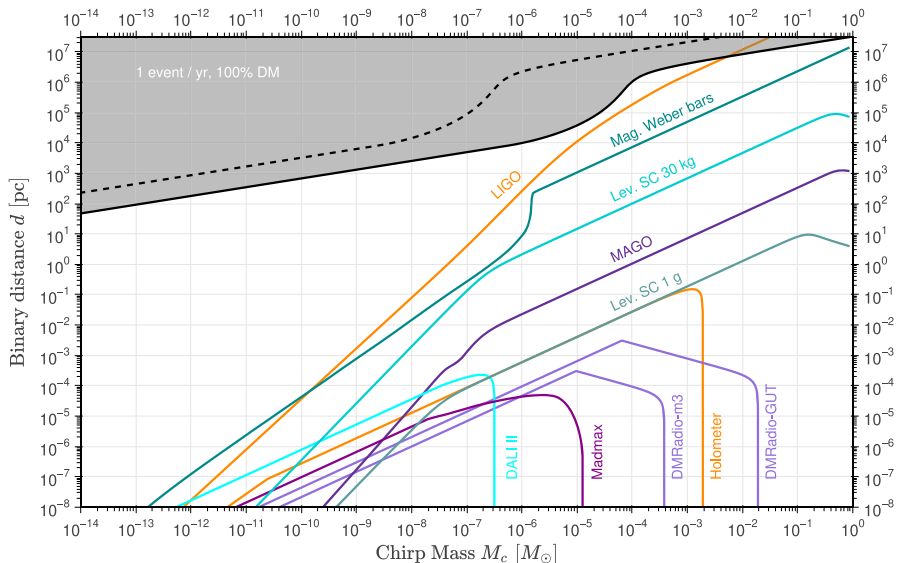
Given the sensitivity curves in Figs. 1 and 2, the detectability of possible signals can be estimated by determining the corresponding signal-to-noise ratio as given in Eqs. (23) and (22). Various types of sources and signals will be comprehensively discussed in Sect. 4; here, we focus on three exemplary cases: a monochromatic signal, a PBH binary inspiral, and a stochastic GW background.

For a **persistent, monochromatic GW signal** (arising e.g. from black hole superradiance, see Sect. 4.1.5) and a detector performing a linear measurement of the GW, the sensitivity to the GW amplitude can be estimated as [see Eq. (31)]

$$h_0^{\text{sens}} \simeq (S_h^{\text{noise}}/t_{\text{int}})^{1/2}. \quad (34)$$

For **mergers of primordial black holes** (see Sect. 4.1.2), Fig. 3 shows the astrophysical reach of a range of proposed broadband UHF GW detectors. This is obtained by integrating the GW waveform across the detector bandwidth using (56) and assuming an SNR threshold of 10. For simplicity, we have here assumed equal mass PBHs, circular orbits, no inclination angle, optimal sky position and we are working in the Newtonian approximation, integrating up to the innermost stable circular orbit, see Sect. 4.1.2 for details. The ‘chirp’ signal of PBH mergers, increasing rapidly in frequency and amplitude as the merger approaches, makes it challenging for resonant detectors to pick up a significant part of the signal strength, and hence these detectors are not shown in Fig. 3. Similarly, single photon detectors suffer from the short duration of these signals as it prevents them from reaching the energy threshold of a single photon per merger event. The corresponding line for LF-IAXO SPD is thus below the plot range shown.

To estimate the **sensitivity to stochastic GW backgrounds (SGWBs)**, we distinguish between broadband detectors (with a typical bandwidth of about a decade in frequency) and resonant detectors, which profit from a resonance with a



**Fig. 3** Distance reach of different broad-band high-frequency GW detectors for equal-mass PBH binaries with chirp mass  $M_c$ . The color code matches the one used in Figs. 1 and 2, with orange, purple and cyan curves indicating published GW results, active R&D efforts, and proposed concepts, respectively. The upper shaded region corresponds to distances within which  $\geq 1$  event/yr is expected, assuming PBHs to account for all of the dark matter in the Universe (solid) or 0.1% of it (dashed)

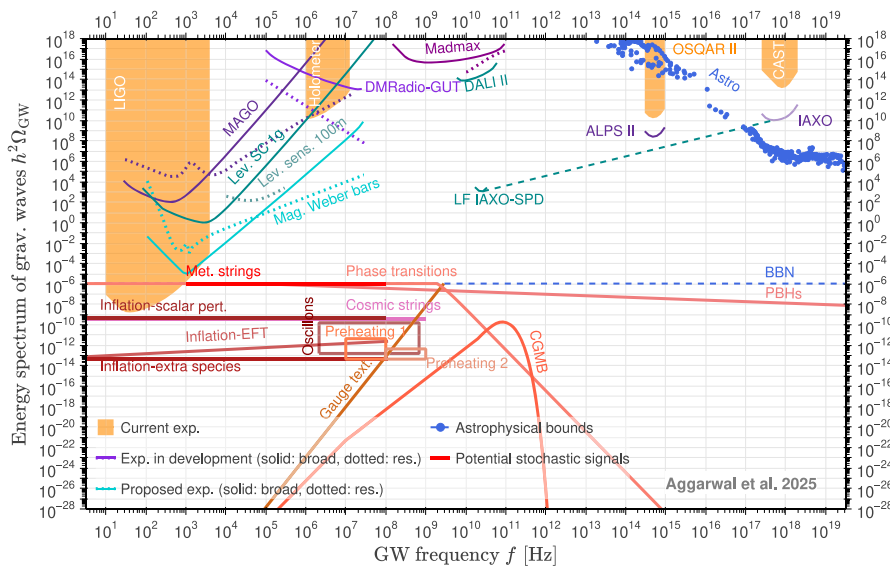
large quality factor  $Q$ , but are sensitive only to a very narrow bandwidth,  $\Delta f_{\text{det}} = f/Q$ . In the latter case, coverage over a wider frequency range can often be achieved by a scanning strategy, amounting to tuning the detector to different frequencies over time.

For broadband detectors, we show power-law integrated sensitivity (PLS) curves in Fig. 4. To obtain these curves, we have fixed the integration time to 1 year and the SNR threshold to  $\text{SNR}_{\text{thr}} = 10$ , and we have then determined the power-law GW templates,

$$\Omega_{\text{GW}} = \Omega_0 (f/f_*)^\alpha, \quad (35)$$

for which Eq. (23) evaluates to  $\text{SNR} = \text{SNR}_{\text{thr}}$ , using Eq. (9) to relate  $S_h$  and  $\Omega_{\text{GW}}$ . An important exception are single photon detectors (OSQAR, ALPS, CAST and IAXO) for which the achievable sensitivity to SGWBs is limited by the requirement of producing at least one photon [see Eq. (122)] during the assumed detector run time of 1 year.

For resonant detectors, we first note that a simple scanning strategy spending an equal amount of time in each frequency bin ( $t_{\text{int}, \Delta f} \sim t_{\text{int}, \text{tot}}/Q$  and  $\Delta f_{\text{det}} \sim f/Q$ ) does not lead to any gain in SNR for a large quality factor  $Q$ , since the increase of the integrand of Eq. (23) by a factor of  $Q$  is compensated by reduced time and frequency interval per bin. However, since SGWBs typically have a broad frequency spectrum, one could consider running a resonant detector at a fixed frequency (no scanning), with  $t_{\text{int}} = 1$  year as above. In this case, the sensitivity to



**Fig. 4** Sensitivity of high-frequency gravitational wave detectors to stochastic gravitational wave backgrounds assuming 1 year of integration time. The solid curves (broadband instruments) are power-law-integrated sensitivity curves, the dashed lines (resonant instruments) indicate the reach when running at fixed frequency for  $t_{\text{int}} = 1$  year. See text for details and caveats. In blue we indicate astrophysical constraints as discussed in Sect. 5.6, where integration time varies dependent on observations Hill et al. (2018). The horizontal dashed blue line indicates the upper bound from BBN on cosmological sources, see Sect. 4.2. The remainder of the color coding is as in Figs. 1 and 2, with orange, purple and cyan curves indicating published GW results, active R&D efforts, and proposed concepts, respectively

$\Omega_{\text{GW}}$  scales as  $Q^{-1/2}$  (with the exception of detectors limited by the single-photon threshold, which do not profit from this scaling). We show this sensitivity as dashed lines in Fig. 4, emphasizing that this indicates the possible reach at a given sensitivity, while fully covering the entire frequency range shown would require an unrealistic amount of time, or an unrealistic number of detectors running in parallel at different resonance frequencies.

Figure 4 shows the resulting exclusion regions, prospective sensitivities and possible signals in units of  $\Omega_{\text{GW}} h^2$ , with  $h = H_0/(100 \text{ km/s/Mpc})$  denoting the dimensionless Hubble parameter. Several comments are in order. Firstly, we note that no proposal above the LIGO–Virgo–KAGRA band currently reaches below the cosmological bound of  $\Omega_{\text{GW}} h^2 \lesssim 10^{-6}$  arising from the limits on excess energy density in relativistic degrees of freedom ( $N_{\text{eff}}$ ) at BBN (see Sect. 4.2). Therefore, cosmological GW sources seem currently out of reach. Scenarios detectable with current sensitivities would for the most part imply values of  $\Omega_{\text{GW}} \gg 1$ , which taken at face value would correspond to a GW dominated universe. In this context, Fig. 4 can be interpreted as (i) showing the sensitivity to local overdensities of GW energy and (ii) indicating the improvement in sensitivity needed to probe cosmological sources. Secondly, we caution that the sensitivity curves shown for laboratory detectors do not take into account the angular response function of the detectors but assume that a local overdensity of GW energy is located in the optimal position with

respect to the field of view. For detectors with a broad field of view, such as interferometer or electromagnetic oscillators, the sky-averaged sensitivity is about a factor 10 smaller than this ideal sensitivity. For detectors with a very narrow field of view, such as some photon regeneration experiments, the degradation can be much more significant. Third, we note that the bandwidth of broadband detectors is limited by the data acquisition system. Here we have assumed a readout covering the entire frequency range of these detectors as shown in Fig. 4, which in some case would require multiple layers of readout systems.

Figure 4 also shows cosmological and astrophysical bounds on UHF GWs. Besides the aforementioned BBN bound and a very similar bound from the CMB, not shown here, this includes limits based on GW-to-photon conversion in astrophysical environments with strong magnetic fields, see Sect. 5.6. The blue points in the upper right corner of Fig. 4 correspond in particular to limits from GW-to-photon conversion in galactic magnetic fields. Additional astrophysical bounds are summarized in Fig. 13 in Sect. 5.6, but the galactic ones are the only limits which translate to constraints  $\Omega_{\text{GW}} h^2 < 10^{15}$ .

Finally, Fig. 4 also shows a representative selection of SGWB sources, discussed in more detail in Sect. 4. The regions bounded by the colored curves illustrate the region of parameter space which may be covered by the corresponding source for appropriate parameter choices as specified below. Except for the cases of inflation with broken spatial reparametrization symmetry and the cosmic gravitational microwave background they should not be mistaken for GW spectra obtained for a fixed model parameter choice. Rather, they show the estimated envelopes of the signals obtained in different classes of models, and should thus be seen as the most optimistic estimate for possible signals.

- In certain models, inflation (Sect. 4.2.1) can yield a signal stretching over a broad frequency range [see Eq. (88)], with an amplitude determined by Eqs. (89) and (91), respectively. Here in the case of inflation with extra-species we have taken the parameter  $\xi$  [defined in Eq. (89)] to be bounded by the perturbative limit, and in the case of inflation described by an effective field theory with broken spatial reparametrization symmetry we have chosen the speed of sound and the spectral tilt to be  $c_T = 1$  and  $n_T = 0.2$ , respectively. Moreover, inflation models with strongly enhanced scalar fluctuations ( $P_\xi \lesssim 10^{-2.5}$ ) can source GWs with  $\Omega_{\text{GW},0} \lesssim 10^{-9}$  at second order in cosmological perturbation theory.
- For preheating (Sect. 4.2.2), we show typical values for models with parametric resonance in quadratic (“preheating 1”) and quartic (“preheating 2”) potentials as well as oscillons. In the latter case the frequency is set by the mass of the scalar field through Eq. (96), where here we have chosen the mass of the scalar field to be  $10^{10} \text{ GeV} < m < 10^{13} \text{ GeV}$  with  $X = 100$ , while the amplitude is the typical value inferred from numerical simulations.
- For the cosmic gravitational microwave background (Sect. 4.2.3), we show the spectrum given by Eq. (97) with  $T_{\text{max}} = 10^{16} \text{ GeV}$ , which is the upper bound on the reheating temperature set by the constraints on the tensor-to-scalar-ratio (Akrami et al. 2020).

- For phase transitions (Sect. 4.2.4), we have obtained an envelope of curves with strength parameter  $\alpha = 10^2$ , duration parameter  $\beta/H_* = 1$ , and  $v_w = 1$ .
- As an example for topological defects (Sect. 4.2.5), cosmic strings lead to a broad spectrum with an amplitude given in Eq. (102), where the string tension for stable cosmic strings is bounded by  $G\mu < 10^{-10}$  from PTA measurements, whereas for metastable cosmic strings it can be as large as  $G\mu \simeq 10^{-3}$  above the LIGO frequency range. The spectrum of gauge textures is described by Eq. (104), where here we have chosen the symmetry breaking scale to be  $10^{12} \text{ GeV} < v < 10^{19} \text{ GeV}$ .
- PBH mergers also produce a SGWB in the late universe, as discussed in Sect. 4.1.2. With the line shown in Fig. 4, we indicate the envelope of the maximal amplitudes reached by such a SGWB, varying the assumed typical population mass  $m_{\text{PBH}}$ , which is related to the peak frequency through (46).

## 4 Sources of gravitational waves at high frequencies

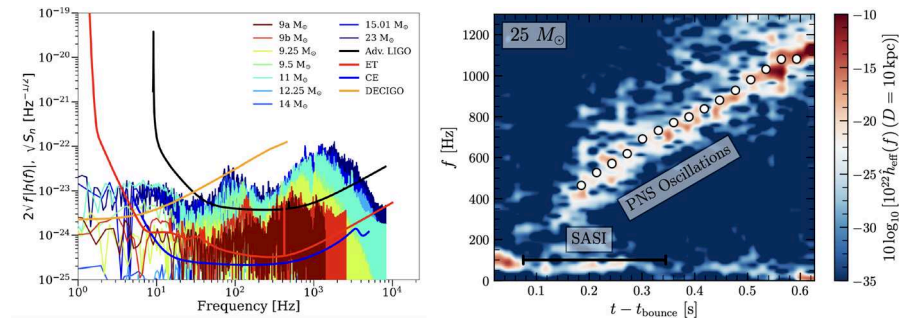
This section reviews various production mechanisms for GW signals in the high-frequency regime, typically in the kHz–GHz range, that fall into two broad classes: late Universe sources and early Universe sources. The former category, which we discuss in Sect. 4.1, corresponds to sources in our cosmological neighborhood, emitting coherent transient and/or monochromatic GW signals. Early Universe sources, which will be the topic of Sect. 4.2, in contrast are sources at cosmological distances which typically lead to a stochastic background of GWs. We emphasize that all proposed sources, with the notable exceptions of the neutron star mergers discussed in Sect. 4.1.1 (kHz range) and the cosmic gravitational microwave background discussed in Sect. 4.2.3, require new physics beyond the Standard Model of particle physics to produce an observable GW signal. Thus, while being admittedly somewhat speculative, these proposals provide unique opportunities to shed light on the fundamental laws of nature, even by ‘only’ setting upper bounds on the existence of GWs in the corresponding frequency range.

### 4.1 Late universe

In the following, we give an overview of high-frequency GW sources that are active in the late Universe. A concise summary of these sources is given in Table 1 in Sect. 4.4.

#### 4.1.1 Known astrophysical systems

*Core-collapse supernovae.* Massive stars reach the end of their lives by exploding in a core-collapse supernova (CCSN), giving birth to neutron stars and black holes (BHs). GW detection from CCSNe is a promising candidate to learn about the inner core dynamics and explosion mechanism, as well as the properties of nuclear matter at high densities (see Abdikamalov et al. 2020 for a review). As the core collapses, forming a proto-neutron star (PNS), it reaches supranuclear densities, and the



**Fig. 5** **Left:** GW spectrum of slowly rotating core-collapse supernovae from several different simulations compared to the sensitivities of interferometric detectors. **Right:** Frequency of the signal from a core-collapse supernova of a  $25M_{\odot}$  progenitor star as a function of time and of the proto-neutron star's oscillatory modes. The white dots denote the eigenfrequencies associated with the quadrupolar f- and g-modes of the PNS. Asymmetric accretion produces an early subdominant peak around 100 Hz and excites the proto-neutron star oscillations which emit the dominant peak around 1 kHz. Images reproduced with permission from [left] Vartanyan et al. (2023), copyright by APS, and [right] Radice et al. (2019), copyright by AAS

stiffness of the PNS stops the in-fall and bounces back a shock wave that triggers the explosion.

For slowly rotating CCSNe, neutrino-driven convection, turbulent flow, and the standing-accretion shock instability (SASI) produce asymmetric flows that generate GWs at  $\sim 100$  Hz. More importantly, though, these mechanisms excite the oscillatory modes of the PNS, which lead to much stronger GW emission at  $\sim 1$  kHz (see Fig. 5). These oscillatory modes depend solely on the mass and equation of state of the PNS, implying that valuable information about the nuclear matter could be obtained by observing them (see e.g. Jakobus et al. 2023; Kunjipurayil et al. 2022). For example, the frequency and the amplitude of the dominant peak both increase with the effective in-medium mass of the nucleons forming the PNS (Andersen et al. 2021). The overall signal contains additional information about the explosion, in particular, the total energy radiated is strongly correlated with the energy in turbulent flow as well as with the compactness of the original star (Vartanyan et al. 2023; Radice et al. 2019).

For fast-rotating stars, the PNS is born with an asymmetry, determining the dominant pulsations. Rotation enhances the GW signal strength until centrifugal forces become too strong and prevent the PNS from acquiring larger densities (Abdikamalov et al. 2014). Furthermore, instabilities associated with rotation produce new signatures in the 100 Hz–1 kHz band (Shibagaki et al. 2020; Hsieh et al. 2024).

If the mass of the PNS is too large, it will eventually collapse into a black hole. In this case, a sudden drop in frequency after the signal peaks at  $\sim 1$  kHz is observed as a signature of the collapse (Cerdá-Durán et al. 2013).

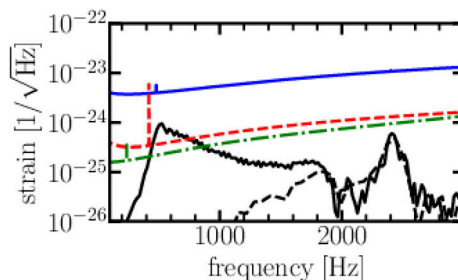
We see that CCSNe are expected to emit GWs at the upper high end of the frequency range covered by ground-based interferometers. However, even higher-frequency GWs could be radiated. For example, if the nuclear matter in the PNS

undergoes a first-order phase transition into quark matter, a rapid contraction and second bounce of the core is expected. In this case, the peak of the GW signal at  $\sim 1$  kHz is shifted to higher frequencies,  $\sim 2\text{--}4$  kHz, associated with the quadrupolar pulsation modes of a more compact body (Abdikamalov et al. 2009; Zha et al. 2020). In addition, the dynamics of the phase transition may give rise to a signal in the MHz band (Cao and Lin 2018; Casallerrey-Solana et al. 2022). Both signals would offer invaluable information about the properties of dense QCD matter.

*Neutron star mergers.* The collisions of neutron stars provide perfect environments for probing the warm and dense region of the QCD phase diagram. The process starts with a long inspiral phase, followed by the post-merger dynamics (see Baiotti and Rezzolla 2017; Sarin and Lasky 2021; Lovato et al. 2022 for reviews).

The full GW spectrum from a binary neutron star merger is shown in Fig. 6. The inspiral phase leads to the emission of a relatively low frequency (hundreds of Hz) GW signal, which carries information about the quadrupole tidal deformability of the stars (and therefore the matter equation of state), the compactness of the stars, and the binary mass ratio (Hinderer 2008; Read et al. 2013; Bernuzzi et al. 2014).

The post-merger dynamics is the process during which most of the GW energy is radiated. The signal features depend more strongly on the underlying equation of state (EoS), including finite-temperature effects. The post-merger signal is present as long as prompt collapse into a black hole is avoided, and it depends on the dynamics of the metastable (or stable) rotating remnant. Simulations for a wide range of EoS show that three peaks are characteristic in this phase (Takami et al. 2014; Bauswein et al. 2016). The dominant peak, at frequency  $f_{\text{peak}}$ , is associated with the fundamental quadrupolar fluid mode, which has been shown to be correlated with the maximum radii of a non-rotating star a given EoS could support (Bauswein et al. 2016). The subdominant part of the spectrum also encodes non-trivial information about the EoS. In particular, a second subdominant peak is produced by the orbital motion of antipodal bulges at the surface of the remnant right after the merger (Bauswein et al. 2016, 2019), while additional features were identified with the coupling to the quasi-radial mode, see Bauswein et al. (2016).



**Fig. 6** GW spectrum of a binary neutron star merger, including the inspiral and the post-merger dynamics. The post-merger emission is in the kHz band and exhibits three characteristic peaks independently of the choice of EoS. This contribution is singled out by the dashed line. Figure taken from Sarin and Lasky (2021). Colored diagonal lines indicates the forecasted sensitivity of future ground based interferometers Advanced LIGO (blue), Einstein Telescope (red) and Cosmic explorer (red)



Whether the remnant eventually collapses to a BH or not is difficult to conclude from the post-merger GW signal. The eventual collapse induces an excess of power at higher frequencies, around the ringdown frequency of the produced black hole, which is absent if the remnant is stable (Dhani et al. 2024). If the merger leads to a prompt collapse, the post-merger emission is shut down and taken over by the ringdown signal of the corresponding rotating black hole. The peak frequency is then shifted towards higher frequencies, up to 10 kHz (Echeverria 1989; Dhani et al. 2024), making it possible to distinguish mergers that lead to a prompt collapse from those that only lead to a delayed collapse, or no collapse at all. Discerning among all these cases would have strong implications on our understanding of the EoS of dense nuclear matter, including the possibility of first-order phase transitions to quark matter in the core (Most et al. 2019; Tootle et al. 2022; Demircik et al. 2022), which we discuss next.

*First-order phase transitions in neutron stars.* An additional potential high-frequency GW signal associated with binary neutron star mergers could arise from the dynamics of a first-order QCD phase transition (FOPT) occurring during the merger (Casalderrey-Solana et al. 2022). In such a phase transition, the core of the star would transition from the hadronic matter phase into a quark matter phase or into a color superconductor.<sup>11</sup> Whether or not this phase transition is accessible at the densities and temperatures realized in a neutron star merger, and whether it is first order, is currently unknown, though indications for a first-order nature exist (Berges and Rajagopal 1999; Buballa 2005). We will assume here that both conditions are met, so that GW emission can occur. Given the adiabaticity of the merger timescale compared to the timescales of the underlying microscopic nuclear processes, ( $1 \text{ ms} \gg 10^{-20} \text{ ms} \simeq 1 \text{ fm}$ ), a realization of the phase transition through bubble nucleation, expansion, and collision is expected, similar to the dynamics of cosmological first-order phase transitions (see e.g. Hindmarsh et al. 2021 for a review).

The peak frequency of the GW signal from a FOPT inside a neutron star is determined by the average size,  $R$ , of the quark matter bubbles at the time they collide.  $R$  is set by the speed of the bubble walls,  $v_w$ , together with the duration of the transition,  $\beta^{-1}$ ,

$$f_{\text{peak}} = R^{-1} = (8\pi)^{-1/3} v_w^{-1} \beta. \quad (36)$$

Most of the uncertainty in the GW spectrum originates from the wall speed as it is a challenging property to compute from first principles for a given theory (see Moore and Prokopec 1995; Dorsch et al. 2018; Lewicki et al. 2022; Laurent and Cline 2022; Jiang et al. 2023; Bigazzi et al. 2021; Bea et al. 2021, 2022; Janik et al. 2022; Sanchez-Garitaonandia and van de Vis 2024 for some computations at weak and strong coupling). The duration of the transition  $\approx \beta^{-1}$  can be estimated from the ratio between the microscopic scale  $\Lambda$  and the macroscopic one,  $\tau$  (Casalderrey-Solana et al. 2022; Hindmarsh et al. 2021), leading to

<sup>11</sup> A similar phenomenon could take place in a neutron star that undergoes quick gravitational collapse during supernova explosion, see Cao and Lin (2018).



$$f_{\text{peak}} \simeq \left( \frac{0.1}{v_w} \right) \left( \frac{1 \text{ ms}}{\tau} \right) \left( 0.62 + \frac{2 \times 10^{-3}}{\pi^{1/3}} \log \left[ \left( \frac{v_w}{0.1} \right)^3 \left( \frac{\tau}{1 \text{ ms}} \right)^4 \frac{A^4}{1 \text{ GeV/fm}^3} \right] \right) \text{MHz} \quad (37)$$

Taking  $A \simeq 1 \text{ GeV/fm}^3$  based on dimensional arguments (Annala et al. 2020), and  $v_w \sim 0.1$ , the peak frequency falls into the Mega-Hertz band,  $f_{\text{peak}} \approx 0.6 \text{ MHz}$ , two orders of magnitude above the signal from macroscopic oscillations of the neutron star, discussed above.

The estimation of the strain is subject to several uncertainties, but a rough approximation can be obtained using results from the cosmological phase transitions literature for the total energy radiated (see e.g. Hindmarsh et al. 2015). This leads to the following expression for the observed strain (Casalderrey-Solana et al. 2022) [written following the notation from Eq. (13)],

$$h_{\text{c,sto}} \simeq 1.8 \times 10^{-25} v_f^2 \times \left( \frac{A^4}{1 \text{ GeV/fm}^3} \right) \left( \frac{L}{1 \text{ km}} \right)^{3/2} \left( \frac{1 \text{ MHz}}{f_{\text{peak}}} \right)^{3/2} \left( \frac{100 \text{ Mpc}}{D} \right), \quad (38)$$

with  $D$  the luminosity distance to the NS merger,  $L$  the size of the region in the NS that undergoes the transition, and  $v_f$  the typical velocity of the fluid after the collision of all bubbles. Using the same numerical parameter values as before, and  $L \simeq 5 \text{ km}$  (Tootle et al. 2022; Demircik et al. 2022), Eq. (38) reduces to

$$h_{\text{c,sto}} \simeq 1.5 \times 10^{-24} v_f^2 \times \left( \frac{100 \text{ Mpc}}{D} \right). \quad (39)$$

These estimates are based on the assumption that GWs are acoustically generated after the bubble collisions. Sound waves are expected to have a lifetime of order a millisecond, setting the duration of the emission. Simulations show that during the merger several regions that undergo the transition cross back to the initial phase later (Tootle et al. 2022; Demircik et al. 2022), thereby undergoing an additional transition. This implies that several signals are expected to come from a single merger, all with a peak frequency around the MHz band.

The detection of such a signal would imply that a FOPT is present in nuclear matter at high densities, it would constrain the location of this phase transition in the QCD phase diagram, and it would elucidate its dynamics. It would therefore provide major insights into the physics of strong interactions that are very difficult to obtain in any other way.

*Disks around supermassive BHs.* In Saito et al. (2021), it was shown that photons emitted from accretion disks around supermassive black holes can be converted into gravitational waves in the black hole's magnetosphere through the Gertsenshtein effect Gertsenshtein (1962), inducing a high-frequency GW signal, which experimentally would manifest itself as a stochastic background. In practice, photons from the accretion disk steadily accumulate around the photon sphere. If their frequency matches the resonance frequency at which the effective photon mass (that receives opposite-sign contributions from plasma effects and magnetic field effects)

vanishes, they are efficiently converted into gravitons of the same frequency by the magnetic field. The characteristic frequency of the resulting GWs is therefore (Saito et al. 2021)

$$f \sim \frac{1}{2\pi} \left( \frac{45}{12k\alpha} \frac{m_e^3}{m_p c^2} \right)^{1/2} \sim 3.3 \times 10^{19} \text{ Hz}, \quad (40)$$

where  $m_e$  and  $m_p$  are the electron and proton mass, respectively, while  $\alpha$  is the electromagnetic fine structure constant, and  $k$  ( $= 2$  or  $7/2$  for the  $+$  and  $\times$  polarizations, respectively) controls the magnetic field contribution to the effective photon mass. Interestingly,  $f$  does not depend on the supermassive BH mass and the magnetic field and inevitably falls in the UHF-GW window.

The GW luminosity can be estimated based on the conversion probability. By integrating the emission from all supermassive black holes in the Universe, one predicts a stochastic gravitational wave background with energy density

$$\Omega_{\text{GW}} \simeq 2 \times 10^{-12} \xi, \quad (41)$$

where  $\xi \lesssim 1$  is the dimensionless ratio between the black hole horizon area and the accretion disk area. This estimate assumes a small tilt of the SMBH mass function, meaning that the mass is taken to follow a mild power-law dependence

$$n(M) \propto M^{-\beta}, \quad (42)$$

with  $\beta \ll 1$ , consistent with current SMBH mass function measurements. Here,  $n(M)$  denotes the comoving number density of SMBHs of mass  $M$ , which we take to be spatially homogeneous across the observable Universe. The observed SMBH mass range spans  $M \sim 10^6 M_\odot - 10^{11} M_\odot$ , and using this mass function with a small tilt leads a parametric dependence omitted in Eq. (41) for simplicity, see Saito et al. (2021) for more detail. For  $\beta \ll 1$ , one maximises the amplitude of the signal, which yield  $\Omega_{\text{GW}}$  at the level of  $10^{-12}$ . Important uncertainties remain due to the unknowns in the SMBH population, particularly the precise number density and mass distribution of these objects across cosmic time.

*GW spectrum of the sun.* The high-temperature plasma within stellar interiors generates stochastic GWs (Weinberg 1972; Gould 1985; García-Cely and Ringwald 2025), with frequencies roughly determined by the temperature at the core. For the Sun, this results in a spectrum spanning the range  $10^{12}$ – $10^{19}$  Hz, peaking at  $10^{18}$  Hz. These GWs are produced through two primary mechanisms:

- **Hydrodynamic fluctuations.** These are sourced by tensor fluctuations of the energy–momentum tensor of the solar plasma and are proportional to the shear viscosity  $\eta$  (Ghiglieri and Laine 2015). The resulting GW emission power is given by García-Cely and Ringwald (2025)

$$\left. \frac{dP}{d\omega} \right|_{\text{Hydrodynamics}} = \frac{16G\omega^2}{\pi} \int_{\text{Sun}} d^3r \eta T, \quad (43)$$

where  $T$  is the temperature of the solar plasma and  $\omega = 2\pi f$ .

- Graviton emission from particle collisions. In contrast to hydrodynamical fluctuations, these correspond to frequencies higher than those of collisions in the solar plasma, so that there is sufficient time for them not to interfere with each other. In this case García-Cely and Ringwald (2025)

$$\left. \frac{dP}{d\omega} \right|_{\text{Collisions}} = \int_{\text{Sun}} d^3r \sum_i \omega \left\langle \frac{d\Gamma^{(i)}(r)}{d\omega dV} \right\rangle, \quad (44)$$

where  $\langle \cdot \rangle$  denotes a thermal average and  $\Gamma^{(i)}$  is the graviton emission rate for each process: *i*) photoproduction  $\gamma Z \rightarrow eh$  and  $\gamma e \rightarrow eh$ ; *ii*) bremsstrahlung  $eZ \rightarrow eZh$ ; *iii*) bremsstrahlung  $ee \rightarrow eeh$ .

The characteristic strain amplitude  $h_c(f)$  of the stochastic gravitational wave background from the Sun can be expressed as

$$h_{c,\text{sto}} = \frac{1}{D_\odot} \left( \frac{2G dP/d\omega}{\omega} \right)^{1/2} \simeq 10^{-42}, \quad (45)$$

where  $D_\odot$  is the distance from the Earth to the Sun. While we use here the same notation as in Eq. (13), it should be kept in mind that the stochastic GW signal from the Sun is highly anisotropic and defined by an integration over the solid angle under which we see the Sun.

In analogy to the Sun, also the other main-sequence stars in the galaxy are expected to emit a similar GW signal; the characteristic strain of their integrated emission has been found to be a few orders of magnitude lower than the one in Eq. (45) (Gould 1985; García-Cely and Ringwald 2025).

#### 4.1.2 Light primordial black holes

The detection of BH mergers by LIGO and Virgo has revived the interest in primordial BHs (PBHs) in the mass range (1–100)  $M_\odot$  (Bird et al. 2016; Clesse and García-Bellido 2017; Sasaki et al. 2016), which could constitute a relevant fraction of the observed dark matter abundance. In this context, detecting a sub-solar mass compact object, and provided large tidal effects are excluded (Crescimbeni et al. 2024), would point to a primordial origin.<sup>12</sup> PBHs can form in a much wider range of masses than what is expected from astrophysical formation mechanisms (see e.g. Bagui et al. 2025; Carr et al. 2024 for recent reviews), with their size typically related by  $\mathcal{O}(1)$  factors to the mass contained within one Hubble sphere at the time of production in the early Universe. Many constraints were set on the abundance of PBHs (usually parameterized as a fraction of the total DM abundance,  $f_{\text{PBH}} \equiv \Omega_{\text{PBH}}/\Omega_{\text{DM}}$ ) across many orders of magnitude in mass, while the so-called

<sup>12</sup> See, however, Kouvaris et al. (2018), Takhistov et al. (2021), Dasgupta et al. (2021), Chakraborty and Bhattacharyya (2024) for other formation channels of sub-solar BHs, such as white dwarf or neutron star transmutation triggered by accretion of dark matter.

asteroid mass range,  $m \sim 10^{-12} M_{\odot}$ , currently remains very challenging to probe (Katz et al. 2018; Carr et al. 2021b). UHF-GWs may allow us to set unprecedented constraints on this elusive population of objects, potentially addressing the question of whether they compose a significant fraction of dark matter.

**PBH mergers.** The GW emission from a binary inspiral is close to maximal at the innermost stable circular orbit (ISCO), which marks the end of the inspiral phase and the beginning of the merger phase.<sup>13</sup> The ISCO frequency is given by

$$f_{\text{ISCO}} = 4400 \text{ Hz} \frac{M_{\odot}}{M}, \quad (46)$$

where we have introduced the total mass of the binary  $M = m_1 + m_2$  and  $M_{\odot}$  denotes the solar mass. Frequencies in the range  $10^4$ – $10^{15}$  Hz correspond to a primordial BH mass range  $10^{-12}$ – $10^{-1} M_{\odot}$ . In particular, the planetary-mass range, in which recent detections of star and quasar microlensing events (Niikura et al. 2019; Hawkins 2020; Bhatiani et al. 2019; Mróz et al. 2024) allow a PBH fraction of  $f_{\text{PBH}} \sim 0.01$ , could be probed in a novel and independent way with GWs.

A good estimate of the GW strain produced by a circular PBH binary at a given frequency  $f$  can be obtained at zeroth post-Newtonian (0-PN) order (Maggiore 2007; Antelis et al. 2018).<sup>14,15</sup>

$$\begin{aligned} h(f) &= \left( \frac{5}{24} \right)^{1/2} \frac{1}{\pi^{2/3}} \frac{1}{D} (GM_c)^{5/6} f^{-7/6} e^{i\psi} Q(\theta, \phi, \varphi) \\ &\approx 2 \times 10^{-37} \text{ sec} \left( \frac{\text{kpc}}{D} \right) \left( \frac{m_{\text{PBH}}}{10^{-12} M_{\odot}} \right)^{5/6} \left( \frac{f}{\text{GHz}} \right)^{-7/6}, \end{aligned} \quad (47)$$

where  $G$  is Newton's constant;  $M_c \equiv (m_1 m_2)^{3/5} / (m_1 + m_2)^{1/5}$  is the chirp mass of a binary with constituent masses  $m_1, m_2$ ;  $D$  is the luminosity distance from the binary to the observer;  $\psi$  is a phase; and  $Q(\theta, \phi, \varphi)$  is a function that depends on the position of the binary with respect to the detector, and the angle  $\varphi$  between the normal of the orbit and the line of sight. In the second line of Eq. (47) we have fixed  $m_1 = m_2 \equiv m_{\text{PBH}}$ . Throughout this section we consider quasi-circular orbits. This is justified by the fact that PBH binaries typically form at high redshift and undergo long periods of GW-driven evolution, which efficiently circularizes their orbits before they become observable. This modeling of the GW signal only describes the inspiral phase of the binary roughly until the ISCO frequency is reached. While it neglects the merger and the ringdown part of the signal, it is sufficient for the

<sup>13</sup> Slightly larger strains are reached during the merger, but we focus on the ISCO here to allow for analytic estimates of the strain.

<sup>14</sup> We assume that GW emission is the dominant effect driving binary evolution. While accretion can speed up binary evolution [also enhancing the merger rates (Ali-Haïmoud et al. 2017; De Luca et al. 2020b)], it is typically small in the subsolar mass range of interest here (see e.g. Ricotti et al. 2008).

<sup>15</sup> Throughout this section we neglect cosmological redshift effects. As illustrated in Fig. 3, the mergers considered here occur at distances of at most  $\mathcal{O}(10)$  Mpc, corresponding to redshifts  $z \sim 10^{-3}$ . At such low redshifts, cosmological corrections (e.g., redshifting of the chirp mass or luminosity distance) are negligible.

present purposes as only the GW signal produced during the inspiral phase can last for a sufficiently long time to allow for a potential detection.

A crucial quantity for determining detection prospects for GWs from PBH binaries is the time, or the number of orbital cycles  $N_{\text{cycles}}$ , the GW signal spends within a given frequency interval. As discussed in Sect. 2.3.2, this time may in particular be shorter than the integration time of the detector, limiting the sensitivity. For an equal mass PBH binary ( $m_1 = m_2 = m_{\text{PBH}}$ ) and assuming energy loss is dominated by GW emission,<sup>16</sup>  $N_{\text{cycles}}$  is given by (Moore et al. 2015)

$$N_{\text{cycles}} = \frac{f^2}{\dot{f}} \simeq 2.2 \times 10^6 \left( \frac{f}{\text{GHz}} \right)^{-5/3} \left( \frac{m_{\text{PBH}}}{10^{-9} M_{\odot}} \right)^{-5/3}, \quad (48)$$

where we have used (Maggiore 2007)

$$\dot{f} = \frac{96}{5} \pi^{8/3} \left( \frac{GM_c}{c^3} \right)^{5/3} f^{11/3} \simeq 4.6 \times 10^{11} \text{ Hz}^2 \left( \frac{m_{\text{PBH}}}{10^{-9} M_{\odot}} \right)^{5/3} \left( \frac{f}{\text{GHz}} \right)^{11/3}. \quad (49)$$

Note that only close to the ISCO frequency, namely in the final phase of the inspiral, the number of cycles becomes of order unity. Note also that  $N_{\text{cycles}}$  determines whether the signal can be approximated as nearly monochromatic, which is the case when  $N_{\text{cycles}} \gg 1$ .

A useful quantity closely related to  $N_{\text{cycles}}$  is the time to coalescence, which is given by (Maggiore 2007)

$$\tau(f) \approx 83 \text{ sec} \left( \frac{m_{\text{PBH}}}{10^{-12} M_{\odot}} \right)^{-5/3} \left( \frac{f}{\text{GHz}} \right)^{-8/3}. \quad (50)$$

*Formation channels for PBH binaries.* There are two main formation channels for primordial BH binaries (see e.g. Raidal et al. 2025):

1. *Primordial binaries.* These are pairs of PBHs that were formed sufficiently close to each other for their dynamics to decouple from the expansion of the Universe before the time of matter–radiation equality (Nakamura et al. 1997; Sasaki et al. 2016). The gravitational influence of one or several PBHs nearby prevents the two BHs from merging directly, leading to the formation of a binary. Typically, the binaries are sufficiently stable, i.e. are not disrupted by interaction with the surrounding environment, and a large fraction of them merge on a timescale on the order of the age of the Universe. If the PBHs have a mass spectrum  $\rho(m)$  and are randomly distributed spatially, and assuming that early formation of PBH clusters does not impact the lifetime of these primordial binaries (a criterion satisfied for  $f_{\text{PBH}} \lesssim 0.1$ ) (Raidal et al. 2019), then the present day merger rate is approximately given by (Kocsis et al. 2018; Raidal et al. 2019; Gow et al. 2020)

<sup>16</sup> Environmental effects such as the presence of accretion disks could speed up binary evolution, but are expected to be subdominant in the subsolar mass range.

$$\frac{dR_{\text{PBH}}}{d(\ln m_1) d(\ln m_2)} = 0.0038 \text{ kpc}^{-3} \text{ yr}^{-1} \times f_{\text{PBH}}^{\frac{53}{37}} \left( \frac{t}{t_0} \right)^{-\frac{34}{37}} \left( \frac{M}{10^{-12} \text{ M}_\odot} \right)^{-\frac{32}{37}} \quad (51)$$

$$\times \left[ \frac{m_1 m_2}{(m_1 + m_2)^2} \right]^{-\frac{34}{37}} S(M, f_{\text{PBH}}, \psi) \rho(m_1) \rho(m_2),$$

where  $f_{\text{PBH}}$  is the integrated dark matter fraction made of primordial BHs,  $m_1$  and  $m_2$  are the masses of the two constituent BHs of the binary, and  $\rho(m)$  is the PBH mass function normalized to one ( $\int \rho(m) d \ln m = 1$ ). Here  $t$  stands for the universe age at the time of merger, and can be approximated with  $t_0$  at sufficiently low redshift. The suppression factor  $S(M, f_{\text{PBH}}, \psi)$  in Eq. (51) corrects the merger rate by introducing the effect of binary interactions with the surrounding environment in both the early- and late-time Universe (see Hütsi et al. 2021 for its analytical parametrization), informed by the numerical simulations performed in Raidal et al. (2019).

2. *Capture in primordial BH halos* The second PBH binary formation channel is through dynamical capture in dense primordial halos. As with any other dark matter candidate, PBHs are expected to form halos during cosmic history. Even more so if they compose a large fraction of dark matter, as structure formation at small scales is boosted by the initial Poisson perturbations in the PBH distribution (Inman and Ali-Haïmoud 2019; De Luca et al. 2020a). For a generic PBH mass function  $\rho(m)$ , an effective formula for the merger rate of binaries formed in the late-time universe is (Clesse and Garcia-Bellido 2022; Carr et al. 2021a)

$$\frac{dR_{\text{PBH}}}{d(\ln m_1) d(\ln m_2)} \approx R_{\text{clust}} f_{\text{PBH}}^2 \rho(m_1) \rho(m_2) \frac{(m_1 + m_2)^{10/7}}{(m_1 m_2)^{5/7}} \text{ yr}^{-1} \text{ Gpc}^{-3}, \quad (52)$$

where  $R_{\text{clust}}$  is a scale factor that depends on the PBH clustering properties, the small-scale halo mass function, and the velocity distribution. This formula assumes that the time it takes for the binary to merge is much shorter than the age of the Universe, as is the case for hard binaries formed through this mechanism (Raidal et al. 2025). For stellar mass PBHs, one finds  $R_{\text{clust}} \sim 10^{2 \pm 3}$  (Clesse and Garcia-Bellido 2022; De Luca et al. 2020a), with weak scaling with the typical PBH mass,  $R_{\text{PBH}}^{\text{cap}} \sim m_{\text{PBH}}^{-11/21}$  (Franciolini et al. 2022a).

As a formation channel for PBH binaries, capture in dense halos is typically subdominant compared to primordial binary formation, at least if one assumes a relatively narrow PBH mass distribution. Let us mention, however, that whether this conclusion remains valid in the case of a very wide PBH mass function (spanning multiple decades in mass) is still subject to uncertainties, related especially to the amount of binaries disrupted by interactions with light PBHs. For definiteness, in the following, we will restrict our analysis to narrow PBH mass functions and therefor retain only the contribution from early binaries.

When considering the merger rate of PBH within  $\mathcal{O}(100 \text{ kpc})$  from Earth, the effect of the local dark matter overdensity needs to be taken into account (see e.g.

Pujolas et al. 2021). We model the Milky Way's dark matter halo as a Navarro–Frenk–White density profile (Navarro et al. 1996, 1997),  $\rho_{\text{DM}}(r) = \rho_0 r_0 / [r(1 + r/r_0)^2]$ , with  $\rho_{\text{DM}}(r = r_\odot) = 7.9 \times 10^{-3} \text{ M}_\odot/\text{pc}^3$  (Cautun et al. 2020) at the location of the solar system,  $r_\odot \simeq 8.0 \text{ kpc}$ , and with  $r_0 = 15.6 \text{ kpc}$ . The average overdensity within a shell at a distance  $r$  from the observer location  $r_\odot$  can then be approximated by

$$\rho(r) = \begin{cases} \rho_{\text{DM}}(r_\odot) & r < r_\odot, \\ \rho_{\text{DM}}(r) & r \gtrsim r_\odot. \end{cases} \quad (53)$$

As we expect the distribution of PBH binaries to roughly follow the dark matter overdensities, the local merger rate is enhanced by an overall factor

$$R_{\text{PBH}}^{\text{local}}(r) = \delta(r) R_{\text{PBH}}, \quad (54)$$

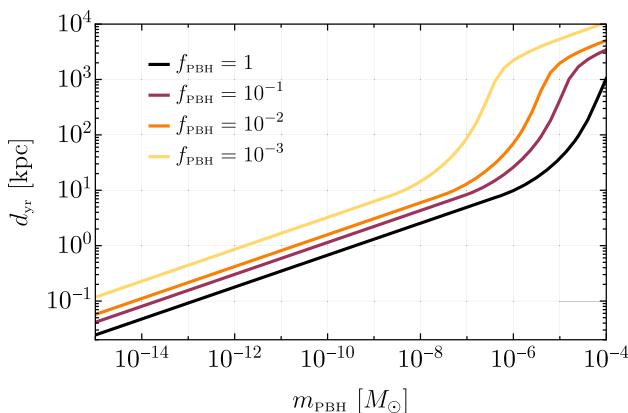
where we defined the overdensity factor  $\delta(r) \equiv \rho_{\text{DM}}(r)/\bar{\rho}_{\text{DM}}$ , with  $\bar{\rho}_{\text{DM}}$  the average cosmological dark matter density. The correction is of order  $\delta(r) \in (1 \div 2 \times 10^5)$ .

Accounting for this local enhancement, one can define the volume  $V_{\text{yr}}$ , corresponding to a distance  $d_{\text{yr}} \equiv (3V_{\text{yr}}/4\pi)^{1/3}$  enclosing the region where on average at least one merger per year takes place (Domcke et al. 2022; Franciolini et al. 2022b). The number of events per year  $N_{\text{yr}}$  within the volume  $V_{\text{yr}}$  is defined as

$$N_{\text{yr}} \equiv \Delta t \int_0^{d_{\text{yr}}} dr 4\pi r^2 R_{\text{PBH}}^{\text{local}}(r), \quad (55)$$

where we set  $\Delta t = 1 \text{ yr}$ .

In Fig. 7, we show the distance  $d_{\text{yr}}$  as a function of the PBH mass and abundance for  $N_{\text{yr}} = 1$ , assuming equal mass binaries. Due to the galactic DM overdensity,  $d_{\text{yr}}$  is smaller than it would be based on the average cosmological density at small  $m_{\text{PBH}}$ .



**Fig. 7** Distance from Earth within which on average one PBH merger event is expected per year. The change in slope around  $10^{-5} \text{ M}_\odot$  is due to the local dark matter overdensity in the Milky Way, which is relevant at distances  $r \lesssim r_\odot$ , relevant for light PBHs, but less important at larger distances. Figure adapted from Franciolini et al. (2022b)

A further convenient way of parameterizing the sensitivity of detectors to inspiralling PBHs is the distance reach,  $d$ , for a fixed SNR, defined for generic transient sources in Eq. (30). For PBH mergers it is given by (Maggiore 2007)

$$d = \left(\frac{5}{24}\right)^{1/2} \frac{1}{\pi^{2/3}} (GM_c)^{5/6} \Delta t^{-(k-1)/4} \left[ \frac{2}{\text{SNR}} \int_{f_{\min}}^{f_{\max}} df \left( \frac{f^{-7/3}}{S_h^{\text{noise}}(f)} \right)^k \right]^{1/2k}, \quad (56)$$

with  $k = 1, 2$  for linear or quadratic detectors, respectively, with  $S_h^{\text{noise}}(f)$  the detector's noise equivalent strain PSD and  $\Delta t$  the integration time interval.<sup>17</sup> Equation (56) is valid under the assumption of an optimally oriented source. The integration limits  $f_{\min}$  and  $f_{\max}$  depend on the detector's broadband sensitivity as well as the source properties. In practice, as we only integrate over the inspiral phase of the signal, we fix  $f_{\max}$  to be the smallest frequency between  $f_{\text{ISCO}}$  and the detector's maximum observable frequency. If  $f_{\text{ISCO}}$  is smaller than the minimum observable frequency, the binary never enters the detector's frequency band and the sensitivity is zero. We have already seen the distance reach for different detector designs in Fig. 3 above. To gain an understanding of the detection prospects for a specific detectors,  $d$  should be compared to  $d_{\text{yr}}$  defined above.

*Stochastic gravitational wave background from PBH binaries.* The superposition of the GW signals from many PBH binaries generates a stochastic GW background (SGWB). Its frequency spectrum is

$$\Omega_{\text{GW}}(f) = \frac{f}{\rho_c} \iint dm_1 dm_2 \int_0^{f_{\text{cut}}/f-1} \frac{dz}{(1+z)H(z)} \frac{d^2 R_{\text{PBH}}(z)}{dm_1 dm_2} \frac{dE_{\text{GW}}(f_s)}{df_s}, \quad (57)$$

with the redshifted source frequency  $f_s = f(1+z)$ , the critical density of the Universe today,  $\rho_c = 3H_0^2/8\pi G$  (where  $H_0$  is the Hubble constant), and the GW energy spectrum of a single binary,  $dE_{\text{GW}}(f_s)/df_s$ . As before,  $R_{\text{PBH}}$  accounts for the local overdensity. The upper boundary of the redshift integral is given by the maximum  $z$  from which GWs with redshifted frequency  $f$  can come if the maximum frequency of the source spectrum is  $f_{\text{cut}}$ .

The GW energy spectrum emitted by the binary is composed of inspiral, merger, and ringdown contributions. Assuming circular orbits, we adopt for the individual contributions the parameterization from Bavera et al. (2022),

$$\frac{dE_{\text{GW}}(f)}{df} = \frac{(G\pi)^{2/3} \mathcal{M}^{5/3}}{3} \begin{cases} f^{-1/3} v_1^2 & f < f_{\text{merger}}, \\ \omega_1 f^{2/3} v_2^2 & f_{\text{merger}} \leq f < f_{\text{ringdown}}, \\ \omega_2 v_3^2 & f_{\text{ringdown}} \leq f < f_{\text{cut}}. \end{cases} \quad (58)$$

The explicit expressions for the dimensionless coefficients  $v_{1,2,3}$  as well as for  $f_{\text{merger}}$ ,  $f_{\text{ringdown}}$ , and  $f_{\text{cut}}$  can be found in Bavera et al. (2022) [see also Ajith et al. (2011), Zhu et al. (2011)]. Parametrically, one expects  $v_i \sim \mathcal{O}(1)$ , while the other characteristic frequencies scale as  $\approx 1/(\pi MG)$ , where  $M = m_1 + m_2$ , with prefactors that depend on the binary mass ratio and individual spins. One can also translate the

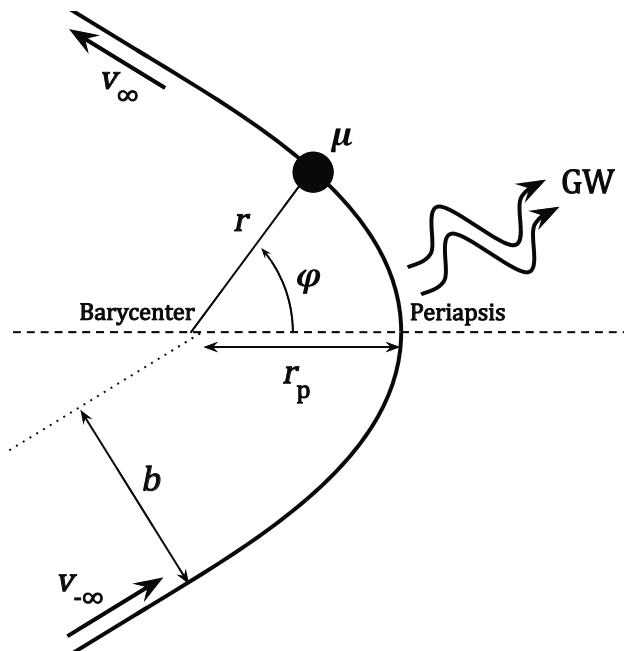
<sup>17</sup> For photon (re-)generation experiments, Eq. (56) should contain an extra Heaviside  $\theta$ -function ensuring that the number of signal photons to be larger than one. See Sect. 5.4 for more details.



energy spectrum  $\Omega_{\text{GW}}$  to a characteristic strain using Eq. (13). The contribution from inspiralling circular binaries, whose evolution is dominated by GW emission, leads to a low-frequency tail that scales as  $\Omega_{\text{GW}}(f) \sim f^{2/3}$  (Moore et al. 2015), or equivalently a characteristic strain scaling as  $h_c(f) \sim f^{-2/3}$ .

Unlike for individual transients, the stochastic signal from binary mergers is stationary, and the available observation time within a frequency band is only dictated by the detector properties, see related discussion in Sect. 2.2. As the SGWB is mostly emitted in the late-time universe, with most of the contribution to the integral in Eq. (57) coming from redshifts  $z \sim \mathcal{O}(10)$ , it is not subject to bounds coming from the number of effective relativistic degrees of freedom in the early universe. However, for realistic PBH populations with  $f_{\text{PBH}} \approx 1$ , the amplitude  $\Omega_{\text{GW}}$  still falls below that range (Franciolini et al. 2022b). The SNR for these signal can be computed in analogy to the SNR for relic GW backgrounds from the early Universe, adopting Eq. (26). Notice, however, that the stochastic signal from PBH mergers would be characterized by potentially much larger anisotropies than a primordial background due to the inevitable Poisson noise in the distribution of the PBH binaries dominating the GW emission.

*PBH encounters.* A fraction of PBH encounters will not lead to the formation of bound systems, which would then inspiral, but will rather produce single scattering events via a hyperbolic encounter. This could happen for instance if the relative velocity or relative distance of the two PBHs is large enough that capture is not possible. We will come back to the rate of such events in the following. The emission of GWs in close encounters of compact bodies has been extensively studied in the literature since the seminal works (Zel'dovich and Polnarev 1974; Turner 1977). It is worth noting that the memory effect, to be discussed below, was first discussed in this context (Braginsky and Thorne 1987). With the advent of interferometric GW detectors, the GW emission from such encounters has been revisited in Kocsis et al. (2006), O’Leary et al. (2009), Capozziello et al. (2008), De Vittori et al. (2012), García-Bellido and Nesseris (2018), Garcia-Bellido and Nesseris (2017), Gröbner et al. (2020), Mukherjee et al. (2021), Morrás et al. (2022), Bini et al. (2024), Kerachian et al. (2024), Codazzo et al. (2024), Dandapat et al. (2023), Teuscher et al. (2024). The waveform and characteristic parameters of the GW emission in such encounters are different from those of the inspiralling binaries, and both provide complementary information that can be used to discover, as well as determine, the mass distribution of PBHs as a function of redshift and their spatial distribution in the clustered scenarios. Hyperbolic encounters generate bursts of GWs, where the majority of the energy is released near the point of closest approach. This leads to a characteristic “tear-drop” shape of the emission in the time-frequency domain. In the Newtonian limit, the frequency of the emitted GWs peaks at periaapsis, and the peak frequency is a function of only three variables: the impact parameter  $b$ , the eccentricity  $e$  and the total mass of the system. The duration of such events is on the order of a few milliseconds to several hours, depending on those parameters (Fig. 8).



**Fig. 8** The scattering of two black holes induces the emission of gravitational waves whose emitted power is maximal at the point of closest approach

More precisely, the peak frequency at periapsis given by Teuscher et al. (2024)

$$f_p = \frac{1}{2\pi} \sqrt{\frac{GM(e+1)}{r_p^3}} \simeq 1.6 \text{ GHz} \times \left( \frac{10^{-5} M_\odot}{M} \right) \left( \frac{R_S}{r_p} \right)^{\frac{2}{3}} \sqrt{\frac{e+1}{2}}, \quad (59)$$

where  $r_p$  is the periapsis radius (or the distance to the hyperbola's focus point at closest approach) and  $R_S = 2GM/c^2$  is the Schwarzschild radius of the system with total mass  $M = m_1 + m_2$ . Note that  $f_p$  depends only on  $M$ , on the ratio  $R_S/r_p$ , and on the eccentricity of the hyperbolic orbit  $e = \sqrt{1 + b^2 v_0^4 / G^2 M^2}$ , where  $v_0$  is the asymptotic relative velocity of the encounter, and  $\beta \equiv v_0/c$ . Introducing  $G(e) \equiv e + 2/(e+1)^{1/3}$  and  $q = m_1/m_2$ , the maximum strain and power of the GW burst at periapsis are respectively given by

$$h_p = 3.6 \times 10^{-25} \times \frac{4q}{(1+q)^2} \frac{G(e)}{G(1)} \left( \frac{M}{10^{-5} M_\odot} \right)^{\frac{5}{3}} \left( \frac{f_p}{1.6 \text{ GHz}} \right)^{\frac{2}{3}} \left( \frac{1 \text{ Mpc}}{D} \right), \quad (60)$$

$$P_p = 3.7 \times 10^{24} L_\odot \times \frac{1}{(e+1)^{\frac{2}{3}}} \left( \frac{4q}{(1+q)^2} \right)^2 \left( \frac{M}{10^{-5} M_\odot} \right)^{\frac{10}{3}} \left( \frac{f_p}{1.6 \text{ GHz}} \right)^{\frac{10}{3}},$$

where  $L_\odot$  is the solar luminosity and  $D$  is the distance of the event from Earth. The signal duration in a detector operating at frequency  $f$  and having a frequency

bandwidth  $\Delta f$  can be computed from the conservation of angular momentum and reads

$$t_{\Delta f}(f, \Delta f, e) = \frac{1}{\pi f} \sqrt{1 + \frac{1}{e}} \sqrt{\frac{\Delta f}{f}}. \quad (61)$$

This estimate shows that the duration of the GW signal from PBH encounters is close to the inverse of the peak GW frequency. This is similar to what happens for PBH mergers close to the ISCO frequency. However, for hyperbolic encounters, the inspiral phase associated with GWs with smaller frequencies and slower frequency evolution is absent.

The rate of close encounters remains rather uncertain. We report an estimate based on the cross-section of a close hyperbolic encounter event, which is given by  $\sigma = \pi b^2 = \pi(GM/v_0^2)^2(e^2 - 1)$ . This leads to (García-Bellido and Nesseris 2018; Garcia-Bellido and Nesseris 2017; García-Bellido et al. 2022)

$$\frac{dR_{\text{PBH}}^{\text{enc}}}{d(\ln m_1) d(\ln m_2)} \approx \frac{1.4 \times 10^{-8}}{\text{yr Gpc}^3} \rho(m_1) \rho(m_2) \left( \frac{\delta_{\text{loc}}}{10^8} \right) \frac{M^2}{m_1 m_2} \frac{e^2 - 1}{(v_0/c)^3}. \quad (62)$$

In this estimate,  $\delta_{\text{loc}}$  characterizes the PBH overdensity compared to the mean DM density today. Notice  $\delta_{\text{loc}}$  is at least as large as the one introduced in Eq. (54), accounting for the local DM concentration at around the solar system in the galaxy, but can also reach larger values due to the small-scale structure induced in light PBH DM scenarios [see e.g. Inman and Ali-Haïmoud (2019)], potentially boosting the encounter rates. This latter effect does not impact the rate of mergers (51) as it is dominated by binaries formed at high redshift. Also, in Eq. (62), we introduced  $v_0$  as the virial velocity of PBHs in a cluster. Given the scaling  $\sim v^{-3}$ , the rate of mergers is dominated by light clusters for which  $v_0$  is small. While a complete determination of the rate would require averaging (62) over encounter parameters such as eccentricity and PBH cluster properties, one expects this rate to be subdominant compared to the one of mergers (51).

*Stochastic gravitational wave background from PBH encounters.* Overlapping GW signals from close PBH encounters can also form a stochastic GW background, in analogy to the SGWB from PBH mergers discussed above. The energy density of this background can be estimated in analogy to the PBH merger case, Eq. (57), accounting for the different event rate and GW energy spectrum for hyperbolic encounters compared to mergers. For hyperbolic encounters, the energy emitted per logarithmic frequency bin is given by [see e.g. García-Bellido et al. (2022)]

$$\frac{dE_{\text{GW}}}{d \ln f} = \frac{4\pi}{45} \frac{G^{7/2} m_1^2 m_2^2 (m_1 + m_2)^{1/2}}{a^{7/2}} v^5 F_e(v), \quad (63)$$

where  $a = GM/v_0^2$  is the semi-major axis and  $v_0$  is the initial relative velocity. We have moreover defined  $v^2 \equiv 4\pi^2 f^2 a^3 / GM$ . The function  $F_e(v)$  describes the dependence on eccentricity  $e$  and is given by

$$F_e(v) \simeq \frac{12(1 - y^2 - 3vy^3 + 4y^4 + 9vy^5 + 6v^2y^6)}{\pi v^3 y(1 + y^2)^2} e^{-2v\xi(y)}, \quad (64)$$

with  $\xi(y) = y - \arctan y$  and  $y = \sqrt{e^2 - 1}$ . The amplitude of the SGWB background induced by hyperbolic PBH encounters is typically smaller than the one from PBH binaries from the same population, but can lead to additional features due to the different frequency dependence (García-Bellido et al. 2022). In particular, the low frequency tail of the SGWB from close encounters can fall as  $f^2$  instead of the  $f^{2/3}$  scaling of the background due to binary mergers. Note that parabolic encounters,  $e \rightarrow 1$ , yield the highest emission rate within the Newtonian approximation, while the cross section in the same limit approaches zero [see Eq. (62)]. This suggests that relativistic effects may play an significant role, particularly dynamical capture must be accounted for.<sup>18</sup>

A final assessment of the magnitude of the SGBW signal from PBH encounters requires a careful population study accounting not only for the PBH number density (and hence  $\delta_{\text{loc}}$ ) but also the distribution of eccentricity  $e$  across the binaries, in addition to the inclusion of relativistic effects. However, given the result for the merger rate (62), the result will likely be subdominant compared to the SGWB signal from PBH mergers of the same population.

#### 4.1.3 Memory effects

The gravitational memory effect occurs when the metric perturbation long after the passage of a GW is different from the metric long before the passage for at least one of the GW polarizations (Braginsky and Grishchuk 1985; Zel'dovich and Polnarev 1974; Braginsky and Thorne 1987). In other words, the effect is characterized by the quantity

$$\delta h_{+, \times}^{\text{mem}} = \lim_{t \rightarrow +\infty} h_{+, \times}(t) - \lim_{t \rightarrow -\infty} h_{+, \times}(t), \quad (65)$$

being non-zero. Here,  $t$  is the observer's coordinate time. The gravitational memory effect thus induces a permanent displacement of free-falling test masses.

While two types of memory exists, related to linear and non-linear effects, we will focus here on the non-linear memory induced by a BH merger (Christodoulou 1991; Wiseman and Will 1991; Blanchet and Damour 1992; Favata 2009a, b; Pollney and Reisswig 2011; Lasky et al. 2016; Hübner et al. 2020; Ebersold and Tiwari 2020; Zhao et al. 2021; Gasparotto et al. 2023). A linear signal can originate or instance from close hyperbolic PBH encounters (Favata 2010; Caldarola et al. 2024), with similar phenomenology.

<sup>18</sup> Dynamical capture systems are those that, under Newtonian gravity, would scatter along hyperbolic trajectories but instead merge due to radiation reaction effects in general relativity. The focus on these systems is motivated by their substantial observational interest, at least at low frequencies (Gamba et al. 2023). For classical work on this topic, see East et al. (2013), Gold and Brügmann (2013).

If we define  $h_0$  as the primary GW strain, the memory strain  $\delta h$  is computed as [see e.g. Ebersold and Tiwari (2020)]

$$\begin{aligned} \delta h^{\ell m} = & -D \sum_{\ell', \ell'' \geq 2} \sum_{m', m''} \sqrt{\frac{(\ell-2)!}{(\ell+2)!}} \int d\Omega Y^{\ell m*}(\Omega) Y_{-2}^{\ell' m'}(\Omega) Y_{-2}^{\ell'' m''*}(\Omega) \\ & \times \int_{-\infty}^t dt' \dot{h}_0^{\ell' m'}(t') \dot{h}_0^{\ell'' m''*}(t'), \end{aligned} \quad (66)$$

with  $D$  being the distance to the source, a dot indicates a derivative with respect to time, and we have introduced the spin-weighted spherical harmonics decomposition

$$h_+ - ih_\times \equiv \sum_{\ell \geq 2} \sum_{|m| \leq \ell} h^{\ell m} Y_{-2}^{\ell m}. \quad (67)$$

The functions  $Y_{-2}^{\ell m}$  are the spin-weighted spherical harmonics, defined for instance in Boetzel et al. (2019).

Phenomenologically, the strain of non-linear memory behaves approximately as

$$h(f) \simeq \frac{\delta h^{\text{mem}}}{2\pi f} \Theta(f_{\text{cut}} - f). \quad (68)$$

where the UV cut-off is approximately placed close to the ISCO frequency at  $f_{\text{cut}} \sim 1/(60M)$  [see e.g. Gasparotto et al. (2023)]. This description neglects features induced by the non-linear dynamics close to the merger, but captures the main properties of the signal at low frequencies. The typical value of the memory strain amplitude at  $f_{\text{ISCO}}$ , averaged over source orientations and sky positions, can be related to the amplitude of the GW signal at its peak frequency by the factor  $\kappa = \sqrt{\langle h_{\text{mem}}^2 \rangle / \langle h_{\text{osc}}^2 \rangle} \simeq 1/20$  (McNeill et al. 2017), where  $h_{\text{osc}}$  is the amplitude of the oscillating primary GW signal. The GW memory strain then turns out to be

$$h(f) \sim 1.2 \times 10^{-24} \text{ sec} \left( \frac{f_{\text{ISCO}}}{f} \right) \left( \frac{M}{10^{-5} M_\odot} \right) \left( \frac{D}{\text{kpc}} \right)^{-1}, \quad (69)$$

where we assumed, for simplicity, an equal mass PBH binary with total mass  $M$ .

The peculiar feature of the GW memory is that it extends to frequencies that are much smaller than  $f_{\text{ISCO}}$ . This implies that low-frequency interferometers could detect memory signals from UHF-GW sources (McNeill et al. 2017; Lasky and Thrane 2021). However, the memory effect of PBH of mergers with masses  $m \lesssim 10^{-4} M_\odot$  at a distance  $d_{\text{yr}}$  [as defined in Eq. (55)] would fall much below the forecasted sensitivity curves of both LISA and third generation ground-based detectors, motivating searches based on UHF-GW observatories (Franciolini et al. 2022b). It is also worth noticing that for binary PBHs, the early inspiral phase is associated with larger strain signals in the sub-kHz range, scaling as  $h_c \sim f^{-7/6}$  down to a very small minimum frequency. Therefore, if the available observation time at the GW observatory is sufficient to map out this signal over long time periods, the low-frequency strain from the inspiral phase may be easier to detect than the one induced by non-linear memory. This conclusion, however, depends on

the distribution of binary parameters in a population of PBH inspiralling sources, and deserves further investigation.

We conclude this section by mentioning that, although the memory strain could eventually cross some of the sensitivity bands of UHF-GW detectors, the memory signal is very different from other HFGW signals (such as plane monochromatic GWs or a stationary stochastic GW background). Therefore, dedicated studies on the sensitivity to GW memory are required.

#### 4.1.4 Exotic compact objects

Beyond the well-known compact astrophysical objects, namely black holes and neutron stars, there are several candidates for stable (or long-lived) exotic compact objects, composed of particles beyond the Standard Model (Giudice et al. 2016; Cardoso and Pani 2019). For instance, they can be composed of exotic fermions such as gravitinos in supergravity theories, giving rise to gravitino stars (Narain et al. 2006), or of dark quarks (Witten 1984; Hong et al. 2020; Gross et al. 2021). They can also be composed of bosons, such as moduli in string compactifications and supersymmetric theories (Krippendorff et al. 2018). Depending on the mechanism that stabilizes bosonic compact objects, they have specific names such as Q-balls, boson stars, oscillatons, and oscillons. Additional proposals include fermion–boson stars (Lee and Pang 1987; Del Grosso et al. 2023; Diedrichs et al. 2023) and anisotropic stars (Raposo et al. 2019), as well as gravastars (Mazur and Mottola 2004).

The masses and radii of the compact objects depend on their constituents, and in particular on their internal pressure that is needed to counterbalance gravity. In regular astrophysical stars, this pressure is thermal, while in stars composed of fermions it is the Fermi degeneracy pressure. For bosons, in contrast, the star is stabilized by the quantum property dictating that particles cannot be localized to scales below their Compton wavelength. Stable configurations that do not collapse can be found below a maximum mass  $M_{\max}$ . For example, for stars composed of bosons with negligible self-interactions one finds (Kaup 1968)

$$M_{\max} = 0.633 \frac{M_{\text{Pl}}^2}{m_B} \approx M_{\odot} \left( \frac{10^{-10} \text{ eV}}{m_B} \right), \quad (70)$$

where  $m_B$  is the boson mass. This means that UHF-GW experiments searching for mergers of subsolar mass objects could detect signals from compact objects composed of ultralight boson particles heavier than around  $10^{-10}$  eV. In the presence of a quartic interactions  $\lambda \phi^4$ , this scaling relation is modified to (Colpi et al. 1986)

$$M_{\max} = 0.06 \sqrt{\lambda} \frac{M_{\text{Pl}}^3}{m_B^2} \approx 10 M_{\odot} \sqrt{\lambda} \left( \frac{100 \text{ MeV}}{m_B} \right)^2, \quad (71)$$

where  $M_{\text{Pl}}$  is the Planck mass. A similar relation can be found for other models (see Cardoso and Pani 2019 for a review), and high-frequency GW detection would generically allow access to new regions of parameter space.

Gravitational wave emission from exotic compact objects will be indistinguishable from the signal of conventional black hole or neutron star mergers during the early inspiral phase, where frequency evolution is slow and allows for long observation time within the experimental frequency band. Close to the merger, on the other hand, the exotic objects' potentially much larger size and tidal deformability comes into play and may lead to significant differences. Therefore, to distinguish different types of compact objects, it will be crucial to observe the final stages of the binary evolution.

The ISCO frequency for a binary system of two exotic compact objects with mass  $M$  and radius  $R$  is given by (Giudice et al. 2016)

$$f_{\text{ISCO}} = \frac{1}{6\sqrt{3}\pi} \frac{C^{3/2}}{GM} \simeq 1 \text{ MHz} \times C^{3/2} \left( \frac{6 \times 10^{-3} M_{\odot}}{M} \right), \quad (72)$$

where  $C = GM/R$  is the compactness of the exotic compact object. This expression is only slightly modified for a boson star binary with two different values of the masses. Note that for a BH the radius is given by the Schwarzschild radius  $R_S = 2GM$ , therefore  $C = 1/2$  is the maximum attainable value for the compactness. The GW strain for an equal-mass binary of exotic objects during the inspiral phase can be calculated as in Sect. 4.1.2, see in particular Eq. (47).

The exact waveform produced by the merger of two exotic compact objects is in general different from the one of black holes or neutron stars. It depends on microphysics details, in particular through tidal deformability effects (Giudice et al. 2016; Palenzuela et al. 2017).<sup>19</sup> Hence, the detection of GWs close to the ISCO frequency from an exotic compact object merger can give valuable information on physics beyond the Standard Model. Additional information on the nature of the exotic objects could be obtained by using mergers to infer their mass function. It is important to keep in mind, though, that cosmological formation scenarios and the expected merger rate of exotic compact objects remain uncertain (see e.g. Frieman et al. 1989; Bai et al. 2022; Croon et al. 2023; Gorghetto et al. 2022; Banks et al. 2023 for some estimates in this direction).

#### 4.1.5 Black hole superradiance

Boson clouds created by gravitational superradiance of BHs are a powerful GW source (Ternov et al. 1978; Zouros and Eardley 1979; Arvanitaki et al. 2010; Arvanitaki and Dubovsky 2011; Arvanitaki and Geraci 2013; Aggarwal et al. 2020; Detweiler 1980; Yoshino and Kodama 2014; Arvanitaki et al. 2015; Brito et al. 2015a, b; Sprague et al. 2024). Superradiance is an enhanced radiation process that is associated with bosonic fields around rotating objects with dissipation. The event horizon of a spinning BH is one such example that provides conditions particularly suitable for this phenomenon to occur (Arvanitaki et al. 2015).

<sup>19</sup> See however Helfer et al. (2019) for more details on the initial conditions.

For a bosonic field of mass  $\mu$  in the vicinity of a rotating BH, there exists a set of quasibound states whose oscillation frequency  $\omega_R \sim \mu$  satisfies the superradiance condition  $\omega_R < m\Omega_H$ , where  $m$  is the azimuthal quantum number (with respect to the BHs rotation axis) and  $\Omega_H$  the angular velocity of an observer at the horizon, as measured by a static observer at infinity. If the superradiance condition is saturated, the boson occupation number grows rapidly over a timescale  $1/\Gamma = 1/(2\omega_I)$ , where  $\omega_I$  is the imaginary part of the boson's oscillation frequency. (Due to the special boundary conditions in the space-time around a black hole, the solution to the Klein–Gordon equation acquires an imaginary part.) Superradiance is strongest when the Compton wavelength of the bosonic field is on the order of the BH radius,  $Gm_{\text{PBH}}\mu \equiv \alpha \sim \mathcal{O}(1)$ , with  $m_{\text{PBH}}$  being the BH mass.

The BH and its superradiant boson cloud form a gravitationally bound ‘atom’, with different atomic ‘levels’ occupied by exponentially large numbers of particles. As the bosonic cloud is non-spherical, it emits nearly monochromatic gravitational waves at a frequency (Brito et al. 2015b)

$$f_{\text{GW}} \sim \omega_R/\pi \sim 5 \text{ MHz} \left( \frac{\mu}{10^{-8} \text{ eV}} \right) \sim 5 \text{ GHz} \left( \frac{10^{-5} \text{ M}_\odot}{m_{\text{PBH}}} \right) \left( \frac{Gm_{\text{PBH}}\mu}{0.1} \right). \quad (73)$$

In the last step we have fixed  $Gm_{\text{PBH}}\mu$  to the typical value required by the resonant condition. In a particle physics context, GW emission from superradiant boson clouds can be interpreted as originating from annihilations (or decays) of the boson field into gravitons.

The peak gravitational strain from a source at luminosity distance  $D$  is approximately (Brito et al. 2015b)<sup>20</sup>

$$h_S \approx 5 \times 10^{-30} \left( \frac{m_{\text{PBH}}}{10^{-5} \text{ M}_\odot} \right) \left( \frac{Gm_{\text{PBH}}\mu_S}{0.1} \right)^7 \left( \frac{\chi_i - \chi_f}{0.5} \right) \left( \frac{\text{kpc}}{D} \right), \quad (74)$$

$$h_{V,T} \approx 10^{-26} \left( \frac{m_{\text{PBH}}}{10^{-5} \text{ M}_\odot} \right) \left( \frac{Gm_{\text{PBH}}\mu_{V,T}}{0.1} \right)^5 \left( \frac{\chi_i - \chi_f}{0.5} \right) \left( \frac{\text{kpc}}{D} \right), \quad (75)$$

where the subscripts  $S, V, T$  refer to scalar, vector and tensor depending on the spin of the boson field. The parameters  $\chi_i$  and  $\chi_f$  stand for the dimensionless BH spin evaluated at the beginning and end of the superradiant growth.

The duration of the gravitational wave signal can be estimated by the time it takes to radiate away half of the cloud's rest energy. The approximate result is (Brito et al. 2015b)

<sup>20</sup> These expressions are obtained in the  $Gm_{\text{PBH}}\mu \ll 1$  limit, but they still provide good estimations when  $Gm_{\text{PBH}}\mu \gtrsim 0.1$ . A detailed analysis has been performed in Isi et al. (2019) for scalar bosons.



$$\tau_S \approx 0.13 \text{ yrs} \left( \frac{m_{\text{PBH}}}{10^{-5} \text{ M}_\odot} \right) \left( \frac{0.1}{Gm_{\text{PBH}}\mu_S} \right)^{15} \left( \frac{0.5}{\chi_i - \chi_f} \right), \quad (76)$$

$$\tau_{V,T} \approx 0.17 \text{ sec} \left( \frac{m_{\text{PBH}}}{10^{-5} \text{ M}_\odot} \right) \left( \frac{0.1}{Gm_{\text{PBH}}\mu_{V,T}} \right)^{11} \left( \frac{0.5}{\chi_i - \chi_f} \right). \quad (77)$$

These estimates, in particular Eq. (76), show that, unlike other astrophysical or cosmological sources discussed in this document, scalar boson clouds around rotating black holes can be considered continuous sources, similar to verification binaries for LISA or pulsars for interferometers in the LIGO / Virgo / KAGRA range.

As mentioned above, GW emission due to superradiance is expected to be almost-monochromatic and coherent. However, given the potentially long signal durations, one may expect very small frequency drifts which should be taken into account in the search strategy. For the case of a scalar cloud with a small self-interaction, Baryakhtar et al. (2021) finds a frequency drift

$$\frac{\dot{f}}{f^2} \simeq 3 \times 10^{-20} \left( \frac{\alpha}{0.1} \right)^{17}. \quad (78)$$

If nonlinear effects, for instance due to boson self-interactions, become important, the GW signature changes. In this case, periodic collapses of the boson cloud are expected, similarly to Bose-Einstein condensate bosonovae. In these explosive events, part of the boson cloud escapes to infinity, accompanied by a gravitational wave burst. Focusing on the QCD axion, the primary frequency component of a bosonova GW burst is (Arvanitaki et al. 2015)

$$f_{\text{bn}} \approx 30 \text{ MHz} \left( \frac{16}{c_{\text{bn}}} \right) \left( \frac{m_{\text{PBH}}}{10^{-5} \text{ M}_\odot} \right)^{-1} \left( \frac{Gm_{\text{PBH}}\mu_a/\ell}{0.4} \right)^2, \quad (79)$$

where  $\ell$  is the orbital quantum number and  $c_{\text{bn}}$  parametrizes the collapse timescale. (The infall time is  $t_{\text{bn}} = c_{\text{bn}} r_{\text{cloud}}$ , where  $r_{\text{cloud}}$  the typical distance between the boson cloud and the black hole (Arvanitaki et al. 2015).) For quadrupole radiation, the strain can be estimated as (Arvanitaki et al. 2015)

$$h(f) \approx 10^{-27} \text{ sec} \left( \frac{\sqrt{\epsilon}/c_{\text{bn}}}{10^{-2}} \right)^2 \left( \frac{Gm_{\text{PBH}}\mu/\ell}{0.4} \right) \left( \frac{m_{\text{PBH}}}{10^{-5} \text{ M}_\odot} \right) \left( \frac{f}{f_a^{\text{max}}} \right)^2 \left( \frac{\text{kpc}}{D} \right), \quad (80)$$

with  $\epsilon \sim 5\%$  being the fraction of the cloud that plunges into the black hole, and  $f_a^{\text{max}}$  the largest value of the QCD axion decay constant for which bosonovae take place.

## 4.2 Early universe

We now turn to sources emitting GWs at cosmological distances, i.e., in the early Universe. For a summary of these sources see Fig. 4 and Table 2 in Sect. 4.4. They

are associated to events in our cosmological history which are triggered, for instance, by the decreasing temperature  $T$  of the thermal bath and typically occur everywhere in the Universe at (approximately) the same time. This results in a stochastic background of GWs which is a superposition of GWs with different wave vectors.

The total energy density of such a GW background,

$$\rho_{\text{GW}} = \int d \log k \frac{d\rho_{\text{GW}}}{d \log k}, \quad (81)$$

with characteristic wavelengths well inside the horizon, decays with the expansion of the Universe as  $\rho_{\text{GW}} \propto a^{-4}$ , as expected for relativistic degrees of freedom. This implies that a GW background acts as an additional radiation field contributing to the background expansion rate of the Universe. Observables that can probe the background evolution of the Universe can therefore be used to constrain  $\rho_{\text{GW}}$ . In particular, two events in cosmic history yield precise measurements of the expansion rate of the Universe: Big Bang Nucleosynthesis (BBN) at temperatures  $T_{\text{BBN}} \sim 0.1 \text{ MeV}$  and the decoupling of the cosmic microwave background (CMB) at recombination ( $T_{\text{CMB}} \sim 0.3 \text{ eV}$ ). An upper bound on the total energy density of a GW background present at the time of BBN or recombination can therefore be derived from the constraint on the amount of radiation tolerable at these cosmic epochs. Obviously, such bounds apply only to GW backgrounds that are present before the epoch considered (BBN or recombination).

Constraints on the presence of ‘extra’ radiation are usually expressed in terms of an effective number of neutrino species,  $N_{\text{eff}}$ , after electron–positron annihilation and neutrino decoupling. The total number of Standard Model relativistic degrees of freedom after  $e^+e^-$  annihilation is  $g_*(T < T_{e^+e^-}) = 2 + \frac{7}{4} N_{\text{eff}} \left(\frac{4}{11}\right)^{4/3}$ , with  $N_{\text{eff}} = 3.043$  (Cielo et al. 2023). As the energy density for thermalized relativistic degrees of freedom in the Universe is given by  $\rho_{\text{rad}} = \frac{\pi^2}{30} g_*(T) T^4$ , an extra amount of radiation,  $\Delta\rho_{\text{rad}}$ , can be parametrized by  $\Delta N_{\text{eff}}$  extra neutrino species using

$$\Delta\rho_{\text{rad}} = \frac{\pi^2}{30} \frac{7}{4} \left(\frac{4}{11}\right)^{4/3} \Delta N_{\text{eff}} T^4. \quad (82)$$

This is independent of whether the extra radiation is in a thermal state or not, as  $N_{\text{eff}}$  is only a parametrization of the total energy density of the extra component, independent of its spectrum. Since the energy density in GWs must satisfy  $\rho_{\text{GW}}(T) \leq \Delta\rho_{\text{rad}}(T)$ , we obtain the limit

$$\left. \frac{\rho_{\text{GW}}}{\rho_\gamma} \right|_{T \leq \text{MeV}} \leq \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} \Delta N_{\text{eff}}^{\text{max}}, \quad (83)$$

with  $\rho_\gamma$  denoting the energy density in photons and  $\Delta N_{\text{eff}}^{\text{max}}$  the constraint on  $\Delta N_{\text{eff}}$  from either BBN or the CMB. Writing the fraction of GW energy density today as<sup>21</sup>

$$\left. \frac{\rho_{\text{GW}} h^2}{\rho_c} \right|_0 = \Omega_{\text{rad},0} h^2 \left( \frac{g_S(T_0)}{g_S(T)} \right)^{4/3} \frac{\rho_{\text{GW}}(T)}{\rho_\gamma(T)}, \quad (84)$$

we obtain a constraint on the redshifted GW energy density today, in terms of the number of extra neutrino species at BBN or at recombination (Caprini and Figueroa 2018)

$$\left. \frac{\rho_{\text{GW}} h^2}{\rho_c} \right|_0 \leq \Omega_{\text{rad},0} h^2 \times \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} \Delta N_{\text{eff}}^{\text{max}} = 5.6 \times 10^{-6} \Delta N_{\text{eff}}^{\text{max}}, \quad (85)$$

where we have inserted  $\Omega_{\text{rad},0} h^2 = (\rho_\gamma/\rho_c)_0 h^2 = 2.47 \times 10^{-5}$ . We recall that this bound applies only to the total GW energy density, integrated over wavelengths well inside the Hubble radius (for super-horizon wavelengths, tensor modes do not propagate as a wave, and hence they do not affect the expansion rate of the Universe). Except for GW spectra with a very narrow peak of width  $\Delta f \ll f$ , the bound can be interpreted as a bound on the amplitude of a GW spectrum as defined in Eq. (6),  $\Omega_{\text{GW},0}(f) h^2 \lesssim 5.6 \times 10^{-6} \Delta N_{\text{eff}}$ , over a wide frequency range.

Current limits on  $\Delta N_{\text{eff}}$  from BBN and from the CMB are similar. In particular, (Cyburt et al. 2016) find  $\Delta N_{\text{eff}} < 0.2$  at 95% confidence level from BBN, while (Smith et al. 2006; Sendra and Smith 2012; Pagano et al. 2016; Clarke et al. 2020) find similar bounds based on the Hubble rate at CMB decoupling. A recent combined analysis of CMB and BBN constraints (Yeh et al. 2022) gives  $\Delta N_{\text{eff}} < 0.18$  (95% confidence level), which, when plugged into Eq. (85) lead to

$$\Omega_{\text{GW},0} h^2 < 1.1 \times 10^{-6}. \quad (86)$$

This constraint applies to stochastic GW backgrounds produced before BBN, with wavelengths inside the Hubble radius at the onset of BBN, corresponding to present-day frequencies  $f \geq 1.5 \times 10^{-12}$  Hz. Even lower-frequency backgrounds, down to  $f \gtrsim 10^{-15}$  Hz, can be constrained using CMB-only limits on  $\Delta N_{\text{eff}}$ , which translate into

$$\Omega_{\text{GW},0} h^2 < 2.9 \times 10^{-7}, \quad (87)$$

for GWs with homogeneous initial conditions (i.e., GW backgrounds with no initial density perturbations) (Clarke et al. 2020). The current theoretical uncertainty on

<sup>21</sup> We write the current value of the Hubble parameter as  $H_0 = h \times 100 \text{ km sec}^{-1} \text{ Mpc}^{-1}$ , following standard conventions in cosmology. We will avoid using in contexts where there could be any confusion with the GW strain, also denoted by  $h$ . Early Universe and late time observations report slightly different values for the Hubble parameter, see Bernal et al. (2016) for a discussion. For our purposes, we will assume  $h = 0.7$  when needed.

the SM prediction for  $N_{\text{eff}}$  is of order  $10^{-3}$ . If CMB experiments were to reach this level of precision, one would obtain an upper bound of  $\Omega_{\text{GW},0} h^2 < 5.6 \times 10^{-9}$ .

Since high-frequency GWs carry a lot of energy,  $\Omega_{\text{GW}} \propto f^3 S_h$ , the above bounds impose severe constraints on possible cosmological sources of high-frequency GWs.

#### 4.2.1 Inflation

Under the standard assumption of scale invariance, the amplitude of GWs produced during inflation is too small ( $\Omega_{\text{GW},0} \lesssim 10^{-16}$ ) to be observable with current technology.<sup>22</sup>

Various inflationary mechanisms have been studied in the literature that can produce a significantly blue-tilted GW signal (that is, a signal with a spectrum that increases towards higher frequency), or a localized bump at some given (momentum) scale, with a potentially visible amplitude. A number of these mechanisms have been explored in Bartolo et al. (2016b) with a focus on the LISA experiment and therefore on GW signals in the mHz range. However, these mechanisms can be easily extended to higher frequencies. Assuming an approximately constant Hubble parameter  $H$  during inflation, a GW signal generated  $N$  Hubble times (e-folds) before the end of inflation with frequency  $H$  is redshifted to a frequency  $f$  today according to

$$\ln \left[ \frac{f}{10^{-18} \text{ Hz}} \right] \simeq N_{\text{CMB}} - N, \quad (88)$$

where  $N_{\text{CMB}}$  is the number of e-folds at which the CMB modes (in particular the conventionally chosen pivot scale of  $0.5 \text{ Mpc}^{-1}$ ) exited the horizon. The numerical value of  $N_{\text{CMB}}$  depends logarithmically on the energy scale of inflation, which is bounded from above by the upper bound on the tensor-to-scalar ratio (Akrami et al. 2020),  $H \lesssim 6 \times 10^{13} \text{ GeV}$ . Saturating this bound implies  $N_{\text{CMB}} \simeq 60$ , and a peak at  $f = 1 \text{ MHz}$  then corresponds to the  $N = 4.7$ , while LIGO frequencies  $f_{\text{LIGO}} \simeq \mathcal{O}(10^2 \text{ Hz})$  correspond to  $N \simeq 14$ . These late stages of inflation are not accessible to electromagnetic probes, making high-frequency GW observations unique.

Bartolo et al. (2016b) discuss three broad categories of mechanisms leading to enhanced GW emission during inflation: the presence of extra fields that are amplified in the later stages of inflation (and therefore affect only scales much smaller than the CMB ones); GW production in the effective field theory framework of broken spatial reparametrizations, and GWs sourced by (large) scalar perturbations. In the following we will briefly summarize these three cases.

*Extra particle species* Several mechanisms of particle production during inflation have recently been considered in the context of GW amplification. Here, for definiteness, we discuss a specific mechanism in which a pseudo-scalar inflaton  $\phi$  produces gauge fields via an axion-like coupling of the form  $(\phi/(4f_a))F\tilde{F}$ , where  $F_{\mu\nu}$  is the gauge field strength tensor,  $\tilde{F}_{\mu\nu}$  is its dual, and  $f_a$  is the decay constant of

<sup>22</sup> However, note that the proposed space-borne detectors Big Bang Observer [BBO, Phinney et al. (2003)] and the deci-Hertz Interferometer Gravitational wave Observatory [DECIGO, Seto et al. (2001)] may reach the necessary sensitivity, assuming that astrophysical GW foregrounds can be subtracted to this accuracy.

$\phi$ . The motion of the inflaton results in a large amplification of one of the two gauge field helicities due to a tachyonic instability. The produced gauge quanta in turn generate inflaton perturbations and GW via  $2 \rightarrow 1$  processes (Barnaby and Peloso 2011; Sorbo 2011). The spectrum of the sourced GWs is (Barnaby and Peloso 2011)

$$\Omega_{\text{GW},0}(f) \simeq 3.6 \cdot 10^{-9} \Omega_{\text{rad},0} \frac{H^4}{M_{\text{Pl}}^4} \frac{e^{4\pi\xi}}{\xi^6}, \quad \text{with } \xi \equiv \frac{\dot{\phi}}{2f_a H}. \quad (89)$$

In this relation,  $H$  and  $\dot{\phi}$  are evaluated when a given mode exits the horizon, and therefore the spectrum in Eq. (89) is in general scale-dependent. In particular, in the  $\xi \gg 1$  regime, the GW amplitude grows exponentially with the speed of the inflaton, which in turn typically increases over the course of inflation in single-field inflation models. As a consequence, the spectrum in Eq. (89) is naturally blue-tilted. The growth of  $\xi$  is limited by the backreaction of the gauge fields on the inflaton. Within the limits of a perturbative description,  $\xi \lesssim 4.7$  (Peloso et al. 2016), and GW amplitudes of  $\Omega_{\text{GW},0} \simeq 10^{-10}$  can be obtained. Domcke et al. (2016), García-Bellido et al. (2016) explored the resulting spectrum for several inflaton potentials. In particular hill-top potentials are characterized by a very small speed close to the top (that is mapped to the early stages of observable inflation), and by a sudden increase of  $\dot{\phi}$  at the very end of inflation. Interestingly, hill-top type potentials are naturally present (Peloso and Unal 2015) in models of multiple axions such as aligned axion inflation (Kim et al. 2005).

The axionic coupling to gauge fields discussed above can also lead to gravitational wave production in contexts that go beyond inflation. If the pseudoscalar  $\phi$  does not play the role of the inflaton, as long as it remains light it is generally expected to remain displaced from its minimum-energy configuration during inflation due to the combined effect of vacuum fluctuations and Hubble friction. The field will only start rolling towards the minimum at a temperature  $T_{\text{osc}} \sim \sqrt{m_\phi M_{\text{Pl}}}$ , activating the tachyonic instability of the gauge field, which results again in gravitational waves (Machado et al. 2019, 2020; Ratzinger et al. 2021; Kitajima et al. 2018; Chatrchyan and Jaeckel 2021; Kitajima et al. 2021). The signal in this case is strongly peaked and chiral, with the peak amplitude scaling as  $\Omega h^2 \sim 10^{-7} (f_\phi/M_{\text{Pl}})^4$ , which can saturate the dark radiation bound of Eq. (87). The peak frequency is determined by  $T_{\text{osc}}$  and thus by the scalar field's mass. Other scenarios that produce similar signals include models of axion kinetic misalignment (Co et al. 2021; Madge et al. 2022) and models with spectator fields that oscillate in the early Universe (Cui et al. 2024).

*Effective field theory of broken spatial reparametrization symmetry* Inflationary scenarios based on modifications of general relativity can give rise to enhanced GW production and to a blue-tilted GW spectrum, rendering this emission relevant to high-frequency GW detectors. From the theoretical point of view, the effective field theory (EFT) approach (Cheung et al. 2008) represents a powerful tool to describe the relevant degrees of freedom at the energy scales of interest and to make predictions for observable quantities.

In the standard single-field effective field theory of inflation (Cheung et al. 2008), only time-translation symmetry ( $t \rightarrow t + \xi_0$ ) is broken by cosmological expansion.

However when space-reparameterization symmetry ( $x_i \rightarrow x_i + \xi_i$ ) is also broken (Bartolo et al. 2016a; Graef and Brandenberger 2015), scalar and tensor perturbations—the latter corresponding to GWs—acquire interesting features. In particular tensor perturbations can acquire a mass  $m_h$  and sound speed  $c_T$ , making them potential targets for high-frequency detectors since in this case the spectrum gets enhanced on small scales. At quadratic order, the EFT Lagrangian for graviton fluctuations  $h_{ij}$  around a conformally flat Friedmann–Lemaître–Robertson–Walker background can be expressed as in (Cannone et al. 2015; Bartolo et al. 2016a; Ricciardone and Tasinato 2017):

$$\mathcal{L}_h = \frac{M_{\text{Pl}}^2}{8} \left[ \dot{h}_{ij}^2 - \frac{c_T^2(t)}{a^2} (\partial_l h_{ij})^2 - m_h^2(t) h_{ij}^2 \right]. \quad (90)$$

The corresponding tensor power spectrum and its spectral tilt are

$$\mathcal{P}_T = \frac{2H^2}{\pi^2 M_{\text{Pl}}^2 c_T^3} \left( \frac{k}{k_*} \right)^{n_T}, \quad n_T = -2\epsilon + \frac{2m_h^2}{3H^2}. \quad (91)$$

The GW energy density is given by  $\Omega_{\text{GW},0} \sim \Omega_{\text{rad},0} \mathcal{P}_T$ . We see that, if the quantity  $m_h/H$  is sufficiently large, the tensor spectrum is blue-tilted with no need to violate the null energy condition in the early Universe. The spectrum is bounded at high frequencies by the observational BBN and CMB bounds, see Eq. (86).

This scenario shows how GW detectors at high frequency might be useful to test modification of gravity at very high-energy scales.

*Second-order GW production from primordial scalar fluctuations* In homogeneous and isotropic backgrounds, scalar, vector and tensor fluctuation modes decouple from each other at first order in perturbation theory. These modes can nevertheless source each other through non-linear effects, starting from second order. In particular, density perturbations (scalar modes) can produce ‘induced’ (or ‘secondary’) GWs (tensor modes) through a  $\zeta + \zeta \rightarrow h$  process, where  $\zeta$  represents a scalar fluctuation and  $h$  the tensor mode (Tomita 1975; Matarrese et al. 1994; Mollerach et al. 2004; Ananda et al. 2007; Baumann et al. 2007) [see also Kohri and Terada (2018), Espinosa et al. (2018), Braglia et al. (2020)]. This production, which involves only gravity, is mostly effective when the modes re-enter the horizon after inflation. (Second-order GWs would also be produced in an early matter-dominated era, see Inomata et al. (2019a, 2019b).) The amplitude of this signal is quadratic in the scalar perturbations.

Scale-invariant  $\mathcal{O}(10^{-5})$  perturbations, as measured on large scales in the CMB, result in GWs with unobservably small amplitude. On the other hand, if the spectrum of scalar perturbations produced during inflation has a localized bump at some scale (significantly smaller than the scales probed by the CMB and by large scale structure), a larger GW signal could be generated (Inomata et al. 2017; García-Bellido et al. 2017; Bartolo et al. 2019). Such bumps in the spectrum of inflationary perturbations are also interesting in other contexts, for instance they can lead to the production of a sizable primordial BH abundance at some specific mass scale. Conversely, the non-detection of a stochastic GW background can also be used to constrain fluctuations (Byrnes et al. 2019; Inomata and Nakama 2019). The induced

GWs have a frequency  $f_*$  parametrically equal to the wave number  $k_*$  of the modes from which they are produced and can hence be related to the number of  $e$ -folds,  $N$ , at which the scalar perturbation exits the horizon through Eq. (88).

The precise GW yield depends on the statistics of the scalar perturbations (Nakama et al. 2017; García-Bellido et al. 2017; Cai et al. 2019; Unal 2019). A reasonable estimate is obtained by simply looking at the scalar two-point function,

$$P_h^{\text{ind}} \propto \langle h^2 \rangle \propto \langle \zeta^4 \rangle \propto P_\zeta^2, \quad (92)$$

where  $P_h^{\text{ind}}$  is the power spectrum (two-point function) of the induced GW background and  $P_\zeta$  is the power spectrum of the gauge invariant scalar density fluctuations such that  $\langle \zeta_{\mathbf{k}} \zeta_{\mathbf{k}'} \rangle \propto \frac{\delta(\mathbf{k}+\mathbf{k}')}{k^3} P_\zeta(k)$ . From this relation, the present-day energy density of the induced stochastic GW background is given by

$$\Omega_{\text{GW},0} \sim \Omega_{\text{rad},0} P_\zeta^2. \quad (93)$$

At the largest scales of our observable Universe,  $P_\zeta \simeq 2 \times 10^{-9}$ , resulting in  $\Omega_{\text{GW},0} \sim \mathcal{O}(10^{-22})$ . Primordial BH limits are compatible with  $P_\zeta$  as large as  $\lesssim 10^{-2.5}$  at some (momentum) scales  $k_*$ . Scalar perturbations saturating this bound would lead to  $\Omega_{\text{GW},0} \sim \mathcal{O}(10^{-9})$ .

#### 4.2.2 (P)reheating

Preheating is an out-of-equilibrium particle production process driven by non-perturbative effects (Traschen and Brandenberger 1990; Kofman et al. 1994; Shtanov et al. 1995; Kaiser 1996; Khlebnikov and Tkachev 1996; Prokopec and Roos 1997; Kaiser 1997; Kofman et al. 1997; Greene et al. 1997; Kaiser 1998), which takes place after inflation in many models of particle physics (see Allahverdi et al. 2010; Amin et al. 2014; Lozanov 2019 for reviews). After inflation, interactions between the different fields may generate non-adiabatic time-dependent terms in the field equations of motion, which can give rise to an exponential growth of the field modes within certain momentum ranges. The field gradients generated during this stage can be an important source of primordial GWs, with the specific features of the GW spectra depending strongly on the considered scenario, see e.g. Khlebnikov and Tkachev (1997), García-Bellido (1998), Easter and Lim (2006), Easter et al. (2007), García-Bellido and Figueroa (2007), García-Bellido et al. (2008), Dufaux et al. (2007), Dufaux et al. (2009), Figueroa et al. (2011), Ringwald and Tamarit (2022). If instabilities are caused by the inflaton field's own self-interactions, we refer to it as *self-resonance*, a scenario which will be discussed in more detail below. Here we consider instead a multi-field preheating scenario, in which a significant fraction of energy is successfully transferred from the inflationary sector to other fields.

For illustrative process, let us focus on a two-field scenario, in which the post-inflationary oscillations of the inflaton excite a second, massless, field. More specifically, let us consider an inflaton with power-law potential  $V(\phi) = \frac{1}{p} \lambda \mu^{4-p} |\phi|^p$ , where  $\lambda$  is a dimensionless coefficient,  $\mu$  is a mass scale, and

$p \geq 2$ . Let us also define  $t_\star$  as the time when inflation ends. For  $t \gtrsim t_\star$ , the inflaton field oscillates with a time-dependent frequency  $\Omega_{\text{osc}} \equiv \omega_\star (t/t_\star)^{1-2/p}$ , where  $\omega_\star \equiv \sqrt{\lambda} \mu^{(2-p/2)} \phi_\star^{(p/2-1)}$  and  $\phi_\star \equiv \phi(t_\star)$  (Turner 1983). Let us now include a quadratic interaction term  $g^2 \phi^2 \chi^2$  between the inflaton and a secondary massless scalar field  $\chi$ , where  $g$  is a dimensionless coupling constant. In this case, the driving post-inflationary particle production mechanism is a parametric resonance (Kofman et al. 1994, 1997; Greene et al. 1997). In particular, if the so-called *resonance parameter*  $q_\star \equiv g^2 \phi_\star^2 / \omega_\star^2$  obeys  $q_\star \gtrsim 1$ , the secondary field gets excited through a process of broad resonance, and the amplitude of the field modes grows exponentially inside a Bose-sphere of radius  $k \lesssim k_\star \sim q_\star^{1/4} \omega_\star$ . The GW spectrum produced during this process has a peak at approximately the frequency and amplitude (Figueroa and Torrenti 2017),

$$f \simeq 8 \times 10^{-9} \text{ Hz} \times \left( \frac{\omega_\star}{\rho_\star^{1/4}} \right) \epsilon_\star^{\frac{1}{4}} q_\star^{\frac{1}{4}+\eta}, \quad (94)$$

$$\Omega_{\text{GW},0}(f) \simeq \mathcal{O}(10^{-9}) \times \epsilon_\star \mathcal{C} \frac{\omega_\star^6}{\rho_\star M_{\text{Pl}}^2} q_\star^{-\frac{1}{2}+\delta}, \quad (95)$$

where  $\rho_\star$  is the total energy density at time  $t = t_\star$ ,  $\eta \sim 0.3\text{--}0.4$  and  $\delta \sim 0.1$  are two parameters that account for non-linear effects while  $\mathcal{C}$  is a constant that characterizes the strength of the resonance with  $\mathcal{C} \omega_\star^6 / (\rho_\star M_{\text{Pl}}^2) \sim 0.01\text{--}0.001$ , depending on the model details. The factor  $\epsilon_\star \equiv (a_\star/a_{\text{RD}})^{1-3w}$  parametrizes the period between the end of inflation and the onset of the radiation dominated era with a transitory effective equation of state parameter  $w$ . If non-linear effects are ignored, the frequency and amplitude scale as  $f \sim q_\star^{1/4}$  and  $\Omega_{\text{GW},0} \sim q_\star^{-1/2}$ , respectively.

The values for  $\mathcal{C}$ ,  $\eta$ , and  $\delta$ , can be determined for specific preheating models with classical lattice simulations. For chaotic inflation with quadratic potential  $V(\phi) \propto \phi^2$ , one finds a frequency in the range  $f \simeq (10^8 - 10^9) \text{ Hz}$  and  $\Omega_{\text{GW},0} \simeq (10^{-12} - 10^{-11})$  for resonance parameters  $q_\star \in (10^4, 10^6)$  (assuming  $\epsilon_\star = 1$ ). Similarly, for a quartic potential  $V(\phi) \propto \phi^4$ , one obtains  $f \simeq (10^7 - 10^8) \text{ Hz}$  and  $\Omega_{\text{GW},0} \simeq (10^{-13} - 10^{-11})$  if  $q_\star \in (1, 10^4)$ . The GW spectrum in the quartic case also features additional peaks (Figueroa and Torrenti 2017; Ringwald and Tamarit 2022).

GWs be efficiently produced also by fields that carry spin, or when the resonant phenomena driving preheating are different from a parametric resonance. For example, GWs can be produced during the out-of-equilibrium production of fermions after inflation, for both spin-1/2 (Enqvist et al. 2012; Figueroa and Meriniemi 2013; Figueroa 2014) and spin-3/2 (Benakli et al. 2019) fields. Similarly, GWs can be generated when the produced particles are Abelian or non-Abelian gauge fields. These gauge fields can for example be coupled to a complex scalar field via a covariant derivative (Dufaux et al. 2010; Figueroa et al. 2016; Tranberg et al. 2018), or to a pseudo-scalar field via an axial coupling (Adshead et al. 2018, 2020a, b). Preheating can be remarkably efficient in the second case, and the



resulting GW energy density can be as large as  $\Omega_{\text{GW}} \sim \mathcal{O}(10^{-6} - 10^{-7})$  for certain coupling strengths, see Adshead et al. (2020a, 2020b) for more details. Production of GWs during preheating with non-minimal couplings to the curvature scalar  $R$  has also been explored in Fu et al. (2018). Finally, the stochastic background of GWs from preheating may develop anisotropies if the inflaton is coupled to a secondary light scalar field, see Bethke et al. (2013, 2014).

*Oscillon production.* Oscillons are long-lived compact scalar field configurations (Gleiser 1994) that can be formed in the early Universe in a variety of post-inflationary scenarios which involve a preheating-like phase (Amin and Shirokoff 2010; Amin et al. 2010, 2012; Zhou et al. 2013; Amin 2013; Lozanov and Amin 2014; Antusch et al. 2016; Antusch and Orani 2016; Antusch et al. 2017, 2018a, b; Lozanov and Amin 2018; Amin et al. 2018; Antusch et al. 2019; Sang and Huang 2019; Lozanov and Amin 2019; Fodor 2019; Hiramatsu et al. 2021). Their dynamics is a possible source of GW production. Oscillons are pseudo-solitonic solutions of real scalar field theories: their existence is due to attractive self-interactions of the scalar field that balance the outward pressure.<sup>23</sup> The real scalar field self-interactions are attractive if the scalar potential is shallower than quadratic at least on one side with respect to the minimum. Oscillons can be thought of as bubbles in which the scalar field is undergoing large oscillations that probe the non-linear part of the potential, while outside the scalar field is oscillating with a very small amplitude around the minimum of the potential.

As discussed in the previous section, during preheating the quantum fluctuations of the scalar field that may ultimately form oscillons are amplified due to a resonant process. The Universe ends up in a very inhomogeneous phase in which the inflaton (or any other scalar field that drives preheating) is fragmented and there are large fluctuations in the energy density. At this point, if the field is subject to attractive self-interactions, the inhomogeneities can clump and form oscillons. The geometric shape of the oscillons initially deviates significantly from being spherically symmetric, therefore their dynamics produce GWs. After many oscillations of the scalar field, oscillons tend to become spherically symmetric and GW production stops. However, during their entire lifetime oscillons can produce GWs also due to interactions and collisions among each other (Helfer et al. 2019). Oscillons are very long-lived: their lifetime is model-dependent but typically  $\gtrsim 10^4/m$  (Gleiser and Sicilia 2008; Amin and Shirokoff 2010; Amin et al. 2010, 2012; Salmi and Hindmarsh 2012; Saffin et al. 2014; Antusch et al. 2019; Gleiser and Krackow 2019; Zhang et al. 2020), where  $m$  is the mass of the scalar field. Oscillons eventually decay through classical (Segur and Kruskal 1987) or quantum radiation (Hertzberg 2010).

<sup>23</sup> If the scalar field is complex and the potential features a global  $U(1)$  symmetry, non-topological solitons like Q-balls (Coleman 1985) can be formed during the post-inflationary stage, giving rise to similar GW signatures (Chiba et al. 2010).

The peak of the GW spectrum at production is centered at a frequency slightly below the mass of the field, which typically lies well above the LIGO range today (Zhou et al. 2013; Antusch et al. 2018a; Lozanov and Amin 2019).<sup>24</sup> Typically, an oscillating massive scalar field forming oscillons quickly comes to dominate the energy density of the Universe until the perturbative decay of the field itself. For the simplest case of a gravitationally coupled massive field that starts oscillating at  $H \simeq m$  and decays at  $H \sim m^3/M_{\text{Pl}}^2$ ) the frequency today can be estimated as

$$f \simeq 10^6 \text{ Hz} \times X \times \left( \frac{m}{10^{12} \text{ GeV}} \right)^{5/6}. \quad (96)$$

Here the factor  $X$ , which is typically in the range  $X \simeq (10 - 10^3)$ , is due to the uncertainty in the precise time at which GWs are produced.  $X$  can be obtained in concrete models from lattice simulations:  $X \simeq 10$  would hold if GWs were produced immediately when the scalar field starts oscillating.<sup>25</sup> On the other hand, the later GWs are produced, the less the frequency is red-shifted and the larger is  $X$ . The maximum value of the GW energy density today for these processes, inferred from numerical simulations, is in the range  $\Omega_{\text{GW},0} \simeq (10^{-13} - 10^{-10})$  (Antusch et al. 2017, 2018a; Amin et al. 2018), see Dufaux et al. (2007) for a discussion on how to compute the GW amplitude.

Depending on the model, gravitational effects can become important and play a crucial role for the existence/stability of the oscillon solution (Seidel and Suen 1991). In particular, the requirement that the potential must be shallower than quadratic is no longer necessary, as the attractive force is provided by gravity (Urena-Lopez et al. 2002). In this case oscillons are equivalent to oscillatons, see Sect. 4.1.4, and can give rise to interesting additional effects, such as the collapse to BHs (Muia et al. 2019; Giblin and Tishue 2019; Kou et al. 2021; Nazari et al. 2021).

#### 4.2.3 The cosmic gravitational microwave background

The hot thermal plasma of the early Universe acts as a source of GWs, which, similarly to the relic photons of the CMB, peak in the  $\sim 100 \text{ GHz}$  range today. This makes this range of frequencies particularly interesting to target, since the source is the well-established Standard Model and the prediction is based on standard cosmology. The spectrum of this signal is determined by the particle content and the maximum temperature  $T_{\text{max}}$  reached by the thermal plasma in the history of the Universe (Ghiglieri and Laine 2015; Ghiglieri et al. 2020; Ringwald et al. 2021).

<sup>24</sup> See however Antusch et al. (2017), Liu et al. (2018), Kitajima et al. (2018) for models that lead to a GW peak at lower frequencies.

<sup>25</sup> This rough estimate assumes that the field starts oscillating when  $H \simeq m$ . Since the potential contains self-interactions, assuming that the field starts at rest, the actual requirement for the start of the oscillations is  $V''(\phi_{\text{in}}) \sim H$ , where  $\phi_{\text{in}}$  is the initial value of the field. Note also that if the field is the inflaton itself, the initial conditions are different from those assumed in Eq. (96), and therefore this estimate does not necessarily hold, see e.g., Antusch et al. (2017).

The energy density in GWs per logarithmic frequency interval can then be written as follows,

$$\Omega_{\text{GW},0}(f) \simeq \frac{1440\sqrt{10}}{2\pi^2} \frac{g_{\star s}(T_{\text{end}})^{1/3}}{g_{\star s}(T_{\text{max}})^{5/6}} \Omega_{\text{rad},0} \times \frac{f^3}{T_0^3} \frac{T_{\text{max}}}{M_{\text{Pl}}} \hat{\eta}\left(T_{\text{max}}, 2\pi\left(\frac{g_{\star s}(T)}{g_{\star s}(T_{\text{end}})}\right)^{1/3} \frac{f}{T_0}\right). \quad (97)$$

In the above expression,  $T_0$  is the temperature of the CMB today, while  $T_{\text{end}}$  denotes the temperature at which thermal production of gravitational waves stopped.  $T_{\text{end}}$  is generally taken as the temperature of the electroweak phase transition. Given that GW production is ultraviolet-dominated this is a reasonable approximation. The function  $\hat{\eta}$  encodes the sources of GW production in the thermal plasma, which is dominated by long range hydrodynamic fluctuations at  $2\pi f < T_0$  and by quasi-particle excitations in the plasma at  $2\pi f \sim T_0$ , see Ghiglieri and Laine (2015), Ghiglieri et al. (2020), Ringwald et al. (2021) for more details. For frequencies corresponding to modes that were superhorizon at the time when  $T = T_{\text{max}}$ , and thus would be prevented from evolving until horizon entry,  $T_{\text{max}}$  in Eq. (97) should be replaced with the horizon crossing temperature  $T_{\text{hc}}(f) \sim M_{\text{Pl}} f / (6 \times 10^{10} \text{ Hz})$  (Drewes et al. 2024). Corrections to  $\hat{\eta}$  from two-graviton emission have been computed in Ghiglieri et al. (2024b, 2024a).

The peak frequency of the spectrum in Eq. (97) is

$$f_{\text{peak}}^{\Omega_{\text{CGMB}}} \approx 79.8 \text{ GHz} \left( \frac{106.75}{g_{\star s}(T_{\text{max}})} \right)^{1/3}. \quad (98)$$

where  $g_{\star s}(T = T_{\text{max}})$  is the number of entropic relativistic degrees of freedom at  $T_{\text{max}}$ . The peak amplitude of  $\Omega_{\text{GW},0}(f)$  approaches the dark radiation bound, Eq. (87), if  $T_{\text{max}} \sim \mathcal{O}(\text{few}) \times 10^{19} \text{ GeV}$ , and thus close to  $M_{\text{Pl}}$ . The CMB constraints on the tensor-to-scalar ratio, however, impose a tighter constraint, namely  $T_{\text{max}} < 6.6 \times 10^{15} \text{ GeV} \times (106.75/g_{\star s}(T_{\text{max}}))^{1/4}$  (Akrami et al. 2020) under the assumption of slow-roll inflation and instantaneous reheating. Therefore the detection of the cosmic gravitational microwave background with a spectrum pointing to  $T_{\text{max}} > 10^{16} \text{ GeV}$  would rule out slow-roll inflation as a viable pre hot Big Bang scenario. Note that since at leading order  $\Omega_{\text{GW},0}(f)$  scales linearly with  $T_{\text{max}}$  and the peak frequency depends on  $g_{\star s}(T_{\text{max}})$ , the detection of the peak of the cosmic gravitational microwave background would determine both  $T_{\text{max}}$  and  $g_{\star s}(T_{\text{max}})$ , see Ringwald et al. (2021) for more details.

Going beyond standard scenarios, the possibility of nonstandard cosmological histories has been considered in Muia et al. (2023). These authors, as well as Drewes et al. (2024), have also considered the possible existence of several decoupled hidden sectors with different temperatures. The impact of strong coupling on the emission rate has been analyzed in Castells-Tiestos and Casallerrey-Solana (2022), and graviton emission from high-temperature fundamental strings has been considered in Frey et al. (2024). The resulting spectrum from the latter process has robust characteristics: it peaks at frequencies of order 50–100 GHz, and contrary the predictions of other

scenarios beyond the Standard Model the amplitude is hierarchically larger than the one in the Standard Model. Notably, it is directly proportional to the string scale, indicating that a potential signal may also determine the string scale.

#### 4.2.4 Phase transitions

A first order phase transition in the early Universe proceeds by the nucleation of bubbles of the low-temperature phase as the Universe cools below the critical temperature (Steinhardt 1982; Hogan 1983).<sup>26</sup> Due to the higher pressure inside, the bubbles expand and collide until the stable phase fills the whole Universe. The process disturbs the fluid, generating shear stress and hence GWs (Witten 1984; Hogan 1986). As the perturbations are mostly compression waves, they can be described as sound waves, and their collisions are often the main source of GWs (Hindmarsh et al. 2014, 2015, 2017a). The peak frequency of an acoustic contribution to the relic GW background from a strong first order transition is controlled by the temperature of the transition,  $T_*$ , and by the mean bubble separation  $R_*$ .<sup>27</sup> Numerical simulations show for bubble wall speeds well above the speed of sound that (Hindmarsh et al. 2017a)

$$f_{\text{peak}} \simeq 260 \text{ MHz} \times \left( \frac{1}{H_* R_*} \right) \left( \frac{T_*}{10^{15} \text{ GeV}} \right) \left( \frac{g_*(T_*)}{100} \right)^{1/6}, \quad (99)$$

where  $H_*$  is the Hubble rate at nucleation. The theoretical expectation is that  $1 \lesssim (H_* R_*)^{-1} \lesssim 10^4$ . Remarkably, phase transitions in the very early universe, possibly associated with grand unification or the breaking of  $B-L$ , a Peccei-Quinn symmetry or flavour symmetries are natural candidates for high frequency gravitational waves. The intensity of the GW emission depends on  $H_* R_*$ , on the fraction  $K$  of the energy density of the Universe which is converted into kinetic energy during the phase transition, and on the lifetime of the source, which can last for up to a Hubble time. With the lifetime of the velocity perturbations given by  $\tau_v \approx 4R_*/(3K)$ , the GW spectrum can be estimated as (Hindmarsh et al. 2015; Guo et al. 2021)

$$\begin{aligned} \Omega_{\text{GW},0}(f) &\simeq 2H_* R_* \left( 1 - (1 + 2H_* \tau_v)^{-1/2} \right) \left( \frac{100}{g_*(T_*)} \right)^{1/3} K^2 \tilde{\Omega}_{\text{GW}} \\ &\times \Omega_{\text{rad},0} S\left(\frac{f}{f_{\text{peak}}}\right), \end{aligned} \quad (100)$$

where  $\tilde{\Omega}_{\text{GW}} \approx 0.058$  is an efficiency factor obtained from simulations. The frequency dependence of  $\Omega_{\text{GW},0}(f)$  is determined by the function  $S(f/f_{\text{peak}})$ , with

<sup>26</sup> The *critical* temperature,  $T_c$ , denotes the temperatures at which the low-temperature vacuum state becomes energetically favorable compared to the high-temperature state that the Universe is in before the phase transition. The *nucleation* temperature,  $T_*$ , denotes the temperature at which the first bubbles form. It is usually similar to  $T_c$ , but can be much lower in the case of supercooled phase transitions.

<sup>27</sup> The subscript  $*$  denotes quantities evaluated at the bubble nucleation time.

$$S(x) = x^3 \left( \frac{7}{4 + 3x^2} \right)^{7/2}, \quad (101)$$

which takes its maximal value of 1 at  $x = 1$ . Numerical simulations indicate  $\tilde{\Omega}_{\text{GW}} = \mathcal{O}(10^{-2})$ . Hence,  $\Omega_{\text{GW},0} \lesssim 10^{-7}$  today, with the upper bound reached only if most of the energy available in the phase transition is turned into kinetic energy. This is only possible if there is significant supercooling.

The calculation of the kinetic energy fraction and the mean bubble separation requires knowledge of the free energy density  $\mathcal{F}(T, \phi)$ , a function of the temperature and the order parameter of the phase transition. If the underlying quantum theory is weakly coupled, and the scalar particle corresponding to  $\phi$  is light compared to the masses gained by gauge bosons in the phase transition, this is easily calculated, and shows that first order transitions are generic in gauge theories in this limit (Kirzhnits 1972; Kirzhnits and Linde 1976), meaning that there is a temperature range in which there are two minima of the free energy as a function of  $\phi$ . The critical temperature is defined as the temperature at which the two minima are degenerate, separated by a local maximum.

The key parameters to be extracted from the underlying theory, besides the critical temperature  $T_c$ , are the nucleation rate  $\beta$ , the strength parameter  $\alpha$  and the bubble wall speed  $v_w$ . The nucleation rate parameter  $\beta = d \log p / dt$ , where  $p$  is the bubble nucleation rate per unit volume, is calculable from  $\mathcal{F}(T, \phi)$  by applying homogeneous nucleation theory (Langer 1969) to fields at high temperature (Linde 1983). This calculation also gives  $T_*$  as the temperature at which the volume-averaged bubble nucleation rate peaks. The strength parameter is roughly, but not precisely, one quarter of the latent heat divided by the thermal energy (see Hindmarsh and Hijazi 2019 for a more precise definition) at the nucleation temperature and also follows from knowing  $\mathcal{F}(T, \phi)$ . The wall speed is a non-equilibrium quantity, which cannot be extracted from the free energy alone, and is rather difficult to calculate accurately (see Dorsch et al. 2018; Laurent and Cline 2020; Ai et al. 2023; Ekstedt et al. 2025 and references therein). In terms of these parameters, it can be shown that  $R_* \approx (8\pi)^{1/3} v_w / \beta$  (Enqvist et al. 1992). The kinetic energy fraction  $K$  can be estimated from the self-similar hydrodynamic flow set up around an isolated expanding bubble, whose solution can be found as a function of the latent heat and bubble wall velocity by a simple one-dimensional integration (Turner et al. 1992; Espinosa et al. 2010; Hindmarsh and Hijazi 2019).  $K$  is usually parameterized in terms of an efficiency factor  $\kappa$  and the phase transition strength  $\alpha$ , with  $K = \kappa \alpha / (1 + \alpha)$ . Approximate fits for  $\kappa$  in terms of  $\alpha$ ,  $v_w$  can be found in Espinosa et al. (2010); for example, in the limit of near-luminal velocity, one has  $\kappa \approx \alpha / (0.73 + 0.083\sqrt{\alpha} + \alpha)$ . Typically,  $K$  falls in the range between  $K = 1$ – $10^{-6}$ .

Current projected sensitivities for Einstein Telescope and Cosmic Explorer indicate that these observatories will be able to probe cosmological first order transition occurring at temperatures of at most few  $\times 100$  TeV assuming a modest amount of supercooling (Abbott et al. 2017a; Punturo et al. 2010; Hild et al. 2011) (i.e., when  $T_* \sim T_c$  and  $(R_* H_*)^{-1} \gtrsim 100$ ). When considering high-scale transitions, it

should be kept in mind that if the transition happens immediately after inflation, the gravitational wave signal could be substantially diluted by an early matter-dominated epoch that typically follows inflation. Additionally, it should be noted that the frequency has an upper bound of  $\sim 10^2$  GHz, since the maximal temperature of the Universe is bounded by CMB observations and the distance scale  $R_*$  cannot be smaller than the mean free path associated with thermal fluctuations,  $\sim 1/T_*$  (Ghiglieri et al. 2024a).

#### 4.2.5 Topological defects

Cosmic strings are one-dimensional topological defect solutions to a field equation which may have formed after a phase transitions in the early Universe if the first homotopy group of the vacuum manifold associated with the symmetry breaking is non-trivial (Kibble 1976; Jeannerot et al. 2003). They can also be fundamental strings from string theory, formed for instance at the end of brane inflation (Dvali and Vilenkin 2004; Copeland et al. 2004), and stretched to cosmological scales. The energy per unit length of a string is  $\mu \sim \eta^2$ , with  $\eta$  the characteristic energy scale. (In the case of topological strings,  $\eta$  is the energy scale of the phase transition that generated the strings.) Typically, the tension of the strings is characterized by the dimensionless combination  $G\mu \sim (\eta/M_{\text{Pl}})^2$ . The current upper bound from the CMB is  $G\mu \lesssim 10^{-7}$ , whereas GW searches in pulsar timing arrays constrain the string tension to  $G\mu \lesssim 10^{-11}$ . Cosmic strings are energetic objects that move at relativistic speeds. The combination of these two factors immediately suggests that strings should be a powerful source of GWs.

When cosmic strings are formed in the early Universe, their dynamics rapidly drive them into an attractor solution, characterized by their fractional energy density relative to the background energy density of the Universe remaining constant. This is known as the ‘scaling’ regime. During this regime, strings will collide and possibly intercommutate. For topological strings the intercommutation probability is  $\mathcal{P} = 1$ , whereas  $\mathcal{P} < 1$  is characteristic for cosmic superstrings networks. Closed string configurations—loops—are consequently formed when a string self-intersects, or when two strings cross. Loops smaller than the horizon decouple from the string network and oscillate under their own tension, which results in the emission of gravitational radiation (eventually leading to the decay of the loop). The relativistic nature of strings typically leads to the formation of *cusps*, corresponding to points where the string momentarily moves at the speed of light (Turok 1984). Furthermore, the intersections of strings generates discontinuities on their tangent vector known as *kinks*. All loops are typically expected to contain cusps and kinks, both of which generate GW bursts (Damour and Vilenkin 2000, 2001). Hence, a network of cosmic (super-)strings formed in the early Universe is expected to radiate GWs throughout the entire cosmological history, producing a stochastic background of GWs from the superposition of many uncorrelated bursts. While searches for cosmic string are normally searched for this stochastic background, an alternative strategy is to search for individual strong bursts, which could manifest as transient GW signals (Aasi et al. 2014; Abbott et al. 2018).

A network of cosmic strings in the scaling regime contains, at every moment of its evolution, sub-horizon loops and long strings that stretch across a Hubble volume. The latter are either infinite strings or they form super-horizon loops, and they are also expected to emit GWs. However, the dominant contribution is generically the one produced by the superposition of radiation from many sub-horizon loops along each line of sight.

The power emitted into gravitational radiation by an isolated string loop of length  $l$  can be calculated using the standard formalism in the weak gravity regime, see Weinberg (1972). More explicitly, we can assume that, on average, the total power emitted by a loop is given by  $P_{\text{Loop}} = \Gamma \times (G\mu) \times \mu$ , where  $\Gamma$  is a dimensionless constant independent of the size and shape of the loops. Estimates from simple loops (Vachaspati and Vilenkin 1985; Burden 1985; Garfinkle and Vachaspati 1987), as well as results from Nambu–Goto simulations (Blanco-Pillado and Olum 2017), suggest that  $\Gamma \simeq 50$ . The GW radiation is only emitted at discrete frequencies by each loop,  $\omega_n = 2\pi n/T$ , where  $T = l/2$  is the oscillation period of the loop, and  $n$  is an integer  $\geq 1$ . We can write  $P_{\text{Loop}} = G\mu^2 \sum_n P_n$ , with  $P_n$  characterizing the power emitted at each frequency  $\omega_n$  for a particular loop, depending on whether the loop contains cusps or kinks, and whether kink–kink collisions occur (Burden 1985; Allen and Shellard 1992). It can be shown that for large  $n$ ,  $P_n = (\Gamma/\zeta(q))n^{-q}$ , where  $\zeta(q)$  is the Riemann zeta function, which appears here as a normalization factor to ensure that the total power of the loop is equal to  $\Gamma = \sum_n P_n$ . The parameter  $q$  takes the values  $4/3$ ,  $5/3$ , or  $2$  depending on whether the emission is dominated by cusps, kinks or kink–kink collisions, respectively, see for e.g. Vachaspati and Vilenkin (1985), Binetruy et al. (2009), Auclair et al. (2020).

The stochastic GW background emitted by loops generated during the radiation domination period is characterized by a scale-invariant energy spectrum, spanning many decades in frequency. The high-frequency cut-off of this spectrum is determined by the temperature of the thermal bath at formation of the string network, with the CMB bound on the reheating temperature,  $T_{\text{max}} \lesssim 10^{16}$  GeV, implying a cut-off frequency of  $f_{\Delta} \lesssim 10^9$  GeV (Gouttenoire et al. 2020). The amplitude of the plateau is given by (Auclair et al. 2020)

$$\Omega_{\text{GW},0}^{\text{plateau}}(f) \approx 8.04 \Omega_{\text{rad},0} \sqrt{\frac{G\mu}{\Gamma}}. \quad (102)$$

Note that this estimate does not depend on the exact form of the loops' individual power spectra, nor on whether the GW emission is dominated by cusps or kinks. Rather, it depends only on the total GW radiation emitted by the loops. Equa-



tion (102) indicates that the stochastic GW background from cosmic strings can be rather strong.<sup>28</sup>

Moreover, if the phase transition responsible for cosmic string formation is originating from symmetry breaking in a grand unified theory (GUT), then, depending on the structure of the GUT symmetry group, cosmic strings may be metastable, decaying via the (exponentially suppressed) production of monopoles (Vilenkin 1982; Monin and Voloshin 2008, 2010; Leblond et al. 2009). In this case, the low-frequency end of the spectrum, corresponding to GW emission at later times, is suppressed and the signal may *only* be detectable at high frequencies (Leblond et al. 2009; Dror et al. 2020; Buchmuller et al. 2020a, b). In this case, the string tension is only constrained by the BBN bound on  $N_{\text{eff}}$ ,  $G\mu \lesssim 10^{-4}$ , and the scale-invariant part of the spectrum may extend from  $10^3$  Hz (LIGO constraint) up to  $10^9$  Hz (network formation).

Finally, let us recall that long strings (infinite and super-horizon loops) also radiate GWs. One contribution to this signal is given by the GWs emitted around the horizon scale at each moment of cosmic history, as the network's energy-momentum tensor adapts itself to the scaling regime (Krauss 1992; Jones-Smith et al. 2008; Fenu et al. 2009; Figueroa et al. 2013, 2020). This emission is expected from any network of cosmic defects in the scaling regime, independent of the topology and origin of the defects (Figueroa et al. 2013). In the case of cosmic string networks modeled by the Nambu-Goto approximation (where the thickness of the string is taken to be zero), this irreducible background represents a very subdominant signal compared to the GW background emitted from sub-horizon loops. In the case of field theory strings (for which simulations to date indicate an absence of 'stable' loops), it is instead the only GW signal emitted by the network.

The GW energy density spectrum of this irreducible background from long strings is predicted to be exactly scale-invariant for the modes emitted during radiation domination (Figueroa et al. 2013). The power spectrum from long strings therefore mimics the spectral shape of the dominant signal from loop decay, but with a smaller amplitude. The amplitude depends on the fine details of the unequal-time correlator of the network's energy-momentum tensor. This correlator can be obtained accurately only from sufficiently large scale lattice simulations. For strings based on a global symmetry (global strings), the scale-invariant GW power spectrum has been obtained numerically from massively parallel lattice field theory simulations, with a predicted energy density of (Figueroa et al. 2013)

<sup>28</sup> *Important remark:* as the characteristic width  $\delta \sim 1/\eta$  of a cosmic string is generally much smaller than the horizon scale, it is commonly assumed that strings can be described by the Nambu-Goto action, which is the leading-order approximation when the curvature scale of the strings is much larger than their thickness. The plateau in Eq. (102) applies only for the case of Nambu-Goto strings. For these strings to reach the scaling regime, GW emission from loops is actually crucial as it is the loss of loops from the network that guarantees scaling, and GW emission provides a mechanism for loops to decay. However, in field theory simulations of string networks (Vincent et al. 1998; Hindmarsh et al. 2009; Daverio et al. 2016; Hindmarsh et al. 2017b), the network of infinite strings reaches a scaling regime thanks to energy loss into classical radiation of the fields involved in the simulations. The simulations show the presence of extensive radiation of massive particles being emitted, and the loops that are formed decay within a Hubble time. This intriguing discrepancy has been under debate for the last  $\sim 20$  years, and has very significant impact on the amplitude of the predicted GW spectrum.



$$\Omega_{\text{GW},0}(f) \simeq 4 \times 10^4 (G\mu)^2 \Omega_{\text{rad},0}. \quad (103)$$

The irreducible background from the more interesting case of an Abelian Higgs model has unfortunately not been studied yet. Despite the large numerical prefactor in Eq. (103), the quadratic dependence on  $(G\mu)^2$  suppresses the energy density significantly, see e.g., Buchmüller et al. (2013) for a comparison among GW signals emitted from the same string network. This amplitude is clearly subdominant when compared to the amplitude of the GW signal from loops, which scales as  $(G\mu)^{1/2}$  according to Eq. (102).

Finally, we point out that, since the irreducible GW emission described above is expected from any network of defects in the scaling regime, global texture networks also emit a GW background due to their self-ordering during scaling (Jones-Smith et al. 2008; Fenu et al. 2009; Giblin et al. 2012; Figueroa et al. 2013, 2020). Textures are formed when the second (or higher) homotopy group of the vacuum manifold is non-trivial (Vilenkin and Shellard 2000). Such conditions can be realized in case of the breaking of a global or gauge symmetry. In the case of a global symmetry, the GW spectrum is scale invariant for radiation domination (Jones-Smith et al. 2008; Fenu et al. 2009; Figueroa et al. 2013), and exhibits a peak at the horizon today for matter domination (Figueroa et al. 2020). In the case of gauged textures one instead expects a peaked spectrum, with the peak frequency and amplitude of the GW background set by the symmetry breaking scale  $v$  (Dror et al. 2020),

$$f \sim 10^{11} \text{ Hz} \times \frac{v}{M_{\text{Pl}}}, \quad \Omega_{\text{GW},0} \sim 2 \times 10^{-4} \left( \frac{v}{M_{\text{Pl}}} \right)^4. \quad (104)$$

Given that the frequency and amplitude both increase with  $v$ , it is not unlikely that such signals will be most easily detectable by high-frequency detectors.

#### 4.2.6 Evaporating primordial black holes

In Sect. 4.1.2, we have discussed GW signals emitted by primordial BHs merging in the late Universe. Very light primordial BHs (with masses smaller than  $10^{11}$  kg), which evaporate before BBN, could produce an  $\mathcal{O}(\text{GHz})$  stochastic spectrum of GWs by merging and scattering (Dolgov and Ejlli 2011). Here we consider yet another source of GWs tied to primordial BHs, namely the emission of gravitons as part of their Hawking radiation. This is particularly relevant for light primordial BHs evaporating either before BBN, or between BBN and the present day.

The graviton emission from a population of primordial BHs induces a stochastic background of GWs (Anantua et al. 2009; Dong et al. 2016; Ireland et al. 2023) that peaks at very high frequencies, between  $f \sim 10^{13}$  Hz and  $10^{22}$  Hz. The shape and amplitude of the resulting GW frequency spectrum depends on multiple factors, such as the primordial BHs' abundance at formation, their mass spectrum, their spin, and the number of degrees of freedom in the particle physics theory. Due to the redshift of the GW amplitude and frequency, the observable GW spectrum today is dominated by the latest stages of primordial BH evolution, and the frequency is

hence set by the evaporation time (which in turn depends on the initial mass) of the primordial BH.

Taking into account the limits on the primordial BH abundance from BBN and from extra-galactic background radiation, the maximum amplitude can be up to  $\Omega_{\text{GW},0} \approx 10^{-7.5}$  for primordial BHs evaporating just before BBN, corresponding to an initial mass  $m_{i\text{PBH}} \lesssim 10^9 \text{ g}$  at formation. For heavier BHs that might have not fully evaporated yet today,  $10^9 \text{ g} \lesssim m_{i\text{PBH}} \lesssim 10^{17} \text{ g}$ , it can be up to  $\Omega_{\text{GW},0} \approx 10^{-6.5}$  (Dong et al. 2016), with a spectrum peaked at frequencies between  $10^{18} \text{ Hz}$  and  $10^{22} \text{ Hz}$ . See also Ireland et al. (2023) for more details. Finally, much lighter primordial BHs that would have completely evaporated long before BBN are of interest as well. Because the primordial BH density decreases  $\propto 1/a^3$  (with  $a$  denoting the scale factor of the expanding Universe), while the radiation density is  $\propto 1/a^4$ , such early decaying primordial BHs can be very abundant in the early Universe, leading to an early matter dominated phase. GWs produced in their decay could then constitute a sizable fraction of the energy density during the subsequent radiation dominated epoch, limited only by the BBN and CMB constraints [see Eq. (87)]. For primordial BHs produced close to the grand unification scale,  $E \sim 10^{15} \text{ GeV}$ , the GW frequency spectrum has a peak around  $10^{15} \text{ Hz}$  and can reach an amplitude  $\Omega_{\text{GW},0}(f) \sim 10^{-8}$  for a Universe with  $\sim 10^3$  degrees of freedom (Anantua et al. 2009).

For primordial BHs in theories with large extra dimensions, the peak frequency can be lowered substantially, since the true bulk Planck scale  $M_*$  can be much smaller than the effective 4d Planck scale. For an optimal choice of parameters, the peak frequency may then be  $< \text{MHz}$  (Ireland et al. 2024).

#### 4.2.7 Miscellaneous

In the following we summarize a few additional sources of high-frequency GWs that require more exotic setups.

*Brane-world scenarios.* In a brane-world scenario (Rubakov and Shaposhnikov 1983), the very weak force of gravity in our  $(3+1)$ -dimensional Universe arises from a stronger gravitational force that is felt in a fifth dimension at a level commensurate with the other forces. This scenario suggests that two  $(3+1)$ -dimensional branes—one of which represents our four-dimensional Universe, while the other is a ‘shadow’ brane—are separated in a fifth dimension by a small distance (Randall and Sundrum 1999; Maartens and Koyama 2010). If violent gravitational events—such as BH mergers—take place on the shadow brane, they would excite oscillations not only in the shadow brane but also in the five-dimensional space separating the branes. This leads to GW production on our visible brane as well (Seahra et al. 2007; Clarkson and Seahra 2007).

*Pre-Big Bang cosmology.* The pre-Big Bang scenario provides an alternative to cosmological inflation as a mechanism for setting the initial conditions for the hot Big Bang. The scenario exploits the fundamental symmetries of string theory to build a model in which the Universe starts in a cold and empty state in the infinite past and moves towards a state of high curvature through accelerated expansion

(Gasperini and Veneziano 2003, 2016). The state of high curvature corresponds to a region in the parameter space in which the theory is strongly coupled. It is then assumed that the strongly coupled theory is able to match this initial accelerated expansion to the usual hot Big Bang cosmology. Interestingly, this scenario predicts a blue spectrum of GWs, with a peak at high frequency (Brustein et al. 1996).

*Quintessential inflation.* If the inflationary epoch is followed by a phase in which the equation of state is stiffer than radiation ( $w > 1/3$ ), the stochastic spectrum of GWs features a growth at high frequency, followed by a sharp cutoff (Giovannini 1999). Such behavior is expected in quintessential models of inflation such as the one investigated in Peebles and Vilenkin (1999). The position of the peak depends very weakly on the number of minimally coupled scalar fields of the model, but it is independent of the final curvature at the end of inflation. Therefore, it is always located at  $\sim 100$  GHz. The amplitude of the GW spectrum can become very large: in Giovannini (1999) the authors present a choice of the parameters such that  $\Omega_{\text{GW},0} \simeq 10^{-6}$  at the peak.

*Magnetars.* Magnetars are neutron stars with extremely large surface magnetic fields  $\sim 10^9$ – $10^{11}$  Te. Wen et al. (2017) suggests that gamma-ray bursts produced by the magnetar or by a companion object in a binary system, and interacting with the surface magnetic field of the magnetar could be a source of high-frequency GW, with frequency around  $10^{20}$  Hz and energy density at Earth up to  $\Omega_{\text{GW},0} \sim 10^{-6}$ .

*Reheating.* The oscillations of the inflaton (or another scalar field in the inflationary sector) around the minimum of its potential at the end of inflation constitutes a model-independent source of stochastic GWs (Ema et al. 2020). The oscillations act as a driving force in the equation of motion for the tensor modes, leading to GW production at high frequency  $\gtrsim 10^5$  Hz. The amplitude of this signal is bound to be quite small: in Ema et al. (2020) the authors present a choice of parameters such that  $\Omega_{\text{GW},0} \lesssim 10^{-21}$ .

*Plasma instabilities.* Servin and Brodin (2003) studied interactions of electromagnetic waves and GWs in a magnetized plasma. In the high-frequency regime, a circularly polarized electromagnetic wave traveling parallel to the background magnetic field present in a plasma generates GWs with the same frequency as the electromagnetic wave. However, no specific estimates for the amplitude and spectrum of the resulting GW background at Earth have been derived yet.

### 4.3 Gravitational wave generation in laboratory setups

The possibility of laboratory control of gravitational fields was considered in the early 1960s in Weber (1960) and Gertsenshtein (1962). The power radiated into gravitational waves at 300 MHz by electrically-induced stresses in a piezoelectric crystal with a size of fifty centimeters on a side was calculated to be up to  $10^{-20}$  W, seventeen orders of magnitude above the maximal power generated by a spinning rod having the same length as the crystal. Assuming isotropy, the corresponding strain is  $h \approx 10^{-38}$  ten meters away from the source.

In 1973, gravitational radiation generated by alternating electromagnetic fields inside resonant cavities has been investigated (Grishchuk and Sazhin 1974).

Assuming a hypothetical rectangular cavity of dimensions  $10^{-2} \text{ m} \times 1 \text{ m} \times 1 \text{ m}$  with an average energy density of  $10^4 \text{ J/m}^3$ , the gravitational energy flux at a distance of  $r = 10 \text{ m}$  is  $10^{-30} \text{ W/m}^2$ . The emitted gravitational waves would have a frequency of  $10^{10} \text{ Hz}$  and a strain of  $h \approx 10^{-43} \times (10 \text{ m}/r)$ .

In the following decade, gravitational waves radiated by circulating bunches of charged particles in high-energy accelerators were considered. In Diambrini Palazzi and Fargion (1987) the radiated power was calculated to be  $5.5 \times 10^{-25} \text{ W}$  for the LEP-2 collider at CERN. The frequency of the generated gravitational waves in this case is  $f \approx 10^4 \text{ Hz}$  and, assuming isotropic emission, the associated strain is  $h \approx 10^{-43}$  a hundred kilometers away from the source. Updates on gravitational radiation emitted by particles circulating in storage rings or by conversion of electromagnetic radiation into GWs can be found in Berlin et al. (2021).

Since the turn of the millennium, advances in high-power and high-energy lasers have provided appealing platforms to study gravitational aspects of light under laboratory conditions. Laser-accelerated ions are potential sources of gravitational waves in the THz band (Gelfer et al. 2016). The generated gravitational strain depends on the total kinetic energy of the accelerated ions, with a maximal value  $h \approx 10^{-43}$  at a distance  $r = 10 \text{ m}$ . Two counter-propagating laser beams are also expected to generate gravitational waves at twice the laser frequency  $1/\lambda_{\text{las}}$ , with a strain given by (Gregori and Vacalis 2023):

$$h \approx 5.2 \times 10^{-38} \times \left( \frac{\lambda_{\text{las}}}{10 \mu\text{m}} \right)^2 \left( \frac{\tau}{10^{-12} \text{ sec}} \right) \left( \frac{I}{10^{23} \text{ W cm}^{-2}} \right) \left( \frac{10 \text{ cm}}{r} \right). \quad (105)$$

Here,  $\tau$  is the duration of the laser pulse and  $I$  is the laser intensity. Refinements with the use of twisted laser beams carrying orbital angular momentum have been proposed in Atonga et al. (2024). Estimations of the produced gravitational strain are compatible with the above expressions. In addition, properties of the emitted gravitational waves, such as polarization, direction of emission, or beaming are all highly controllable by the experimental setup.

Beyond the generation of classical waves, controlled emission of gravitons has also been considered. Notably, the rate at which gravitons are spontaneously emitted by the quadrupolar transition  $3d(m=2) \rightarrow 1s$  in a hydrogen atom has been performed in Weinberg (1972). This was later improved upon in Boughn and Rothman (2006), resulting in  $\Gamma(3d \rightarrow 1s) \approx 10^{-40} \text{ Hz}$ . This rate can be substantially increased by considering spontaneous or stimulated emission of gravitons in macroscopic quantum systems [see e.g. Tobar et al. (2024)]. However, the achievable event rates remain orders of magnitude too small for conceivable applications.

#### 4.4 Summary of sources

**Table 1** Summary of late universe sources

| Source                                    | Typical frequency                                                                                                   | Amplitude                                                                                                                                                                                                                                                                       |
|-------------------------------------------|---------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Neutron star mergers                      | $\lesssim (1 - 5) \text{ kHz}$                                                                                      | $h(f) \lesssim 10^{-26} \text{ sec}$                                                                                                                                                                                                                                            |
| Phase transitions in neutron star mergers | $\simeq 0.6 \text{ MHz} \times \left( \frac{0.1}{v_w} \right) \left( \frac{1 \text{ ms}}{\tau} \right)$             | $h_{c,\text{sto}} \simeq 1.5 \times 10^{-24} v_f^2 \left( \frac{100 \text{ Mpc}}{D} \right)$                                                                                                                                                                                    |
| Disk around supermassive BHs              | $\simeq 3.3 \times 10^{19} \text{ Hz}$                                                                              | $h_{c,\text{sto}} \lesssim 3 \times 10^{-44}$                                                                                                                                                                                                                                   |
| Sun                                       | $\simeq 10^{14} \text{ Hz}$                                                                                         | $h_{c,\text{sto}} \lesssim 3 \times 10^{-42}$                                                                                                                                                                                                                                   |
| Primordial BH mergers                     | $\lesssim \frac{4400}{(m_1 + m_2)} \text{ Hz}$                                                                      | $h(f) \approx 10^{-31} \text{ sec} \left( \frac{\text{kpc}}{D} \right) \left( \frac{m_{\text{PBH}}}{10^{-5} M_\odot} \right)^{5/6} \left( \frac{f}{\text{GHz}} \right)^{-7/6}$                                                                                                  |
| Primordial BH mergers: SGWB               | $\lesssim \frac{4400}{(m_1 + m_2)} \text{ Hz}$                                                                      | $h_{c,\text{sto}} \approx 5 \times 10^{-31} \left( \frac{f_{\text{ISCO}}}{\text{GHz}} \right)^{-1.07}$                                                                                                                                                                          |
| Primordial BH mergers: memory             | $\lesssim \frac{4400}{(m_1 + m_2)} \text{ Hz}$                                                                      | $h(f) \approx 5 \times 10^{-25} \text{ sec} \left( \frac{f_{\text{ISCO}}}{f} \right) \left( \frac{m_{\text{PBH}}}{10^{-5} M_\odot} \right) \left( \frac{\text{kpc}}{D} \right)$                                                                                                 |
| Primordial BH hyperbolic encounters       | $\simeq 0.5 \text{ GHz} \left( \frac{10^{-5} M_\odot}{m_{\text{PBH}}} \right) \left( \frac{R_s}{r_p} \right)^{3/2}$ | $h(f) \approx 10^{-24} \text{ sec} \left( \frac{f}{\text{GHz}} \right)^{2/3} \left( \frac{m_{\text{PBH}}}{10^{-5} M_\odot} \right)^{5/3} \left( \frac{\text{Mpc}}{D} \right)$                                                                                                   |
| Exotic compact objects                    | $\lesssim C^{3/2} \left( \frac{6 \times 10^{-3} M_\odot}{M} \right) \text{ MHz}$                                    | $h(f) \approx 10^{-31} \text{ sec} \left( \frac{f}{\text{GHz}} \right)^{-7/6} \left( \frac{m_{\text{PBH}}}{10^{-5} M_\odot} \right)^{5/6} \left( \frac{\text{kpc}}{D} \right)$                                                                                                  |
| Superradiance: annihilation               | $\simeq 5 \text{ MHz} \left( \frac{\mu}{10^{-8} \text{ eV}} \right)$                                                | $h_s(f) \approx 5 \times 10^{-30} \text{ sec} \left( \frac{m_{\text{PBH}}}{10^{-5} M_\odot} \right) \left( \frac{\text{kpc}}{D} \right)$<br>$h_{v,T}(f) \approx 10^{-26} \text{ sec} \left( \frac{m_{\text{PBH}}}{10^{-5} M_\odot} \right) \left( \frac{\text{kpc}}{D} \right)$ |
| Superradiance: nonlinear effects          | $\simeq 5 \text{ MHz} \left( \frac{\mu}{10^{-8} \text{ eV}} \right)$                                                | $h(f) \approx 10^{-27} \text{ sec} \left( \frac{m_{\text{PBH}}}{10^{-5} M_\odot} \right) \left( \frac{\text{kpc}}{D} \right)$                                                                                                                                                   |

We distinguish between coherent and stochastic sources by reporting the strain  $h(f)$  or characteristic strain  $h_{c,\text{sto}}$ , respectively. See Sect. 4.1 for details on these expressions and the assumptions made

**Table 2** Summary of stochastic sources

| Source                                         | Frequency Range                                   | Amplitude<br>$\Omega_{\text{GW}}(f)$                    | Characteristic Strain<br>$h_{c,\text{sto}}$                                         |
|------------------------------------------------|---------------------------------------------------|---------------------------------------------------------|-------------------------------------------------------------------------------------|
| Inflation: vacuum amplitude                    | Flat in the range<br>( $10^{-16}$ – $10^8$ ) Hz   | $\lesssim 10^{-16}$                                     | $\lesssim 10^{-32} \left( \frac{\text{MHz}}{f} \right)$                             |
| Inflation: extra-species                       | ( $10^5$ – $10^8$ ) Hz                            | $\lesssim 10^{-10}$                                     | $\lesssim 10^{-29} \left( \frac{\text{MHz}}{f} \right)$                             |
| Inflation: broken spatial<br>reparametrization | Blue in the range<br>( $10^{-16}$ – $10^8$ ) Hz   | $\lesssim 10^{-10}$                                     | $\lesssim 10^{-29} \left( \frac{\text{MHz}}{f} \right)$                             |
| Inflation: secondary GW<br>production          | Flat or bump                                      | $\lesssim 10^{-8}$                                      | $\lesssim 10^{-28} \left( \frac{\text{MHz}}{f} \right)$                             |
| Preheating                                     | ( $10^6$ – $10^9$ ) Hz                            | $\lesssim 10^{-10}$                                     | $\lesssim 10^{-29} \left( \frac{\text{MHz}}{f} \right)$                             |
| Oscillons                                      | ( $10^6$ – $10^9$ ) Hz                            | $\lesssim 10^{-10}$                                     | $\lesssim 10^{-29} \left( \frac{\text{MHz}}{f} \right)$                             |
| Cosmic gravitational<br>microwave background   | $f_{\text{peak}} \sim (10 - 100)$<br>GHz          | $\Omega_{\text{GW}}(f_{\text{peak}}) \lesssim 10^{-6}$  | $h_c(f_{\text{peak}}) \lesssim 10^{-31} \left( \frac{\text{MHz}}{f} \right)$        |
| Phase transitions                              | $\lesssim 10^9$ Hz                                | $\lesssim 10^{-8}$                                      | $\lesssim 10^{-28} \left( \frac{\text{MHz}}{f} \right)$                             |
| Defects                                        | Scale invariant                                   | $\Omega_{\text{rad},0} \frac{v^4}{M_{\text{Pl}}^4} F_U$ | $10^{-26} \frac{v^4}{M_{\text{Pl}}^4} F_U \left( \frac{\text{MHz}}{f} \right)$      |
| Gauge textures                                 | $\sim 10^{11} \frac{v}{M_{\text{Pl}}} \text{ Hz}$ | $\lesssim 10^{-4} \frac{v^4}{M_{\text{Pl}}^4}$          | $\lesssim 10^{-26} \frac{v^4}{M_{\text{Pl}}^4} \left( \frac{\text{MHz}}{f} \right)$ |
| Grand unification<br>primordial BH evaporation | ( $10^{18}$ – $10^{15}$ ) Hz                      | $\lesssim 10^{-8}$                                      | $\lesssim 10^{-28} \left( \frac{\text{MHz}}{f} \right)$                             |

For the conversion between energy density  $\Omega_{\text{GW}}$  and characteristic strain, see Eqs. (9) and (12). The amplitudes reported are maximum values; for all the details on how to obtain these expressions, the dependence on the parameters of the models and the assumptions behind them, see the corresponding sections above

## 5 Detection of gravitational waves at high frequencies

After the first detection of GWs at frequencies in the range (0.1–2.0) kHz (Abbott et al. 2019) and indications of a stochastic GW signal at pulsar timing arrays (Agazie et al. 2023; Antoniadis et al. 2023; Reardon et al. 2023; Xu et al. 2023), expanding the frequency coverage of the worldwide gravitational wave program is a natural next step—as it was for electromagnetic observations in the 1950s when radio, X-ray and UV astronomy became possible with new technology. As detailed in the previous section, many exciting questions in astrophysics, cosmology, and fundamental physics are tied to GW signals with frequencies well above the capabilities of current detectors or their upgrades. Even GW upper limits in regions of parameter space with no known Standard Model sources may be valuable in restricting current or future physical theories.

The detection of gravitational waves at LIGO, Virgo, and KAGRA requires measuring minuscule space-time deformations, smaller than the size of a proton (see Sect. 5.1). Achieving this has required the development of highly efficient mechanical-to-electromagnetic transducers. Similarly, a large class of high-

frequency GW detector concepts relies on detecting mechanical deformations (see Sect. 5.2), with the main differences between different detector designs being the method used to engineer these transducers. A second large class of high-frequency GW detectors relies instead on the direct coupling between gravity and electromagnetism (see Sects. 5.3 to 5.6). In electromagnetism in curved spacetime, the effect of a GW is to alter the vacuum's dielectric properties, to generate effective currents that source induced electromagnetic fields, and to allow for GW–photon mixing. Relying on the coupling of GW to electromagnetism removes the need for a mechanical-to-electromagnetic transducer, though at the cost of working with a stiff system: Maxwell's equation in vacuum, governed by the speed of light, are more difficult to deform by a GW-induced force than typical materials of, e.g., resonant bars, which are characterized by the speed of sound  $v_s/c \sim 10^{-5}$  rather than the speed of light. While the technological challenges differ between observational methods, the core concepts are often closely linked to specific ranges of GW frequency, which explains the use of very different technologies across the frequency spectrum, also in the high frequency range. For a heuristic approach to estimate the sensitivity for a range of these concepts, see D'Agnolo and Ellis (2024).

In the frequency range from kHz to GHz, the GW frequency can be matched to the mechanical or electromagnetic resonant modes of a detector. One can thus profit from resonant enhancements, which can significantly boost the sensitivity, provided that the experiment's reaction time (ring-up time) is compatible with the duration of the GW source. For a meter-scale experiment, mechanical resonances lie in kHz regime, while EM resonances lie in the GHz regime. Weber bars are the most well-known examples of mechanical resonant mass detectors, and modern versions with improved mechanical-to-electromagnetic transducers are being developed particularly for detecting high-frequency gravitational waves (Sect. 5.2). Regarding the electromagnetic coupling, GWs can induce an oscillating electromagnetic field within a microwave cavity placed in a static magnetic field, or the oscillating EM field can be read out through a resonant LC circuit (Sect. 5.3).

At frequencies much higher than GHz, it becomes increasingly challenging to design an apparatus that is small enough to match the GW wavelength for resonant enhancement. In this frequency range, photon regeneration experiments offer an alternative (Sect. 5.4). Although these experiments were initially developed for axion searches, they can be optimized for detecting high-frequency gravitational waves. The detection range typically depends on the type of photon detector used (CCDs, X-ray detectors, etc.). As photon counting detectors these instruments are typically sensitive to the GW intensity (i.e., the square of the GW strain). A lower limit to the frequency range in which such detectors are sensitive often arises due to the detector vessel functioning as an electromagnetic waveguide with limited transmissivity at low frequencies, and due to challenges of implementing single photon detection at infrared frequencies. Instead of GW interactions with a laboratory setup, the magnetic fields of astrophysical or cosmological objects, such as neutron stars or large-scale galactic and cosmological structures, can also be leveraged for GW detection (see Sect. 5.6). However, backgrounds are more difficult to control in these environments compared to laboratory-based

experiments. Other proposals that leverage the direct coupling between gravity and electromagnetism are based on observing modifications in atomic quantum states (see Sect. 5.7). These include detection methods based on the interaction of GWs and fermion spins, or on alterations in electron wave functions.

In this section, we will often use the short-hand notation  $S_n = S_h^{\text{noise}}$  to denote the noise-equivalent strain sensitivity (or strain sensitivity for short) of detectors. We will do this in particular when quoting sensitivities from the literature throughout the text, whereas we will use the more explicit notation  $S_h^{\text{noise}}$  introduced in Sect. 2 when there is a danger of confusing different power spectral densities in the discussion.

## 5.1 Laser interferometers and resonant mass detectors and their limitations

The first GWs were detected by the Advanced LIGO (Abbott et al. 2016a) detectors in the US and the Advanced Virgo detector in Italy (Acernese et al. 2015). In early 2020, the Japanese KAGRA detector (Aso et al. 2013) joined LIGO's third observing run. These detectors are all Fabry–Perot interferometers, using large suspended mirrors several kilometers apart. Several other detectors of this type are in the design phase. These detectors typically have their peak sensitivity at frequencies of a few hundred Hz.

However, some future detectors are designed specifically to expand the detection band towards either lower or higher frequencies. To efficiently probe frequencies below 10 Hz in terrestrial detectors, cryogenically cooled mirrors, large beam diameters, and operation underground are considered (Abernathy et al. 2011; Adhikari et al. 2020). LISA, also based on laser interferometry, is a planned satellite-based detector to increase the arm length beyond the possibilities on Earth and to reduce environmental noise sources such as seismics (Amaro-Seoane et al. 2017). LISA will have its peak sensitivity in the mHz range. To increase interferometer sensitivity towards higher frequencies, options are an increase of laser power and/or resonant operation. The planned Australian NEMO detector will be targeting frequencies of up to several kHz, see Sect. 5.1.1 below.

While increasing the arm length of an interferometer increases the strain signal in some frequency bands, longer arms are only really beneficial as long as the GW wavelength is longer than the interferometer arms. For significantly shorter wavelengths (frequencies  $\gtrsim$  MHz), interferometers with arm lengths of order meters are more suitable, but are of course at the same time limited by the smaller strain sensitivity achievable with shorter arms. This constitutes the main limitation of laser interferometers, used as direct strain meters, towards higher GW signal frequencies.

A concept to detect GWs which existed prior to interferometers are resonant bar detectors, initially proposed and built by Joseph Weber in the 1960s. Their modern successors, resonant spheres, have peak sensitivities at several kHz. In Sect. 5.1.3, we will give a summary of these resonant spheres.



### 5.1.1 Neutron star extreme matter observatory (NEMO)

The first detection of a binary neutron star merger in 2017 (Abbott et al. 2017b) has increased the interest in the development of GW detectors with sensitivity in the few kHz regime, capable of detecting the merger and ringdown part of the waveform (Martynov et al. 2019). It is expected that such detectors will need to have strain sensitivities approaching  $\sqrt{S_n} \simeq 10^{-24} \text{ Hz}^{-1/2}$  in the frequency range (1–4) kHz to observe several events per year. This sensitivity should be achieved by the third generation terrestrial GW detectors that are anticipated to come online in the later half of the 2030s (Abbott et al. 2017a; Punturo et al. 2010). The Australian GW community is currently exploring the feasibility of a new detector, ‘NEMO’, dedicated to detecting this merger phase and the following ringdown as well as testing third generation technology on a smaller scale (Ackley et al. 2020; Bailes et al. 2019; Adya et al. 2020). The planned sensitivity of this detector would reach  $\sqrt{S_n} \simeq 10^{-24} \text{ Hz}^{-1/2}$  in the range (1–2.5) kHz (Ackley et al. 2020). This detector will work in collaboration with the existing second generation GW detector network that will provide sky localization for electromagnetic follow-up.

The dominant high-frequency noise source for interferometric GW detectors is quantum phase noise, or shot noise as it is otherwise called. The magnitude of this noise source is inversely proportional to the square of the product of the circulating power incident on the test masses and the length of the arms of the detector. This generally necessitates extremely high powers in the arms of the interferometers ( $\approx 5 \text{ MW}$  in the case of NEMO). Such high circulating power leads to technical issues such as parametric and tilt instabilities, as well as thermally induced distortions. These issues can be challenging to deal with, but a dedicated high-frequency detector promises to make their mitigation easier. This is because sacrificing some sensitivity at low frequencies permits larger actuation on the test masses to correct instabilities and distortions. Further, relaxing the low-frequency sensitivity relaxes requirements on seismic isolation and test mass suspension systems, significantly reducing the cost of these systems.

### 5.1.2 Interferometers up to 100 MHz

As was first pointed out in Mizuno (1995), in laser interferometers the total stored energy in the form of circulating laser power sets a limit on the achievable sensitivity and bandwidth as a consequence of the quantum Cramér–Rao bound. For a given laser power, large bandwidth and good strain sensitivity need to be balanced against each other, as increasing both at the same time is impossible. While opto-mechanical resonances can be introduced in the signal response of interferometers to shape the sensitivity curve for specific frequencies (Somiya et al. 2016; Korobko et al. 2018), it appears unlikely that the stored laser power can be further increased by several orders of magnitude. Therefore, broadband interferometric detectors reaching into the MHz range (while maintaining LIGO or Virgo-level strain sensitivity) seem not to be a viable option when taking also the arm-length argument from above into account.

Nevertheless there are three notable efforts (two existing and one under construction) of laser interferometers in the MHz range, which currently set the best experimental upper limits on GWs in their respective frequency bands.

One option is to build interferometers with a bandwidth of order kHz, but centered around much higher frequencies. See Akutsu et al. (2008) for upper limits from such a system operating at 100 MHz. The detector uses a synchronous recycling architecture based on a resonant recycling cavity of dimension 75 cm and a Nd:YAG laser with a power output of 0.5 W. The limit on stochastic GW signals was reported to be  $\sqrt{S_n} \sim 10^{-16} \text{ Hz}^{-1/2}$ , setting a bound on the characteristic strain of  $h_{c,\text{sto}} \lesssim 7 \times 10^{-14}$ . A study of the potential of this technique (Nishizawa et al. 2008) showed that a sensitivity of  $10^{-20} \text{ Hz}^{-1/2}$  is possible at 100 MHz with a bandwidth of 2 kHz, but the sensitivity decreases with increasing frequency and is not competitive above 1 GHz.

The sensitivity of a single instrument can be surpassed by correlating two co-located instruments when searching for stochastic signals. An example is the *Holometer* experiment at Fermilab, which consisted of two co-located power recycled Michelson interferometers with 40-meter long arms. While their primary research target has been signatures of quantization of spacetime, they are also excellent GW detectors, reaching a sensitivity of  $\sqrt{S_n} \simeq 10^{-21} \text{ Hz}^{-1/2}$  in the band (1–13) MHz when cross-correlating both detectors (Chou et al. 2017) over a 103 hr dataset. See Chou et al. (2017) for both a search for stochastic GW backgrounds and monochromatic GWs. Using a 704 hr dataset from, Martinez and Kamai (2020) concluded that there are no identifiable sources with harmonic frequency patterns (i.e. emitting in integer multiples of a fundamental frequency) such as cosmic string loops and eccentric BH binaries emitting in the frequency range (1–25) MHz.

Following a similar detection concept is the Quantum-Enhanced Space-Time (QUEST) experiment at Cardiff University. It consists of two wide-band table-top interferometers sensitive in the (1–100) MHz band (Vermeulen et al. 2021). Cross-correlating these detectors in a coincident observing run of  $10^4$  s, upper limits of about  $\sqrt{S_n} \simeq 3 \times 10^{-20} \text{ Hz}^{-1/2}$  on a stochastic GW background between 13 and 80 MHz have been achieved (Patra et al. 2025). The team plans to increase the bandwidth to 200 MHz and to increase the sensitivity by another two orders of magnitude.

### 5.1.3 Spherical resonant masses

The principle of a *resonant mass detector* is that its vibrational eigenmodes can get excited by a GW. These mechanical oscillations are transformed into electromagnetic signals, using electromechanical transducers, and amplified by electrical amplifiers. These resonant detectors have a relatively small bandwidth, usually of less than 100 Hz. Thermal noise, Johnson–Nyquist noise, pump phase noise (if the transducer is parametric), back-action noise, and amplifier noise are the internal noise sources in this kind of detector. The resonant mass antenna and transducers must be made of high-quality factor materials in order to decrease thermal (mechanical) and Johnson–Nyquist (electrical) noise.

The idea of a spherical resonant mass antenna for GW detection has a long history and was first proposed in Forward (1971), followed by several decades of exploration and proposals (Wagoner and Paik 1977; Hamilton 1990; Johnson and Merkowitz 1993). More recently, the Mario Schenberg detector (Aguiar 2011; Da Silva Costa and Aguiar 2014) in São Paulo, Brazil, and Mini-GRAIL (Gottardi et al. 2007), in Leiden, Netherlands have developed the concept further. At present, both detectors have been decommissioned, but Schenberg is planned to be reassembled at INPE, in São José dos Campos, about 100 km from its initial site at the University of São Paulo.<sup>29</sup> Such detectors have a bandwidth of 50–100 Hz with peak frequencies around 3 kHz for the quadrupole modes. To increase the frequency range, a xylophone configuration of several spheres has been proposed (Harry et al. 1996).

In 2004, Mini-GRAIL operating at a temperature of 5 K reached a peak strain sensitivity of  $\sqrt{S_n} \simeq 1.5 \times 10^{-20} \text{ Hz}^{-1/2}$  at a frequency of 2942.9 Hz. Over a bandwidth of 30 Hz, the strain sensitivity was about  $\sqrt{S_n} \simeq 5 \times 10^{-20} \text{ Hz}^{-1/2}$  (Gottardi et al. 2007). Schenberg, operating also at 5 K, reached strain sensitivities of  $\sqrt{S_n} \simeq 1.1 \times 10^{-19} \text{ Hz}^{-1/2}$  for its quadrupolar modes ( $\sim 3.2$  kHz) and  $\sqrt{S_n} \simeq 1.2 \times 10^{-20} \text{ Hz}^{-1/2}$  for its monopolar mode ( $\sim 6.5$  kHz) in 2015 (Oliveira and Aguiar 2016). Both Schenberg and Mini-GRAIL could reach sensitivities around  $\sqrt{S_n} \simeq 10^{-22} \text{ Hz}^{-1/2}$  when operating at 15 mK. Schenberg, because it uses parametric transducers, can reach higher sensitivities if it implements squeezing of the signal. On a similar time scale the resonant bar detector AURIGA near Padua, Italy, reported reaching strain sensitivities of  $\sqrt{S_n} \simeq 10^{-20} \text{ Hz}^{-1/2}$  at frequencies around 900 Hz over a bandwidth of 100 Hz (Vinante 2006).

Spherical antennas provide more information compared to the classical bar antennas because of their quadrupole modes, while also being significantly more sensitive due to their favorable geometry (they offer a larger cross-section at identical mass). From the output of six transducers tuned to the quadrupole modes of a sphere, one can obtain complete information about the polarization and direction of the incoming wave.

The conceptual difficulties in pushing this technology to higher frequencies are similar to the issues faced by laser interferometers: it requires smaller resonating spheres and consequently measuring smaller absolute displacements to achieve the same strain sensitivity. Contrary to laser interferometers, resonant mass detectors have not yet reached the standard quantum limit. It thus seems unlikely that this technology can be pushed significantly beyond the kHz region.

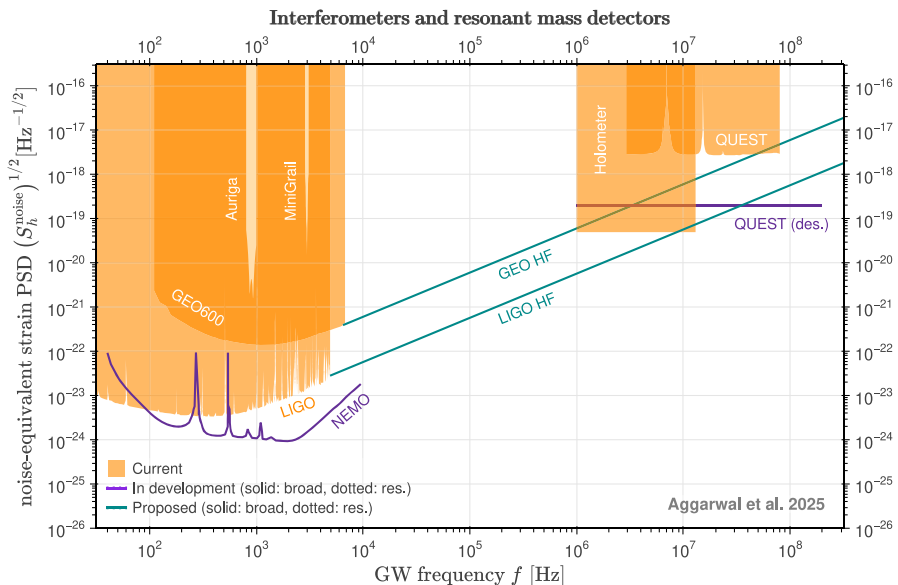
An additional challenge for resonant detectors in general is their small bandwidth,  $\Delta f_{\text{det}} \sim f/Q$ , where the quality factor  $Q \gg 1$  plays a key role in enhancing the sensitivity on resonance. For transient high-frequency GW signals

<sup>29</sup> These detectors had much smaller masses (1.15 and 1.3 tonnes, respectively) and diameters (65 and 68 cm, respectively) than originally proposed in the 1990s (up to 120 tonnes, 3 m, resonant around  $\sim 700$  Hz).

with  $\dot{f} \sim f^2$  (such as PBH binaries shortly before the merger, see Sect. 4.1.2) this implies that the signal spends only a very short amount of time, of order  $(fQ)^{-1}$ , inside the sensitivity band. This time window is often too short to fully ring up the resonance, in which case the high quality factor is not fully brought to bear. This needs to be taken into account when computing the sensitivity of resonant detectors to transient signals.

### 5.1.4 Summary: sensitivities of interferometers and resonant mass detectors

Figure 9 provides an overview of the typical strain sensitivities achieved by the interferometers and resonant mass detectors described in this section. As in Fig. 1, instruments which have placed limits on (or detected) GWs are shown in orange, concepts under active R&D are shown in purple, and other proposals are shown in cyan. Note that LIGO, the Holometer and QUEST consist of two separate detectors each and can thus increase their sensitivity by cross-correlating the data streams. Figure 9 shows the strain sensitivity of a single interferometer. Moreover, we use the cyan color to show a naive extrapolation of the LIGO and GEO sensitivities to higher frequencies [see also Schnabel and Korobko (2025)]. Extending the sensitivity band of these detectors in practice requires overcoming challenges in data acquisition, noise control, and calibration, which requires dedicated R&D.



**Fig. 9** Strain sensitivity of (individual) interferometers [LIGO O4a (Soni et al. 2025), GEO600 (Lough et al. 2021), Holometer (Chou et al. 2017), QUEST (Patra et al. 2025)] and resonant mass detectors [AURIGA (Vinante 2006), Mini-GRAIL (Gottardi et al. 2007)], together with the projected sensitivity of the interferometer NEMO (Ackley et al. 2020) and an extrapolation of the LIGO and GEO sensitivity to higher frequencies (see text). Color coding as in Fig. 1

Most likely the sensitivities shown here cannot be reached while simultaneously optimizing the sensitivity around 100 Hz.

## 5.2 Modern resonant mass detectors

Since Joseph Weber's pioneering developments in the late 1960s, the ability to detect and measure geometrical changes in various systems has progressed significantly. This progress is in particular due to techniques that go beyond the traditional use of large bars or spheres, which relied on monitoring *massive* resonant systems with high quality factors,  $Q$ . (Modern versions of such systems are discussed in Sect. 5.1.3.) In particular, using smaller resonators allows for cutting-edge sensing methods, four of which we will explore in this section: optically levitated sensors, bulk acoustic-wave devices, microwave cavities and magnetic Weber bars.

### 5.2.1 Optically levitated sensors

Optically levitated dielectric sensors have been identified as a promising technique for resonant GW searches over a wide range of frequencies from a few kHz to  $\sim 300$  kHz (Arvanitaki and Geraci 2013; Aggarwal et al. 2020). A dielectric nanoparticle suspended at the anti-node of a standing laser wave within an optical cavity will experience a force when a passing GW causes a time-varying strain on the physical length of the cavity. The particle will be displaced from the location of the trapping light anti-node, resulting in periodic kicks on the particle at the frequency of the GW space-time disturbance. The trapping frequency and mechanical resonance linewidth are widely tunable based on the laser intensity and laser cooling parameters chosen.

When detecting the resulting displacement of the particle at the trapping resonance frequency, the sensitivity is limited by Brownian thermal noise in the particle itself rather than the displacement detection of the particle. This results in improved sensitivity at higher frequency (unlike traditional interferometer style detectors which experience decreased sensitivity at high frequency due to laser shot noise) (Arvanitaki and Geraci 2013). The low-friction environment made possible by optical levitation in ultra-high vacuum enables extremely sensitive force detection (Ranjit et al. 2016), which becomes ultimately quantum-limited by photon-recoil heating from discrete scattering events of individual trap laser photons (Jain et al. 2016).

A 1-meter prototype Michelson-interferometer configuration detector called the 'Levitated Sensor Detector' (LSD) is under construction at Northwestern University in the US, with a target sensitivity of better than  $\sqrt{S_n} \sim 10^{-19} \text{ Hz}^{-1/2}$  at  $f \approx 10$  kHz and  $\sqrt{S_n} \sim 10^{-21} \text{ Hz}^{-1/2}$  at  $f \approx 100$  kHz (Aggarwal et al. 2020; Winstone et al. 2022). In addition, fiber-based approaches are being investigated to permit longer cavities without the need for expensive optics (Pontin et al. 2018). The ultimate strain sensitivity of a 10-meter room-temperature instrument is estimated to be better than approximately  $\sqrt{S_n} \sim 10^{-20} \text{ Hz}^{-1/2}$  at  $f \approx 10$  kHz and

$\sqrt{S_n} \sim 10^{-22} \text{ Hz}^{-1/2}$  at  $f \approx 100 \text{ kHz}$ . For a cryogenic 100-meter apparatus, this can be improved by more than an order of magnitude across much of the frequency range (Aggarwal et al. 2020). A detailed analysis of the search reach for GWs produced by axions via the BH superradiance process is provided in Aggarwal et al. (2020).

Another interesting direction is the use of optically-trapped levitated membranes (Chang et al. 2012). This idea is based on the use of nano-mechanical resonators which constitute chip-scale implementations of a harmonic oscillator of thin films with high tensile stress, achieving extremely high  $Q$ -factors ( $> 10^{10}$ ) (Beccari et al. 2022). They have a wide range of applications in sensing and cavity optomechanics (Aspelmeyer et al. 2014). Work towards the design of a corresponding prototype detector is in progress at DESY, together with related R&D studies (Reinhardt et al. 2024). The realization of this detector, comprising membranes with  $Q > 10^{12}$ , is a longer term goal.

Among other possible ideas for optomechanical systems to detect GWs, it has also been suggested to use of a volume of superfluid  $^4\text{He}$  that responds to mechanical forces. This effect may be read-out by a membrane monitored using interferometric methods. A sensitivity of  $\sqrt{S_n} < 8 \times 10^{-19} \text{ Hz}^{-1/2}$  has been claimed around  $f \approx 100 \text{ kHz}$  (Vadakkumbatt et al. 2021).

The field of optically levitated sensors is rapidly developing, see, e.g., Millen et al. (2020), Gonzalez-Ballesterio et al. (2021), Winstone et al. (2023). In this regard, it is plausible to assume that the efforts of (Arvanitaki and Geraci 2013; Aggarwal et al. 2020; Winstone et al. 2022) are only the first steps towards detectors with much better sensitivity to HFGWs in the near future.<sup>30</sup>

A related approach based on detecting the motion of superconducting spheres levitated in a magnetic field has been proposed in Carney et al. (2025), and is discussed in Sect. 5.2.4.

### 5.2.2 Bulk acoustic wave devices

Bulk acoustic wave (BAW) devices are one of the pillars of frequency control and frequency metrology (Galliou et al. 2013). In the simplest case, a piece of piezoelectric material is sandwiched between two electrodes, converting acoustic waves inside the material into electrical signals. With its relatively compact size and robustness, this technology gives one of the best levels of frequency stability near one second of integration time. More recently, it was demonstrated that quartz bulk acoustic wave devices exhibit extremely high-quality factors (up to  $8 \times 10^9$ ) at cryogenic temperatures for various overtones of the longitudinal mode covering the frequency range (5–700) MHz (Galliou et al. 2013; Goryachev et al. 2013). For this reason, it was proposed to use the technology for various tests of fundamental physics (Galliou et al. 2013) such as Lorentz invariance tests (Lo et al. 2016),

<sup>30</sup> Sensitivities to forces down to yocto-Newtons have been theoretically claimed (Liang et al. 2023). These studies are far from being realistic, but they show that there is ample space for progress.

quantum gravity research (Bushev et al. 2019) and searches for high-frequency GWs (Goryachev and Tobar 2014). For the latter purpose, a bulk acoustic wave device represents a resonant mass detector whose vibration could be read out through the piezoelectric effect and Superconducting Quantum Interference Devices (SQUIDs). The approach has the following advantages: (i) highest quality factor (high-sensitivity); (ii) internal (piezoelectric) coupling to SQUIDs (Goryachev et al. 2014; iii) allows parametric detection methods; (iv) a large number of sensitive modes ( $> 100$ ) in a single device; (v) modes scattered over a wide frequency range (1–700) MHz; (vi) well-established and relatively inexpensive technology (mass production); (vii) high-precision (insensitive to external influences such as seismic vibration and temperature fluctuations), and (viii) the possibility of building arrays of detectors to extend the frequency range towards lower frequencies and/or to achieve better sensitivity. On the other hand, in practice, identically manufactured devices exhibit significant dispersion in mode frequencies at low temperatures, thus limiting the accuracy of such arrays. The level of sensitivity of bulk acoustic wave detectors is estimated to be at the level of  $\sqrt{S_n} \simeq 2 \times 10^{-22} \text{ Hz}^{-1/2}$ , depending on the mode geometry (Goryachev and Tobar 2014). With additional investment into research and development, this sensitivity could be improved and the frequency range extended down to hundreds of kHz.

A search for high-frequency GWs with single bulk acoustic wave devices and two modes, operated at  $\sim 4 \text{ K}$ , has been running at the University of Western Australia since November 2018. Recently, two interesting events were observed in these searches, at different frequencies around few MHz (Goryachev et al. 2021). The origin of these events cannot be determined with current data, but given their strength they are not considered to be viable GW candidates [see also Lasky and Thrane (2021)]. These results have triggered significant interest in further advancing this detection technique. In this context, the possibility of building arrays of BAWs and multimode read-out is being pursued by the Bulk Acoustic Wave Sensors for a High-frequency Antenna (BAUSCIA) program in Milano and by the Multimode Acoustic Gravitational Wave Experiment (MAGE) at the University of Western Australia (Campbell et al. 2023b). The goal is to build networks of  $O(10)$  BAWs, accessing  $O(100)$  frequency modes.

Further improvements could come from reaching the quantum ground state of the system (Campbell et al. 2023a), or, in general, from counting phonons, and performing quantum state tomography or quantum manipulation and characterization of the states of a BAW resonator (Chu et al. 2018; von Lüpke et al. 2022; Bild et al. 2023). Recent theoretical characterization aiming at optimizing the searches of HFGWs with phonons can be found in Kahn et al. (2024). Finally, a multi-mode resonant bar concept has been proposed in Tobar et al. (2025) to absorb GWs with a large mass object, while reading it out with a much lighter one. With the individual components studied in earlier works, see e.g. Tobar (1995), Tobar et al. (2000), a key next step would be the construction of a prototype to understand and verify in more detail their interplay and the achievable sensitivity of this proposal.



### 5.2.3 Deformation of microwave cavities

An electromagnetic resonator prepared such that it has two nearly degenerate modes,  $\omega_1$  and  $\omega_2$ , may act as a sensitive device to detect GWs. The idea is to inject power into only one of the modes, while an incident GW can resonantly transfer power from this loaded mode 1 into the otherwise quiet mode 2 if the condition  $|\omega_2 - \omega_1| - \omega_G \lesssim \Delta\omega_2$  is met, where  $\Delta\omega_2$  is the width of mode 2, which is typically wider than the width of mode 1. This process of combining signals with two frequencies is often called “*heterodyning*”, hence the name given to the general approach of *heterodyne detection*. Two mechanisms exist whereby the GW can transfer power from the loaded mode into the quiet mode: directly through the interaction with the electromagnetic energy stored in the cavity in mode 1, or indirectly by deforming the cavity walls in such a way that mode 1 is coupled to mode 2. The latter effect dominates in most of the frequency range of interest (sub-GHz) due to the small speed of sound in materials.

The first studies considering the mechanical coupling of GWs to electromagnetic resonators appeared in the late 70 s. Pegoraro et al. (1978b, 1978a) proposed and studied a system with a sharp resonance at about 1 GHz, while Caves (1979) contains a theoretical study of a microwave cavity with a high mechanical quality factor. The first experimental efforts based on these ideas were reported in Reece et al. (1982, 1984). These schemes offered sensitivity to a range of frequencies from few kHz to GHz, limited by different noise sources, particularly thermal noise at low frequencies. The idea was further developed and eventually started to take shape in the Microwave Apparatus for Gravitational waves Observation (MAGO) (Ballantini et al. 2005), which we now describe.

MAGO consists of two microwave resonators (spheres in this case, to maximize the sensitivity), coupled through an *a priori* tunable link. This allows for a control of the frequency split of the ground states of the coupled system and achieve resonance modes with characteristic frequency  $\sim$  GHz, but with energy differences as low as  $\mathcal{O}(10)$  kHz. As a result, the device can in principle detect GWs from 10 kHz up to MHz and beyond. This detection concept led to the MAGO proposal for a scaled-up experiment with 500 MHz cavities as a CERN–INFN collaboration. Although the final project was not funded, three SRF cavities were built during the R&D activities. The first one (a pill-box cavity) was used as a proof-of-principle experiment, which demonstrated the working principle and the development of an RF system to drive and read out the cavity with the necessary precision (Ballantini et al. 2005). The third cavity was a spherical 2-cell cavity with an optimized geometry, which was never treated and tested (it was placed on display at the University of Genoa after the R&D efforts stopped).

The idea was revived in recent work (Berlin et al. 2023) with an improved theoretical treatment and estimate of the various noise sources, as well as the resulting sensitivity of a cavity similar to the third MAGO prototype. The authors found that the noise-equivalent strain PSD could reach  $\sqrt{S_n} \sim 10^{-21} \text{ Hz}^{-1/2}$  in the frequency range  $100 \text{ kHz} \lesssim 2\pi f \lesssim \text{GHz}$ . Furthermore, the authors pointed out that by overcoupling to the signal mode of the cavity, the experiment can be run in



broadband mode. (Overcoupling refers to a situation where the energy leaking through the coupling mechanism exceeds the intrinsic loss within the cavity. This effectively reduces the quality factor of the cavity, but increases the bandwidth.) In broadband mode, sensitivities better than  $\sqrt{S_n} \lesssim 10^{-18} \text{ Hz}^{-1/2}$  across two decades in frequency centered around 100 kHz could be achieved in a single measurement.

These results lead to a renewed interest in the heterodyne detection with microwave cavities. Currently, with the third MAGO cavity that was on display in Genoa, DESY, the University of Hamburg, and Fermilab continue collaborative R&D studies (Fischer et al. 2024). The first goal is to obtain a measurement with the MAGO prototype cavity in an existing cryostat at Fermilab, which would lead to a first (albeit weak) bound in the 10–100 kHz range. Long-term goals include developing an improved cavity design, engineering a dedicated low-noise cryostat and suspension system to significantly improve the sensitivity, and ultimately establish coordinated HFGW observatories at DESY and Fermilab.

Further improvements may be possible with larger cavity masses and volumes, as well as with better read-out strategies. Also, the cost of MAGO-like cavities is low enough that operating networks of detectors in different geographic locations may be realistic strategy for enhancing the sensitivity. These efforts are notably pursued within the GravNet collaboration (GravNet collaboration 2024) including partners from INFN Frascati (Italy), IFAE/ICREA Barcelona (Spain), as well as the Universities of Bonn and Mainz (Germany).

### 5.2.4 Magnetic Weber bars

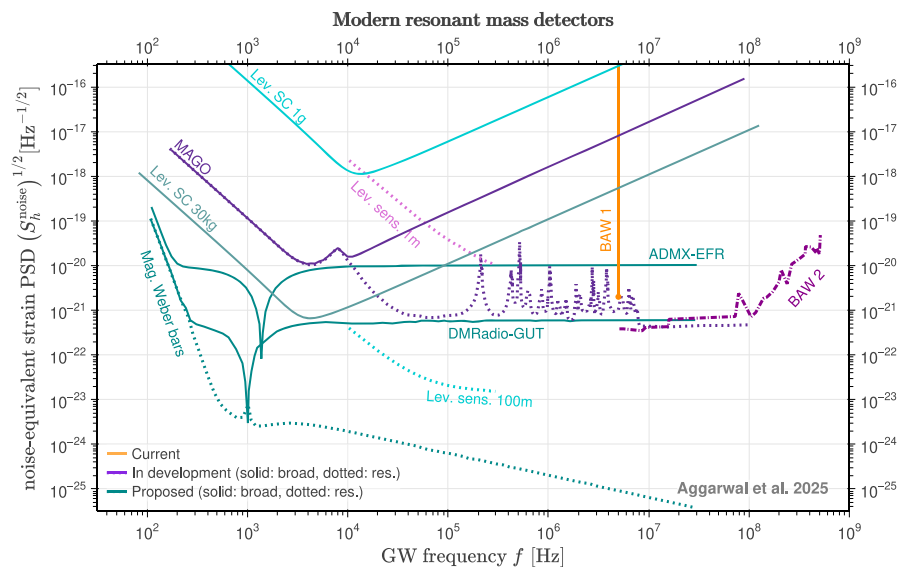
A key challenge in resonant mass detectors is the efficient readout of the energy stored in mechanical deformation. In view of this, Domcke et al. (2025b) proposed a superconducting magnet, operated in persistent mode, as a resonant mass detector. A passing gravitational wave leads to a deformation of the current-carrying superconducting coils, modifying the magnetic field. A pickup loop placed close the end caps of a solenoidal magnet and coupled to a SQUID can detect this small, oscillating change in the background magnetic field. The advantage of this setup is that the induced magnetic fields, which are of  $\mathcal{O}(hB_0)$ , can profit from the large amount of energy stored in the background magnetic field  $B_0$  without any significant transducer loss. In particular, the MRI magnet that is being deployed for the ADMX-EFR experiment would allow for an estimated broadband GW strain sensitivity of  $\sqrt{S_n} \sim 10^{-20} \text{ Hz}^{-1/2}$  for frequencies from a few kHz to about 10 MHz, with a peak sensitivity down to  $\sqrt{S_n} \sim 10^{-22} \text{ Hz}^{-1/2}$  at a kHz, exploiting a mechanical resonance.

A related approach was proposed in Carney et al. (2025), considering a levitated superconducting sphere in a magnetic field. The superconducting sphere expels the magnetic field, thus leading to a rather inhomogeneous field configuration in its vicinity. A passing gravitational wave results in an oscillation of the superconducting sphere with respect to a pickup loop placed in its vicinity, and consequently to an oscillation of the magnetic flux measured by the pickup loop. Such a system

could achieve broadband strain noise sensitivity of  $\sqrt{S_n} \sim 10^{-19} \text{ Hz}^{-1/2}$  for frequencies from 10 kHz to 1 MHz.

### 5.2.5 Summary: strain sensitivities of modern resonant mass detectors

Figure 10 provides an overview of the projected strain sensitivities of a range of modern resonant mass detectors. As in Fig. 1, instruments which have placed limits on (or detected) GWs are shown in orange, concepts under active R&D are shown in purple, and other proposals are shown in cyan. Solid lines indicate broadband sensitivities whereas dashed lines indicate a resonant search requiring a scanning strategy. Where available, we show both the projected sensitivity from the initial stage of an experiment as well as possible upgrades. In particular, for levitated sensors we show the 1 m disc prototype and a future 100 m stack setup (Aggarwal et al. 2020), for bulk acoustic wave devices we show estimates for a multimodal cavity cooled to 20 mK (Goryachev and Tobar 2014), for microwave cavities we show the projected thermal noise limited broadband and resonant sensitivities (Berlin et al. 2023), for magnetic Weber bars we show the estimated sensitivities using an MRI magnet as well as the larger magnet envisioned for the DMRadioGUT axion experiment, assuming moreover a resonant readout strategy for the latter (Domcke et al. 2024b), and for levitated superconducting spheres we show the estimated sensitivity for 1 g and 30 kg spheres (Carney et al. 2024).



**Fig. 10** (Projected) strain sensitivity of modern resonant mass detectors: levitated sensors (Lev. sens.) (Aggarwal et al. 2020), bulk acoustic wave devices (BAW) (Goryachev and Tobar 2014), MAGO 2.0 (Berlin et al. 2023), magnetic Weber bars (Domcke et al. 2025b) and levitated superconducting spheres (Lev. SC) (Carney et al. 2025). Color coding as in Fig. 1

### 5.3 Electromagnetic oscillators

Combining Einstein's theory of general relativity with classical electromagnetism reveals a coupling between gravitational and electromagnetic (EM) waves. This coupling allows for a range of applications for electromagnetic GW detectors, including the conversion of GWs to photons and vice versa (Gertsenshtein 1962; Boccaletti et al. 1970; Füzfa 2016, 2017).

To see this, let us consider the action of electromagnetism in curved spacetime with the metric  $g_{\mu\nu}$  (Landau and Lifshitz 1975),

$$S = \int d^4x \sqrt{-g} \left( -\frac{1}{4} g^{\mu\alpha} g^{\nu\beta} F_{\mu\nu} F_{\alpha\beta} \right), \quad (106)$$

with  $g \equiv \det g_{\mu\nu}$ , and with  $F_{\mu\nu} \equiv \partial_\mu A_\nu - \partial_\nu A_\mu$  the electromagnetic field strength tensor. Expressing the metric as  $g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$  with  $\eta_{\mu\nu}$  denoting a flat Minkowski background and  $h_{\mu\nu}$  a GW with  $|h_{\mu\nu}| \ll 1$ , we obtain

$$S = \int d^4x \left( -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + j_{\text{eff}}^\mu A_\mu \right), \quad (107)$$

where

$$j_{\text{eff}}^\mu \equiv \partial_\nu \left( -\frac{1}{2} h F_0^{\mu\nu} + h^\nu{}_\alpha F_0^{\mu\alpha} - h^\mu{}_\alpha F_0^{\nu\alpha} \right) + \mathcal{O}(h^2), \quad (108)$$

with  $h = h^\mu{}_\mu$ , and with  $F_0^{\mu\nu}$  denoting the flat space background EM field. Therefore, in the presence of a background magnetic field ( $F_0^{\mu\nu}$ ) a GW generates an effective current oscillating with the GW frequency, which sources induced electromagnetic signals. (See Appendix for other theoretical approaches to GW–EM couplings.)

Expressing the impact of a GW as an effective current highlights possible synergies with axion searches, given that an axion background field  $a$  also leads to an effective current. In the axion case, the current is of the form  $j_{\text{eff}}^a \sim (\partial_\nu a) \tilde{F}^{\mu\nu}$ , with  $\tilde{F}_{\mu\nu} \equiv \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} F_{\rho\sigma}$ . This has motivated a range of proposals relying on existing or planned axion experiments (Ejlli et al. 2019; Berlin et al. 2022; Domcke and García-Cely 2021; Tobar et al. 2022). These experiments typically feature a strong magnetic field and then search for EM signals induced by an axion or axion-like particle. Identical or similar experimental arrangements can also be used to search for GWs, as detailed below.

Many factors enter when estimating the sensitivity of a given experimental setup. The GW couples not only to the electromagnetic fields but also to the mechanical support structure. In the limiting cases of a GW frequency far above or below the mechanical resonance frequencies, this can be treated fairly easily in the free-falling or rigid limit, respectively, whereas the intermediate regime requires a more careful treatment (Ratzinger et al. 2024). When estimating the signal strength, it is moreover important to account not only for the effective current in the bulk of the magnetic volume but also for effective surface currents on its boundary (Domcke et al. 2024).

The data analysis of axion searches is optimized for persistent coherent signals, so dedicated searches are necessary to search, e.g., for PBH mergers or stochastic signals, which lead to signals of low coherence and/or very short duration. The sensitivity of techniques relying on relatively long integration times and/or high signal coherence (such as the ring-up of cavities) need to be carefully re-evaluated in this regime. Moreover, in most of the proposals outlined below, the coupling factor between the GW and the instrument has been calculated analytically relying on some simplifying assumptions. In a realistic setup, numerical simulations and calibration measurements will be required to determine the relevant order one corrections accurately. Below, all this has been taken into account to the best of our knowledge, unless specified otherwise.

### 5.3.1 Microwave cavities

There are many axion experiments utilizing microwave cavities in strong magnetic fields, such as ADMX Bartram et al. (2021), CAPP Kwon et al. (2021), HAYSTAC Zhong et al. (2018), or ORGAN Quiskamp et al. (2022, 2024). These experiments are designed to detect coherently oscillating axion signals with wavelengths comparable to the detector size of order cm–meters. Thanks to high quality factors  $Q \sim 10^{4-5}$ , the induced electromagnetic field is resonantly enhanced within the cavity. In a similar fashion, the coupling of coherent GWs to an electromagnetic resonance mode results in an induced EM field which depends on the incoming direction and polarization of the GW. A comparison between the power spectral density expected for such signals and the noise of the instrument provides an estimate of the achievable GW strain sensitivity. One finds  $h_0 \sim 10^{-22} - 10^{-21}$  at  $\mathcal{O}(\text{GHz})$  frequencies (Berlin et al. 2022).

In the following we estimate the noise-equivalent strain sensitivity of microwave cavities. The EM field induced by a GW is

$$\tilde{E}_h(f) \simeq \eta Q (2\pi f L) B_0 \tilde{h}(f), \quad (109)$$

where  $\eta \simeq 0.1$  indicates the coupling coefficient between the GW and the EM mode,  $Q$  is the cavity's quality factor,  $L$  its length, and  $B_0$  the magnetic field. From this we can estimate the power  $P$  delivered to the cavity on resonance as

$$P_{\text{sig}} \simeq \frac{1}{2} Q L^5 (2\pi f)^3 B_0^2 \eta^2 S_h(f) \Delta f, \quad (110)$$

with  $\Delta f$  being the width of the cavity resonance. We read off corresponding the power spectral density as

$$S_{P,\text{sig}}(f) \simeq \frac{Q}{4} L^5 (2\pi f)^3 B_0^2 \eta^2 S_h(f). \quad (111)$$

Contrasting this with the power injected by thermal Johnson–Nyquist noise

$$P_{\text{noise}} \simeq k_B T_{\text{sys}} \Delta f \quad \rightarrow \quad S_{P,\text{noise}}(f) \simeq k_B T_{\text{sys}} / 2 \quad (112)$$

yields the noise-equivalent strain sensitivity [see Eq. (16)]

$$S_h^{\text{noise}}(f) \simeq \frac{2k_B T_{\text{sys}}}{(2\pi f)^3 \eta^2 Q B_0^2 L^5}. \quad (113)$$

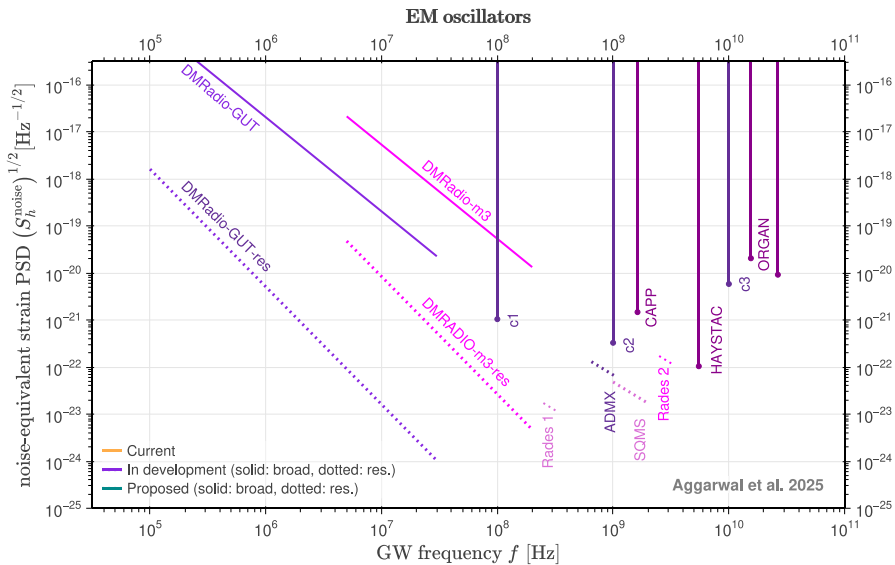
Table 3 lists experimental parameters for a range of experiments. These also serve as reference values for the sensitivities shown in Fig. 11 below. These proposals are all based on resonant readout.

The basic idea was further developed in Navarro et al. (2024) using realistic simulations of radio frequency resonant cavities and suggesting a cubic resonator design for the cavity to allow for simultaneous determination of the polarization and the direction of the incoming GW. The geometry of a quarterly split cavity was proposed in Gao et al. (2024). The use of a cavity with tunable resonance frequencies was investigated in Reina-Valero et al. (2025), studying in particular the RADES-BabyIAXO cavity proposed to search for a dark matter axion background field (Ahyoune et al. 2023) within the BabyIAXO helioscope (Abeln et al. 2021) setup. Capdevilla et al. (2024) estimated that tunable plasma cavities (as being developed by the ALPHA collaboration (Millar et al. 2023) for axion

**Table 3** Benchmark parameters for microwave cavities (Sect. 5.3.1) and low-mass axion haloscopes (Sect. 5.3.2) from (Berlin et al. 2022; Navarro et al. 2024; Reina-Valero et al. 2025; Domcke et al. 2024)

|                               | $f$ [GHz]                     | $Q$                | $B_0$ [T] | $L$ [m] | $T_{\text{sys}}$ [K] |
|-------------------------------|-------------------------------|--------------------|-----------|---------|----------------------|
| ADMX                          | (0.65, 1.02)                  | $8 \times 10^4$    | 7.5       | 0.51    | 0.6                  |
| HAYSTAC                       | (5.6, 5.8)                    | $3 \times 10^4$    | 9         | 0.13    | 0.13                 |
| CAPP                          | (1.6, 1.65)                   | $4 \times 10^4$    | 7.3       | 0.15    | 1.2                  |
| ORGAN                         | (15,16), (26,27)              | $10^4$             | 11.5      | 0.023   | 5.3                  |
| <i>SQMS</i>                   | (1, 2)                        | $10^6$             | 5         | 0.46    | 1                    |
| <i>Cubic cavity 1</i>         | 0.1                           | $6.27 \times 10^5$ | 0.6       | 2.1     | 8                    |
| <i>Cubic cavity 2</i>         | 1                             | $1.98 \times 10^5$ | 12        | 0.21    | 1                    |
| <i>Cubic cavity 3</i>         | 10                            | $6.25 \times 10^4$ | 12        | 0.021   | 1                    |
| <i>RADES-BabyIAXO</i>         | (0.25, 0.33), (2.5–3.4)       | $10^5$             | 2         | (0.5,5) | 4.6                  |
| ABRACADABRA                   | ( $10^{-4}$ , 0.002)          | 1                  | 1         | 0.096   | 0.5                  |
| SHAFT                         | ( $3 \times 10^{-6}$ , 0.003) | 1                  | 1.51      | 0.046   | 4.2                  |
| ADMX SLIC                     | 0.043                         | $3 \times 10^3$    | 7         | 0.2     | 20                   |
| BASE                          | $4 \times 10^{-4}$            | $4 \times 10^4$    | 1.85      | 0.025   | 5.7                  |
| WISPLC                        | ( $3 \times 10^{-5}$ , 0.005) | $10^4$             | 14        | 0.29    | 4                    |
| <i>DMRadio- m<sup>3</sup></i> | (0.005, 0.2)                  | $10^5$             | 4         | 1.3     | 0.02                 |
| <i>DMRadio-GUT</i>            | ( $10^{-4}$ , 0.03)           | $2 \times 10^7$    | 16        | 2.2     | 0.01                 |

For more details on the individual setups see Bartram et al. (2021) (ADMX), Zhong et al. (2018) (HAYSTAC), Kwon et al. (2021) (CAPP), Quiskamp et al. (2022, 2024) (ORGAN), Posen (2021) (SQMS), Navarro et al. (2024) (*cubic cavities*), Abeln et al. (2021), Ahyoune et al. (2023) (RADES-BabyIAXO), Salemi et al. (2021) (ABRACADABRA), Gramolin et al. (2021) (SHAFT), Crisosto et al. (2020) (ADMX SLIC), Devlin et al. (2021) (BASE), Zhang et al. (2022) (WISPLC), and Brouwer et al. (2022a), Brouwer et al. (2022b) (DMRadio). Experiments which are proposed or under development are indicated in *italics*



**Fig. 11** Projected strain sensitivity of electromagnetic oscillators employed for gravitational wave detection. The experimental parameters and references used as input for these curves are listed in Table 3. Color coding as in Fig. 1

searches) can be sensitive to persistent coherent GWs with amplitudes of  $h_0 \sim 3 \times 10^{-24} - 10^{-22}$  in the  $\mathcal{O}(10 - 50)$  GHz frequency range, depending on the choice of an isotropic or anisotropic medium permeating the cavity (see also (Gatti et al. 2024) for earlier work).

Moreover, the static external field can be substituted by loading the cavity with a pump mode, as demonstrated in the MAGO prototype designed for GW searches (Ballantini et al. 2003, 2005) [see also Berlin et al. (2023)]. For the sensitivity of MAGO to the mechanical coupling of the GW, see Sect. 5.2.3.

It has been suggested in Herman et al. (2021, 2023) that the rapidly-oscillating cross-term between the GW-induced EM field and the background magnetic field can lead to improved sensitivity. For stochastic GW backgrounds with  $\langle h(f) \rangle = 0$ , the term linear in the strain averages to zero, so only a term quadratic in the strain will lead to non-zero signal, since  $\langle h(f)^2 \rangle \neq 0$ . For signals with  $\langle h(f) \rangle \neq 0$ , the linear signal can arise, but the sensitivity in this case is independent of the background EM field, contrary to the claims made in Herman et al. (2021, 2023). This can be understood by recalling that a DC magnetic field will not lead to an AC current in an antenna. The appropriate comparison of signal and noise is therefore between the AC signal field and the AC component of the background field sourced by voltage fluctuations in the readout system.

### 5.3.2 Low-mass axion haloscopes

Low-mass axion haloscopes based on LC circuits such as ABRACADABRA (Salemi et al. 2021), ADMX SLIC (Crisosto et al. 2020), BASE (Devlin et al. 2021), DMRadio (Brouwer et al. 2022a, 2022b), SHAFT (Gramolin et al. 2021), and WISP-LC (Zhang et al. 2022) target a non-relativistic, wave-like dark matter axion background. They feature a strong static magnetic field, which in the presence of an axion (or gravitational wave) leads to an oscillating effective current which in turn induces small oscillating EM fields. A resonant LC circuit is placed to read out the tiny induced oscillating magnetic flux.

The resulting magnetic flux induced by a coherent GW can be quantified using conventional electromagnetism methods starting from the expression of the effective current in Eq. (108). It can schematically be written as (Domcke et al. 2022)

$$\tilde{\Phi}_h(f) \simeq \eta B_0 (2\pi f L)^2 L^2 \tilde{h}(f) \quad (114)$$

where the coupling constant  $\eta \simeq 0.1$  is determined by the detector's geometry (Domcke et al. 2024).<sup>31</sup> By recasting the sensitivities obtained or projected for axion searches, Domcke et al. (2022, 2024) demonstrated that strain sensitivities of  $h_0 \sim 10^{-9}$  (2 MHz, ABRA),  $h_0 \sim 10^{-16}$  (40 MHz, ADMX SLIC),  $h_0 \sim 10^{-15}$  (6 MHz, WISP-LC) and  $h_0 \sim 10^{-21}$  (100 MHz, DMRadio-m<sup>3</sup>) can be reached for coherent, persistent GW signals.

In terms of power spectral densities, the flux PSD at the readout SQUID is given by

$$S_{\phi, \text{sig}}^{\text{SQUID}}(f) = (\mathcal{T}_1 \mathcal{T}_2)^2 S_h(f) \sim \eta^2 (2\pi f)^4 B_0^2 L^8 Q^2 \alpha^2 \frac{L_{\text{sq}}}{4L_p} S_h(f). \quad (115)$$

where  $B_0$  is the magnetic field strength,  $L_p$  denotes the inductance of the pickup loop, and  $L_{\text{sq}}$  the inductance of the SQUID. A typical value (for the example of DMRadio) is  $L_{\text{sq}} \simeq 1$  nH.

The transfer function  $\mathcal{T}_1$  translates from GW strain to flux at the pickup loop [see Eq. (114)], while  $\mathcal{T}_2$  describes the transmission through the LC circuit. The transfer functions are given by

$$\mathcal{T}_1 = \eta^2 (2\pi f L)^2 B_0 L^2, \quad \mathcal{T}_2 = \frac{\alpha \sqrt{L_{\text{sq}}}}{2\sqrt{L_p}} Q. \quad (116)$$

The coupling coefficient between the LC circuit and the SQUID is denoted by  $\alpha$ , for which  $\alpha = 1/\sqrt{2}$  is a typical value (Foster et al. 2018). Further,  $Q$  denotes the quality factor of the LC resonator which we have assumed to operate on resonance in the expression for  $\mathcal{T}_2$ .

In resonant readout mode the dominant noise source is the thermal noise of the LC circuit, subject to the same transfer function  $\mathcal{T}_2$  as the signal. This yields the noise-equivalent strain sensitivity

<sup>31</sup> This expression assumes a detector sensitive to the leading order term in the GW induced flux (in an  $(fL)$ -expansion). This can be achieved by suitable detector geometries in which cylindrical symmetry, often employed to maximize the sensitivity to the axion signal, is broken (Domcke et al. 2024).

$$S_h^{\text{noise}}(f) \simeq \frac{2T_{\text{sys}}}{(2\pi f)^5 \eta^2 B_0^2 L^7 Q} \quad (\text{resonant}). \quad (117)$$

In broadband mode the sensitivity is set by SQUID noise with  $S_n^{\text{sq}} = (10^{-6} \Phi_0)^2 / \text{Hz}$  (with  $\Phi_0 = \pi \hbar / e$ ). On the signal side, the enhancement by the quality factor  $Q$  is absent in broadband mode, such that we obtain

$$S_h^{\text{noise}}(f) \simeq \frac{(10^{-6} \Phi_0)^2 \text{Hz}^{-1}}{2\pi^4 \eta^2 f^4 B_0^2 L^7 L_{\text{sq}}} \quad (\text{broadband}). \quad (118)$$

Sensitivity curves for several LC circuit-based haloscopes, (namely variations of the DMRadio program) are shown in Fig. 11, based on the benchmark parameters given in Table 3.

For ABRACADBRA, results of a prototype optimized for GW searches (‘figure-8 loop’) were recently published (Pappas et al. 2025), and while the sensitivity is still very far from realistic sources, these studies provide important input for designing detector geometries and optimizing data analysis strategies in the future.

We note that while for axion searches, the advantages of a resonant search are undeniable, a dedicated HFGW search would likely benefit from a broadband search, given the signal expectations discussed in Sect. 4.1.

### 5.3.3 Summary: strain sensitivities of electromagnetic oscillators

Figure 11 provides an overview of the projected strain sensitivities of a range of electromagnetic gravitational wave detectors, in particular low-mass haloscopes and microwave cavities. The experimental parameters on which these sensitivity curves are based are shown in Table 3. All detector concepts shown are under active experimental development, most of them primarily for axion searches. Solid lines indicate broadband sensitivities whereas dashed lines indicate resonant searches requiring a scanning strategy. Where available, we show both the projected sensitivity at an initial stage as well as the impact of possible upgrades.

## 5.4 Photon (re-)generation experiments

### 5.4.1 Light-shining-through-a-wall experiments and axion helioscopes

Axion searches based on photon regeneration target relativistic axions originating from the Sun (axion helioscopes) or from powerful lasers in laboratories (light-shining-through-a-wall experiments, LSW). In both cases, axions have to traverse a layer of shielding, which blocks out incoming photons, and are subsequently converted into photons in a conversion region permeated by a strong magnetic field. In a similar manner, GWs can be converted into photons in this conversion region through the *inverse Gertsenshtein effect*, or magnetic conversion effect (Gertsenshtein 1962; Raffelt and Stodolsky 1988). An advantage of GW searches in such experiments is that, unlike axions, they are strictly massless, implying that the conversion to photons occurs on resonance. On laboratory scales, the conversion



probability can be obtained by solving Maxwell's equations with the GW-induced effective current from Eq. (108) (see also [Appendix](#)). On astronomical scales, the back-conversion of EM waves into gravitational waves, dictated by the contribution of the EM waves to the energy-momentum tensor in Einstein's equation, becomes relevant and leads to an oscillation between GW and EM waves, see Sect. 5.6.

Ejlli et al. (2019) set first upper limits on stochastic GW backgrounds at optical and X-ray frequencies (i.e., around 500 THz and  $10^6$  THz, respectively) using data from light-shining-through-a-wall experiments (ALPS, OSQAR) and axion helioscopes (CAST). As pointed out in Liu et al. (2024), when interpreted as constraints on an isotropic stochastic GW background, these sensitivities should be reduced by a factor taking into account the field of view of these experiments resulting in sensitivities of  $h_{c,\text{sto}} \simeq 4 \times 10^{-23}$  at optical frequencies (OSQAR II), and  $h_{c,\text{sto}} \simeq 8 \times 10^{-26}$  at X-ray frequencies (CAST).

Currently, significant R&D effort is ongoing in designing more powerful instruments. Notably, ALPS II (Bähre et al. 2013), featuring a magnetic field of 5.6 T and a conversion length of 100 m, is currently taking data, and the next generation helioscope (Baby)IAXO (Armengaud et al. 2014) is under active development. Remarkably, these instruments succeed in operating far below the standard quantum limit. Given the strong motivation to search for high-frequency GWs, a dual usage of these detectors could be imagined with dedicated instruments and operational modes to search for GWs.

To estimate the noise-equivalent strain sensitivity of these detectors we start from the GW-induced EM field in frequency space (Ejlli et al. 2019),

$$\tilde{E}_h(f), \tilde{B}_h(f) \simeq 2\pi f L B_0 \tilde{h}(f). \quad (119)$$

Here,  $E_h$  and  $B_h$  are the GW-induced electric/magnetic fields respectively,  $B_0$  is the background magnetic field, and  $2\pi f L \gg 1$  is the enhancement from resonant conversion in vacuum over the length  $L$  of the instrument. (See also [Appendix](#) for more details.) From this we compute the time-averaged Poynting vector which gives the power per unit area at the receiver as

$$\langle S \rangle = \frac{1}{T} \int_{-T/2}^{T/2} dt E_h \times B_h \simeq \int df (2\pi f L B_0)^2 S_h(f). \quad (120)$$

The total power is obtained as  $P_{\text{sig}} = A \langle S \rangle$ , with  $A$  the area of the receiver. This yields for the power PSD of the signal,

$$P_{\text{sig}} = \int df S_{P,\text{sig}}(f) \rightarrow S_{P,\text{sig}}(f) \simeq A (2\pi f L B_0)^2 S_h(f). \quad (121)$$

Noting that a GW of frequency  $f$  will create a photon of the same frequency, we can also compute the number of detected photons,

$$N_{\gamma,\text{sig}} = \frac{\epsilon P_{\text{sig}}}{2\pi f} \Delta t \rightarrow S_{N,\text{sig}} \simeq 2\pi \epsilon f A L^2 B_0^2 S_h(f), \quad (122)$$

with  $\epsilon$  the single photon detection efficiency and  $\Delta t$  the observation time. The use of a resonant regeneration cavity could further increase the number of signal photons at the resonant frequency by the finesse factor  $\mathcal{F}$  of the cavity. The signal strength degrades at low frequencies due to waveguide effects, which become important when the GW wavelength becomes comparable to the dimensions of the cavity, specifically at frequencies below (Ringwald et al. 2021)

$$f \sim \frac{L}{4\pi A}, \quad (123)$$

for an elongated cylindrical cavity of length  $L$  and cross-sectional area  $A$ .

For a single-photon detection scheme, as implemented in current optical and X-ray instruments, we need to compare this with the dark count rate  $\Gamma_D(f)$  in a frequency bin of width  $\Delta f$  (Ejlli et al. 2019),

$$N_{\gamma, \text{noise}} = \Gamma_D \Delta t \simeq \int df S_{N, \text{noise}} \rightarrow S_{N, \text{noise}} = \frac{\Gamma_D(f)}{2\Delta f} \Delta t. \quad (124)$$

This yields the noise-equivalent strain sensitivity [see Eq. (16)],

$$S_h^{\text{noise}}(f) \simeq \frac{\Gamma_D(f)/\Delta f}{2\epsilon A(2\pi f)L^2 B^2} \quad (\text{single photon}). \quad (125)$$

We note that that any detection requires  $N_{\gamma, \text{sig}} \geq 1$ , which for very short signals (as is typically the case, e.g., PBH mergers) can impose a constraint which is more stringent than overcoming the dark count rate. Close to this limit, one can moreover not rely on match filtering techniques. Hence, when estimating the sensitivity to PBH mergers, we do not employ Eq. (56), but instead require directly that  $N_{\gamma, \text{sig}}$  as introduced in Eq. (122), accumulated over the signal duration during the detector run time, is larger than one. Similarly, we employ this criterion instead of the PLS curves used commonly in linear detectors to evaluate the sensitivity to stochastic backgrounds.

The inverse Gertsenshtein effect can in principle be exploited over a very broad range of frequencies, and in particular has substantial potential at GHz frequencies where many early Universe signals converge. This would require fitting existing or planned instruments with different electromagnetic receivers. For example, Ringwald et al. (2021) provides estimates for the sensitivity achievable by a IAXO-type experiment in the GHz region, finding  $h_c \lesssim 10^{-22}$  using heterodyne radio receivers (HET) and  $h_c \lesssim 10^{-25}$  with single photon detectors (SPD) around a frequency of  $f \simeq 4 \times 10^{10}$  Hz. This illustrates that single-photon detection at microwave frequencies could be key to unlocking a significant improvement in sensitivity. While the implementation of these techniques in the GHz range is highly challenging, we note that single-photon detection at microwave frequencies is an area of rapidly advancing experimental development, actively pursued also for dark photon and dark matter searches (see e.g. Lescanne et al. 2020; Dixit et al. 2021; Chiles et al. 2022; Graham et al. 2024; Braggio et al. 2025; Pankratov et al. 2025).

In the mean time, current photon (re)generation experiments operating in the GHz regime perform a power measurement with the signal PSD given by Eq. (121),

and the noise PSD given by the thermal noise [see Eq. (112)], see also next subsection and heterodyne radio receivers (HET) proposed in Ringwald et al. (2021). Combining these yields the noise-equivalent strain sensitivity

$$S_h^{\text{noise}}(f) \simeq \frac{k_B T_{\text{sys}}}{8\pi^2 f^2 B^2 L^2 A} \quad (\text{thermal}). \quad (126)$$

Importantly, we note that LSW experiments and helioscopes can be designed as broadband instruments, with a bandwidth of about one order of magnitude in frequency. In broadband mode, one cannot employ a resonant cavity and thus does not profit from an enhancement originating from a large finesse.

Benchmark parameters for existing (or decommissioned) experiments as well as upcoming and proposed instruments are shown in Table 4, and the resulting sensitivity curves can be found in Fig. 11.

### 5.4.2 Dielectric axion haloscopes

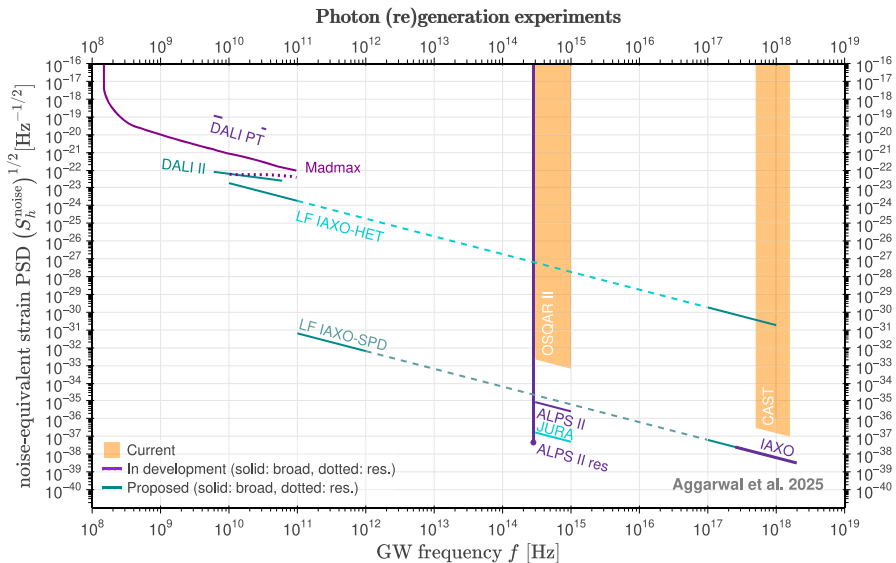
At frequencies around 10 GHz, dielectric haloscopes are currently being developed for axion searches. Compared to traditional photon regeneration experiments they profit from enhanced axion-to-photon conversion at the surfaces of a stack of dielectric disks. If the disk separation is suitably tuned, the EM waves generated at the surfaces of the different disks interfere constructively. This idea is implemented in MADMAX (Brun et al. 2019), which has very recently taken first data with a prototype instrument (Egge et al. 2025).

MADMAX can also be used to search for gravitational waves. Compared to the axion case, the relativistic nature of the GWs enhances conversion in the vacuum region between the disks, but imposes a challenging new requirement to adapt the

**Table 4** Benchmark parameters of light-shining-through-a-wall and helioscope experiments, see Ejlli et al. (2019), Ringwald et al. (2021)

|                 | $f$ [GHz]                | $B_0$ [T] | $L$ [m] | $A$ [m <sup>2</sup> ] | $\Gamma_D$ [Hz]       | $\epsilon$ |
|-----------------|--------------------------|-----------|---------|-----------------------|-----------------------|------------|
| OSQAR I         | $(0.3, 0.8) \times 10^6$ | 9         | 14.3    | $5 \times 10^{-4}$    | $1.76 \times 10^{-3}$ | 0.5        |
| OSQAR II        | $(0.3, 1) \times 10^6$   | 9         | 14.3    | $5 \times 10^{-4}$    | $1.14 \times 10^{-3}$ | 0.9        |
| ALPS I          | $(0.3, 1) \times 10^6$   | 5         | 9       | $5 \times 10^{-4}$    | $6.1 \times 10^{-4}$  | 0.1        |
| ALPS II         | $(0.3, 1) \times 10^6$   | 5.3       | 106     | $2 \times 10^{-3}$    | $10^{-6}$             | 0.75       |
| <i>JURA</i>     | $(0.3, 1) \times 10^6$   | 13        | 960     | $8 \times 10^{-3}$    | $10^{-6}$             | 1          |
| CAST            | $(0.5, 1.6) \times 10^9$ | 9         | 9.26    | $2.9 \times 10^{-3}$  | $1.5 \times 10^{-4}$  | 0.7        |
| <i>BabyIAXO</i> | $(0.25, 2) \times 10^9$  | 2.5       | 10      | 0.77                  | $10^{-3}$             | 1          |
| <i>IAXO</i>     | $(0.25, 2) \times 10^9$  | 2.5       | 20      | 3.08                  | $10^{-4}$             | 1          |

For details on the individual setups see Ballou et al. (2015) (OSQAR), Bähre et al. (2013), Albrecht et al. (2021) (ALPS), Beacham et al. (2020) (*JURA*), Anastassopoulos et al. (2017) (CAST), Abeln et al. (2021) (*BabyIAXO*) and Armengaud et al. (2019) (*IAXO*). Experiments which are proposed or under development are indicated in *italics*



**Fig. 12** Projected strain sensitivities of gravitational wave detectors based on photon regeneration, with parameters and references listed in Tables 4 and 5. Color coding as in Fig. 1

**Table 5** Benchmark parameters of dielectric haloscopes, see Brun et al. (2019) (MADMAX) and De Miguel et al. (2024) (DALI prototype and phase II)

|         | $f$ [GHz]         | $B_0$ [T] | $L$ [m] | $A$ [m <sup>2</sup> ] | $T_{\text{sys}}$ [K] |
|---------|-------------------|-----------|---------|-----------------------|----------------------|
| MADMAX  | (0.2, 100)        | 10        | 1       | 1.23                  | 4.2                  |
| DALI PT | (6, 8) & (29, 37) | 1         | 0.35    | 0.03                  | 30                   |
| DALI II | (6, 60)           | 11.7      | 1.1     | 1.5                   | 1.5                  |

effective disk thickness to a particular GW frequency. Operated in fully resonant mode, the noise-equivalent strain sensitivity has been estimated as (Domcke et al. 2025a)

$$(S_h^{\text{noise}})^{1/2} \sim 10^{-22} \text{ Hz}^{-1/2} \times \left( \frac{1 \text{ M}^2}{L^2} \right) \left( \frac{10 \text{ T}}{B_0} \right) \left( \frac{43}{N_d} \right) \left( \frac{10 \text{ GHz}}{f} \right), \quad (127)$$

with  $N_d \lesssim 50$  the number of dielectric disks inserted. (If the number of disks becomes too large, the sensitivity actually *decreases*.) A sensitivity estimate for a MADMAX-like detector operating in resonant mode and assuming the benchmark parameters from Eq. (127) is shown as a dotted purple line in Fig. 12. The sensitivity of the same instrument, but *without* the dielectric disks is shown as a solid line. This corresponds to operating as a standard photon (re)generation experiment, though at radio frequencies. The noise-equivalent strain sensitivity is given by Eq. (126), and the detector parameters are listed in Table 5. As discussed in Domcke et al. (2025a), it seems, however, most beneficial to operate in a hybrid mode, where part of the detector volume is filled with dielectric disks, while the rest is empty.

Such a setup still profits from resonant enhancement in a narrow frequency range, but also has broadband sensitivity similar to the photon (re)generation experiments discussed in Sect. 5.4.1 above.

A related approach to search for both axions and gravitational waves is pursued in DALI, which features a superconducting solenoid magnetizing a stack of ceramic wafers, and an array of antennas for readout. A scaled-down prototype (DALI PT) is currently under construction, with upgrades to DALI Phase II (henceforth DALI II) in planning (De Miguel 2021; De Miguel et al. 2024).

### 5.4.3 Summary: strain sensitivities of photon (re-)generation experiments

Figure 12 provides an overview of the projected strain sensitivities of a range of laboratory electromagnetic gravitational wave detectors based on photon regeneration. As in Fig. 1, instruments which have placed limits on (or detected) GWs are shown in orange, concepts under active R&D are shown in purple and, other proposals are shown in cyan. Where available, we show both the projected sensitivity at an initial stage, as well as possible upgrades. In particular, we show sensitivity projections for light-shining-through-a-wall experiments (OSQAR II, ALPS II, and JURA, with parameters given in Table 4 and with the dashed curve corresponding to resonant operation of ALPS II with  $\mathcal{F} = 40\,000$ ), helioscopes (CAST and IAXO, with parameters given in Table 4), and dielectric haloscopes [DALI, MADMAX, with parameter for broadband operation given in Table 5, and with the sensitivity for MADMAX in resonant mode taken from Domcke et al. (2025a)]. For helioscopes, the upper line refers to a thermal noise limited readout whereas the lower line refers to single photon detection. We also show (in lighter green) the extrapolation to lower frequencies assuming an adapted readout system.

We caution that in the transfer functions used to estimate these sensitivities we have dropped the dependence on the incident angle of the GW, that is, we have not taken into account the antenna pattern. In this sense, these sensitivities should be seen as sensitivities to GWs reaching the detector under an optimal angle. While this is a relatively small effect for many GW detectors, which have rather broad angular response functions, it is a much more important consideration for experiments such as ALPS, which is maximally sensitive only in a very small field of view.

## 5.5 Other electromagnetic gravitational wave detectors

### 5.5.1 High energy pulsed lasers

Vacalis et al. (2023) proposed a method for detecting high-frequency gravitational waves using high-energy pulsed lasers rather than constant magnetic fields. In this approach, GW interactions with the laser field create an electromagnetic signal via the inverse Gertsenshtein effect, and resonance occurs when the frequency of the GW is twice the laser frequency. The method is particularly suitable in the optical frequency range due to the availability of long, high-intensity pulses in this frequency regime. Single-photon counting techniques are used to detect the

electromagnetic signal. Targeting the frequency range  $(10^{13} - 10^{19})$  Hz, this technique can reach strain sensitivities of  $h_0 \lesssim 10^{-20}$ . With the next generation of optical lasers, strains down to  $h_0 \sim 10^{-26}$  may be reachable at specific frequencies.

### 5.5.2 GW to electromagnetic-wave conversion in a static electric field

Lupanov (1966) considered the inverse Gertsenshtein effect in a static electric field rather than a static magnetic field.<sup>32</sup> The physics is essentially the same in the two cases but the intensity of electric fields in laboratory settings is limited due to their tendency to pull electrons from any support structure. Consequently, the energy densities reachable in electric fields are about a million times smaller than those of magnetic fields in the several Tesla range.

This limitation can be overcome by focusing on graviton-to-photon conversion in *atomic* electric fields, which can be much stronger (Dai and Liang 2023). The conversion happens when the wavelength under consideration is shorter than the atomic radius, making the method sensitive at frequencies of  $10^{20}$ – $10^{24}$  Hz, or graviton energies between 100 keV and 1 GeV. Dai and Liang (2023) proposed to search for the generated photons in current and future neutrino detectors, for instance JUNO. A downside of this technique is the limitation to very high frequencies, at which it seems difficult to envisage sufficiently strong GW sources.

### 5.5.3 Resonant polarization rotation

Cruise (1983) showed that a GW could induce a rotation of the plane of polarization of electromagnetic waves in certain geometries, some of which might be relevant astronomically. In 2000, the idea of resonant polarization rotation was extended to a situation in which the electromagnetic wave was a circulating wave in a microwave waveguide ring (Cruise 2000). The effect is amplified by the (potentially significant) quality factor of the waveguide ring. A proof of concept apparatus was constructed by Cruise and Ingley (2005, 2006). Such a device would be narrowband, achieving a sensitivity to a stochastic GW background of  $\sqrt{S_n} \lesssim 10^{-14} \text{ Hz}^{-1/2}$  at frequencies around 100 MHz by cross-correlating two detectors. It is difficult to see the sensitivity of this GW detection scheme increasing very far beyond this limit though. Recently, this concept has been revisited in the context of optical cavities, emphasizing parallels with axion birefringence searches (García-Cely et al. 2025). Notably, it has been pointed out that the existing ALPS II infrastructure at DESY can be adapted to measure polarization effects induced by GWs. Utilizing realistic cavity properties and current technology, this approach could, within a few years, enable the exploration of HFGWs in the frequency range of 0.1 MHz to 0.1 THz with sensitivities comparable to the aforementioned  $\sqrt{S_n}$ .

<sup>32</sup> Electric fields are usually not considered in the context of axion searches, as the coupling of non-relativistic axions to electric fields is suppressed compared to their coupling to magnetic fields. For GWs, on the other hand, there is no such suppression.

### 5.5.4 Heterodyne enhancement of magnetic conversion

References Li and Yang (2004), Li et al. (2006, 2009), Baker et al. (2008) suggested enhancing the efficiency of magnetic conversion detectors by seeding the conversion volume with a locally generated electromagnetic wave at the same frequency as the GW being searched for. Concerns were raised in Woods (2012) and Eardley (2008). Furthermore, the claims of outstanding sensitivity rely on technology that does not yet exist, and no experimental results have been produced to suggest it is feasible.

### 5.6 Astrophysical and cosmological detection concepts

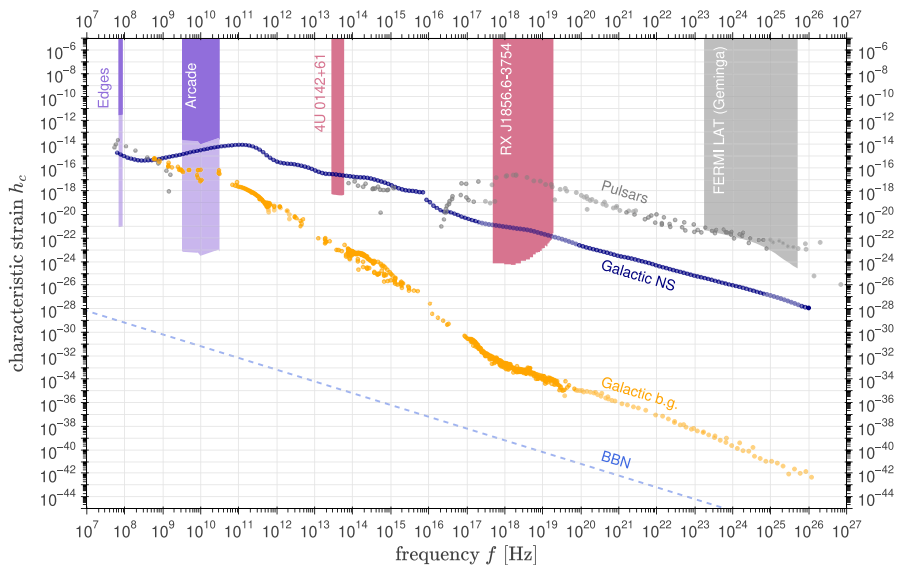
The majority of indirect astrophysical and cosmological probes of high-frequency gravitational waves exploit the inverse Gertsenshtein effect, in which gravitational waves convert into photons in cosmological or astrophysical magnetic fields. Schematically, the conversion probability is

$$P_{h \rightarrow \gamma} \sim \frac{1}{M_{\text{Pl}}^2} (BL)^2, \quad (128)$$

where  $L$  is the characteristic physical length scale over which conversion takes place, and  $B$  is the characteristic magnetic field strength. The product  $BL$  therefore provides a useful figure of merit for determining the strength of graviton–photon mixing. Typical values are  $BL \simeq 10^{13} \text{ G km} \times (B/\text{nG}) (L/\text{Gpc})$  in a cosmological setting, whilst neutron stars can reach  $BL \simeq 10^{13} \text{ G km} \times (B/10^{12} \text{ G}) (L/10 \text{ km})$  (and even larger values in the case of magnetars) (Domcke and Garcia-Cely 2021). This comparison shows how the relative weakness of cosmological magnetic fields can be compensated for by large effective conversion lengths. Beyond this rough figure of merit, the suitability of a given system to search for GWs depends on the details of the environment in question (in particular the effective photon mass, which can be non-vanishing, resulting in suppressed, non-resonant conversion between GWs and photons), and the flux of background or foreground photons.

Neutron stars have already been used to search for other low-mass particles, notably dark matter axions (Raffelt and Stodolsky 1988; Pshirkov and Popov 2009; Huang et al. 2018; Hook et al. 2018). This initiative has now grown into an established field in its own right, with a wide range of observations and sophisticated modeling. Neutron stars as high-frequency GW detectors have only become an active topic of study recently. Ito et al. (2024b) produced tentative constraints on stochastic gravitational waves in the radio frequency band 0.1–1 GHz and in the range  $10^{13}$ – $10^{27}$  Hz spanning the IR, UV, Visible and X-ray regimes. Resulting strain sensitivities range from  $h_c \lesssim 10^{-14}$  to  $h_c \lesssim 10^{-18}$  in the radio band, and from  $h_c \lesssim 10^{-16}$  to  $h_c \lesssim 10^{-26}$  in the high-frequency band based on non-resonant conversion of gravitational waves into photons. More recently, McDonald and Ellis (2024) explored the role of resonant conversion in setting constraints.

It should be emphasized that the modeling in the pioneering work Ito et al. (2024b) remained rudimentary, both in terms of the treatment of graviton–photon



**Fig. 13** Tentative astrophysical and cosmological constraints on isotropic stochastic gravitational wave backgrounds. We display constraints from non-resonant conversion (Ito et al. 2024b) (gray) and resonant conversion (McDonald and Ellis 2024) (pink) in individual neutron stars. In purple we show constraints from spectral distortions of the CMB (Domcke and Garcia-Cely 2021), where the light/dark regions correspond to the range of allowed intergalactic magnetic field values. We also display limits from conversion in galactic magnetic fields (Ito et al. 2024a; Lella et al. 2024) (orange) and neutron star populations (Dandoy et al. 2024) (dark blue) (taking the conservative decaying magnetic field scenario). We caution that in the case of galactic, Geminga, Crab and neutron star population constraints, points indicate that the underlying spectral data [see e.g. Hill et al. (2018)] may not have continuous frequency coverage, such that there may be gaps in these constraints between observing bins. We refer the reader to the original works for more details

mixing in 3D magnetized plasmas<sup>33</sup> and the transport of photons through the magnetosphere. Fortunately, much of the machinery for addressing these issues more accurately has been developed already in the context axion physics, see McDonald et al. (2023) for improved calculations of the conversion probability, and McDonald and Witte (2023) for a discussion of photon transport via ray-tracing techniques, which allow for accurate computation of the photon flux in a non-trivial magnetosphere geometry. Some of these more advanced techniques from axion physics have been applied to graviton–photon conversion in McDonald and Witte (2023). As a cautionary note, in the axion context, the predicted photon signatures from state-of-the-art ray tracing techniques (McDonald and Witte 2023) differ markedly from more naive early studies (Hook et al. 2018; Leroy et al. 2020).

More recently, some early studies have been carried out using entire populations of neutron stars to place constraints on gravitational waves (Dandoy et al. 2024). Results are shown as a dashed blue line in Fig. 13. Again, we caution that these constraints would benefit from more state-of-the-art approaches to in population modeling, photon production, and photon transport.

<sup>33</sup> See Macedo and Nelson (1983) for more systematic attempts in homogeneous plasmas.



Gravitational wave detection using cosmological magnetic fields has been considered in (Pshirkov and Baskaran 2009; Chen 1995; Dolgov and Ejlli 2012; Cillis and Harari 1996; Domcke and Garcia-Cely 2021). In this case, the magnetic field is weaker and the background is much harder to control, but cosmological magnetic fields can extend coherently over kpc or even Mpc, implying an enormous ‘detector volume’. Of particular interest is the frequency range from 100 MHz to 30 GHz, i.e. the Rayleigh–Jeans tail of the cosmic microwave background, which is the target of several existing and upcoming radio telescopes. For example, the data of ARCADE 2 (Fixsen et al. 2011) and EDGES (Bowman et al. 2018) can be recast into constraints at the level of  $h_{c,sto} < 10^{-24}(10^{-14})$  in the range  $3 \text{ GHz} \lesssim f \lesssim 30 \text{ GHz}$  (ARCADE 2) and  $h_{c,sto}(f \approx 78 \text{ MHz}) < 10^{-12}(10^{-21})$  (EDGES) for the strongest (weakest) cosmic magnetic fields in accordance with current astrophysical data (Domcke and Garcia-Cely 2021). The large uncertainty in these constraints resides in the unknown power spectrum of the cosmological magnetic fields in the early Universe. Clearly, more accurate modeling of magnetic fields is needed to improve on the 10 orders of magnitude uncertainty in these constraints on  $h_c$ .

Galactic and planetary magnetic fields have also been used recently to place constraints on stochastic gravitational wave backgrounds (Ito et al. 2024a; Lella et al. 2024; Liu et al. 2024), though more work is needed to accurately model the conversion and the magnetic fields within the galaxy. Results are displayed in Fig. 13. Roughly similar sensitivities in the frequency range 100 TeV—PeV have been found using LHAASO to search for GW-to-photon conversion in the Milky Way (Ramazanov et al. 2023). Prospects for future radio telescopes and CMB spectrometers are discussed in He et al. (2024), though under very optimistic assumptions regarding the magnetic fields and instrumental sensitivities.

Result from astrophysical searches for high-frequency GWs are summarized in Fig. 13. All of these results apply to isotropic stochastic gravitational wave backgrounds. They are compared with laboratory searches for SGWBs and with possible signals in Fig. 4. An important direction of future study is the sensitivity of astrophysical detection techniques to GW signals that are localized in time and/or in space GW, such as typical signals generated by sources in the late Universe.

## 5.7 Other concepts

In the following, we list several detection concepts not covered in the previous sections.

### 5.7.1 Superconductors as GW detectors

GW interactions with matter are typically extremely weak because of “impedance mismatch”, that is, a mismatch between the way a GW propagates in vacuum and the way deformation waves travel in medium. This impedance mismatch may be significantly reduced in superconductors and superfluids thanks to the macroscopic wave functions of these systems. This has led Anandan and Chiao (1982), Chiao (2002) to discuss a detection concept exploiting spin–spin interactions between

GWs and vortices in superfluids. The proposed detector consists of a toroidal tube filled with superfluid helium and interrupted by a Josephson junction. An incoming GW leads to a phase difference in the superfluid's wave function across the junction. This phase difference, in turn, leads to a mass current, against which the apparatus recoils. It is proposed to read out this recoil using an electromechanical transducer. But while Chiao (2002) speculates about strain sensitivities at the  $h_0 \sim 10^{-30}$  level around 10 GHz, it should be kept in mind that this is based on very conceptual and preliminary studies.

An alternative proposal was suggested shortly after in Anandan (1985), based on the mechanical force exerted by a GW on a superconducting solenoidal magnet. As the magnet coils are infinitesimally deformed by the GW, flux quantization enforces a change in the magnetic field. A suitably constructed and placed pickup loop could read out this change in the magnetic field using a SQUID. Anandan (1985) estimates a possible strain sensitivity of  $h \sim 10^{-21}$ , under optimistic assumptions regarding the experimental challenges.

A good review of the issues surrounding the interaction of mesoscopic quantum systems such as superfluids and superconductors with gravity can be found in Kiefer and Weber (2005), casting in particular doubt on some of the assumptions made in Anandan and Chiao (1982), Chiao (2002).

### 5.7.2 Graviton–magnon resonance

As pointed out in Ito et al. (2020), a GW passing through a ferromagnetic insulator can resonantly excite magnons (collective excitations of particle spins) thanks to an interaction between the GW and the fermion spins (Ito and Soda 2020). These collective spin excitations are analogous to the excitation of phonons in resonant bar detectors. The readout is achieved by placing the magnetic sample inside a microwave cavity and coupling the magnon to a cavity photon mode. This idea builds on the technique of ferromagnetic haloscopes proposed for axion searches (Crescini et al. 2018; Flower et al. 2019). By reinterpreting the data from these axion searches, Ito et al. (2020), Ito and Soda (2020) have shown that the sensitivity of the magnon GW detector reaches strains of  $\sqrt{S_n} \lesssim 7.6 \times 10^{-22} \text{ Hz}^{-1/2}$  at 14 GHz and  $\sqrt{S_n} \simeq 1.2 \times 10^{-20} \text{ Hz}^{-1/2}$  at 8.2 GHz (Ito et al. 2020; Ito and Soda 2020).

Ito and Soda (2023) showed that the sensitivity of the magnon GW detector is maximized when the size of the ferromagnetic insulator is comparable to the wavelength of the GW. Then, the sensitivity could in principle be improved to  $h_0 \sim 10^{-20}$  around GHz by using a bigger sample (Ito and Soda 2023). As another possibility, the sensitivity of this approach can be improved by incorporating single photon counters instead of linear amplifiers. For counters available today, Lamoreaux et al. (2013) estimates a sensitivity improvement by several orders of magnitude for axion detection.

### 5.7.3 Atomic precision measurements

Frequencies of photons in a GW background are modulated, an effect that is exploited for instance in nHz GW measurements using pulsar timing. Bringmann et al. (2023) extended this concept and proposed to probe high-frequency GWs with optical atomic clock techniques. These techniques have achieved remarkable precision, allowing for photon frequency measurements with an accuracy of  $\lesssim 10^{-20}$  (Bothwell et al. 2022; Zheng et al. 2022). They therefore hold promise for probing the tiny frequency modulation of photons caused by GWs.

However, at high frequencies combined with long experimental integration times, this modulation would average to zero. To overcome this challenge, Bringmann et al. (2023) proposed an “optical rectifier”, which blocks the optical signal during half of each GW period using a shutter. The projected sensitivity to high-frequency GWs under optimistic assumptions for the achievable experimental sensitivity is  $h_0 \lesssim 10^{-17}$  to  $10^{-21}$  at frequencies from 10 kHz to 10 GHz for one second of integration time. To estimate the corresponding noise-equivalent strain sensitivity we use 31 for a linear narrow-band detector, yielding  $\sqrt{S_n} = 10^{-17} \text{ Hz}^{-1/2}$  and  $10^{-17} \text{ Hz}^{-1/2}$ , respectively.

### 5.7.4 One-electron quantum cyclotron

An electron in a background magnetic field experiences cyclotron motion and spin precession. By cooling the electron, one can observe the quantization of the energy levels corresponding to the cyclotron motion, that is, the Landau levels. Such a one-electron quantum cyclotron has been utilized to measure the anomalous magnetic moment of the electron  $(g - 2)_e$  with a remarkable precision of approximately  $10^{-13}$ . To achieve this, an electron in a Penning trap is prepared in the lowest Landau level, which in theory has an infinite degeneracy, with the different degenerate states corresponding to wave functions of different spatial size  $R$ . Ito and Kitano (2024) proposed to utilize a similar setup for a gravitational wave search. The excitation rate from the ground state to the first excited state depends on the size of the electron wave function: an electron with a larger wave function feels the effect of a gravitational wave more strongly (in the limit  $2\pi fR \lesssim 1$ ). Interestingly, this enhancement is a particular feature of the excitation by gravitational waves, in contrast to excitations caused by electromagnetic fields (dipole excitation), whose excitation rate is insensitive to the size of the wave function.

The readout in such a setup would be via “quantum jump spectroscopy”: an additional weak magnetic field is applied to couple the cyclotron motion of the electron to its axial motion (oscillations about the cyclotron orbit). This axial motion can be read out via the currents it induces.

From the dark count rate reported in the context of dark photon searches in Fan et al. (2022), Ito and Kitano (2024) estimated that an existing one-electron quantum cyclotron could probe GW strains down to  $h_0 \sim 3.8 \times 10^{-20}$  at frequencies around 100 GHz. The sensitivity can be improved by preparing the initial state of the electron even more carefully. In particular, it is possible to prepare the electron in a state with a particularly large wave function. This could allow the experiment to achieve a sensitivity of  $h_0 \lesssim 6.9 \times 10^{-23}$  (Ito and Kitano 2024). Although a GW search with a one-electron quantum cyclotron is a narrow band resonance experiment, it could scan over a frequency range from 20 GHz to 200 GHz by adjusting the strength of the magnetic field and the frequencies of driving fields, while maintaining the above-mentioned sensitivities (Fan et al. 2022).

### 5.7.5 Rydberg atoms

Rydberg atoms have proven to be a unique type of quantum sensor for numerous applications. A method of exploiting their unusual properties for heterodyne detection of axions (Engelhardt et al. 2024) lends itself also to the detection of gravitational waves with  $\mathcal{O}(\text{GHz})$  frequencies (Kanno et al. 2025). The method is based on electromagnetically induced transparency (EIT) (Kocharovskaya and Khanin 1986; Fleischhauer et al. 2005), the starting point for which is a system of three atomic energy levels  $|1\rangle$ ,  $|2\rangle$ ,  $|3\rangle$ , where  $|1\rangle$  and  $|2\rangle$  are low-lying states and  $|3\rangle$  is a Rydberg state. Two laser beams drive the  $|1\rangle \leftrightarrow |2\rangle$  (“probe laser”) and  $|2\rangle \leftrightarrow |3\rangle$  (“control laser”) transitions, respectively, leading to two interfering Rabi oscillations. For instance, a transition  $|1\rangle \rightarrow |2\rangle$  can either happen directly, or via  $|1\rangle \rightarrow |2\rangle \rightarrow |3\rangle \rightarrow |2\rangle$ , and the two amplitudes interfere. This interference can be destructive, leading to a characteristic narrow absorption feature in the transmission spectrum of the probe laser.

Consider now a second Rydberg level,  $|4\rangle$ . An incoming gravitational wave can induce an oscillating electric field when coupled to an external magnetic field, and this electric field can drive Rabi oscillations  $|3\rangle \leftrightarrow |4\rangle$  if the gravitational wave frequency matches the corresponding energy difference ( $\ll \text{eV}$  since both  $|3\rangle$  and  $|4\rangle$  are Rydberg states). These extra Rabi oscillations split the absorption line that the probe laser experiences into two lines, though the effect is very small (quadratic in the gravitational wave strain). As first proposed in Jing et al. (2020) in a different context, and applied to the case of high-frequency gravitational wave detection in Kanno et al. (2025), detection prospects can be significantly enhanced by applying in addition to the probe and control lasers a third laser field (the “local laser”) tuned to the  $|3\rangle \leftrightarrow |4\rangle$  transition. The effect of the local laser is to split the absorption line even in absence of a gravitational wave; the presence of the gravitational wave then changes the separation between the two lines by a small amount. If the splitting

induced by the local laser is of order the width of the lines, the change in transmissivity in between the lines becomes *linear* in the strain.

Kanno et al. (2025) estimate that strain sensitivities of  $h_0 \lesssim \text{few} \times 10^{-20}$  could be possible at a frequency of order 30 GHz. In a hypothetical quantum noise-limited detector, this could be improved to  $h_0 \lesssim 10^{-23}$ , and with entangled Rydberg atoms, an improvement by a further three orders of magnitude may be possible.

## 5.8 Cross-correlating multiple detectors

The first observations of gravitational waves from coalescing binaries by the LIGO and Virgo collaborations were performed using template matching techniques. This was possible because, for a coalescing binary, the expected waveform of the GW can be modeled, so the observed data can be compared to a set of signal templates.

Unfortunately, a similar approach is unsuitable for many of the sources of interest to high-frequency GW searches. For instance, many cosmological processes produce a GW signal that can be described as a superposition of a very large number of contributions. The waveform in this case is stochastic. Even for sources that can be modeled deterministically, the number of free parameters is often too large to make template matching practical. The problem is that the set of expected signals does not have the structure of a linear space in the sense that the linear combination of two possible signals does in general *not* produce a possible signal. For this reason the computational cost of a search over a template bank grows very fast with the number of free parameters.

With template matching impractical, high-frequency GW could still be detected as excess noise in the apparatus. A robust result of this kind would, however, require very good understanding of instrumental and environmental noise sources, which is typically not available. A more promising discovery strategy is therefore the cross-correlation of data from multiple detectors (Allen 1997; Michelson 1987). The basic principle is to compare the signal from two detectors. This means comparing a random signal with another stationary, stochastic, isotropic, Gaussian signal from the same source. Similar to template matching as a means of detecting discrete sources, in this case the template itself is random, and this affects the statistical gain from performing a cross correlation between two detectors.

### 5.8.1 The overlap reduction function

In the cross-correlation approach, the quantity of interest for the detection and parameter estimation of a Gaussian stochastic GW background is the correlation between the strain at two different points  $\mathbf{x}$  and  $\mathbf{y}$ . Focussing on GWs of frequency  $f$ ,

$$\begin{aligned} & \langle h_{ij}^*(\mathbf{x}, f) h_{kl}(\mathbf{y}, f)^* \rangle \\ & \propto \sum_{a, a'} \int d\hat{\mathbf{k}} d\hat{\mathbf{k}}' \langle \tilde{h}_a^*(\hat{\mathbf{k}}, f) \tilde{h}_{a'}(\hat{\mathbf{k}}', f) \rangle e_{ij}^a(\hat{\mathbf{k}}) e_{kl}^{a'}(\hat{\mathbf{k}}') e^{-2\pi i f(\hat{\mathbf{k}}\mathbf{x} - \hat{\mathbf{k}}'\mathbf{y})} \end{aligned} \quad (129)$$

We use here the notation from Sect. 2, and a hat over the wave vectors  $\mathbf{k}$ ,  $\mathbf{k}'$  indicates a unit vector in the corresponding direction.

We see that the correlation is influenced by two effects. First, the detectors will not be in the same position, therefore the phase factor in the integral will oscillate, and the correlation will be reduced. This reduction becomes important when the separation  $d$  between the two detectors is larger than the wavelength,  $d \gtrsim 1/(2\pi f)$ . A further reduction of the correlation can be caused if the two detectors are coupled differently to the GW modes, for example because they are oriented differently.

The reduction of correlation is quantified by the overlap reduction function  $\Gamma(f)$  [see Eq. (24)], a frequency dependent factor with modulus always less than one, which is simply the coherence between the two signal of interest. A derivation of  $\Gamma(f)$  can be found in Michelson (1987), and Allen (1997) has outlined the process of optimizing the detection efficiency by optimal filtering in the time domain for two detectors with arbitrary separation and orientation.

An interesting possibility with small-scale detectors, like many of the setups envisioned for high-frequency GW detection, is to move detectors relative to one another, hence changing the value of the overlap function  $\Gamma$ . In this way the correlation of the signal can be modulated, and a detection of this modulation pattern could provide credible evidence of detection.

### 5.8.2 Signal switching

As an alternative to cross-correlating signals from different detectors, it may be possible in high-frequency GW searches to turn the sensitivity of a single detector on and off without affecting its other performance properties. If the temporal pattern of switching on and off can be seen in the signal output at a statistically significant level then a credible claim for detection could be made with just a single detector.

Signal switching is possible, for instance, in the case of magnetic conversion detectors, where it is possible to modulate the amplitude of the field and its direction, thereby modulating the instrument's sensitivity. In addition, electromagnetic conversion detectors are sometimes filled with gas to counteract waveguide effects: if the transverse dimensions of the detector are comparable to, or smaller than, the GW wavelength, waveguide effects increase the phase velocity of the generated electromagnetic wave above the vacuum speed of light. This leads to a phase mismatch between the GW and the EM wave, an effect which the

introduction of a gas with a sizable refractive index can counteract. By varying the gas pressure, one can then modulate the GW sensitivity of the device.

Note that, statistically, signal switching is a more effective correlation process than cross-correlating two similar detectors because for signal switching, the detector output is compared with an a priori determined template (namely the operational pattern) instead of a random one. The minimum detectable signal in this case is  $\propto t_{\text{int}}^{-1/2}$  allowing a faster gain in sensitivity with time.

### 5.8.3 Issues related to data acquisition and long term storage

To detect correlated periodic events at GHz frequencies at a signal-to-noise ratio of 8, systematic errors related to timing should be of the order of 20 ps. This necessitates very accurate timing calibration, a high DAQ sampling rate, and consequently significant data storage capacity of up to several petabytes.<sup>34</sup>

Timing calibration is challenging as low noise amplifiers, anti-aliasing electronics, and other components of the readout add delay to the data acquisition system. Moreover, quantization errors from the analog-to-digital converters add further bias, and to minimize this effect, the sampling rate would need to be higher than the desired timing resolution. At such sampling rates, making use of super-conducting oversampling ADCs which achieve high dynamic ranges over narrow frequency ranges by pushing quantization noise outside the band-of-interest could turn out to be a viable option.

To avoid excessive storage requirements, real-time analysis (as proposed for instance for the Square Kilometer Array (SKA) radio telescope) could be an option. In this approach, the raw data is discarded after the low latency retrieval of relevant information.

In general, it is reassuring that the combined analysis of time-series data from several sources has been successfully demonstrated by various radio astronomy collaborations. Utilizing cloud storage and grid computing tools, the handling of large datasets seems of no major concern. In addition, data folding techniques based on inherent symmetries, such as the Earth's sidereal rotation, have proven effective to decrease data volume in stochastic background searches at audio-band frequencies (Ain et al. 2015). Stacking years of data into a single day while preserving all the statistical properties would even make it possible to carry out the final analysis on personal computing devices.

<sup>34</sup> Note that storage requirements are not proportional to the frequency of interest, but to the bandwidth, as the typical observation frequency can always be scaled down with an appropriate heterodyne technique.

### 5.8.4 Coincidence counting experiments

We have seen in Sect. 5 that single photon detection capabilities in the GHz range could boost the sensitivity of many planned and proposed instruments. Even though in such setups, no continuous time series data is recorded, correlations between multiple detectors can still be exploited. Every detected photon can be timestamped with  $\mu\text{s}$  resolution or better, allowing for offline coincidence searches involving any number of experiments. This approach is in particular interesting for short transient signals like those from PBH mergers.

For a given coincidence time interval  $\tau$ , determined by the duration of the signal or by the detector's time resolution, the overall efficiency  $\epsilon_{\text{tot}}$  can be adjusted via the number of required coincidences  $k$  in a system of  $N$  detectors:

$$\epsilon_{\text{tot}} = \sum_{i \geq k} \binom{N}{i} \epsilon_{\text{det}}^i (1 - \epsilon_{\text{det}})^{N-i}, \quad (130)$$

where  $\epsilon_{\text{det}}$  is the probability for each individual detector to see a signal photon. The corresponding rate of accidental coincidences,  $R_{\text{acc}}$ , depends on the dark count rate  $R_{\text{dark}}$  in an individual detector and is given by:

$$R_{\text{acc}} = \tau^{-1} \sum_{i \geq k} \binom{N}{i} (\tau R_{\text{dark}})^i [1 - (\tau R_{\text{dark}})]^{N-i}, \quad (131)$$

Note that the coincidence counting approach also allows the combination of information from several narrow band detectors operating at different frequencies if the time evolution of the signal frequency spectrum is known.

## 5.9 Summary of detector sensitivities

Table 6 summarizes the existing and proposed technologies for high-frequency GW detection, referring to the sections above for details. We also specify the maturity of each technology, that is, whether the experiment has been built, is under active R&D, or only the physical mechanism has been identified theoretically. In the frequency column, square brackets indicate a range of frequencies that can be scanned in the case of resonant detectors, whereas round brackets indicate the bandwidths of broadband detectors. Entries marked with a star (\*) correspond to setup for which we consider both resonant and broadband operation. Table 7 gives an overview of the different concepts by technical approach, stating the signal and sensing process used, and what kind of resonant enhancement the setup provides.



**Table 6** Summary of existing and proposed detectors and the frequency ranges in which they are sensitive. See Sect. 5.9 for details

| Technology                                                                                                   | Operational frequency         |
|--------------------------------------------------------------------------------------------------------------|-------------------------------|
| <b>Laser Interferometers</b> , Sect. 5.1.1, Sect. 5.1.2                                                      |                               |
| NEMO (R&D), Ackley et al. (2020), Bailes et al. (2019)                                                       | (1–2.5) kHz                   |
| 0.75 m interferometer (built), Akutsu et al. (2008), Nishizawa et al. (2008)                                 | 100 MHz                       |
| Holometer (built) Chou et al. (2017)                                                                         | (1–13) MHz                    |
| Twin table-top 3D interferometers (built), Patra et al. (2025)                                               | (1–250) MHz                   |
| <b>Spherical Resonant Mass Detectors</b> , Sect. 5.1.3, Forward (1971)                                       |                               |
| Mini-GRAIL (built), Gottardi et al. (2007)                                                                   | 2942.9 Hz                     |
| Schenberg antenna (built), Aguiar (2011)                                                                     | 3.2 kHz                       |
| <b>Optically Levitated Sensors</b> , Sect. 5.2.1, Arvanitaki and Geraci (2013)                               |                               |
| Levitated Sensor Detector 1-meter prototype (R&D), Aggarwal et al. (2022)                                    | [10–100] kHz                  |
| Levitated Sensor Detector 100-meter instrument (proposed), Aggarwal et al. (2022)                            | [10–100] kHz                  |
| <b>Bulk Acoustic Wave Resonators</b> , Sect. 5.2.2                                                           |                               |
| Goryachev's detector (built), Goryachev et al. (2014)                                                        | [1–1000] MHz                  |
| <b>Deformation of Microwave Cavities</b> , Sect. 5.2.3, Pegoraro et al. (1978a, 1978b), Berlin et al. (2023) |                               |
| Caves' detector (proposed), Caves (1979)                                                                     | 500 Hz                        |
| Reece's 1st detector (built), Reece et al. (1984)                                                            | MHz                           |
| Reece's 2nd detector (built), Reece et al. (1982)                                                            | 10 GHz                        |
| Pegoraro's detector (proposed), Pegoraro et al. (1978b)                                                      | [1–10] GHz                    |
| DESY/UHH–FNAL collaboration (R&D), Fischer et al. (2025)                                                     | (kHz–GHz)                     |
| <b>Magnetic Weber Bar</b> , Sect. 5.2.4, Domcke et al. (2025b), Carney et al. (2025)                         | (10 kHz–1 MHz)                |
| <b>RF Cavities</b> , Sect. 5.3.1, Berlin et al. (2022)                                                       |                               |
| ADMX (built), Bartram et al. (2021)                                                                          | [0.65–1.02] GHz               |
| HAYSTAC (built), Zhong et al. (2018)                                                                         | [5.6–5.8] GHz                 |
| CAPP (built), Kwon et al. (2021)                                                                             | [1.6–1.65] GHz                |
| ORGAN (built), Quiskamp et al. (2022, 2024)                                                                  | [15–16], [26–27] GHz          |
| SQMS (R&D), Posen (2021)                                                                                     | [1–2] GHz                     |
| Cubic cavities 1, 2, 3 (R&D), Navarro et al. (2024)                                                          | 0, 1, 1, 10 GHz               |
| <b>LC-circuit Axion Haloscopes</b> , Sect. 5.3.2, Domcke et al. (2022, 2024)                                 |                               |
| ABRACADABRA (built), Salemi et al. (2021)                                                                    | (0.1–2) MHz                   |
| SHAFT (built), Gramolin et al. (2021)                                                                        | (3 kHz–3 MHz)                 |
| ADMX SLIC (built), Crisosto et al. (2020)                                                                    | 0.043 GHz                     |
| BASE (built), Devlin et al. (2021)                                                                           | 0.4 MHz                       |
| WISPLC (R&D), Zhang et al. (2022)                                                                            | (0.03–5) MHz                  |
| DMRadio- $m^3$ (R&D), Brouwer et al. (2022a)                                                                 | [5–200]* MHz                  |
| DMRadio-GUT (R&D), Brouwer et al. (2022b)                                                                    | [0.1–30]* MHz                 |
| <b>Light Shining through a Wall</b> , Sect. 5.4.1, Ejlli et al. (2019), Ringwald et al. (2021)               |                               |
| OSQAR I (built), Ballou et al. (2015)                                                                        | $(0.3 - 0.8) \times 10^6$ GHz |
| OSQAR II (built), Ballou et al. (2015)                                                                       | $(0.3 - 1) \times 10^6$ GHz   |
| ALPS I (built), Bähre et al. (2013)                                                                          | $(0.3 - 1) \times 10^6$ GHz   |
| ALPS II (built), Bähre et al. (2013), Albrecht et al. (2021)                                                 | $[0.3 - 1]^* \times 10^6$ GHz |

**Table 6** continued

| Technology                                                                             | Operational frequency                  |
|----------------------------------------------------------------------------------------|----------------------------------------|
| JURA (proposed), Beacham et al. (2020)                                                 | $[0.3 - 1]^* \times 10^6$ GHz          |
| <b>Axion Helioscopes</b> , Sect. 5.4.1, Ejlli et al. (2019), Ringwald et al. (2021)    |                                        |
| CAST (built), Anastassopoulos et al. (2017)                                            | $(0.5 - 1.6) \times 10^9$ GHz          |
| BabyIAXO (R&D), Abeln et al. (2021)                                                    | $(0.25 - 2) \times 10^9$ GHz           |
| IAXO (R&D), Armengaud et al. (2019)                                                    | $(0.25 - 2) \times 10^9$ GHz           |
| <b>Dielectric Axion Haloscopes</b> , Sect. 5.4.2, Domcke et al. (2025a)                |                                        |
| Madmax (R&D), Brun et al. (2019)                                                       | $[100 \text{ MHz} - 10 \text{ GHz}]^*$ |
| DALI prototype (R&D), De Miguel et al. (2024)                                          | 7, 33 GHz                              |
| DALI phase II (proposed), De Miguel et al. (2024)                                      | (6 – 60) GHz                           |
| <b>High Energy Pulsed Lasers</b> , Sect. 5.5.1, Vacalis et al. (2023)                  | $[10^4 - 10^{10}]$ GHz                 |
| <b>Conversion in a Static Electric Field</b> , Sect. 5.5.2                             |                                        |
| Atomic electric field, Dai and Liang (2023)                                            | $(10^{11} - 10^{15})$ GHz              |
| <b>Resonant Polarization Rotation</b> , Sect. 5.5.2, Cruise (1983)                     |                                        |
| Cruise's detector (proposed), Cruise (2000)                                            | $[0.1 - 10^5]$ GHz                     |
| Cruise & Ingley's detector (prototype), Cruise and Ingley (2005, 2006)                 | 100 MHz                                |
| Optical cavities of ALPS II (built), García-Cely et al. (2025)                         | $[0.1 \text{ MHz} - 0.1 \text{ THz}]$  |
| <b>Superconducting Rings</b> , Sect. 5.7.1, Anandan and Chiao (1982), Chiao (2002)     | 10 GHz                                 |
| <b>Graviton–Magnon Resonance</b> , Sect. 5.7.2, Ito et al. (2020), Ito and Soda (2023) | [8–14] GHz                             |
| <b>Atomic Precision Measurement</b> , Sect. 5.7.3, Bringmann et al. (2023)             | [10 kHz–10 GHz]                        |
| <b>One-Electron Quantum Cyclotron</b> , Sect. 5.7.4, Ito and Soda (2023)               | [20–200] GHz                           |
| <b>Rydberg Atoms</b> , Sect. 5.7.5, Kanno et al. (2025)                                | [0.3–16] GHz                           |

## 6 Discussion and conclusions

The search for high-frequency gravitational waves is a promising and challenging endeavor. Given the scarcity of astrophysical sources at frequencies  $\gtrsim$  kHz, it offers in particular unique opportunities to test theories beyond the Standard Model that could not be tested otherwise.

In fact, numerous models proposed to address open questions in particle physics and cosmology predict gravitational-wave signals in the frequency range  $f \simeq (10^3 - 10^{10})$  Hz. These can be coherent signals, for example from mergers of sub-solar mass compact objects or from axion superradiance around black holes; or they can be stochastic signals, for instance from certain models of cosmic inflation or from first-order phase transition in the very early Universe. In the latter case, physics at higher energies, or equivalently earlier cosmological epochs, corresponds to higher gravitational wave frequencies and correspondingly smaller experimental devices. As can be seen from Fig. 4, the ultra-high frequency band, ranging from

**Table 7** Overview of the different detection concepts for high-frequency gravitational waves by technical approach

| Technology                                                             | Signal                                           | Sensing                                                             | Resonator                                                       |
|------------------------------------------------------------------------|--------------------------------------------------|---------------------------------------------------------------------|-----------------------------------------------------------------|
| Laser Interferometers                                                  | Movement of test masses (mirrors)                | Interferometric monitoring of test mass positions                   | Optical cavity                                                  |
| Spherical Resonant Mass                                                | Deformation of test mass                         | Capacitive or superconducting electromechanical transducers         | Vibrational eigenmodes of test mass                             |
| Optically Levitated Sensors                                            | Movement of levitated nanoparticle               | Interferometric measurement of levitated sensor and mirror movement | Resonance with trapping frequency of levitated sensor           |
| Bulk Acoustic Wave Resonators                                          | Deformation of test mass                         | Electromechanical transducer                                        | Vibrational eigenmodes of test mass                             |
| Deformation of Microwave Cavities                                      | Electromagnetic mode mixing                      | Power in empty cavity mode                                          | Resonant energy transfer to cavity eigenmode                    |
| Magnetic Weber Bar                                                     | Deformation of superconducting coils             | SQUID-based sensing of oscillating magnetic field                   | Vibrational eigenmodes of coils, optionally resonant LC circuit |
| SRF Cavities                                                           | Induced effective current in magnetic field      | Power in empty cavity mode                                          | Electromagnetic cavity eigenmodes                               |
| LC-circuit Axion Haloscopes                                            | Induced current                                  | SQUID-based low current sensing                                     | Resonant LC circuit (or none for broadband)                     |
| Light Shining through a Wall, Axion Helioscopes, Dielectric Haloscopes | Magnetic conversion                              | Heterodyne, correlation, single photon counting                     | Optical cavity eigenmodes (or none for broadband)               |
| Astrophysical and Cosmological Detection                               | Magnetic conversion                              | Radio, IR, optical, UV, X-ray, $\gamma$ -ray telescopes             | None                                                            |
| Superconducting Rings                                                  | Josephson current induced by GW–spin interaction | Electromechanical transducer                                        | None                                                            |
| Graviton–Magnon Resonance                                              | Magnon excitation in ferromagnet                 | Coupling the magnon to an eigenmode of a microwave cavity           | Magnon modes                                                    |
| Atomic Precision Measurement                                           | Modulation of photon frequencies                 | Optical atomic clock readout protocol                               | None                                                            |
| One-Electron Quantum Cyclotron                                         | Excitation of electron in Penning trap           | Quantum jump spectroscopy                                           | Penning trap cyclotron modes                                    |
| Rydberg Atoms                                                          | Electromagnetically induced transparency         | Absorption spectroscopy                                             | Atomic transition                                               |

MHz to GHz, is an exciting window to explore fundamental physics up to the grand unification or string theory scales of order ( $10^{16}$ – $10^{17}$ ) GeV. It would be remarkable if the experimental test of fundamental physics at the highest energies and of the earliest times in the history of the Universe could eventually be achieved not with huge particle accelerators or with satellite interferometry, but with small table-top experiments.

Many of cosmological gravitational wave sources can lead to relatively large signals corresponding to an  $\mathcal{O}(1)$  fraction of the energy density in the early Universe being converted to gravitational waves. This energy is red-shifted in the expanding Universe, rendering even these strong signals challenging to detect today. Moreover, in many cases the amplitude of the signal depends sensitively on the model parameters and may be significantly lower in large parts of the model parameter space. In Sect. 4 of this review, we have given an overview of high-frequency gravitational wave sources, and a concise summary can be found in Tables 1 and 2.

The high-frequency band comes with particular challenges and opportunities. High-frequency gravitational waves carry a high energy density, implying that cosmological bounds on the energy density in relativistic species translate to stringent bounds on the characteristic gravitational-wave strain. This poses a severe challenge for detection, as the magnitude of observable effects is typically governed by the strain and not by the energy density. The detection of cosmological sources of high-frequency gravitational waves is therefore much more challenging than comparable searches at lower frequencies. On the other hand, the lack of known astrophysical gravitational-wave sources in this frequency range presents a unique opportunity for foreground free searches for new physics.

At the moment, there is no general consensus on the most promising detection strategy in this frequency band, though many proposals have been put forward in the past decades. The proposals that we are aware of are summarized in Table 6, and their sensitivities are plotted in Figs. 1 and 2. We emphasize that a given sensitivity in terms of noise equivalent strain at a higher frequency typically implies a reduced sensitivity to the viable parameter space of a given cosmological source than at lower frequency. Detectors based on magnetic conversion seem to be particularly promising avenues at very high frequencies (above  $\sim$ GHz) while relying on mechanical coupling of GWs seems advantageous at lower frequencies. It should be kept in mind, however, that more careful studies of noise levels and of the margin of improvement with foreseeable technology development is needed in many cases. We hope that this document will stimulate the necessary discussion.

None of the detection concepts listed in this report currently reach the sensitivity needed to probe realistic sources. Even under optimistic assumptions, they fall short by at least several orders of magnitude. However, we recall that, one hundred years ago, the technological gap in strain sensitivity in both the LIGO and LISA frequency ranges was about 15–16 orders of magnitude (Chen et al. 2017). Also, about 50 years ago, Misner, Thorne and Wheeler declared that ‘*such detectors have so low sensitivity that they are of little experimental interest*’ (Misner et al. 1973), referring to laser interferometers. The first laser interferometer gravitational-wave

detector, built at Hughes Research Laboratories in the 1970s (Forward 1978) had a sensitivity which was eight orders of magnitudes below the design sensitivity of the currently operating LIGO/Virgo/KAGRA detectors. Today, there are clear development paths towards detectors with sensitivities of  $\sqrt{S_n} \simeq 10^{-38} \text{ Hz}^{-1/2}$  using, e.g., magnetic conversion at optical frequencies (see Sect. 5.4).

We therefore take the past history of laser interferometry as an encouraging lesson for the development of gravitational-wave detectors in the high-frequency band. The challenges are formidable, but the opportunities and potential rewards are unique.

This White Paper sets the stage for the launch of the Ultra-High-Frequency Gravitational Wave (UHF-GW) initiative,<sup>35</sup> a network of researchers with the common goal of further pushing the boundaries of gravitational-wave science in the high-frequency range and to collaboratively work towards the long-term goal of a first detection of a signal in this frequency range.

We strongly encourage feedback regarding additional sources or detection techniques which we may have missed, as well as critical assessments of the ones presented here.

## Appendix: Electromagnetic Signals Generated by GWs

We have seen in Sect. 5 that many promising detection techniques for high-frequency GWs rely on graviton-to-photon conversion in a magnetic field. Here, we review several calculation methods relevant to such signals.

The starting point are Maxwell's equations in curved spacetime (Landau and Lifshitz 1975)

$$\begin{aligned}\nabla_\nu F_{\alpha\beta} + \nabla_\alpha F_{\beta\nu} + \nabla_\beta F_{\nu\alpha} &= \partial_\nu F_{\alpha\beta} + \partial_\alpha F_{\beta\nu} + \partial_\beta F_{\nu\alpha} = 0, \\ \partial_\nu (\sqrt{-g} F^{\mu\nu}) &= \sqrt{-g} j^\mu.\end{aligned}\quad (132)$$

Here, as usual,  $g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$  is the metric, separated into the Minkowski part and the perturbation. The field and the current may be separated accordingly as

$$F_{\mu\nu} = F_{0\mu\nu} + F_{h\mu\nu} + \mathcal{O}(h^2) \quad \text{and} \quad j^\mu = j_0^\mu + j_h^\mu + \mathcal{O}(h^2). \quad (133)$$

Here subscript 0 represents quantities in the absence of GWs, and the subscript  $h$  indicates terms linear in the metric perturbation. The current  $j_h^\mu$  may be attributed to the effect of the GW on the motion of electric charges. At GW frequencies higher the mechanical eigenfrequencies associated with the experimental apparatus, the system is effectively in free fall (Bringmann et al. 2023; Ratzinger et al. 2024), and it is hence convenient to adopt the transverse-traceless (TT) gauge for the GWs. In these coordinates, the system remains at rest while the GW passes, so we can neglect the effect of the GW on external currents, that is,  $j_h^\mu = 0$ .

For concreteness, let us consider a  $+$ -polarized GW propagating in the  $x$ -direction through a region of length  $L$  with a uniform magnetic field  $B_0$  pointing in the  $z$ -direction:

<sup>35</sup> <http://www.ctc.cam.ac.uk/activities/UHF-GW.php>.

$$h_{\mu\nu} = h_+ (\delta_{\mu 2} \delta_{\nu 2} - \delta_{\mu 3} \delta_{\nu 3}) e^{-i\omega(t-x)} + \text{c.c.}, \quad (134)$$

$$F_{0\mu\nu} = \begin{cases} B_0 (\delta_{\mu 1} \delta_{\nu 2} - \delta_{\mu 2} \delta_{\nu 1}) & |x| < \frac{L}{2} \\ 0 & \text{otherwise} \end{cases}. \quad (135)$$

This situation corresponds to an external current,  $j_0^\mu = \partial_\nu F_0^{\mu\nu}$  consisting of two Dirac- $\delta$  peaks at  $x = \pm L/2$ , thereby sourcing the external field in the region  $|x| < L/2$ . The solution of Eq. (132) for any  $x$  with the appropriated boundary conditions can be readily found as

$$F_{h\mu\nu} = \begin{cases} \frac{1}{4} (-F_{\mu\nu}^{(E)} + F_{\mu\nu}^{(B)}) (e^{i\omega L} - e^{-i\omega L}) e^{-i\omega(t+x)} + \text{c.c.} & x < -\frac{L}{2} \\ \frac{1}{4} (-F_{\mu\nu}^{(E)} + F_{\mu\nu}^{(B)}) e^{i\omega L} e^{-i\omega(t+x)} \\ + \frac{1}{4} [F_{\mu\nu}^{(E)} + i\omega L (1 + \frac{2x}{L}) (F_{\mu\nu}^{(E)} + F_{\mu\nu}^{(B)}) \\ + 3F_{\mu\nu}^{(B)}] e^{-i\omega(t-x)} + \text{c.c.} & |x| < \frac{L}{2} \\ \frac{i}{2} (F_{\mu\nu}^{(E)} + F_{\mu\nu}^{(B)}) \omega L e^{-i\omega(t-x)} + \text{c.c.} & x > \frac{L}{2} \end{cases} \quad (136)$$

where  $F_{\mu\nu}^{(E)} \equiv h_+ B_0 (\delta_{\mu 2} \delta_{\nu 0} - \delta_{\mu 0} \delta_{\nu 2})$  and  $F_{\mu\nu}^{(B)} \equiv h_+ B_0 (\delta_{\mu 1} \delta_{\nu 2} - \delta_{\mu 2} \delta_{\nu 1})$ . It follows that an electromagnetic signal is generated even at  $|x| > L/2$ , where the external field vanishes. In these regions, the electromagnetic energy-momentum tensor

$$\mathcal{T}^{\mu\nu} = \left( g^{\mu\rho} g^{\nu\sigma} - \frac{1}{4} g^{\mu\nu} g^{\rho\sigma} \right) g^{\alpha\beta} F_{\rho\alpha} F_{\sigma\beta}, \quad (137)$$

averaged over several periods of the signal, is

$$\langle \mathcal{T}^{\mu\nu} \rangle \Big|_{x > \frac{L}{2}} = \frac{1}{2} h_+^2 B_0^2 \omega^2 L^2 \begin{pmatrix} 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix} \quad (138)$$

$$\langle \mathcal{T}^{\mu\nu} \rangle \Big|_{x < -\frac{L}{2}} = \frac{1}{2} h_+^2 B_0^2 \sin^2(\omega L) \begin{pmatrix} 1 & -1 & 0 & 0 \\ -1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}. \quad (139)$$

The probability of GW conversion into photons can be calculated by taking the ratio of the Poynting vector (the off-diagonal component of  $\langle \mathcal{T}^{\mu\nu} \rangle$ ) and the flux of gravitational waves,  $h_+^2 \omega^2 / (8\pi G)$ . In the limit  $\omega L \gg 1$ , one finds

$$P|_{x > \frac{L}{2}} = 4\pi G B_0^2 L^2, \quad (140)$$

and  $P|_{x < -\frac{L}{2}} \simeq 0$ . Using the same method, one finds the same conversion probability for  $\times$ -polarized GWs. This is the inverse Gertsenshtein effect, discussed first in Gertsenshtein and Pustovöit (1962) [see also Boccaletti et al. (1970)], using an approach very similar to the one just described.

These results can also be derived in other ways without directly solving Maxwell's equations in curved spacetime:

*Effective current approach* This method consists of recasting Eq. (132) as a standard electrodynamics problem in Minkowski spacetime, with an effective current sourcing the field  $F_{\mu\nu}$ . Concretely, in the TT frame,  $\sqrt{-g} \simeq \mathcal{O}(h^2)$  and the expression in parenthesis in the inhomogeneous Maxwell equation [second line of Eq. (132)] can be written as

$$\sqrt{-g} g^{\alpha\mu} F_{\alpha\beta} g^{\beta\nu} \simeq F^{\mu\nu} + F_h^{\mu\nu} - h^{\alpha\mu} F_{0\alpha}{}^\nu - F_0{}^\mu{}_\beta h^{\beta\nu} + \mathcal{O}(h^2), \quad (141)$$

where we have raised indices with  $\eta$ , as we will continue to do. Employing Eq. (133) and taking  $j_h^\mu = 0$  in the TT frame as explained above, one finds

$$\partial_\nu F_h^{\mu\nu} = j_{\text{eff}}^\nu, \quad \text{with} \quad j_{\text{eff}}^\nu \equiv \partial_\nu (F_0^{\mu\alpha} h^\nu{}_\alpha - F_0^{\nu\alpha} h^\mu{}_\alpha). \quad (142)$$

Note that there are fewer terms here than in Eq. (108) in Sect. 5.3 because in the TT frame  $h_\mu{}^\mu = 0$ . The effective current can also be expressed as (Domcke et al. 2022)

$$j_{\text{eff}}^\mu = (-\nabla \cdot \mathbf{P}, \nabla \times \mathbf{M} + \partial_t \mathbf{P}), \quad (143)$$

introducing the effective polarization,  $P_i \equiv -h_{ij}E_{0j}$ , and magnetization,  $M_i \equiv -h_{ij}B_{0j}$ . As an example, for the specific case of Eq. (135),  $\mathbf{P} = 0$  and  $\mathbf{M} = 2h_+ B_0 \cos(kt - kx) \Theta(L/2 - |x|) \hat{\mathbf{z}}$ . Imposing the appropriated boundary condition, this oscillating magnetization leads to the induced field  $F_{h\mu\nu}$  reported above, and consequently to the conversion probability in Eq. (140). This method readily generalizes to other GW frames beyond the TT gauge, for instance the proper detector frame, and is particularly convenient for studying complicated setups such as resonant cavities, low-mass axion haloscopes or dielectric haloscopes (Berlin et al. 2022; Domcke et al. 2022, 2024, 2025a).

*S-matrix approach* This method exploits the fact that GWs couple to the energy-momentum tensor of the electromagnetic field. Concretely, this coupling is given by

$$\mathcal{L} \supset \frac{1}{2} h_{\mu\nu} T^{\mu\nu} = h_{\mu\nu} F_h{}^\nu{}_\alpha F_0^{\mu\alpha} + \dots, \quad (144)$$

where we have used Eq. (133) and (137). This permits an interpretation of the Gertsenshtein effect in terms of Feynman diagrams as conversion of a gravitational perturbation into a photon as it scatters off an external electromagnetic field.

It is easy to see that the *S*-matrix approach yields the same conversion rates as the effective current method by noting that  $\mathcal{L}$  can be rewritten as  $\mathcal{L} \supset A_{\mu\nu} j_{\text{eff}}^\mu + \dots$ , which follows from writing  $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$  in Eq. (144) and integrating by parts. However, the *S*-matrix approach does not provide the induced

electromagnetic field,  $F_{\mu\nu}$ , at each point in space. Instead, it gives the probability amplitude at large distances, or equivalently, the scattering cross sections.

This method was employed in the seminal paper Raffelt and Stodolsky (1988) to calculate Eq. (140) and to point out the close analogy with axion–photon conversion. The method has been used to calculate graviton-to-photon conversion rates for various external field configurations, including both uniform and dipole electric and magnetic fields, including setup from Eq. (139) above (De Logi and Mickelson 1977).

*Geometric optics.* It is known that in a slowly varying background Maxwell’s equations admit solutions that correspond to geometric optics in classical electrodynamics. Exploiting the analogy between axions and GWs and allowing for a plasma mass, this has been recently studied for GWs in McDonald and Millington (2024). This approach yields the conversion probabilities given in Eq. (140) in the limit of very high frequencies. Notably, the geometric optics method has been employed recently to calculate conversion rates in the magnetospheres of neutron stars (McDonald and Ellis 2024), see also Sect. 5.6. Its advantage in this context is that it can account for three-dimensional effects that extend beyond the approximations presented in the classical work Raffelt and Stodolsky (1988). Moreover, as shown by these authors, the geometric optics limit enables the investigation of polarization effects.

Finally, it is important to emphasize that while the formal separation of the electromagnetic field and current in Eq. (133) is generally straightforward for specific experimental setups, its interpretation requires caution as it is neither coordinate invariant nor gauge invariant (Ratzinger et al. 2024). This difficulty is exacerbated by the existence of multiple methods for calculating a given observable, meaning that only well-defined (gauge-invariant) quantities can be used to compare different calculation methods. Alternatively, one may adopt a coordinate-independent formalism such as the one proposed in Ratzinger et al. (2024).

**Acknowledgements** We thank ICTP Trieste and CERN TH for hosting the first three editions of ultra-high frequency gravitational wave workshops which were key for providing input and organizing this Living Review and its update. A special thank you to all speakers and participants of these workshops, whose contributions were key in shaping this report. We moreover thank Masha Baryakhtar, William Campbell, Yiwen Chu, Virgile Dandoy, Aldo Ejlli, Javier de Miguel, Juan García-Bellido, Ken-Ichi Herada, Alessandro Lella, Axel Lindner, Sotatsu Otabe, Christoph Reinhardt, Seyed Mohammad Sadegh Movahed, Mikel Sanchez, Tommaso Tabarelli, Yutong He for valuable input. We also thank the referees of *Living Reviews in Relativity* for their supportive and well-thought reports. The Australian High-Frequency Gravitational Wave Effort is supported by the Australian Research Council Centre of Excellence for Gravitational Wave Discovery (OzGrav), Grant number CE170100004. N.A. is supported by NSF grant PHY-1806671 and a CIERA Postdoctoral Fellowship from the Center for Interdisciplinary Exploration and Research in Astrophysics at Northwestern University. A.B. acknowledges support by the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation programme under grant agreement No. 759253 and by Deutsche Forschungsgemeinschaft (DFG, German Research Foundation)—Project-ID 279384907—SFB 1245 and—Project-ID 138713538—SFB 881 (‘The Milky Way System’, subproject A10). O.D.A. thanks FAPESP / Brazil (grant numbers 1998/13468-9 and 2006/56041-3) and CNPq/Brazil (grants numbers 306467\_2003\_8, 303310\_2009-0, 307176\_2013-4, and 302841/2017-2). This project has received funding from the Deutsche Forschungsgemeinschaft under Germany’s Excellence Strategy – EXC 2121 ‘Quantum Universe’, 390833306 (V.D., F.M., K.P., A.R.), and EXC 2118 ‘Precision Physics, Fundamental Interactions and Structure of Matter’ (PRISMA+), 390831469 (J.K., C.T.). D.G.F. (ORCID 0000-0002-4005-8915) is supported by a Ramón y Cajal contract



by Spanish Ministry MINECO, with Ref. RYC-2017-23493, and by the grant ‘SOM: Sabor y Origen de la Materia’, from Spanish Ministry of Science and Innovation, under no. FPA2017-85985-P. A.G. is supported in part by NSF grants PHY-1806686 and PHY-1806671, the Heising-Simons Foundation, the W.M. Keck Foundation, the John Templeton Foundation, and ONR Grant N00014-18-1-2370. M.G. and M.E.T. were funded by the ARC Centre for Excellence for Engineered Quantum Systems, CE170100009, and the ARC Centre for Excellence for Dark Matter Particle Physics, CE200100008, as well as ARC grant DP190100071. F.M. is funded by a UKRI/EPSRC Stephen Hawking fellowship, grant reference EP/T017279/1. This work has been partially supported by STFC consolidated grant ST/P000681/1. A.R. acknowledges funding from Italian Ministry of Education, University and Research (MIUR) through the ‘Dipartimenti di eccellenza’ project Science of the Universe. S.S. was supported by MIUR in Italy under Contract(No. PRIN 2015P5SBHT) and ERC Ideas Advanced Grant (No. 267985) ‘DaMeSyFla’. F.T. acknowledges support from the Swiss National Science Foundation (project number 200020/175502). C.U. is supported by European Structural and Investment Funds and the Czech Ministry of Education, Youth and Sports (Project CoGraDS—CZ.02.1.01/0.0/0.0/15\_003/0000437) and partially supported by ICTP. D.B. acknowledges the support from the Departament de Recerca i Universitats from Generalitat de Catalunya to the Grup de Recerca 00649 (Codi: 2021 SGR 00649). The research leading to these results has received funding from the Spanish Ministry of Science and Innovation (PID2020-115845GB-I00/AEI/10.13039/501100011033). This publication is part of the grant PID2023-146686NB-C31 funded by MICIU/AEI/10.13039/501100011033/ and by FEDER, UE. IFAE is partially funded by the CERCA program of the Generalitat de Catalunya. J.M. acknowledges support from the Science and Technology Facilities Council (STFC) [Grant No. ST/X00077X/1]. C.G.C. is supported by a Ramón y Cajal contract with Ref. RYC2020-029248-I, the Spanish National Grant PID2022-137268NA-C55 and Generalitat Valenciana through the grant CIPROM/22/69. D.B. and V.D. acknowledge the support by the European Research Area (ERA) via the UNDARK project (project number 101159929).

**Open Access** This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit <http://creativecommons.org/licenses/by/4.0/>.

## References

- Aasi J et al (2014) Constraints on cosmic strings from the LIGO-Virgo gravitational-wave detectors. *Phys Rev Lett* 112:131101. <https://doi.org/10.1103/PhysRevLett.112.131101>. arXiv:1310.2384 [gr-qc]
- Aasi J et al (2015) Advanced LIGO. *Class Quantum Grav* 32:074001. <https://doi.org/10.1088/0264-9381/32/7/074001>
- Abbott BP et al (2016a) GW150914: The advanced LIGO detectors in the era of first discoveries. *Phys Rev Lett* 116:131103. <https://doi.org/10.1103/PhysRevLett.116.131103>. arXiv:1602.03838 [gr-qc]
- Abbott BP et al (2016b) Observation of gravitational waves from a binary black hole merger. *Phys Rev Lett* 116:061102. <https://doi.org/10.1103/PhysRevLett.116.061102>. arXiv:1602.03837 [gr-qc]
- Abbott BP et al (2017a) Exploring the sensitivity of next generation gravitational wave detectors. *Class Quantum Gravity* 34:044001. <https://doi.org/10.1088/1361-6382/aa51f4>. arXiv:1607.08697 [astro-ph.IM]
- Abbott BP et al (2017b) GW170817: Observation of gravitational waves from a binary neutron star inspiral. *Phys Rev Lett* 119(16):161101. <https://doi.org/10.1103/PhysRevLett.119.161101>. arXiv:1710.05832 [gr-qc]

- Abbott BP et al (2018) Constraints on cosmic strings using data from the first Advanced LIGO observing run. *Phys Rev D* 97:102002. <https://doi.org/10.1103/PhysRevD.97.102002>. arXiv:1712.01168 [gr-qc]
- Abbott BP et al (2019) GWTC-1: a gravitational-wave transient catalog of compact binary mergers observed by LIGO and virgo during the first and second observing runs. *Phys Rev X* 9:031040. <https://doi.org/10.1103/PhysRevX.9.031040>. arXiv:1811.12907 [astro-ph.HE]
- Abdikamalov E, Gossan S, DeMaio AM, Ott CD (2014) Measuring the angular momentum distribution in core-collapse supernova progenitors with gravitational waves. *Phys Rev D* 90(4):044001. <https://doi.org/10.1103/PhysRevD.90.044001>. arXiv:1311.3678 [astro-ph.SR]
- Abdikamalov E, Pagliaroli G, Radice D (2020) Gravitational waves from core-collapse supernovae. In: Bambi C, Katsanevas S, Kokkotas KD (eds) *Handbook of gravitational wave astronomy*. Springer, Singapore. [https://doi.org/10.1007/978-981-15-4702-7\\_21-1](https://doi.org/10.1007/978-981-15-4702-7_21-1). arXiv:2010.04356 [astro-ph.SR]
- Abdikamalov EB, Dimmelmeier H, Rezzolla L, Miller JC (2009) Relativistic simulations of the phase-transition-induced collapse of neutron stars. *Mon Not R Astron Soc* 394:52–76. <https://doi.org/10.1111/j.1365-2966.2008.14056.x>. arXiv:0806.1700 [astro-ph]
- Abeln A et al (2021) Conceptual design of BabyIAXO, the intermediate stage towards the International Axion Observatory. *JHEP* 05:137. [https://doi.org/10.1007/JHEP05\(2021\)137](https://doi.org/10.1007/JHEP05(2021)137). arXiv:2010.12076 [physics.ins-det]
- Abernathy M, Acernese F, Ajith P, Allen B, Amaro-Seoane P, Andersson N, Aoudia S, Astone P, Krishnan B, Barack L et al (2011) Einstein gravitational wave telescope (ET) conceptual design study. <https://www.et-gw.eu/et/index.php/etdsdocument>
- Acernese F, Agathos M, Aiello L, Allocca A, Amato A, Ansoldi S, Antier S, Arène M, Arnaud N, Ascenzi S et al (2019) Increasing the astrophysical reach of the Advanced Virgo detector via the application of squeezed vacuum states of light. *Phys Rev Lett* 123:231108. <https://doi.org/10.1103/PhysRevLett.123.231108>
- Acernese F et al (2015) Advanced Virgo: a second-generation interferometric gravitational wave detector. *Class Quantum Gravity* 32:024001. <https://doi.org/10.1088/0264-9381/32/2/024001>
- Ackley K, Adya V, Agrawal P, Altin P, Ashton G, Bailes M, Baltinas E, Barbuio A, Beniwal D, Blair C et al (2020) Neutron star extreme matter observatory: a kilohertz-band gravitational-wave detector in the global network. *PASA* 37:e047. <https://doi.org/10.1017/pasa.2020.39>. arXiv:2007.03128
- Adhikari RX et al (2020) A cryogenic silicon interferometer for gravitational-wave detection. *Class Quantum Gravity* 37:165003. <https://doi.org/10.1088/1361-6382/ab9143>. arXiv:2001.11173 [astro-ph.IM]
- Adshead P, Giblin JT, Weiner ZJ (2018) Gravitational waves from gauge preheating. *Phys Rev D* 98:043525. <https://doi.org/10.1103/PhysRevD.98.043525>. arXiv:1805.04550 [astro-ph.CO]
- Adshead P, Giblin JT, Pieroni M, Weiner ZJ (2020a) Constraining axion inflation with gravitational waves across 29 decades in frequency. *Phys Rev Lett* 124:171301. <https://doi.org/10.1103/PhysRevLett.124.171301>. arXiv:1909.12843 [astro-ph.CO]
- Adshead P, Giblin JT, Pieroni M, Weiner ZJ (2020b) Constraining axion inflation with gravitational waves from preheating. *Phys Rev D* 101:083534. <https://doi.org/10.1103/PhysRevD.101.083534>. arXiv:1909.12842 [astro-ph.CO]
- Adya VB, Yap MJ, Töyrä D, McRae TG, Altin PA, Sarre LK, Meijerink M, Kijbunchoo N, Slagmolen BJJ, Ward RL, McClelland DE (2020) Quantum enhanced kHz gravitational wave detector with internal squeezing. *Class Quantum Gravity* 37(7):07LT02. <https://doi.org/10.1088/1361-6382/ab7615>
- Agazie G et al (2023) The NANOGrav 15 yr data set: evidence for a gravitational-wave background. *Astrophys J Lett* 951(1):L8. <https://doi.org/10.3847/2041-8213/acdac6>. arXiv:2306.16213 [astro-ph.HE]
- Aggarwal N, Winstone GP, Teo M, Baryakhtar M, Larson SL, Kalogera V, Geraci AA (2022) Searching for new physics with a levitated-sensor-based gravitational-wave detector. *Phys Rev Lett* 128:111101. <https://doi.org/10.1103/PhysRevLett.128.111101>. arXiv:2010.13157 [gr-qc]
- Aguiar OD (2011) The past, present and future of the resonant-mass gravitational wave detectors. *Res Astron Astrophys* 11:1–42. <https://doi.org/10.1088/1674-4527/11/1/001>. arXiv:1009.1138 [astro-ph.IM]
- Ahyoune S et al (2023) A proposal for a low-frequency axion search in the 1–2  $\mu$  eV range and below with the BabyIAXO magnet. *Annalen Phys* 535(12):2300326. <https://doi.org/10.1002/andp.202300326>. arXiv:2306.17243 [physics.ins-det]

- Ai WY, Laurent B, van de Vis J (2023) Model-independent bubble wall velocities in local thermal equilibrium. *JCAP* 07:002. <https://doi.org/10.1088/1475-7516/2023/07/002>. [arXiv:2303.10171](https://arxiv.org/abs/2303.10171) [astro-ph.CO]
- Ain A, Dalvi P, Mitra S (2015) Fast gravitational wave radiometry using data folding. *Phys Rev D* 92:022003. <https://doi.org/10.1103/PhysRevD.92.022003>. [arXiv:1504.01714](https://arxiv.org/abs/1504.01714) [gr-qc]
- Ajith P et al (2011) Inspiral-merger-ringdown waveforms for black-hole binaries with non-precessing spins. *Phys Rev Lett* 106:241101. <https://doi.org/10.1103/PhysRevLett.106.241101>. [arXiv:0909.2867](https://arxiv.org/abs/0909.2867) [gr-qc]
- Akrami Y et al (2020) Planck 2018 results. X. Constraints on inflation. *Astron Astrophys* 641:A10. <https://doi.org/10.1051/0004-6361/201833887>. [arXiv:1807.06211](https://arxiv.org/abs/1807.06211) [astro-ph.CO]
- Akutsu T et al (2008) Search for a stochastic background of 100-MHz gravitational waves with laser interferometers. *Phys Rev Lett* 101:101101. <https://doi.org/10.1103/PhysRevLett.101.101101>. [arXiv:0803.4094](https://arxiv.org/abs/0803.4094) [gr-qc]
- Akutsu T et al (2019) KAGRA: 2.5 generation interferometric gravitational wave detector. *Nat Astron* 3:35–40. <https://doi.org/10.1038/s41550-018-0658-y>. [arXiv:1811.08079](https://arxiv.org/abs/1811.08079) [gr-qc]
- Albrecht C, Barbanotti S, Hintz H, Jensch K, Klos R, Maschmann W, Sawlanski O, Stolper M, Trines D (2021) Straightening of superconducting HERA dipoles for the any-light-particle-search experiment ALPS II. *EPJ Tech Instrum* 8(1):5. <https://doi.org/10.1140/epjti/s40485-020-00060-5>. [arXiv:2004.13441](https://arxiv.org/abs/2004.13441) [physics.ins-det]
- Ali-Haïmoud Y, Kovetz ED, Kamionkowski M (2017) Merger rate of primordial black-hole binaries. *Phys Rev D* 96(12):123523. <https://doi.org/10.1103/PhysRevD.96.123523>. [arXiv:1709.06576](https://arxiv.org/abs/1709.06576) [astro-ph.CO]
- Allahverdi R, Brandenberger R, Cyr-Racine FY, Mazumdar A (2010) Reheating in inflationary cosmology: theory and applications. *Annu Rev Nucl Part Sci* 60:27–51. <https://doi.org/10.1146/annurev.nucl.012809.104511>. [arXiv:1001.2600](https://arxiv.org/abs/1001.2600) [hep-th]
- Allen B (1997) The stochastic gravity-wave background: sources and detection. In: Marck JA, Lasota JP (eds) *Relativistic gravitation and gravitational radiation: proceedings of the Les Houches School of Physics*. Cambridge University Press, Cambridge, p 373. [arXiv:gr-qc/9604033](https://arxiv.org/abs/gr-qc/9604033) [gr-qc]
- Allen B, Romano JD (1999) Detecting a stochastic background of gravitational radiation: signal processing strategies and sensitivities. *Phys Rev D* 59:102001. <https://doi.org/10.1103/PhysRevD.59.102001>. [arXiv:gr-qc/9710117](https://arxiv.org/abs/gr-qc/9710117)
- Allen B, Shellard EPS (1992) Gravitational radiation from cosmic strings. *Phys Rev D* 45:1898–1912. <https://doi.org/10.1103/PhysRevD.45.1898>
- Amaro-Seoane P et al (2017) Laser Interferometer Space Antenna. *arXiv e-prints* [arXiv:1702.00786](https://arxiv.org/abs/1702.00786) [astro-ph.IM]
- Amin MA (2013) K-oscillons: Oscillons with noncanonical kinetic terms. *Phys Rev D* 87:123505. <https://doi.org/10.1103/PhysRevD.87.123505>. [arXiv:1303.1102](https://arxiv.org/abs/1303.1102) [astro-ph.CO]
- Amin MA, Shirokoff D (2010) Flat-top oscillons in an expanding universe. *Phys Rev D* 81:085045. <https://doi.org/10.1103/PhysRevD.81.085045>. [arXiv:1002.3380](https://arxiv.org/abs/1002.3380) [astro-ph.CO]
- Amin MA, Easther R, Finkel H (2010) Inflaton fragmentation and oscillon formation in three dimensions. *JCAP* 1012:001. <https://doi.org/10.1088/1475-7516/2010/12/001>. [arXiv:1009.2505](https://arxiv.org/abs/1009.2505) [astro-ph.CO]
- Amin MA, Easther R, Finkel H, Flauger R, Hertzberg MP (2012) Oscillons after inflation. *Phys Rev Lett* 108:241302. <https://doi.org/10.1103/PhysRevLett.108.241302>. [arXiv:1106.3335](https://arxiv.org/abs/1106.3335) [astro-ph.CO]
- Amin MA, Hertzberg MP, Kaiser DI, Karouby J (2014) Nonperturbative dynamics of reheating after inflation: a review. *Int J Mod Phys D* 24:1530003. <https://doi.org/10.1142/S0218271815300037>. [arXiv:1410.3808](https://arxiv.org/abs/1410.3808) [hep-ph]
- Amin MA, Braden J, Copeland EJ, Giblin JT, Solorio C, Weiner ZJ, Zhou SY (2018) Gravitational waves from asymmetric oscillon dynamics? *Phys Rev D* 98:024040. <https://doi.org/10.1103/PhysRevD.98.024040>. [arXiv:1803.08047](https://arxiv.org/abs/1803.08047) [astro-ph.CO]
- Ananda KN, Clarkson C, Wands D (2007) The Cosmological gravitational wave background from primordial density perturbations. *Phys Rev D* 75:123518. <https://doi.org/10.1103/PhysRevD.75.123518>. [arXiv:gr-qc/0612013](https://arxiv.org/abs/gr-qc/0612013) [gr-qc]
- Anandan J (1985) Detection of gravitational radiation using superconducting circuits. *Phys Lett A* 110:446–450. [https://doi.org/10.1016/0375-9601\(85\)90551-1](https://doi.org/10.1016/0375-9601(85)90551-1)
- Anandan J, Chiao RY (1982) Gravitational radiation antennas using the Sagnac effect. *Gen Relativ Gravit* 14:515–521. <https://doi.org/10.1007/BF00756213>

- Anantua R, Easter R, Giblin JT (2009) GUT-scale primordial black holes: consequences and constraints. *Phys Rev Lett* 103:111303. <https://doi.org/10.1103/PhysRevLett.103.111303>. arXiv:0812.0825 [astro-ph]
- Anastassopoulos V et al (2017) New CAST limit on the axion-photon interaction. *Nat Phys* 13:584–590. <https://doi.org/10.1038/nphys4109>. arXiv:1705.02290 [hep-ex]
- Andersen OE, Zha S, da Silva SA, Betranhandy A, Couch SM, O'Connor EP (2021) Equation-of-state dependence of gravitational waves in core-collapse supernovae. *Astrophys J* 923(2):201. <https://doi.org/10.3847/1538-4357/ac294c>. arXiv:2106.09734 [astro-ph.HE]
- Annala E, Gorda T, Kurkela A, Nättilä J, Vuorinen A (2020) Evidence for quark-matter cores in massive neutron stars. *Nat Phys* 16(9):907–910. <https://doi.org/10.1038/s41567-020-0914-9>. arXiv:1903.09121 [astro-ph.HE]
- Antelis JM, Hernández JM, Moreno C (2018) Post-Newtonian approximation of gravitational waves from the inspiral phase. *J Phys: Conf Ser* 1030:012005. <https://doi.org/10.1088/1742-6596/1030/1/012005>
- Antoniadis J et al (2023) The second data release from the European Pulsar Timing Array—III. Search for gravitational wave signals. *Astron Astrophys* 678:A50. <https://doi.org/10.1051/0004-6361/202346844>. arXiv:2306.16214 [astro-ph.HE]
- Antusch S, Orani S (2016) Impact of other scalar fields on oscillons after hilltop inflation. *JCAP* 1603:026. <https://doi.org/10.1088/1475-7516/2016/03/026>. arXiv:1511.02336 [hep-ph]
- Antusch S, Cefala F, Nolde D, Orani S (2016) Parametric resonance after hilltop inflation caused by an inhomogeneous inflaton field. *JCAP* 1602:044. <https://doi.org/10.1088/1475-7516/2016/02/044>. arXiv:1510.04856 [hep-ph]
- Antusch S, Cefala F, Orani S (2017) Gravitational waves from oscillons after inflation. *Phys Rev Lett* 118:011303. <https://doi.org/10.1103/PhysRevLett.118.011303>. erratum: *Phys Rev Lett* 120:219901 (2018). arXiv:1607.01314 [astro-ph.CO]
- Antusch S, Cefala F, Krippendorf S, Muia F, Orani S, Quevedo F (2018a) Oscillons from string moduli. *JHEP* 01:083. [https://doi.org/10.1007/JHEP01\(2018\)083](https://doi.org/10.1007/JHEP01(2018)083). arXiv:1708.08922 [hep-th]
- Antusch S, Cefala F, Orani S (2018b) What can we learn from the stochastic gravitational wave background produced by oscillons? *JCAP* 1803:032. <https://doi.org/10.1088/1475-7516/2018/03/032>. arXiv:1712.03231 [astro-ph.CO]
- Antusch S, Cefala F, Torrenti F (2019) Properties of oscillons in hilltop potentials: energies, shapes, and lifetimes. *JCAP* 1910:002. <https://doi.org/10.1088/1475-7516/2019/10/002>. arXiv:1907.00611 [hep-ph]
- Armengaud E et al (2014) Conceptual design of the International Axion Observatory (IAXO). *JINST* 9:T05002. <https://doi.org/10.1088/1748-0221/9/05/T05002>. arXiv:1401.3233 [physics.ins-det]
- Armengaud E et al (2019) Physics potential of the International Axion Observatory (IAXO). *JCAP* 06:047. <https://doi.org/10.1088/1475-7516/2019/06/047>. arXiv:1904.09155 [hep-ph]
- Arvanitaki A, Dubovsky S (2011) Exploring the string axiverse with precision black hole physics. *Phys Rev D* 83:044026. <https://doi.org/10.1103/PhysRevD.83.044026>. arXiv:1004.3558 [hep-th]
- Arvanitaki A, Geraci AA (2013) Detecting high-frequency gravitational waves with optically levitated sensors. *Phys Rev Lett* 110:071105. <https://doi.org/10.1103/PhysRevLett.110.071105>
- Arvanitaki A, Dimopoulos S, Dubovsky S, Kaloper N, March-Russell J (2010) String axiverse. *Phys Rev D* 81:123530. <https://doi.org/10.1103/PhysRevD.81.123530>. arXiv:0905.4720 [hep-th]
- Arvanitaki A, Baryakhtar M, Huang X (2015) Discovering the QCD axion with black holes and gravitational waves. *Phys Rev D* 91:084011. <https://doi.org/10.1103/PhysRevD.91.084011>. arXiv:1411.2263 [hep-ph]
- Aso Y, Michimura Y, Somiya K, Ando M, Miyakawa O, Sekiguchi T, Tatsumi D, Yamamoto H (2013) Interferometer design of the KAGRA gravitational wave detector. *Phys Rev D* 88:043007. <https://doi.org/10.1103/PhysRevD.88.043007>. arXiv:1306.6747 [gr-qc]
- Aspelmeyer M, Kippenberg TJ, Marquardt F (2014) Cavity optomechanics. *Rev Mod Phys* 86:1391–1452. <https://doi.org/10.1103/RevModPhys.86.1391>
- Atonga E et al (2024) Gravitational waves from high-power twisted light. *Phys Rev D* 110(4):044023. <https://doi.org/10.1103/PhysRevD.110.044023>. arXiv:2309.04191 [gr-qc]
- Auclair P et al (2020) Probing the gravitational wave background from cosmic strings with LISA. *JCAP* 04:034. <https://doi.org/10.1088/1475-7516/2020/04/034>. arXiv:1909.00819 [astro-ph.CO]
- Bagui E et al (2025) Primordial black holes and their gravitational-wave signatures. *Living Rev Relativ* 28:1. <https://doi.org/10.1007/s41114-024-00053-w>. arXiv:2310.19857 [astro-ph.CO]
- Bähre R et al (2013) Any light particle search II—technical design report. *JINST* 8:T09001. <https://doi.org/10.1088/1748-0221/8/09/T09001>. arXiv:1302.5647 [physics.ins-det]

- Bai Y, Lu S, Orlofsky N (2022) Origin of nontopological soliton dark matter: solitosynthesis or phase transition. *JHEP* 10:181. [https://doi.org/10.1007/JHEP10\(2022\)181](https://doi.org/10.1007/JHEP10(2022)181). arXiv:2208.12290 [hep-ph]
- Bailes M et al (2019) Ground-based gravitational-wave astronomy in Australia: 2019 white paper. arXiv e-prints arXiv:1912.06305 [astro-ph.IM]
- Baiotti L, Rezzolla L (2017) Binary neutron star mergers: a review of Einstein's richest laboratory. *Rept Prog Phys* 80(9):096901. <https://doi.org/10.1088/1361-6633/aa67bb>. arXiv:1607.03540 [gr-qc]
- Baker RML Jr, Stephenson GV, Li F (2008) Proposed ultra-high sensitivity high-frequency gravitational wave detector. *AIP Conf Proc* 969(1):1045–1054. <https://doi.org/10.1063/1.2844941>
- Ballantini R, Bernard P, Chiaveri E, Chincarini A, Gemme G, Losito R, Parodi R, Picasso E (2003) A detector of high frequency gravitational waves based on coupled microwave cavities. *Class Quantum Grav* 20:3505–3522. <https://doi.org/10.1088/0264-9381/20/15/316>
- Ballantini R et al (2005) Microwave apparatus for gravitational waves observation. arXiv e-prints arXiv:gr-qc/0502054
- Ballou R et al (2015) New exclusion limits on scalar and pseudoscalar axionlike particles from light shining through a wall. *Phys Rev D* 92(9):092002. <https://doi.org/10.1103/PhysRevD.92.092002>. arXiv:1506.08082 [hep-ex]
- Banks H, Grabowska DM, McCullough M (2023) Gravitational wave backgrounds from colliding exotic compact objects. *Phys Rev D* 108(3):035017. <https://doi.org/10.1103/PhysRevD.108.035017>. arXiv:2302.07887 [gr-qc]
- Barnaby N, Peloso M (2011) Large nongaussianity in axion inflation. *Phys Rev Lett* 106:181301. <https://doi.org/10.1103/PhysRevLett.106.181301>. arXiv:1011.1500 [hep-ph]
- Bartolo N, Cannone D, Ricciardone A, Tasinato G (2016a) Distinctive signatures of space-time diffeomorphism breaking in EFT of inflation. *JCAP* 1603:044. <https://doi.org/10.1088/1475-7516/2016/03/044>. arXiv:1511.07414 [astro-ph.CO]
- Bartolo N, De Luca V, Franciolini G, Peloso M, Racco D, Riotto A (2019) Testing primordial black holes as dark matter with LISA. *Phys Rev D* 99:103521. <https://doi.org/10.1103/PhysRevD.99.103521>. arXiv:1810.12224 [astro-ph.CO]
- Bartolo N et al (2016b) Science with the space-based interferometer LISA. IV: probing inflation with gravitational waves. *JCAP* 1612:026. <https://doi.org/10.1088/1475-7516/2016/12/026>. arXiv:1610.06481 [astro-ph.CO]
- Bartram C et al (2021) Search for invisible axion dark matter in the 3.3–4.2  $\mu\text{eV}$  mass range. *Phys Rev Lett* 127(26):261803. <https://doi.org/10.1103/PhysRevLett.127.261803>. arXiv:2110.06096 [hep-ex]
- Baryakhtar M, Galanis M, Lasenby R, Simon O (2021) Black hole superradiance of self-interacting scalar fields. *Phys Rev D* 103(9):095019. <https://doi.org/10.1103/PhysRevD.103.095019>. arXiv:2011.11646 [hep-ph]
- Baumann D, Steinhardt PJ, Takahashi K, Ichiki K (2007) Gravitational wave spectrum induced by primordial scalar perturbations. *Phys Rev D* 76:084019. <https://doi.org/10.1103/PhysRevD.76.084019>. arXiv:hep-th/0703290 [hep-th]
- Bauswein A, Stergioulas N, Janka HT (2016) Exploring properties of high-density matter through remnants of neutron-star mergers. *Eur Phys J A* 52(3):56. <https://doi.org/10.1140/epja/i2016-16056-7>. arXiv:1508.05493 [astro-ph.HE]
- Bauswein A, Bastian NUF, Blaschke DB, Chatziioannou K, Clark JA, Fischer T, Oertel M (2019) Identifying a first-order phase transition in neutron star mergers through gravitational waves. *Phys Rev Lett* 122(6):061102. <https://doi.org/10.1103/PhysRevLett.122.061102>. arXiv:1809.01116 [astro-ph.HE]
- Bavera SS, Franciolini G, Cusin G, Riotto A, Zevin M, Fragos T (2022) Stochastic gravitational-wave background as a tool for investigating multi-channel astrophysical and primordial black-hole mergers. *Astron Astrophys* 660:A26. <https://doi.org/10.1051/0004-6361/202142208>. arXiv:2109.05836 [astro-ph.CO]
- Bea Y, Casallerrey-Solana J, Giannakopoulos T, Mateos D, Sanchez-Garitaonandia M, Zilhão M (2021) Bubble wall velocity from holography. *Phys Rev D* 104(12):L121903. <https://doi.org/10.1103/PhysRevD.104.L121903>. arXiv:2104.05708 [hep-th]
- Bea Y, Casallerrey-Solana J, Giannakopoulos T, Jansen A, Mateos D, Sanchez-Garitaonandia M, Zilhão M (2022) Holographic bubbles with Jecco: expanding, collapsing and critical. *JHEP* 09:008. [https://doi.org/10.1007/JHEP09\(2022\)008](https://doi.org/10.1007/JHEP09(2022)008). [Erratum: *JHEP* 03, 225 (2023)]. arXiv:2202.10503 [hep-th]
- Beacham J et al (2020) Physics beyond colliders at CERN: beyond the standard model working group report. *J Phys G* 47(1):010501. <https://doi.org/10.1088/1361-6471/ab4cd2>. arXiv:1901.09966 [hep-ex]

- Beccari A, Visani DA, Fedorov SA, Bereyhi MJ, Boureau V, Engelsen NJ, Kippenberg TJ (2022) Strained crystalline nanomechanical resonators with quality factors above 10 billion. *Nat Phys* 18(4):436–441. <https://doi.org/10.1038/s41567-021-01498-4>. arXiv:2107.02124 [cond-mat.mes-hall]
- Benakli K, Chen Y, Cheng P, Lafforgue-Marmet G (2019) Stochastic gravitational waves from spin-3/2 fields. *Phys Rev D* 99(9):095032. <https://doi.org/10.1103/PhysRevD.99.095032>. arXiv:1811.11774 [hep-ph]
- Berges J, Rajagopal K (1999) Color superconductivity and chiral symmetry restoration at nonzero baryon density and temperature. *Nucl Phys B* 538:215–232. [https://doi.org/10.1016/S0550-3213\(98\)00620-8](https://doi.org/10.1016/S0550-3213(98)00620-8). arXiv:hep-ph/9804233
- Berlin A, Blas D, Tito D'Agnolo R, Ellis SAR, Harnik R, Kahn Y, Schütte-Engel J (2022) Detecting high-frequency gravitational waves with microwave cavities. *Phys Rev D* 105(11):116011. <https://doi.org/10.1103/PhysRevD.105.116011>. arXiv:2112.11465 [hep-ph]
- Berlin A, Blas D, Tito D'Agnolo R, Ellis SAR, Harnik R, Kahn Y, Schütte-Engel J, Wentzel M (2023) Electromagnetic cavities as mechanical bars for gravitational waves. *Phys Rev D* 108(8):084058. <https://doi.org/10.1103/PhysRevD.108.084058>. arXiv:2303.01518 [hep-ph]
- Berlin A et al (2021) Storage rings and gravitational waves: summary and outlook. In: ARIES WP6 workshop: storage rings and gravitational waves. arXiv:2105.00992 [physics.acc-ph]
- Bernal JL, Verde L, Riess AG (2016) The trouble with  $H_0$ . *JCAP* 1610:019. <https://doi.org/10.1088/1475-7516/2016/10/019>. arXiv:1607.05617 [astro-ph.CO]
- Bernuzzi S, Nagar A, Balmelli S, Dietrich T, Ujevic M (2014) Quasiuniversal properties of neutron star mergers. *Phys Rev Lett* 112:201101. <https://doi.org/10.1103/PhysRevLett.112.201101>. arXiv:1402.6244 [gr-qc]
- Bethke L, Figueroa DG, Rajantie A (2013) Anisotropies in the gravitational wave background from preheating. *Phys Rev Lett* 111:011301. <https://doi.org/10.1103/PhysRevLett.111.011301>. arXiv:1304.2657 [astro-ph.CO]
- Bethke L, Figueroa DG, Rajantie A (2014) On the anisotropy of the gravitational wave background from massless preheating. *JCAP* 1406:047. <https://doi.org/10.1088/1475-7516/2014/06/047>. arXiv:1309.1148 [astro-ph.CO]
- Bhatiani S, Dai X, Guerras E (2019) Confirmation of planet-mass objects in extragalactic systems. *Astrophys J* 885:77. <https://doi.org/10.3847/1538-4357/ab46ac>. arXiv:1909.11610 [astro-ph.GA]
- Bigazzi F, Caddeo A, Canneti T, Cotrone AL (2021) Bubble wall velocity at strong coupling. *JHEP* 08:090. [https://doi.org/10.1007/JHEP08\(2021\)090](https://doi.org/10.1007/JHEP08(2021)090). arXiv:2104.12817 [hep-ph]
- Bild M, Fadel M, Yang Y, von Lüpke U, Martin P, Bruno A, Chu Y (2023) Schrödinger cat states of a 16-microgram mechanical oscillator. *Science* 380(6642):adf7553. <https://doi.org/10.1126/science.adf7553>. arXiv:2211.00449 [quant-ph]
- Binetruy P, Bohe A, Hertog T, Steer DA (2009) Gravitational wave bursts from cosmic superstrings with Y-junctions. *Phys Rev D* 80:123510. <https://doi.org/10.1103/PhysRevD.80.123510>. arXiv:0907.4522 [hep-th]
- Bini S, Tiwari S, Xu Y, Smith L, Ebersold M, Principe G, Haney M, Jetzer P, Prodi GA (2024) Search for hyperbolic encounters of compact objects in the third LIGO-Virgo-KAGRA observing run. *Phys Rev D* 109(4):042009. <https://doi.org/10.1103/PhysRevD.109.042009>. arXiv:2311.06630 [gr-qc]
- Bird S, Cholis I, Muñoz JB, Ali-Haïmoud Y, Kamionkowski M, Kovetz ED, Raccanelli A, Riess AG (2016) Did LIGO detect dark matter? *Phys Rev Lett* 116(20):201301. <https://doi.org/10.1103/PhysRevLett.116.201301>. arXiv:1603.00464 [astro-ph.CO]
- Blanchet L, Damour T (1992) Hereditary effects in gravitational radiation. *Phys Rev D* 46:4304–4319. <https://doi.org/10.1103/PhysRevD.46.4304>
- Blanco-Pillado JJ, Olum KD (2017) Stochastic gravitational wave background from smoothed cosmic string loops. *Phys Rev D* 96:104046. <https://doi.org/10.1103/PhysRevD.96.104046>. arXiv:1709.02693 [astro-ph.CO]
- Boccaletti D, De Sabbata V, Fortini P, Gualdi C (1970) Conversion of photons into gravitons and vice versa in a static electromagnetic field. *Nuovo Cimento B* 70:129–146. <https://doi.org/10.1007/BF02710177>
- Boetzel Y, Mishra CK, Faye G, Gopakumar A, Iyer BR (2019) Gravitational-wave amplitudes for compact binaries in eccentric orbits at the third post-Newtonian order: Tail contributions and postadiabatic corrections. *Phys Rev D* 100(4):044018. <https://doi.org/10.1103/PhysRevD.100.044018>. arXiv:1904.11814 [gr-qc]



- Bothwell T, Kennedy CJ, Aepli A, Kedar D, Robinson JM, Oelker E, Staron A, Ye J (2022) Resolving the gravitational redshift within a millimeter atomic sample. *Nature* 602:420–424. <https://doi.org/10.1038/s41586-021-04349-7>. arXiv:2109.12238 [physics.atom-ph]
- Boughn S, Rothman T (2006) Aspects of graviton detection: graviton emission and absorption by atomic hydrogen. *Class Quant Grav* 23:5839–5852. <https://doi.org/10.1088/0264-9381/23/20/006>. arXiv:gr-qc/0605052
- Bowman JD, Rogers AEE, Monsalve RA, Mozdzen TJ, Mahesh N (2018) An absorption profile centred at 78 megahertz in the sky-averaged spectrum. *Nature* 555(7694):67–70. <https://doi.org/10.1038/nature25792>. arXiv:1810.05912 [astro-ph.CO]
- Braggio C et al (2025) Quantum-enhanced sensing of axion dark matter with a transmon-based single microwave photon counter. *Phys Rev X* 15:021031. <https://doi.org/10.1103/PhysRevX.15.021031>. arXiv:2403.02321 [quant-ph]
- Braginsky VB, Grishchuk LP (1985) Kinematic resonance and memory effect in free mass gravitational antennas. *Sov Phys JETP* 62:427–430
- Braginsky VB, Thorne KS (1987) Gravitational-wave bursts with memory and experimental prospects. *Nature* 327:123–125. <https://doi.org/10.1038/327123a0>
- Braglia M, Hazra DK, Finelli F, Smoot GF, Sriramkumar L, Starobinsky AA (2020) Generating PBHs and small-scale GWs in two-field models of inflation. *JCAP* 08:001. <https://doi.org/10.1088/1475-7516/2020/08/001>. arXiv:2005.02895 [astro-ph.CO]
- Bringmann T, Domcke V, Fuchs E, Kopp J (2023) High-frequency gravitational wave detection via optical frequency modulation. *Phys Rev D* 108(6):L061303. <https://doi.org/10.1103/PhysRevD.108.L061303>. arXiv:2304.10579 [hep-ph]
- Brito R, Cardoso V, Pani P (2015a) Black holes as particle detectors: evolution of superradiant instabilities. *Class Quantum Grav* 32:134001. <https://doi.org/10.1088/0264-9381/32/13/134001>. arXiv:1411.0686 [gr-qc]
- Brito R, Cardoso V, Pani P (2015b) Superradiance. *Lecture Notes in Physics*, vol 906. Springer, Cham. <https://doi.org/10.1007/978-3-319-19000-6>. arXiv:1501.06570 [gr-qc]
- Brouwer L et al (2022a) Projected sensitivity of DMRadio-m3: a search for the QCD axion below 1  $\mu\text{eV}$ . *Phys Rev D* 106(10):103008. <https://doi.org/10.1103/PhysRevD.106.103008>. arXiv:2204.13781 [hep-ex]
- Brouwer L et al (2022b) Proposal for a definitive search for GUT-scale QCD axions. *Phys Rev D* 106(11):112003. <https://doi.org/10.1103/PhysRevD.106.112003>. arXiv:2203.11246 [hep-ex]
- Brun P et al (2019) A new experimental approach to probe QCD axion dark matter in the mass range above 40  $\mu\text{eV}$ . *Eur Phys J C* 79(3):186. <https://doi.org/10.1140/epjc/s10052-019-6683-x>. arXiv:1901.07401 [physics.ins-det]
- Brustein R, Gasperini M, Giovannini M, Veneziano G (1996) Gravitational radiation from string cosmology. In: Lemonne J, Vander Velde C, Verbeure F (eds) *Proceedings of the international europsychics conference on high energy physics (HEP 95)*. World Scientific, Singapore, pp 408–409. arXiv:hep-th/9510081
- Buballa M (2005) NJL model analysis of quark matter at large density. *Phys Rep* 407:205–376. <https://doi.org/10.1016/j.physrep.2004.11.004>. arXiv:hep-ph/0402234
- Buchmüller W, Domcke V, Kamada K, Schmitz K (2013) The gravitational wave spectrum from cosmological  $B - L$  breaking. *JCAP* 1310:003. <https://doi.org/10.1088/1475-7516/2013/10/003>. arXiv:1305.3392 [hep-ph]
- Buchmüller W, Domcke V, Murayama H, Schmitz K (2020a) Probing the scale of grand unification with gravitational waves. *Phys Lett B* 809:135764. <https://doi.org/10.1016/j.physletb.2020.135764>. arXiv:1912.03695 [hep-ph]
- Buchmüller W, Domcke V, Schmitz K (2020b) From NANOGrav to LIGO with metastable cosmic strings. *Phys Lett B* 811:135914. <https://doi.org/10.1016/j.physletb.2020.135914>. arXiv:2009.10649 [astro-ph.CO]
- Buikema A, Cahillane C, Mansell GL, Blair CD, Abbott R, Adams C, Adhikari RX, Ananyeva A, Appert S, Arai K et al (2020) Sensitivity and performance of the advanced LIGO detectors in the third observing run. *Phys Rev D* 102:062003. <https://doi.org/10.1103/PhysRevD.102.062003>
- Burden CJ (1985) Gravitational radiation from a particular class of cosmic strings. *Phys Lett* 164B:277–281. [https://doi.org/10.1016/0370-2693\(85\)90326-0](https://doi.org/10.1016/0370-2693(85)90326-0)
- Bushev PA, Bourhill J, Goryachev M, Kukharchyk N, Ivanov E, Galliou S, Tobar ME, Danilishin S (2019) Testing the generalized uncertainty principle with macroscopic mechanical oscillators and

- pendulums. *Phys Rev D* 100:066020. <https://doi.org/10.1103/PhysRevD.100.066020>. arXiv:1903.03346 [quant-ph]
- Byrnes CT, Cole PS, Patil SP (2019) Steepest growth of the power spectrum and primordial black holes. *JCAP* 1906:028. <https://doi.org/10.1088/1475-7516/2019/06/028>. arXiv:1811.11158 [astro-ph.CO]
- Rg C, Pi S, Sasaki M (2019) Gravitational waves induced by non-Gaussian scalar perturbations. *Phys Rev Lett* 122:201101. <https://doi.org/10.1103/PhysRevLett.122.201101>. arXiv:1810.11000 [astro-ph.CO]
- Caldarola M, Kuroyanagi S, Nesseris S, Garcia-Bellido J (2024) Effects of orbital precession on hyperbolic encounters. *Phys Rev D* 109(6):064001. <https://doi.org/10.1103/PhysRevD.109.064001>. arXiv:2307.00915 [gr-qc]
- Campbell WM, Galliou S, Tobar ME, Goryachev M (2023a) Electro-mechanical tuning of high-Q bulk acoustic phonon modes at cryogenic temperatures. *Appl Phys Lett* 122(3):032202. <https://doi.org/10.1063/5.0131361>. arXiv:2207.01176 [physics.app-ph]
- Campbell WM, Goryachev M, Tobar ME (2023b) The multi-mode acoustic gravitational wave experiment: MAGE. *Sci Rep* 13(1):10638. <https://doi.org/10.1038/s41598-023-35670-y>. arXiv:2307.00715 [gr-qc]
- Cannone D, Tasinato G, Wands D (2015) Generalised tensor fluctuations and inflation. *JCAP* 1501:029. <https://doi.org/10.1088/1475-7516/2015/01/029>. arXiv:1409.6568 [astro-ph.CO]
- Cao G, Lin S (2018) Gravitational wave from phase transition inside neutron stars. arXiv e-prints arXiv:1810.00528 [nucl-th]
- Capdevilla R, Gelmini GB, Hyman J, Millar AJ, Vitagliano E (2024) Gravitational wave detection with plasma haloscopes. arXiv e-prints arXiv:2412.14450 [hep-ph]
- Capozziello S, De Laurentis M, De Paolis F, Ingrosso G, Nucita A (2008) Gravitational waves from hyperbolic encounters. *Mod Phys Lett A* 23:99–107. <https://doi.org/10.1142/S0217732308026236>. arXiv:0801.0122 [gr-qc]
- Caprini C, Figueroa DG (2018) Cosmological Backgrounds of Gravitational Waves. *Class Quantum Grav* 35:163001. <https://doi.org/10.1088/1361-6382/aac608>. arXiv:1801.04268 [astro-ph.CO]
- Cardoso V, Pani P (2019) Testing the nature of dark compact objects: a status report. *Liv Rev Relativ* 22:4. <https://doi.org/10.1007/s41114-019-0020-4>. arXiv:1904.05363 [gr-qc]
- Carney D, Higgins G, Marocco G, Wentzel M (2025) A superconducting levitated detector of gravitational waves. *Phys Rev Lett* 134:181402. <https://doi.org/10.1103/PhysRevLett.134.181402>. arXiv:2408.01583 [hep-ph]
- Carr B, Clesse S, Garcia-Bellido J, Kühnel F (2021a) Cosmic conundra explained by thermal history and primordial black holes. *Phys Dark Univ* 31:100755. <https://doi.org/10.1016/j.dark.2020.100755>. arXiv:1906.08217 [astro-ph.CO]
- Carr B, Kohri K, Sendouda Y, Yokoyama J (2021b) Constraints on primordial black holes. *Rept Prog Phys* 84(11):116902. <https://doi.org/10.1088/1361-6633/ac1e31>. arXiv:2002.12778 [astro-ph.CO]
- Carr B, Clesse S, Garcia-Bellido J, Hawkins M, Kuhnle F (2024) Observational evidence for primordial black holes: a positivist perspective. *Phys Rep* 1054:1–68. <https://doi.org/10.1016/j.physrep.2023.11.005>. arXiv:2306.03903 [astro-ph.CO]
- Casalderrey-Solana J, Mateos D, Sanchez-Garitaonandia M (2022) Mega-hertz gravitational waves from neutron star mergers. arXiv e-prints arXiv:2210.03171 [hep-th]
- Castells-Tiestos L, Casalderrey-Solana J (2022) Thermal emission of gravitational waves from weak to strong coupling. *JHEP* 10:049. [https://doi.org/10.1007/JHEP10\(2022\)049](https://doi.org/10.1007/JHEP10(2022)049). arXiv:2202.05241 [hep-th]
- Cautun M, Benitez-Llambay A, Deason AJ, Frenk CS, Fattahi A, Gómez FA, Grand RJJ, Oman KA, Navarro JF, Simpson CM (2020) The Milky Way total mass profile as inferred from Gaia DR2. *Mon Not R Astron Soc* 494(3):4291–4313. <https://doi.org/10.1093/mnras/staa1017>. arXiv:1911.04557 [astro-ph.GA]
- Caves C (1979) Microwave cavity gravitational radiation detectors. *Phys Lett* 80:323–326. [https://doi.org/10.1016/0370-2693\(79\)90227-2](https://doi.org/10.1016/0370-2693(79)90227-2)
- Cerdá-Durán P, DeBrye N, Aloy MA, Font JA, Obergaulinger M (2013) Gravitational wave signatures in black-hole-forming core collapse. *Astrophys J Lett* 779:L18. <https://doi.org/10.1088/2041-8205/779/2/L18>. arXiv:1310.8290 [astro-ph.SR]
- Chakraborty C, Bhattacharyya S (2024) Near- and sub-solar-mass naked singularities and black holes from transmutation of white dwarfs. *JCAP* 06:007. <https://doi.org/10.1088/1475-7516/2024/06/007>. arXiv:2401.08462 [astro-ph.HE]



- Chang DE, Ni K, Painter O, Kimble HJ (2012) Ultrahigh-q mechanical oscillators through optical trapping. *New J Phys* 14(4):045002
- Chatrchyan A, Jaeckel J (2021) Gravitational waves from the fragmentation of axion-like particle dark matter. *JCAP* 02:003. <https://doi.org/10.1088/1475-7516/2021/02/003>. arXiv:2004.07844 [hep-ph]
- Chen CM, Nester JM, Ni WT (2017) A brief history of gravitational wave research. *Chin J Phys* 55:142–169. <https://doi.org/10.1016/j.cjph.2016.10.014>. arXiv:1610.08803 [gr-qc]
- Chen P (1995) Resonant photon-graviton conversion and cosmic microwave background fluctuations. *Phys Rev Lett* 74:634–637. <https://doi.org/10.1103/PhysRevLett.74.634>
- Cheung C, Creminelli P, Fitzpatrick AL, Kaplan J, Senatore L (2008) The effective field theory of inflation. *JHEP* 03:014. <https://doi.org/10.1088/1126-6708/2008/03/014>. arXiv:0709.0293 [hep-th]
- Chiao RY (2002) Conceptual tensions between quantum mechanics and general relativity: are there experimental consequences, e.g., superconducting transducers between electromagnetic and gravitational radiation? arXiv e-prints arXiv:gr-qc/0208024 [gr-qc]
- Chiao RY (2002) Superconductors as transducers and antennas for gravitational and electromagnetic radiation. arXiv e-prints arXiv:gr-qc/0204012
- Chiba T, Kamada K, Yamaguchi M (2010) Gravitational waves from Q-ball formation. *Phys Rev D* 81:083503. <https://doi.org/10.1103/PhysRevD.81.083503>. arXiv:0912.3585 [astro-ph.CO]
- Chiles J et al (2022) New constraints on dark photon dark matter with superconducting nanowire detectors in an optical haloscope. *Phys Rev Lett* 128(23):231802. <https://doi.org/10.1103/PhysRevLett.128.231802>. arXiv:2110.01582 [hep-ex]
- Chou AS et al (2017) MHz gravitational wave constraints with decameter Michelson interferometers. *Phys Rev D* 95(6):063002. <https://doi.org/10.1103/PhysRevD.95.063002>. arXiv:1611.05560 [astro-ph.IM]
- Christodoulou D (1991) Nonlinear nature of gravitation and gravitational wave experiments. *Phys Rev Lett* 67:1486–1489. <https://doi.org/10.1103/PhysRevLett.67.1486>
- Chu Y, Kharel P, Yoon T, Frunzio L, Rakich PT, Schoelkopf RJ (2018) Creation and control of multiphonon Fock states in a bulk acoustic-wave resonator. *Nature* 563(7733):666–670. <https://doi.org/10.1038/s41586-018-0717-7>
- Cielo M, Escudero M, Mangano G, Pisanti O (2023) Neff in the standard model at NLO is 3.043. *Phys Rev D* 108(12):L121301. <https://doi.org/10.1103/PhysRevD.108.L121301>. arXiv:2306.05460 [hep-ph]
- Cillis AN, Harari DD (1996) Photon-graviton conversion in a primordial magnetic field and the cosmic microwave background. *Phys Rev D* 54:4757–4759. <https://doi.org/10.1103/PhysRevD.54.4757>. arXiv:astro-ph/9609200 [astro-ph]
- Clarke TJ, Copeland EJ, Moss A (2020) Constraints on primordial gravitational waves from the cosmic microwave background. *JCAP* 10:002. <https://doi.org/10.1088/1475-7516/2020/10/002>. arXiv:2004.11396 [astro-ph.CO]
- Clarkson C, Seahra SS (2007) A gravitational wave window on extra dimensions. *Class Quantum Grav* 24:F33–F40. <https://doi.org/10.1088/0264-9381/24/9/F01>
- Clesse S, García-Bellido J (2017) The clustering of massive Primordial Black Holes as Dark Matter: measuring their mass distribution with Advanced LIGO. *Phys Dark Univ* 15:142–147. <https://doi.org/10.1016/j.dark.2016.10.002>. arXiv:1603.05234 [astro-ph.CO]
- Clesse S, García-Bellido J (2022) GW190425, GW190521 and GW190814: three candidate mergers of primordial black holes from the QCD epoch. *Phys Dark Univ* 38:101111. <https://doi.org/10.1016/j.dark.2022.101111>. arXiv:2007.06481 [astro-ph.CO]
- Co RT, Harigaya K, Pierce A (2021) Gravitational waves and dark photon dark matter from axion rotations. *JHEP* 12:099. [https://doi.org/10.1007/JHEP12\(2021\)099](https://doi.org/10.1007/JHEP12(2021)099). arXiv:2104.02077 [hep-ph]
- Codazzo E, Di Giovanni M, Harms J (2024) Gravitational wave signals from long-lasting binary-single black hole encounters. *Eur Phys J Plus* 139(1):40. <https://doi.org/10.1140/epjp/s13360-023-04808-2>. arXiv:2311.18032 [gr-qc]
- Coleman SR (1985) Q balls. *Nucl Phys B* 262:263. [https://doi.org/10.1016/0550-3213\(85\)90286-X](https://doi.org/10.1016/0550-3213(85)90286-X). erratum: *Nucl Phys B* 269:744 (1986)
- Colpi M, Shapiro SL, Wasserman I (1986) Boson stars: gravitational equilibria of selfinteracting scalar fields. *Phys Rev Lett* 57:2485–2488. <https://doi.org/10.1103/PhysRevLett.57.2485>
- Copeland EJ, Myers RC, Polchinski J (2004) Cosmic F and D strings. *JHEP* 06:013. <https://doi.org/10.1088/1126-6708/2004/06/013>. arXiv:hep-th/0312067 [hep-th]

- Cowan G, Cranmer K, Gross E, Vitells O (2011) Asymptotic formulae for likelihood-based tests of new physics. *Eur Phys J C* 71:1554. <https://doi.org/10.1140/epjc/s10052-011-1554-0>. [Erratum: *Eur.-Phys.J.C* 73, 2501 (2013)]. [arXiv:1007.1727](https://arxiv.org/abs/1007.1727) [physics.data-an]
- Crescimbeni F, Franciolini G, Pani P, Riotto A (2024) Can we identify primordial black holes? Tidal tests for subsolar-mass gravitational-wave observations. *Phys Rev D* 109(12):124063. <https://doi.org/10.1103/PhysRevD.109.124063>. [arXiv:2402.18656](https://arxiv.org/abs/2402.18656) [astro-ph.HE]
- Crescini N et al (2018) Operation of a ferromagnetic axion haloscope at  $m_a = 58 \mu\text{eV}$ . *Eur Phys J C* 78(9):703. <https://doi.org/10.1140/epjc/s10052-018-6163-8>. [Erratum: *Eur. Phys. J. C* 78, 813 (2018)]. [arXiv:1806.00310](https://arxiv.org/abs/1806.00310) [hep-ex]
- Crisosto N, Sikivie P, Sullivan NS, Tanner DB, Yang J, Rybka G (2020) ADMX SLIC: results from a superconducting  $LC$  circuit investigating cold axions. *Phys Rev Lett* 124(24):241101. <https://doi.org/10.1103/PhysRevLett.124.241101>. [arXiv:1911.05772](https://arxiv.org/abs/1911.05772) [astro-ph.CO]
- Croon D, Ipek S, McKeen D (2023) Gravitational wave constraints on extended dark matter structures. *Phys Rev D* 107(6):063012. <https://doi.org/10.1103/PhysRevD.107.063012>. [arXiv:2205.15396](https://arxiv.org/abs/2205.15396) [astro-ph.CO]
- Cruise AM (1983) An interaction between gravitational and electromagnetic waves. *Mon Not R Astron Soc* 204:485–492. <https://doi.org/10.1093/mnras/204.2.485>
- Cruise AM (2000) An electromagnetic detector for very high frequency gravitational waves. *Class Quantum Grav* 17:2525. <https://doi.org/10.1088/0264-9381/17/13/305>
- Cruise AM, Ingle RMJ (2005) A correlation detector for very high frequency gravitational waves. *Class Quantum Grav* 22:S479. <https://doi.org/10.1088/0264-9381/22/10/046>
- Cruise AM, Ingle RMJ (2006) A prototype gravitational wave detector for 100-MHz. *Class Quantum Grav* 23:6185–6193. <https://doi.org/10.1088/0264-9381/23/22/007>
- Cui Y, Saha P, Sfakianakis EI (2024) Gravitational wave symphony from oscillating spectator scalar fields. *Phys Rev Lett* 133(2):021004. <https://doi.org/10.1103/PhysRevLett.133.021004>. [arXiv:2310.13060](https://arxiv.org/abs/2310.13060) [hep-ph]
- Cybert RH, Fields BD, Olive KA, Yeh TH (2016) Big Bang nucleosynthesis: 2015. *Rev Mod Phys* 88:015004. <https://doi.org/10.1103/RevModPhys.88.015004>. [arXiv:1505.01076](https://arxiv.org/abs/1505.01076) [astro-ph.CO]
- Da Silva Costa CF, Aguiar OD (2014) Spherical gravitational wave detectors: MiniGRAIL and mario schenberg. *J Phys: Conf Ser* 484:012012. <https://doi.org/10.1088/1742-6596/484/1/012012>
- D'Agnolo RT, Ellis SAR (2024) Classical (and quantum) heuristics for gravitational wave detection. *arXiv e-prints* [arXiv:2412.17897](https://arxiv.org/abs/2412.17897) [gr-qc]
- Dai J, Liang GR (2023) Graviton-photon conversion in atoms and the detection of gravitons. *arXiv e-prints* [arXiv:2302.07044](https://arxiv.org/abs/2302.07044) [gr-qc]
- Damour T, Vilenkin A (2000) Gravitational wave bursts from cosmic strings. *Phys Rev Lett* 85:3761–3764. <https://doi.org/10.1103/PhysRevLett.85.3761>. [arXiv:gr-qc/0004075](https://arxiv.org/abs/gr-qc/0004075) [gr-qc]
- Damour T, Vilenkin A (2001) Gravitational wave bursts from cusps and kinks on cosmic strings. *Phys Rev D* 64:064008. <https://doi.org/10.1103/PhysRevD.64.064008>. [arXiv:gr-qc/0104026](https://arxiv.org/abs/gr-qc/0104026) [gr-qc]
- Dandapat S, Ebersold M, Susobhanan A, Rana P, Gopakumar A, Tiwari S, Haney M, Lee HM, Kolhe N (2023) Gravitational waves from black-hole encounters: prospects for ground and galaxy-based observatories. *Phys Rev D* 108(2):024013. <https://doi.org/10.1103/PhysRevD.108.024013>. [arXiv:2305.19318](https://arxiv.org/abs/2305.19318) [gr-qc]
- Dandoy V, Bertólez-Martínez T, Costa F (2024) High frequency gravitational wave bounds from galactic neutron stars. *JCAP* 12:023. <https://doi.org/10.1088/1475-7516/2024/12/023>. [arXiv:2402.14092](https://arxiv.org/abs/2402.14092) [gr-qc]
- Dasgupta B, Laha R, Ray A (2021) Low mass black holes from dark core collapse. *Phys Rev Lett* 126(14):141105. <https://doi.org/10.1103/PhysRevLett.126.141105>. [arXiv:2009.01825](https://arxiv.org/abs/2009.01825) [astro-ph.HE]
- Daverio D, Hindmarsh M, Kunz M, Lizarraga J, Urrestilla J (2016) Energy-momentum correlations for Abelian Higgs cosmic strings. *Phys Rev D* 93:085014. <https://doi.org/10.1103/PhysRevD.93.085014>. erratum: *Phys Rev D* 95:049903 (2017). [arXiv:1510.05006](https://arxiv.org/abs/1510.05006) [astro-ph.CO]
- De Logi WK, Mickelson AR (1977) Electrogravitational conversion cross-sections in static electromagnetic fields. *Phys Rev D* 16:2915–2927. <https://doi.org/10.1103/PhysRevD.16.2915>
- De Luca V, Desjacques V, Franciolini G, Riotto A (2020a) The clustering evolution of primordial black holes. *JCAP* 11:028. <https://doi.org/10.1088/1475-7516/2020/11/028>. [arXiv:2009.04731](https://arxiv.org/abs/2009.04731) [astro-ph.CO]
- De Luca V, Franciolini G, Pani P, Riotto A (2020b) Primordial black holes confront LIGO/Virgo data: current situation. *JCAP* 06:044. <https://doi.org/10.1088/1475-7516/2020/06/044>. [arXiv:2005.05641](https://arxiv.org/abs/2005.05641) [astro-ph.CO]
- De Miguel J (2021) A dark matter telescope probing the 6 to 60 GHz band. *JCAP* 04:075. <https://doi.org/10.1088/1475-7516/2021/04/075>. [arXiv:2003.06874](https://arxiv.org/abs/2003.06874) [physics.ins-det]

- De Miguel J, Hernández-Cabrera JF, Hernández-Suárez E, Joven-Álvarez E, Otani C, Rubiño Martín JA (2024) Discovery prospects with the Dark-photons & Axion-like particles Interferometer. *Phys Rev D* 109(6):062002. <https://doi.org/10.1103/PhysRevD.109.062002>. arXiv:2303.03997 [hep-ph]
- De Vittori L, Jetzer P, Klein A (2012) Gravitational wave energy spectrum of hyperbolic encounters. *Phys Rev D* 86:044017. <https://doi.org/10.1103/PhysRevD.86.044017>. arXiv:1207.5359 [gr-qc]
- Del Grosso L, Franciolini G, Pani P, Urbano A (2023) Fermion soliton stars. *Phys Rev D* 108(4):044024. <https://doi.org/10.1103/PhysRevD.108.044024>. arXiv:2301.08709 [gr-qc]
- Demircik T, Ecker C, Järvinen M, Rezzolla L, Tootle S, Topolski K (2022) Exploring the phase diagram of V-QCD with neutron star merger simulations. *EPJ Web Conf* 274:07006. <https://doi.org/10.1051/epjconf/20227407006>. arXiv:2211.10118 [astro-ph.HE]
- Detweiler SL (1980) Klein-Gordon equation and rotating black holes. *Phys Rev D* 22:2323–2326. <https://doi.org/10.1103/PhysRevD.22.2323>
- Devlin JA et al (2021) Constraints on the coupling between axionlike dark matter and photons using an antiproton superconducting tuned detection circuit in a cryogenic penning trap. *Phys Rev Lett* 126(4):041301. <https://doi.org/10.1103/PhysRevLett.126.041301>. arXiv:2101.11290 [astro-ph.CO]
- Dhani A, Radice D, Schütte-Engel J, Gardner S, Sathyaprakash B, Logoteta D, Perego A, Kashyap R (2024) Prospects for direct detection of black hole formation in neutron star mergers with next-generation gravitational-wave detectors. *Phys Rev D* 109(4):044071. <https://doi.org/10.1103/PhysRevD.109.044071>. arXiv:2306.06177 [gr-qc]
- Diambrini Palazzi G, Fargion D (1987) On gravitational radiation emitted by circulating particles in high energy accelerators. *Phys Lett B* 197(1–2):302–306. [https://doi.org/10.1016/0370-2693\(87\)90388-1](https://doi.org/10.1016/0370-2693(87)90388-1)
- Diedrichs RF, Becker N, Jockel C, Christian JE, Sagunski L, Schaffner-Bielich J (2023) Tidal deformability of fermion-boson stars: neutron stars admixed with ultralight dark matter. *Phys Rev D* 108(6):064009. <https://doi.org/10.1103/PhysRevD.108.064009>. arXiv:2303.04089 [gr-qc]
- Dixit AV, Chakram S, He K, Agrawal A, Naik RK, Schuster DI, Chou A (2021) Searching for dark matter with a superconducting qubit. *Phys Rev Lett* 126(14):141302. <https://doi.org/10.1103/PhysRevLett.126.141302>. arXiv:2008.12231 [hep-ex]
- Dolgov AD, Ejlli D (2011) Relic gravitational waves from light primordial black holes. *Phys Rev D* 84:024028. <https://doi.org/10.1103/PhysRevD.84.024028>. arXiv:1105.2303 [astro-ph.CO]
- Dolgov AD, Ejlli D (2012) Conversion of relic gravitational waves into photons in cosmological magnetic fields. *JCAP* 12:003. <https://doi.org/10.1088/1475-7516/2012/12/003>. arXiv:1211.0500 [gr-qc]
- Domcke V, García-Cely C (2021) Potential of radio telescopes as high-frequency gravitational wave detectors. *Phys Rev Lett* 126:021104. <https://doi.org/10.1103/PhysRevLett.126.021104>. arXiv:2006.01161 [astro-ph.CO]
- Domcke V, Pieroni M, Binétruy P (2016) Primordial gravitational waves for universality classes of pseudoscalar inflation. *JCAP* 1606:031. <https://doi.org/10.1088/1475-7516/2016/06/031>. arXiv:1603.01287 [astro-ph.CO]
- Domcke V, García-Cely C, Rodd NL (2022) Novel search for high-frequency gravitational waves with low-mass axion haloscopes. *Phys Rev Lett* 129(4):041101. <https://doi.org/10.1103/PhysRevLett.129.041101>. arXiv:2202.00695 [hep-ph]
- Domcke V, Ellis SAR, Kopp J (2025a) Dielectric haloscopes as gravitational wave detectors. *Phys Rev D* 111:035031. <https://doi.org/10.1103/PhysRevD.111.035031>. arXiv:2409.06462 [hep-ph]
- Domcke V, Ellis SAR, Rodd NL (2025b) Magnets are Weber bar gravitational wave detectors. *Phys Rev Lett* 134:231401. <https://doi.org/10.1103/PhysRevLett.134.231401>. arXiv:2408.01483 [hep-ph]
- Domcke V, García-Cely C, Lee SM, Rodd NL (2024) Symmetries and selection rules: optimising axion haloscopes for gravitational wave searches. *JHEP* 03:128. [https://doi.org/10.1007/JHEP03\(2024\)128](https://doi.org/10.1007/JHEP03(2024)128). arXiv:2306.03125 [hep-ph]
- Dong R, Kinney WH, Stojkovic D (2016) Gravitational wave production by Hawking radiation from rotating primordial black holes. *JCAP* 1610:034. <https://doi.org/10.1088/1475-7516/2016/10/034>. arXiv:1511.05642 [astro-ph.CO]
- Dorsch GC, Huber SJ, Konstandin T (2018) Bubble wall velocities in the Standard Model and beyond. *JCAP* 1812:034. <https://doi.org/10.1088/1475-7516/2018/12/034>. arXiv:1809.04907 [hep-ph]
- Drewes M, Georis Y, Klaric J, Klose P (2024) Upper bound on thermal gravitational wave backgrounds from hidden sectors. *JCAP* 06:073. <https://doi.org/10.1088/1475-7516/2024/06/073>. arXiv:2312.13855 [hep-ph]
- Dror JA, Hiramatsu T, Kohri K, Murayama H, White G (2020) Testing the seesaw mechanism and leptogenesis with gravitational waves. *Phys Rev Lett* 124(4):041804. <https://doi.org/10.1103/PhysRevLett.124.041804>. arXiv:1908.03227 [hep-ph]

- Dufaux JF, Bergman A, Felder GN, Kofman L, Uzan JP (2007) Theory and numerics of gravitational waves from preheating after inflation. *Phys Rev D* 76:123517. <https://doi.org/10.1103/PhysRevD.76.123517>. [arXiv:0707.0875](https://arxiv.org/abs/0707.0875) [astro-ph]
- Dufaux JF, Felder G, Kofman L, Navros O (2009) Gravity waves from tachyonic preheating after hybrid inflation. *JCAP* 0903:001. <https://doi.org/10.1088/1475-7516/2009/03/001>. [arXiv:0812.2917](https://arxiv.org/abs/0812.2917) [astro-ph]
- Dufaux JF, Figueroa DG, García-Bellido J (2010) Gravitational waves from Abelian gauge fields and cosmic strings at preheating. *Phys Rev D* 82:083518. <https://doi.org/10.1103/PhysRevD.82.083518>. [arXiv:1006.0217](https://arxiv.org/abs/1006.0217) [astro-ph.CO]
- Dvali G, Vilenkin A (2004) Formation and evolution of cosmic D strings. *JCAP* 0403:010. <https://doi.org/10.1088/1475-7516/2004/03/010>. [arXiv:hep-th/0312007](https://arxiv.org/abs/hep-th/0312007) [hep-th]
- Eardley D (2008) High frequency gravitational waves. <https://irp.fas.org/agency/dod/jason/gravwaves.pdf>
- East WE, McWilliams ST, Levin J, Pretorius F (2013) Observing complete gravitational wave signals from dynamical capture binaries. *Phys Rev D* 87(4):043004. <https://doi.org/10.1103/PhysRevD.87.043004>. [arXiv:1212.0837](https://arxiv.org/abs/1212.0837) [gr-qc]
- Easter R, Lim EA (2006) Stochastic gravitational wave production after inflation. *JCAP* 0604:010. <https://doi.org/10.1088/1475-7516/2006/04/010>. [arXiv:astro-ph/0601617](https://arxiv.org/abs/astro-ph/0601617) [astro-ph]
- Easter R, Giblin JT Jr, Lim EA (2007) Gravitational wave production at the end of inflation. *Phys Rev Lett* 99:221301. <https://doi.org/10.1103/PhysRevLett.99.221301>. [arXiv:astro-ph/0612294](https://arxiv.org/abs/astro-ph/0612294) [astro-ph]
- Ebersold M, Tiwari S (2020) Search for nonlinear memory from subsolar mass compact binary mergers. *Phys Rev D* 101(10):104041. <https://doi.org/10.1103/PhysRevD.101.104041>. [arXiv:2005.03306](https://arxiv.org/abs/2005.03306) [gr-qc]
- Echeverria F (1989) Gravitational-wave measurements of the mass and angular momentum of a black hole. *Phys Rev D* 40:3194–3203. <https://doi.org/10.1103/PhysRevD.40.3194>
- EGGE J et al (2025) First search for dark photon dark matter with a MADMAX prototype. *Phys Rev Lett* 134:151004. <https://doi.org/10.1103/PhysRevLett.134.151004>. [arXiv:2408.02368](https://arxiv.org/abs/2408.02368) [hep-ex]
- Ejlli A, Ejlli D, Cruise AM, Pisano G, Grote H (2019) Upper limits on the amplitude of ultra-high-frequency gravitational waves from graviton to photon conversion. *Eur Phys J C* 79(12):1032. <https://doi.org/10.1140/epjc/s10052-019-7542-5>. [arXiv:1908.00232](https://arxiv.org/abs/1908.00232) [gr-qc]
- Ekstedt A, Gould O, Hirvonen J, Laurent B, Niemi L, Schicho P, van de Vis J (2025) How fast does the WallGo? A package for computing wall velocities in first-order phase transitions. *JHEP* 04(2025):101. [https://doi.org/10.1007/JHEP04\(2025\)101](https://doi.org/10.1007/JHEP04(2025)101). [arXiv:2411.04970](https://arxiv.org/abs/2411.04970) [hep-ph]
- Ema Y, Jinno R, Nakayama K (2020) High-frequency graviton from inflaton oscillation. *JCAP* 09:015. <https://doi.org/10.1088/1475-7516/2020/09/015>. [arXiv:2006.09972](https://arxiv.org/abs/2006.09972) [astro-ph.CO]
- Engelhardt G, Bhoonah A, Liu WV (2024) Detecting axion dark matter with Rydberg atoms via induced electric dipole transitions. *Phys Rev Res* 6:023017. <https://doi.org/10.1103/PhysRevResearch.6.023017>. [arXiv:2304.05863](https://arxiv.org/abs/2304.05863) [hep-ph]
- Enqvist K, Ignatius J, Kajantie K, Rummukainen K (1992) Nucleation and bubble growth in a first order cosmological electroweak phase transition. *Phys Rev D* 45:3415–3428. <https://doi.org/10.1103/PhysRevD.45.3415>
- Enqvist K, Figueroa DG, Meriniemi T (2012) Stochastic background of gravitational waves from fermions. *Phys Rev D* 86:061301. <https://doi.org/10.1103/PhysRevD.86.061301>. [arXiv:1203.4943](https://arxiv.org/abs/1203.4943) [astro-ph.CO]
- Espinosa JR, Konstandin T, No JM, Servant G (2010) Energy budget of cosmological first-order phase transitions. *JCAP* 1006:028. <https://doi.org/10.1088/1475-7516/2010/06/028>. [arXiv:1004.4187](https://arxiv.org/abs/1004.4187) [hep-ph]
- Espinosa JR, Racco D, Riotto A (2018) A cosmological signature of the SM Higgs instability: gravitational waves. *JCAP* 1809:012. <https://doi.org/10.1088/1475-7516/2018/09/012>. [arXiv:1804.07732](https://arxiv.org/abs/1804.07732) [hep-ph]
- Fan X, Gabrielse G, Graham PW, Harnik R, Myers TG, Ramani H, Sukra BAD, Wong SSY, Xiao Y (2022) One-electron quantum cyclotron as a milli-eV dark-photon detector. *Phys Rev Lett* 129(26):261801. <https://doi.org/10.1103/PhysRevLett.129.261801>. [arXiv:2208.06519](https://arxiv.org/abs/2208.06519) [hep-ex]
- Favata M (2009a) Gravitational-wave memory revisited: memory from the merger and recoil of binary black holes. *J Phys: Conf Ser* 154:012043. <https://doi.org/10.1088/1742-6596/154/1/012043>. [arXiv:0811.3451](https://arxiv.org/abs/0811.3451) [astro-ph]
- Favata M (2009b) Nonlinear gravitational-wave memory from binary black hole mergers. *Astrophys J Lett* 696:L159–L162. <https://doi.org/10.1088/0004-637X/696/2/L159>. [arXiv:0902.3660](https://arxiv.org/abs/0902.3660) [astro-ph.SR]
- Favata M (2010) The gravitational-wave memory effect. *Class Quantum Grav* 27:084036. <https://doi.org/10.1088/0264-9381/27/8/084036>. [arXiv:1003.3486](https://arxiv.org/abs/1003.3486) [gr-qc]

- Fenu E, Figueroa DG, Durrer R, García-Bellido J (2009) Gravitational waves from self-ordering scalar fields. *JCAP* 0910:005. <https://doi.org/10.1088/1475-7516/2009/10/005>. arXiv:0908.0425 [astro-ph.CO]
- Figueroa DG (2014) A gravitational wave background from the decay of the standard model Higgs after inflation. *JHEP* 2014(11):145. [https://doi.org/10.1007/JHEP11\(2014\)145](https://doi.org/10.1007/JHEP11(2014)145). arXiv:1402.1345 [astro-ph.CO]
- Figueroa DG, Meriniemi T (2013) Stochastic background of gravitational waves from Fermions—theory and applications. *JHEP* 10:101. [https://doi.org/10.1007/JHEP10\(2013\)101](https://doi.org/10.1007/JHEP10(2013)101). arXiv:1306.6911 [astro-ph.CO]
- Figueroa DG, Torrenti F (2017) Gravitational wave production from preheating: parameter dependence. *JCAP* 1710:057. <https://doi.org/10.1088/1475-7516/2017/10/057>. arXiv:1707.04533 [astro-ph.CO]
- Figueroa DG, García-Bellido J, Rajantie A (2011) On the transverse-traceless projection in lattice simulations of gravitational wave production. *JCAP* 1111:015. <https://doi.org/10.1088/1475-7516/2011/11/015>. arXiv:1110.0337 [astro-ph.CO]
- Figueroa DG, Hindmarsh M, Urrestilla J (2013) Exact scale-invariant background of gravitational waves from cosmic defects. *Phys Rev Lett* 110:101302. <https://doi.org/10.1103/PhysRevLett.110.101302>. arXiv:1212.5458 [astro-ph.CO]
- Figueroa DG, García-Bellido J, Torrentí F (2016) Gravitational wave production from the decay of the standard model Higgs field after inflation. *Phys Rev D* 93:103521. <https://doi.org/10.1103/PhysRevD.93.103521>. arXiv:1602.03085 [astro-ph.CO]
- Figueroa DG, Hindmarsh M, Lizarraga J, Urrestilla J (2020) Irreducible background of gravitational waves from a cosmic defect network: update and comparison of numerical techniques. *Phys Rev D* 102:103516. <https://doi.org/10.1103/PhysRevD.102.103516>. arXiv:2007.03337 [astro-ph.CO]
- Fischer L et al (2025) First characterisation of the MAGO cavity, a superconducting RF detector for kHz-MHz gravitational waves. *Class Quantum Grav* 42:115015. <https://doi.org/10.1088/1361-6382/add8da>. arXiv:2411.18346 [gr-qc]
- Fixsen DJ, Kogut A, Levin S, Limon M, Lubin P, Mirel P, Seiffert M, Singal J, Wollack E, Villela T, Wuensche CA (2011) Arcade 2 measurement of the absolute sky brightness at 3–90 GHz. *Astrophys J* 734(1):5. <https://doi.org/10.1088/0004-637x/734/1/5>
- Fleischhauer M, Imamoglu A, Marangos JP (2005) Electromagnetically induced transparency: optics in coherent media. *Rev Mod Phys* 77:633–673. <https://doi.org/10.1103/RevModPhys.77.633>
- Flower G, Bourhill J, Goryachev M, Tobar ME (2019) Broadening frequency range of a ferromagnetic axion haloscope with strongly coupled cavity-magnon polaritons. *Phys Dark Univ* 25:100306. <https://doi.org/10.1016/j.dark.2019.100306>. arXiv:1811.09348 [physics.ins-det]
- Fodor G (2019) A review on radiation of oscillons and oscillatons. PhD thesis, Wigner RCP, Budapest. arXiv:1911.03340 [hep-th]
- Forward RL (1971) Multidirectional, multipolarization antennas for scalar and tensor gravitational radiation. *Gen Relativ Gravity* 2:149–159. <https://doi.org/10.1007/BF02450446>
- Forward RL (1978) Wideband laser-interferometer gravitational-radiation experiment. *Phys Rev D* 17:379–390. <https://doi.org/10.1103/PhysRevD.17.379>
- Foster JW, Rodd NL, Safdi BR (2018) Revealing the dark matter halo with axion direct detection. *Phys Rev D* 97(12):123006. <https://doi.org/10.1103/PhysRevD.97.123006>. arXiv:1711.10489 [astro-ph.CO]
- Franciolini G, Kritos K, Berti E, Silk J (2022a) Primordial black hole mergers from three-body interactions. *Phys Rev D* 106(8):083529. <https://doi.org/10.1103/PhysRevD.106.083529>. arXiv:2205.15340 [astro-ph.CO]
- Franciolini G, Maharana A, Muia F (2022b) Hunt for light primordial black hole dark matter with ultrahigh-frequency gravitational waves. *Phys Rev D* 106(10):103520. <https://doi.org/10.1103/PhysRevD.106.103520>. arXiv:2205.02153 [astro-ph.CO]
- Frey AR, Mahanta R, Maharana A, Quevedo F, Villa G (2024) Gravitational waves from high temperature strings. *JHEP* 12:174. [https://doi.org/10.1007/JHEP12\(2024\)174](https://doi.org/10.1007/JHEP12(2024)174). arXiv:2408.13803 [hep-th]
- Frieman JA, Olinto AV, Gleiser M, Alcock C (1989) Cosmic evolution of nontopological solitons. 1. *Phys Rev D* 40:3241. <https://doi.org/10.1103/PhysRevD.40.3241>
- Fu C, Wu P, Yu H (2018) Production of gravitational waves during preheating with nonminimal coupling. *Phys Rev D* 97:081303. <https://doi.org/10.1103/PhysRevD.97.081303>. arXiv:1711.10888 [gr-qc]
- Füßfa A (2016) How current loops and solenoids curve spacetime. *Phys Rev D* 93(2):024014. <https://doi.org/10.1103/PhysRevD.93.024014>. arXiv:1504.00333 [gr-qc]



- Füzfá A (2017) Electromagnetic gravitational waves antennas for directional emission and reception. arXiv e-prints [arXiv:1702.06052](https://arxiv.org/abs/1702.06052) [gr-qc]
- Galliou S, Goryachev M, Bourquin R, Abbe P, Aubry JP, Tobar ME (2013) Extremely low loss phonon-trapping cryogenic acoustic cavities for future physical experiments. *Sci Rep* 3:2132. <https://doi.org/10.1038/srep02132>
- Gamba R, Breschi M, Carullo G, Albanesi S, Rettegno P, Bernuzzi S, Nagar A (2023) GW190521 as a dynamical capture of two nonspinning black holes. *Nat Astron* 7(1):11–17. <https://doi.org/10.1038/s41550-022-01813-w>. [arXiv:2106.05575](https://arxiv.org/abs/2106.05575) [gr-qc]
- Gao CT, Gao Y, Liu Y, Sun S (2024) Novel high-frequency gravitational waves detection with split cavity. *Phys Rev D* 109(8):084004. <https://doi.org/10.1103/PhysRevD.109.084004>. [arXiv:2305.00877](https://arxiv.org/abs/2305.00877) [gr-qc]
- García-Bellido J (1998) Preheating the universe in hybrid inflation. In: *Fundamental parameters in cosmology: 33rd Rencontres de Moriond*. Editions Frontières, pp 29–34. [arXiv:hep-ph/9804205](https://arxiv.org/abs/hep-ph/9804205)
- García-Bellido J, Figueroa DG (2007) A stochastic background of gravitational waves from hybrid preheating. *Phys Rev Lett* 98:061302. <https://doi.org/10.1103/PhysRevLett.98.061302>. [arXiv:astro-ph/0701014](https://arxiv.org/abs/astro-ph/0701014) [astro-ph]
- García-Bellido J, Nesseris S (2017) Gravitational wave bursts from Primordial Black Hole hyperbolic encounters. *Phys Dark Univ* 18:123–126. <https://doi.org/10.1016/j.dark.2017.10.002>. [arXiv:1706.02111](https://arxiv.org/abs/1706.02111) [astro-ph.CO]
- García-Bellido J, Nesseris S (2018) Gravitational wave energy emission and detection rates of Primordial Black Hole hyperbolic encounters. *Phys Dark Univ* 21:61–69. <https://doi.org/10.1016/j.dark.2018.06.001>. [arXiv:1711.09702](https://arxiv.org/abs/1711.09702) [astro-ph.HE]
- García-Bellido J, Figueroa DG, Sastre A (2008) A gravitational wave background from reheating after hybrid inflation. *Phys Rev D* 77:043517. <https://doi.org/10.1103/PhysRevD.77.043517>. [arXiv:0707.0839](https://arxiv.org/abs/0707.0839) [hep-ph]
- García-Bellido J, Peloso M, Unal C (2016) Gravitational waves at interferometer scales and primordial black holes in axion inflation. *JCAP* 12:031. <https://doi.org/10.1088/1475-7516/2016/12/031>. [arXiv:1610.03763](https://arxiv.org/abs/1610.03763) [astro-ph.CO]
- García-Bellido J, Peloso M, Unal C (2017) Gravitational Wave signatures of inflationary models from Primordial Black Hole Dark Matter. *JCAP* 1709:013. <https://doi.org/10.1088/1475-7516/2017/09/013>. [arXiv:1707.02441](https://arxiv.org/abs/1707.02441) [astro-ph.CO]
- García-Bellido J, Jaraba S, Kuroyanagi S (2022) The stochastic gravitational wave background from close hyperbolic encounters of primordial black holes in dense clusters. *Phys Dark Univ* 36:101009. <https://doi.org/10.1016/j.dark.2022.101009>. [arXiv:2109.11376](https://arxiv.org/abs/2109.11376) [gr-qc]
- García-Cely C, Ringwald A (2025) Complete gravitational-wave spectrum of the sun. *Phys Rev Lett* 135:061001. <https://doi.org/10.1103/ptwg-pr41>. [arXiv:2407.18297](https://arxiv.org/abs/2407.18297) [hep-ph]
- García-Cely C, Marsili L, Ringwald A, Spector AD (2025) Polarimetric searches for axion dark matter and high-frequency gravitational waves using optical cavities. *Phys Rev D* 112:023031. <https://doi.org/10.1103/26vg-wcfx>. [arXiv:2501.08382](https://arxiv.org/abs/2501.08382) [hep-ph]
- Garfinkle D, Vachaspati T (1987) Radiation from kinky, cusplless cosmic loops. *Phys Rev D* 36:2229. <https://doi.org/10.1103/PhysRevD.36.2229>
- Gasparotto S, Vicente R, Blas D, Jenkins AC, Barausse E (2023) Can gravitational-wave memory help constrain binary black-hole parameters? A LISA case study. *Phys Rev D* 107(12):124033. <https://doi.org/10.1103/PhysRevD.107.124033>. [arXiv:2301.13228](https://arxiv.org/abs/2301.13228) [gr-qc]
- Gasperini M, Veneziano G (2003) The pre-Big Bang scenario in string cosmology. *Phys Rep* 373:1–212. [https://doi.org/10.1016/S0370-1573\(02\)00389-7](https://doi.org/10.1016/S0370-1573(02)00389-7). [arXiv:hep-th/0207130](https://arxiv.org/abs/hep-th/0207130)
- Gasperini M, Veneziano G (2016) String theory and pre-big bang cosmology. *Nuovo Cim C* 38(5):160. <https://doi.org/10.1393/ncc/i2015-15160-8>. [arXiv:hep-th/0703055](https://arxiv.org/abs/hep-th/0703055)
- Gatti C, Visinelli L, Zantedeschi M (2024) Cavity detection of gravitational waves: where do we stand? *Phys Rev D* 110(2):023018. <https://doi.org/10.1103/PhysRevD.110.023018>. [arXiv:2403.18610](https://arxiv.org/abs/2403.18610) [gr-qc]
- Gelfer E, Kadlecová H, Klimo O, Weber S, Korn G (2016) Gravitational waves generated by laser accelerated relativistic ions. *Phys Plasmas* 23:093107. <https://doi.org/10.1063/1.4962520>. [arXiv:1512.07188](https://arxiv.org/abs/1512.07188) [physics.plasm-ph]
- Gertsenshtein ME (1962) Wave resonance of light and gravitational waves. *Sov Phys JETP* 14:84
- Gertsenshtein ME, Pustovöit VI (1962) Gravitational radiation by a relativistic particle. *Sov Phys JETP* 15(1)

- Ghiglieri J, Laine M (2015) Gravitational wave background from standard model physics: qualitative features. JCAP 07:022. <https://doi.org/10.1088/1475-7516/2015/07/022>. arXiv:1504.02569 [hep-ph]
- Ghiglieri J, Jackson G, Laine M, Zhu Y (2020) Gravitational wave background from standard model physics: complete leading order. JHEP 07:092. [https://doi.org/10.1007/JHEP07\(2020\)092](https://doi.org/10.1007/JHEP07(2020)092). arXiv:2004.11392 [hep-ph]
- Ghiglieri J, Laine M, Schütte-Engel J, Speranza E (2024a) Double-graviton production from standard model plasma. JCAP 04:062. <https://doi.org/10.1088/1475-7516/2024/04/062>. arXiv:2401.08766 [hep-ph]
- Ghiglieri J, Schütte-Engel J, Speranza E (2024b) Freezing-in gravitational waves. Phys Rev D 109(2):023538. <https://doi.org/10.1103/PhysRevD.109.023538>. arXiv:2211.16513 [hep-ph]
- Giblin JT, Tishue AJ (2019) Preheating in full general relativity. Phys Rev D 100:063543. <https://doi.org/10.1103/PhysRevD.100.063543>. arXiv:1907.10601 [gr-qc]
- Giblin JT Jr, Price LR, Siemens X, Vlcck B (2012) Gravitational waves from global second order phase transitions. JCAP 1211:006. <https://doi.org/10.1088/1475-7516/2012/11/006>. arXiv:1111.4014 [astro-ph.CO]
- Giovannini M (1999) Production and detection of relic gravitons in quintessential inflationary models. Phys Rev D 60:123511. <https://doi.org/10.1103/PhysRevD.60.123511>. arXiv:astro-ph/9903004
- Giudice GF, McCullough M, Urbano A (2016) Hunting for dark particles with gravitational waves. JCAP 2016:001–001. <https://doi.org/10.1088/1475-7516/2016/10/001>
- Gleiser M (1994) Pseudostable bubbles. Phys Rev D 49:2978–2981. <https://doi.org/10.1103/PhysRevD.49.2978>. arXiv:hep-ph/9308279 [hep-ph]
- Gleiser M, Krackow M (2019) Resonant configurations in scalar field theories: can some oscillons live forever? Phys Rev D 100:116005. <https://doi.org/10.1103/PhysRevD.100.116005>. arXiv:1906.04070 [hep-th]
- Gleiser M, Sicilia D (2008) Analytical characterization of oscillon energy and lifetime. Phys Rev Lett 101:011602. <https://doi.org/10.1103/PhysRevLett.101.011602>. arXiv:0804.0791 [hep-th]
- Gold R, Brügmann B (2013) Eccentric black hole mergers and zoom-whirl behavior from elliptic inspirals to hyperbolic encounters. Phys Rev D 88(6):064051. <https://doi.org/10.1103/PhysRevD.88.064051>. arXiv:1209.4085 [gr-qc]
- Gonzalez-Ballester C, Aspelmeier M, Novotny L, Quidant R, Romero-Isart O (2021) Levitodynamics: levitation and control of microscopic objects in vacuum. Science 374(6564):abg3027. <https://doi.org/10.1126/science.abg3027>. arXiv:2111.05215 [quant-ph]
- Gorghetto M, Hardy E, March-Russell J, Song N, West SM (2022) Dark photon stars: formation and role as dark matter substructure. JCAP 08(08):018. <https://doi.org/10.1088/1475-7516/2022/08/018>. arXiv:2203.10100 [hep-ph]
- Goryachev M, Tobar ME (2014) Gravitational wave detection with high frequency phonon trapping acoustic cavities. Phys Rev D 90(10):102005. <https://doi.org/10.1103/PhysRevD.90.102005>. [Erratum: Phys. Rev. D 108, 129901 (2023)]. arXiv:1410.2334 [gr-qc]
- Goryachev M, Creedon DL, Galliou S, Tobar ME (2013) Observation of Rayleigh phonon scattering through excitation of extremely high overtones in low-loss cryogenic acoustic cavities for hybrid quantum systems. Phys Rev Lett 111:085502. <https://doi.org/10.1103/physrevlett.111.085502>
- Goryachev M, Ivanov EN, van Kann F, Galliou S, Tobar ME (2014) Observation of the fundamental nyquist noise limit in an ultra-high  $Q$ -factor cryogenic bulk acoustic wave cavity. Appl Phys Lett 105:153505. <https://doi.org/10.1063/1.4898813>. arXiv:1410.4293 [physics.ins-det]
- Goryachev M, Campbell WM, Heng IS, Galliou S, Ivanov EN, Tobar ME (2021) Rare events detected with a bulk acoustic wave high frequency gravitational wave antenna. Phys Rev Lett 127(7):071102. <https://doi.org/10.1103/PhysRevLett.127.071102>. arXiv:2102.05859 [gr-qc]
- Gottardi L, de Waard A, Usenko A, Frossati G, Podt M, Flokstra J, Bassan M, Fafone V, Minenkov Y, Rocchi A (2007) Sensitivity of the spherical gravitational wave detector MiniGRAIL operating at 5 K. Phys Rev D 76:102005. <https://doi.org/10.1103/PhysRevD.76.102005>. arXiv:0705.0122 [gr-qc]
- Gould RJ (1985) The graviton luminosity of the sun and other stars. Astrophys J 288:789–794. <https://doi.org/10.1086/162848>
- Gouttenoire Y, Servant G, Simakachorn P (2020) Beyond the standard models with cosmic strings. JCAP 07:032. <https://doi.org/10.1088/1475-7516/2020/07/032>. arXiv:1912.02569 [hep-ph]
- Gow AD, Byrnes CT, Hall A, Peacock JA (2020) Primordial black hole merger rates: distributions for multiple LIGO observables. JCAP 2001:031. <https://doi.org/10.1088/1475-7516/2020/01/031>. arXiv:1911.12685 [astro-ph.CO]

- Graef L, Brandenberger R (2015) Breaking of spatial diffeomorphism invariance, inflation and the spectrum of cosmological perturbations. *JCAP* 1510:009. <https://doi.org/10.1088/1475-7516/2015/10/009>. [arXiv:1506.00896](https://arxiv.org/abs/1506.00896) [astro-ph.CO]
- Graham E et al (2024) Rydberg-atom-based single-photon detection for haloscope axion searches. *Phys Rev D* 109(3):032009. <https://doi.org/10.1103/PhysRevD.109.032009>. [arXiv:2310.15352](https://arxiv.org/abs/2310.15352) [hep-ex]
- Gramolin AV, Aybas D, Johnson D, Adam J, Sushkov AO (2021) Search for axion-like dark matter with ferromagnets. *Nat Phys* 17(1):79–84. <https://doi.org/10.1038/s41567-020-1006-6>. [arXiv:2003.03348](https://arxiv.org/abs/2003.03348) [hep-ex]
- GravNet collaboration (2024) Global network of cavities to search for gravitational waves. <https://www.pi.uni-bonn.de/gravnet/en>
- Greene PB, Kofman L, Linde AD, Starobinsky AA (1997) Structure of resonance in preheating after inflation. *Phys Rev D* 56:6175–6192. <https://doi.org/10.1103/PhysRevD.56.6175>. [arXiv:hep-ph/9705347](https://arxiv.org/abs/hep-ph/9705347) [hep-ph]
- Gregori G, Vacalis G (2023) Pulsed lasers. <https://indico.cern.ch/event/1257532/contributions/5668686/>, presented at the 2023 meeting: ultra-high frequency gravitational waves: where to next?
- Grishchuk L, Sazhin M (1974) Emission of gravitational waves by an electromagnetic cavity. *JETP* 38
- Gröbner M, Jetzer P, Haney M, Tiwari S, Ishibashi W (2020) A note on the gravitational wave energy spectrum of parabolic and hyperbolic encounters. *Class Quantum Grav* 37(6):067002. <https://doi.org/10.1088/1361-6382/ab6be2>. [arXiv:2001.05187](https://arxiv.org/abs/2001.05187) [gr-qc]
- Gross C, Landini G, Strumia A, Teresi D (2021) Dark Matter as dark dwarfs and other macroscopic objects: multiverse relics? *JHEP* 09:033. [https://doi.org/10.1007/JHEP09\(2021\)033](https://doi.org/10.1007/JHEP09(2021)033). [arXiv:2105.02840](https://arxiv.org/abs/2105.02840) [hep-ph]
- Guo HK, Sinha K, Vagie D, White G (2021) Phase transitions in an expanding universe: stochastic gravitational waves in standard and non-standard histories. *JCAP* 1:001. <https://doi.org/10.1088/1475-7516/2021/01/001>. [arXiv:2007.08537](https://arxiv.org/abs/2007.08537) [hep-ph]
- Hamilton WO (1990) Resonant bar and microwave gravitational wave experiments. In: General relativity and gravitation, 1989: proceedings of the 12th international conference on general relativity and gravitation. Cambridge University Press, Cambridge, pp 349–356. <https://doi.org/10.1017/cbo9780511564178.029>
- Harry GM, Stevenson TR, Paik HJ (1996) Detectability of gravitational wave events by spherical resonant-mass antennas. *Phys Rev D* 54:2409–2420. <https://doi.org/10.1103/PhysRevD.54.2409>
- Hawkins MRS (2020) The signature of primordial black holes in the dark matter halos of galaxies. *Astron Astrophys* 633:A107. <https://doi.org/10.1051/0004-6361/201936462>. [arXiv:2001.07633](https://arxiv.org/abs/2001.07633) [astro-ph.GA]
- He Y, Giri SK, Sharma R, Mchedlidze S, Georgiev I (2024) Inverse Gertsenshtein effect as a probe of high-frequency gravitational waves. *JCAP* 05:051. <https://doi.org/10.1088/1475-7516/2024/05/051>. [arXiv:2312.17636](https://arxiv.org/abs/2312.17636) [astro-ph.CO]
- Helfer T, Lim EA, Garcia MAG, Amin MA (2019) Gravitational wave emission from collisions of compact scalar solitons. *Phys Rev D* 99:044046. <https://doi.org/10.1103/PhysRevD.99.044046>. [arXiv:1802.06733](https://arxiv.org/abs/1802.06733) [gr-qc]
- Herman N, Füzfa A, Lehoucq L, Clesse S (2021) Detecting planetary-mass primordial black holes with resonant electromagnetic gravitational-wave detectors. *Phys Rev D* 104(2):023524. <https://doi.org/10.1103/PhysRevD.104.023524>. [arXiv:2012.12189](https://arxiv.org/abs/2012.12189) [gr-qc]
- Herman N, Lehoucq L, Füzfa A (2023) Electromagnetic antennas for the resonant detection of the stochastic gravitational wave background. *Phys Rev D* 108(12):124009. <https://doi.org/10.1103/PhysRevD.108.124009>. [arXiv:2203.15668](https://arxiv.org/abs/2203.15668) [gr-qc]
- Hertzberg MP (2010) Quantum radiation of oscillons. *Phys Rev D* 82:045022. <https://doi.org/10.1103/PhysRevD.82.045022>. [arXiv:1003.3459](https://arxiv.org/abs/1003.3459) [hep-th]
- Hild S et al (2011) Sensitivity studies for third-generation gravitational wave observatories. *Class Quantum Grav* 28:094013. <https://doi.org/10.1088/0264-9381/28/9/094013>. [arXiv:1012.0908](https://arxiv.org/abs/1012.0908) [gr-qc]
- Hill R, Masui KW, Scott D (2018) The Spectrum of the Universe. *Appl Spectrosc* 72(5):663–688. <https://doi.org/10.1177/0003702818767133>. [arXiv:1802.03694](https://arxiv.org/abs/1802.03694) [astro-ph.CO]
- Hinderer T (2008) Tidal Love numbers of neutron stars. *Astrophys J* 677:1216–1220. <https://doi.org/10.1086/533487>. [Erratum: *Astrophys. J.* 697, 964 (2009)]. [arXiv:0711.2420](https://arxiv.org/abs/0711.2420) [astro-ph]
- Hindmarsh M, Hijazi M (2019) Gravitational waves from first order cosmological phase transitions in the sound shell model. *JCAP* 12:062. <https://doi.org/10.1088/1475-7516/2019/12/062>. [arXiv:1909.10040](https://arxiv.org/abs/1909.10040) [astro-ph.CO]
- Hindmarsh M, Stuckey S, Bevis N (2009) Abelian Higgs cosmic strings: small scale structure and loops. *Phys Rev D* 79:123504. <https://doi.org/10.1103/PhysRevD.79.123504>. [arXiv:0812.1929](https://arxiv.org/abs/0812.1929) [hep-th]



- Hindmarsh M, Huber SJ, Rummukainen K, Weir DJ (2014) Gravitational waves from the sound of a first order phase transition. *Phys Rev Lett* 112:041301. <https://doi.org/10.1103/PhysRevLett.112.041301>. arXiv:1304.2433 [hep-ph]
- Hindmarsh M, Huber SJ, Rummukainen K, Weir DJ (2015) Numerical simulations of acoustically generated gravitational waves at a first order phase transition. *Phys Rev D* 92(12):123009. <https://doi.org/10.1103/PhysRevD.92.123009>. arXiv:1504.03291 [astro-ph.CO]
- Hindmarsh M, Huber SJ, Rummukainen K, Weir DJ (2017a) Shape of the acoustic gravitational wave power spectrum from a first order phase transition. *Phys Rev D* 96(10):103520. <https://doi.org/10.1103/PhysRevD.96.103520>. arXiv:1704.05871 [astro-ph.CO]
- Hindmarsh M, Lizarraga J, Urrestilla J, Daverio D, Kunz M (2017b) Scaling from gauge and scalar radiation in Abelian Higgs string networks. *Phys Rev D* 96:023525. <https://doi.org/10.1103/PhysRevD.96.023525>. arXiv:1703.06696 [astro-ph.CO]
- Hindmarsh MB, Lüben M, Lumma J, Pauly M (2021) Phase transitions in the early universe. *SciPost Phys Lect Notes* 24:1. <https://doi.org/10.21468/SciPostPhysLectNotes.24>. arXiv:2008.09136 [astro-ph.CO]
- Hiramatsu T, Sfakianakis EI, Yamaguchi M (2021) Gravitational wave spectra from oscillon formation after inflation. *JHEP* 03:21. [https://doi.org/10.1007/jhep03\(2021\)021](https://doi.org/10.1007/jhep03(2021)021). arXiv:2011.12201 [hep-ph]
- Hogan CJ (1983) Nucleation of cosmological phase transitions. *Phys Lett B* 133:172–176. [https://doi.org/10.1016/0370-2693\(83\)90553-1](https://doi.org/10.1016/0370-2693(83)90553-1)
- Hogan CJ (1986) Gravitational radiation from cosmological phase transitions. *Mon Not R Astron Soc* 218:629–636. <https://doi.org/10.1093/mnras/218.4.629>
- Hong JP, Jung S, Xie KP (2020) Fermi-ball dark matter from a first-order phase transition. *Phys Rev D* 102(7):075028. <https://doi.org/10.1103/PhysRevD.102.075028>. arXiv:2008.04430 [hep-ph]
- Hook A, Kahn Y, Safdi BR, Sun Z (2018) Radio signals from axion dark matter conversion in neutron star magnetospheres. *Phys Rev Lett* 121(24):241102. <https://doi.org/10.1103/PhysRevLett.121.241102>. arXiv:1804.03145 [hep-ph]
- Hsieh HF, Cabezón R, Ma LT, Pan KC (2024) A new kilohertz gravitational-wave feature from rapidly rotating core-collapse supernovae. *Astrophys J* 961(2):194. <https://doi.org/10.3847/1538-4357/ad08c2>. arXiv:2310.20411 [astro-ph.HE]
- Huang FP, Kadota K, Sekiguchi T, Tashiro H (2018) Radio telescope search for the resonant conversion of cold dark matter axions from the magnetized astrophysical sources. *Phys Rev D* 97(12):123001. <https://doi.org/10.1103/PhysRevD.97.123001>. arXiv:1803.08230 [hep-ph]
- Hübner M, Talbot C, Lasky PD, Thrane E (2020) Measuring gravitational-wave memory in the first LIGO/Virgo gravitational-wave transient catalog. *Phys Rev D* 101(2):023011. <https://doi.org/10.1103/PhysRevD.101.023011>. arXiv:1911.12496 [astro-ph.HE]
- Hütsi G, Raidal M, Vaskonen V, Veermäe H (2021) Two populations of LIGO-Virgo black holes. *JCAP* 03:068. <https://doi.org/10.1088/1475-7516/2021/03/068>. arXiv:2012.02786 [astro-ph.CO]
- Inman D, Ali-Haïmoud Y (2019) Early structure formation in primordial black hole cosmologies. *Phys Rev D* 100(8):083528. <https://doi.org/10.1103/PhysRevD.100.083528>. arXiv:1907.08129 [astro-ph.CO]
- Inomata K, Nakama T (2019) Gravitational waves induced by scalar perturbations as probes of the small-scale primordial spectrum. *Phys Rev D* 99:043511. <https://doi.org/10.1103/PhysRevD.99.043511>. arXiv:1812.00674 [astro-ph.CO]
- Inomata K, Kawasaki M, Mukaida K, Tada Y, Yanagida TT (2017) Inflationary primordial black holes for the LIGO gravitational wave events and pulsar timing array experiments. *Phys Rev D* 95:123510. <https://doi.org/10.1103/PhysRevD.95.123510>. arXiv:1611.06130 [astro-ph.CO]
- Inomata K, Kohri K, Nakama T, Terada T (2019a) Enhancement of gravitational waves induced by scalar perturbations due to a sudden transition from an early matter era to the radiation era. *Phys Rev D* 100:043532. <https://doi.org/10.1103/PhysRevD.100.043532>. arXiv:1904.12879 [astro-ph.CO]
- Inomata K, Kohri K, Nakama T, Terada T (2019b) Gravitational waves induced by scalar perturbations during a gradual transition from an early matter era to the radiation era. *JCAP* 10:071. <https://doi.org/10.1088/1475-7516/2019/10/071>. arXiv:1904.12878 [astro-ph.CO]
- Ireland A, Profumo S, Scharnhorst J (2023) Primordial gravitational waves from black hole evaporation in standard and nonstandard cosmologies. *Phys Rev D* 107(10):104021. <https://doi.org/10.1103/PhysRevD.107.104021>. arXiv:2302.10188 [gr-qc]
- Ireland A, Profumo S, Scharnhorst J (2024) Gravitational waves from primordial black hole evaporation with large extra dimensions. *JCAP* 08:033. <https://doi.org/10.1088/1475-7516/2024/08/033>. arXiv:2312.08508 [gr-qc]

- Isi M, Sun L, Brito R, Melatos A (2019) Directed searches for gravitational waves from ultralight bosons. *Phys Rev D* 99(8):084042. <https://doi.org/10.1103/PhysRevD.99.084042>. [Erratum: *Phys. Rev. D* 102, 049901 (2020)]. [arXiv:1810.03812](https://arxiv.org/abs/1810.03812) [gr-qc]
- Ito A, Kitano R (2024) Macroscopic quantum response to gravitational waves. *JCAP* 04:068. <https://doi.org/10.1088/1475-7516/2024/04/068>. [arXiv:2309.02992](https://arxiv.org/abs/2309.02992) [gr-qc]
- Ito A, Soda J (2020) A formalism for magnon gravitational wave detectors. *Eur Phys J C* 80(6):545. <https://doi.org/10.1140/epjc/s10052-020-8092-6>. [arXiv:2004.04646](https://arxiv.org/abs/2004.04646) [gr-qc]
- Ito A, Soda J (2023) Exploring high-frequency gravitational waves with magnons. *Eur Phys J C* 83(8):766. <https://doi.org/10.1140/epjc/s10052-023-11876-2>. [arXiv:2212.04094](https://arxiv.org/abs/2212.04094) [gr-qc]
- Ito A, Ikeda T, Miuchi K, Soda J (2020) Probing GHz gravitational waves with graviton-magnon resonance. *Eur Phys J C* 80:179. <https://doi.org/10.1140/epjc/s10052-020-7735-y>. [arXiv:1903.04843](https://arxiv.org/abs/1903.04843) [gr-qc]
- Ito A, Kohri K, Nakayama K (2024a) Gravitational wave search through electromagnetic telescopes. *PTEP* 2:023E03. <https://doi.org/10.1093/ptep/ptae004>. [arXiv:2309.14765](https://arxiv.org/abs/2309.14765) [gr-qc]
- Ito A, Kohri K, Nakayama K (2024b) Probing high frequency gravitational waves with pulsars. *Phys Rev D* 109(6):063026. <https://doi.org/10.1103/PhysRevD.109.063026>. [arXiv:2305.13984](https://arxiv.org/abs/2305.13984) [gr-qc]
- Jain V, Gieseler J, Moritz C, Dellago C, Quidant R, Novotny L (2016) Direct measurement of photon recoil from a levitated nanoparticle. *Phys Rev Lett* 116:243601. <https://doi.org/10.1103/PhysRevLett.116.243601>
- Jakobus P, Müller B, Heger A, Zha S, Powell J, Motornenko A, Steinheimer J, Stoecker H (2023) Gravitational waves from a core g mode in supernovae as probes of the high-density equation of state. *Phys Rev Lett* 131(19):191201. <https://doi.org/10.1103/PhysRevLett.131.191201>. [arXiv:2301.06515](https://arxiv.org/abs/2301.06515) [astro-ph.HE]
- Janik RA, Jarvinen M, Soltanpanahi H, Sonnenschein J (2022) Perfect fluid hydrodynamic picture of domain wall velocities at strong coupling. *Phys Rev Lett* 129(8):081601. <https://doi.org/10.1103/PhysRevLett.129.081601>. [arXiv:2205.06274](https://arxiv.org/abs/2205.06274) [hep-th]
- Jeannerot R, Rocher J, Sakellariadou M (2003) How generic is cosmic string formation in SUSY GUTs. *Phys Rev D* 68:103514. <https://doi.org/10.1103/PhysRevD.68.103514>. [arXiv:hep-ph/0308134](https://arxiv.org/abs/hep-ph/0308134) [hep-ph]
- Jiang S, Huang FP, Wang X (2023) Bubble wall velocity during electroweak phase transition in the inert doublet model. *Phys Rev D* 107(9):095005. <https://doi.org/10.1103/PhysRevD.107.095005>. [arXiv:2211.13142](https://arxiv.org/abs/2211.13142) [hep-ph]
- Jing M, Hu Y, Ma J, Zhang H, Zhang L, Xiao L, Jia S (2020) Atomic superheterodyne receiver based on microwave-dressed Rydberg spectroscopy. *Nat Phys* 16(9):911–915. <https://doi.org/10.1038/s41567-020-0918-5>. [arXiv:1902.11063](https://arxiv.org/abs/1902.11063) [physics.atom-ph]
- Johnson WW, Merkowitz SM (1993) Truncated icosahedral gravitational wave antenna. *Phys Rev Lett* 70:2367–2370. <https://doi.org/10.1103/PhysRevLett.70.2367>
- Jones-Smith K, Krauss LM, Mathur H (2008) A nearly scale invariant spectrum of gravitational radiation from global phase transitions. *Phys Rev Lett* 100:131302. <https://doi.org/10.1103/PhysRevLett.100.131302>. [arXiv:0712.0778](https://arxiv.org/abs/0712.0778) [astro-ph]
- Kahn Y, Schütte-Engel J, Trickle T (2024) Searching for high-frequency gravitational waves with phonons. *Phys Rev D* 109(9):096023. <https://doi.org/10.1103/PhysRevD.109.096023>. [arXiv:2311.17147](https://arxiv.org/abs/2311.17147) [hep-ph]
- Kaiser DI (1996) Post inflation reheating in an expanding universe. *Phys Rev D* 53:1776–1783. <https://doi.org/10.1103/PhysRevD.53.1776>. [arXiv:astro-ph/9507108](https://arxiv.org/abs/astro-ph/9507108)
- Kaiser DI (1997) Preheating in an expanding universe: analytic results for the massless case. *Phys Rev D* 56:706–716. <https://doi.org/10.1103/PhysRevD.56.706>. [arXiv:hep-ph/9702244](https://arxiv.org/abs/hep-ph/9702244)
- Kaiser DI (1998) Resonance structure for preheating with massless fields. *Phys Rev D* 57:702–711. <https://doi.org/10.1103/PhysRevD.57.702>. [arXiv:hep-ph/9707516](https://arxiv.org/abs/hep-ph/9707516)
- Kanno S, Soda J, Taniguchi A (2025) Search for high-frequency gravitational waves with Rydberg atoms. *Eur Phys J C* 85:31. <https://doi.org/10.1140/epjc/s10052-024-13736-z>. [arXiv:2311.03890](https://arxiv.org/abs/2311.03890) [gr-qc]
- Katz A, Kopp J, Sibiryakov S, Xue W (2018) Femtolensing by dark matter revisited. *JCAP* 12:005. <https://doi.org/10.1088/1475-7516/2018/12/005>. [arXiv:1807.11495](https://arxiv.org/abs/1807.11495) [astro-ph.CO]
- Kaup DJ (1968) Klein-Gordon Geon. *Phys Rev* 172:1331–1342. <https://doi.org/10.1103/PhysRev.172.1331>
- Kerachian M, Mukherjee S, Lukes-Gerakopoulos G, Mitra S (2024) Detectability of stochastic gravitational wave background from weakly hyperbolic encounters. *Astron Astrophys* 684:A17. <https://doi.org/10.1051/0004-6361/202348747>. [arXiv:2311.16634](https://arxiv.org/abs/2311.16634) [gr-qc]

- Khlebnikov S, Tkachev II (1996) Classical decay of inflaton. *Phys Rev Lett* 77:219–222. <https://doi.org/10.1103/PhysRevLett.77.219>. arXiv:hep-ph/9603378
- Khlebnikov SY, Tkachev II (1997) Relic gravitational waves produced after preheating. *Phys Rev D* 56:653–660. <https://doi.org/10.1103/PhysRevD.56.653>. arXiv:hep-ph/9701423 [hep-ph]
- Kibble TWB (1976) Topology of cosmic domains and strings. *J Phys A* 9:1387–1398. <https://doi.org/10.1088/0305-4470/9/8/029>
- Kiefer C, Weber C (2005) On the interaction of mesoscopic quantum systems with gravity. *Annalen Phys* 14:253–278. <https://doi.org/10.1002/andp.200410119>. arXiv:gr-qc/0408010
- Kim JE, Nilles HP, Peloso M (2005) Completing natural inflation. *JCAP* 0501:005. <https://doi.org/10.1088/1475-7516/2005/01/005>. arXiv:hep-ph/0409138 [hep-ph]
- Kirzhnits DA (1972) Weinberg model in the hot universe. *JETP Lett* 15:529–531
- Kirzhnits DA, Linde AD (1976) Symmetry behavior in Gauge theories. *Ann Phys* 101:195–238. [https://doi.org/10.1016/0003-4916\(76\)90279-7](https://doi.org/10.1016/0003-4916(76)90279-7)
- Kitajima N, Soda J, Urakawa Y (2018) Gravitational wave forest from string axiverse. *JCAP* 1810:008. <https://doi.org/10.1088/1475-7516/2018/10/008>. arXiv:1807.07037 [astro-ph.CO]
- Kitajima N, Soda J, Urakawa Y (2021) Nano-Hz gravitational-wave signature from axion dark matter. *Phys Rev Lett* 126(12):121301. <https://doi.org/10.1103/PhysRevLett.126.121301>. arXiv:2010.10990 [astro-ph.CO]
- Kocharovskaya OA, Khanin YI (1986) Population trapping and coherent bleaching of a three-level medium by a periodic train of ultrashort pulses. *Sov JETP* 63(5):945
- Kocsis B, Gaspar ME, Marka S (2006) Detection rate estimates of gravity-waves emitted during parabolic encounters of stellar black holes in globular clusters. *Astrophys J* 648:411–429. <https://doi.org/10.1086/505641>. arXiv:astro-ph/0603441
- Kocsis B, Suyama T, Tanaka T, Yokoyama S (2018) Hidden universality in the merger rate distribution in the primordial black hole scenario. *Astrophys J* 854:41. <https://doi.org/10.3847/1538-4357/aaa7f4>. arXiv:1709.09007 [astro-ph.CO]
- Kofman L, Linde AD, Starobinsky AA (1994) Reheating after inflation. *Phys Rev Lett* 73:3195–3198. <https://doi.org/10.1103/PhysRevLett.73.3195>. arXiv:hep-th/9405187 [hep-th]
- Kofman L, Linde AD, Starobinsky AA (1997) Towards the theory of reheating after inflation. *Phys Rev D* 56:3258–3295. <https://doi.org/10.1103/PhysRevD.56.3258>. arXiv:hep-ph/9704452 [hep-ph]
- Kohri K, Terada T (2018) Semianalytic calculation of gravitational wave spectrum nonlinearly induced from primordial curvature perturbations. *Phys Rev D* 97:123532. <https://doi.org/10.1103/PhysRevD.97.123532>. arXiv:1804.08577 [gr-qc]
- Korobko M, Khalili FY, Schnabel R (2018) Engineering the optical spring via intra-cavity optical-parametric amplification. *Phys Lett A* 382:2238–2244. <https://doi.org/10.1016/j.physleta.2017.08.008>. arXiv:1709.03055 [quant-ph]
- Kou XX, Tian C, Zhou SY (2021) Oscillon preheating in full general relativity. *Class Quantum Grav* 38:045005. <https://doi.org/10.1088/1361-6382/abd09f>. arXiv:1912.09658 [gr-qc]
- Kouvaris C, Tinyakov P, Tytgat MHG (2018) NonPrimordial solar mass black holes. *Phys Rev Lett* 121:221102. <https://doi.org/10.1103/PhysRevLett.121.221102>. arXiv:1804.06740 [astro-ph.HE]
- Krauss LM (1992) Gravitational waves from global phase transitions. *Phys Lett B* 284:229–233. [https://doi.org/10.1016/0370-2693\(92\)90425-4](https://doi.org/10.1016/0370-2693(92)90425-4)
- Krippendorff S, Muia F, Quevedo F (2018) Moduli stars. *JHEP* 08:070. [https://doi.org/10.1007/JHEP08\(2018\)070](https://doi.org/10.1007/JHEP08(2018)070). arXiv:1806.04690 [hep-th]
- Kunjipurayil A, Zhao T, Kumar B, Agrawal BK, Prakash M (2022) Impact of the equation of state on f- and p- mode oscillations of neutron stars. *Phys Rev D* 106(6):063005. <https://doi.org/10.1103/PhysRevD.106.063005>. arXiv:2205.02081 [nucl-th]
- Kwon O et al (2021) First results from an axion haloscope at CAPP around 10.7  $\mu\text{eV}$ . *Phys Rev Lett* 126(19):191802. <https://doi.org/10.1103/PhysRevLett.126.191802>. arXiv:2012.10764 [hep-ex]
- Lamoreaux SK, van Bibber KA, Lehnert KW, Carosi G (2013) Analysis of single-photon and linear amplifier detectors for microwave cavity dark matter axion searches. *Phys Rev D* 88:035020. <https://doi.org/10.1103/PhysRevD.88.035020>. arXiv:1306.3591 [physics.ins-det]
- Landau LD, Lifshitz EM (1975) The classical theory of fields, course of theoretical physics, vol 2. Pergamon Press, Oxford
- Langer JS (1969) Statistical theory of the decay of metastable states. *Ann Phys* 54:258–275. [https://doi.org/10.1016/0003-4916\(69\)90153-5](https://doi.org/10.1016/0003-4916(69)90153-5)
- Lasky PD, Thrane E (2021) Did Goryachev et al. detect megahertz gravitational waves? *Phys Rev D* 104(10):103017. <https://doi.org/10.1103/PhysRevD.104.103017>. arXiv:2110.13319 [gr-qc]

- Lasky PD, Thrane E, Levin Y, Blackman J, Chen Y (2016) Detecting gravitational-wave memory with LIGO: implications of GW150914. *Phys Rev Lett* 117(6):061102. <https://doi.org/10.1103/PhysRevLett.117.061102>. arXiv:1605.01415 [astro-ph.HE]
- Laurent B, Cline JM (2020) Fluid equations for fast-moving electroweak bubble walls. *Phys Rev D* 102:063516. <https://doi.org/10.1103/PhysRevD.102.063516>. arXiv:2007.10935 [hep-ph]
- Laurent B, Cline JM (2022) First principles determination of bubble wall velocity. *Phys Rev D* 106(2):023501. <https://doi.org/10.1103/PhysRevD.106.023501>. arXiv:2204.13120 [hep-ph]
- Leblond L, Shlaer B, Siemens X (2009) Gravitational waves from broken cosmic strings: the bursts and the beads. *Phys Rev D* 79:123519. <https://doi.org/10.1103/PhysRevD.79.123519>. arXiv:0903.4686 [astro-ph.CO]
- Lee TD, Pang Y (1987) Fermion soliton stars and black holes. *Phys Rev D* 35:3678. <https://doi.org/10.1103/PhysRevD.35.3678>
- Lella A, Calore F, Carena P, Mirizzi A (2024) Constraining gravitational-wave backgrounds from conversions into photons in the Galactic magnetic field. *Phys Rev D* 110(8):083042. <https://doi.org/10.1103/PhysRevD.110.083042>. arXiv:2406.17853 [hep-ph]
- Leroy M, Chianese M, Edwards TDP, Weniger C (2020) Radio signal of axion-photon conversion in neutron stars: a ray tracing analysis. *Phys Rev D* 101(12):123003. <https://doi.org/10.1103/PhysRevD.101.123003>. arXiv:1912.08815 [hep-ph]
- Lescanne R, Deléglise S, Albertinale E, Réglade U, Capelle T, Ivanov E, Jacqmin T, Leghtas Z, Flurin E (2020) Irreversible qubit-photon coupling for the detection of itinerant microwave photons. *Phys Rev X* 10(2):021038. <https://doi.org/10.1103/PhysRevX.10.021038>
- Lewicki M, Merchand M, Zych M (2022) Electroweak bubble wall expansion: gravitational waves and baryogenesis in Standard Model-like thermal plasma. *JHEP* 02:017. [https://doi.org/10.1007/JHEP02\(2022\)017](https://doi.org/10.1007/JHEP02(2022)017). arXiv:2111.02393 [astro-ph.CO]
- Li F, Baker Jr RML, Chen Z (2006) Perturbative photon flux generated by high-frequency relic gravitational waves and utilization of them for their detection. arXiv e-prints arXiv:gr-qc/0604109 [gr-qc]
- Li F, Yang N, Fang Z, Baker J, Robert ML, Stephenson GV, Wen H (2009) Signal photon flux and background noise in a coupling electromagnetic detecting system for high frequency gravitational waves. *Phys Rev D* 80:064013. <https://doi.org/10.1103/PhysRevD.80.064013>. arXiv:0909.4118 [gr-qc]
- Li FY, Yang N (2004) Resonant interaction between a weak gravitational wave and a microwave beam in the double polarized states through a static magnetic field. *Chin Phys Lett* 21:2113–2116. <https://doi.org/10.1088/0256-307X/21/11/011>. arXiv:gr-qc/0410060
- Liang T et al (2023) Yoctonewton force detection based on optically levitated oscillator. *Fund Res* 3:57–62. <https://doi.org/10.1016/j.fmre.2022.09.021>
- Linde AD (1983) Decay of the false vacuum at finite temperature. *NuclPhys B* 216:421. [https://doi.org/10.1016/0550-3213\(83\)90293-6](https://doi.org/10.1016/0550-3213(83)90293-6)
- Liu J, Guo ZK, Cai RG, Shiu G (2018) Gravitational waves from oscillons with cuspy potentials. *Phys Rev Lett* 120:031301. <https://doi.org/10.1103/PhysRevLett.120.031301>. arXiv:1707.09841 [astro-ph.CO]
- Liu T, Ren J, Zhang C (2024) Limits on high-frequency gravitational waves in planetary magnetospheres. *Phys Rev Lett* 132(13):131402. <https://doi.org/10.1103/PhysRevLett.132.131402>. arXiv:2305.01832 [hep-ph]
- Lo A, Haslinger P, Mizrahi E, Anderegg L, Müller H, Hohensee M, Goryachev M, Tobar ME (2016) Acoustic tests of Lorentz symmetry using quartz oscillators. *Phys Rev X* 6:011018. <https://doi.org/10.1103/PhysRevX.6.011018>. arXiv:1412.2142 [gr-qc]
- Lough J et al (2021) First demonstration of 6 dB quantum noise reduction in a kilometer scale gravitational wave observatory. *Phys Rev Lett* 126(4):041102. <https://doi.org/10.1103/PhysRevLett.126.041102>. arXiv:2005.10292 [physics.ins-det]
- Lovato A et al (2022) Long range plan: dense matter theory for heavy-ion collisions and neutron stars. arXiv e-prints arXiv:2211.02224 [nucl-th]
- Lozanov KD (2019) Lectures on reheating after inflation. arXiv e-prints arXiv:1907.04402 [astro-ph.CO]
- Lozanov KD, Amin MA (2014) End of inflation, oscillons, and matter-antimatter asymmetry. *Phys Rev D* 90:083528. <https://doi.org/10.1103/PhysRevD.90.083528>. arXiv:1408.1811 [hep-ph]
- Lozanov KD, Amin MA (2018) Self-resonance after inflation: oscillons, transients and radiation domination. *Phys Rev D* 97:023533. <https://doi.org/10.1103/PhysRevD.97.023533>. arXiv:1710.06851 [astro-ph.CO]

- Lozanov KD, Amin MA (2019) Gravitational perturbations from oscillons and transients after inflation. *Phys Rev D* 99:123504. <https://doi.org/10.1103/PhysRevD.99.123504>. arXiv:1902.06736 [astro-ph.CO]
- Lupanov GA (1966) A capacitor in the field of a gravitational wave. *Sov Phys JETP* 25:76–79
- von Lüpke U, Yang Y, Bild M, Michaud L, Fadel M, Chu Y (2022) Parity measurement in the strong dispersive regime of circuit quantum acoustodynamics. *Nat Phys* 18(7):794–799. <https://doi.org/10.1038/s41567-022-01591-2>. arXiv:2110.00263 [quant-ph]
- Maartens R, Koyama K (2010) Brane-world gravity. *Liv Rev Relativ* 13:5. <https://doi.org/10.12942/lrr-2010-5>. arXiv:1004.3962 [hep-th]
- Macedo PG, Nelson AH (1983) Propagation of gravitational waves in a magnetized plasma. *Phys Rev D* 28:2382–2392. <https://doi.org/10.1103/PhysRevD.28.2382>
- Machado CS, Ratzinger W, Schwaller P, Stefanek BA (2019) Audible axions. *JHEP* 01:053. [https://doi.org/10.1007/JHEP01\(2019\)053](https://doi.org/10.1007/JHEP01(2019)053). arXiv:1811.01950 [hep-ph]
- Machado CS, Ratzinger W, Schwaller P, Stefanek BA (2020) Gravitational wave probes of axionlike particles. *Phys Rev D* 102(7):075033. <https://doi.org/10.1103/PhysRevD.102.075033>. arXiv:1912.01007 [hep-ph]
- Madge E, Ratzinger W, Schmitt D, Schwaller P (2022) Audible axions with a booster: stochastic gravitational waves from rotating ALPs. *SciPost Phys* 12(5):171. <https://doi.org/10.21468/SciPostPhys.12.5.171>. arXiv:2111.12730 [hep-ph]
- Maggiore M (2007) Gravitational waves. Vol. 1: theory and experiments. Oxford University Press, Oxford. <https://doi.org/10.1093/acprof:oso/9780198570745.001.0001>
- Martinez JGC, Kamai B (2020) Searching for MHz gravitational waves from harmonic sources. *Class Quantum Grav* 37:205006. <https://doi.org/10.1088/1361-6382/aba669>. arXiv:2010.06118 [astro-ph.IM]
- Martynov D et al (2019) Exploring the sensitivity of gravitational wave detectors to neutron star physics. *Phys Rev D* 99(10):102004. <https://doi.org/10.1103/PhysRevD.99.102004>. arXiv:1901.03885 [astro-ph.IM]
- Matarrese S, Pantano O, Saez D (1994) General relativistic dynamics of irrotational dust: cosmological implications. *Phys Rev Lett* 72:320–323. <https://doi.org/10.1103/PhysRevLett.72.320>. arXiv:astro-ph/9310036
- Mazur PO, Mottola E (2004) Gravitational vacuum condensate stars. *Proc Nat Acad Sci* 101:9545–9550. <https://doi.org/10.1073/pnas.0402717101>. arXiv:gr-qc/0407075
- McDonald JJ, Ellis SAR (2024) Resonant conversion of gravitational waves in neutron star magnetospheres. *Phys Rev D* 110(10):103003. <https://doi.org/10.1103/PhysRevD.110.103003>. arXiv:2406.18634 [hep-ph]
- McDonald JJ, Millington P (2024) Axion-photon mixing in 3D: classical equations and geometric optics. *JCAP* 09:072. <https://doi.org/10.1088/1475-7516/2024/09/072>. arXiv:2407.11192 [hep-ph]
- McDonald JJ, Witte SJ (2023) Generalized ray tracing for axions in astrophysical plasmas. *Phys Rev D* 108(10):103021. <https://doi.org/10.1103/PhysRevD.108.103021>. arXiv:2309.08655 [hep-ph]
- McDonald JJ, Garbrecht B, Millington P (2023) Axion-photon conversion in 3D media and astrophysical plasmas. *JCAP* 12:031. <https://doi.org/10.1088/1475-7516/2023/12/031>. arXiv:2307.11812 [hep-ph]
- McNeill LO, Thrane E, Lasky PD (2017) Detecting gravitational wave memory without parent signals. *Phys Rev Lett* 118(18):181103. <https://doi.org/10.1103/PhysRevLett.118.181103>. arXiv:1702.01759 [astro-ph.IM]
- Michelson P (1987) On detecting stochastic background gravitational radiation with terrestrial detectors. *Mon Not R Astron Soc* 277:933–941. <https://doi.org/10.1093/mnras/227.4.933>
- Millar AJ et al (2023) Searching for dark matter with plasma haloscopes. *Phys Rev D* 107(5):055013. <https://doi.org/10.1103/PhysRevD.107.055013>. arXiv:2210.00017 [hep-ph]
- Millen J, Monteiro TS, Petit R, Vamivakas AN (2020) Optomechanics with levitated particles. *Rep Prog Phys* 83(2):026401. <https://doi.org/10.1088/1361-6633/ab6100>. arXiv:1907.08198 [physics.optics]
- Misner CW, Thorne KS, Wheeler JA (1973) *Gravitation*. W. H. Freeman, San Francisco
- Mizuno J (1995) Comparison of optical configurations for laser-interferometric gravitational-wave detectors. PhD thesis, Universität Hannover
- Mollerach S, Harari D, Matarrese S (2004) CMB polarization from secondary vector and tensor modes. *Phys Rev D* 69:063002. <https://doi.org/10.1103/PhysRevD.69.063002>. arXiv:astro-ph/0310711 [astro-ph]
- Monin A, Voloshin MB (2008) The spontaneous breaking of a metastable string. *Phys Rev D* 78:065048. <https://doi.org/10.1103/PhysRevD.78.065048>. arXiv:0808.1693 [hep-th]



- Monin A, Voloshin MB (2010) Destruction of a metastable string by particle collisions. *Phys Atom Nucl* 73:703–710. <https://doi.org/10.1134/S1063778810040162>. arXiv:0902.0407 [hep-th]
- Moore CJ, Cole RH, Berry CPL (2015) Gravitational-wave sensitivity curves. *Class Quantum Grav* 32:015014. <https://doi.org/10.1088/0264-9381/32/1/015014>. arXiv:1408.0740 [gr-qc]
- Moore GD, Prokopec T (1995) How fast can the wall move? A Study of the electroweak phase transition dynamics. *Phys Rev D* 52:7182–7204. <https://doi.org/10.1103/PhysRevD.52.7182>. arXiv:hep-ph/9506475 [hep-ph]
- Morrás G, García-Bellido J, Nesseris S (2022) Search for black hole hyperbolic encounters with gravitational wave detectors. *Phys Dark Univ* 35:100932. <https://doi.org/10.1016/j.dark.2021.100932>. arXiv:2110.08000 [astro-ph.HE]
- Most ER, Papenfort LJ, Dexheimer V, Hanauske M, Schramm S, Stöcker H, Rezzolla L (2019) Signatures of quark-hadron phase transitions in general-relativistic neutron-star mergers. *Phys Rev Lett* 122(6):061101. <https://doi.org/10.1103/PhysRevLett.122.061101>. arXiv:1807.03684 [astro-ph.HE]
- Mróz P et al (2024) No massive black holes in the Milky Way halo. *Nature* 632(8026):749–751. <https://doi.org/10.1038/s41586-024-07704-6>. arXiv:2403.02386 [astro-ph.GA]
- Muia F, Cicoli M, Clough K, Pedro F, Quevedo F, Vacca GP (2019) The fate of dense scalar stars. *JCAP* 1907:044. <https://doi.org/10.1088/1475-7516/2019/07/044>. arXiv:1906.09346 [gr-qc]
- Muia F, Quevedo F, Schachner A, Villa G (2023) Testing BSM physics with gravitational waves. *JCAP* 09:006. <https://doi.org/10.1088/1475-7516/2023/09/006>. arXiv:2303.01548 [hep-ph]
- Muia F, Ringwald A, Tamarit C (2025a) High frequency gravitational wave plotter Noise- equivalent strain. <https://doi.org/10.5281/zenodo.15720342>
- Muia F, Ringwald A, Tamarit C (2025b) High frequency gravitational wave plotter Stochastic signals. <https://doi.org/10.5281/zenodo.15720443>
- Mukherjee S, Mitra S, Chatterjee S (2021) Gravitational wave observatories may be able to detect hyperbolic encounters of black holes. *Mon Not R Astron Soc* 508(4):5064–5073. <https://doi.org/10.1093/mnras/stab2721>. arXiv:2010.00916 [gr-qc]
- Nakama T, Silk J, Kamionkowski M (2017) Stochastic gravitational waves associated with the formation of primordial black holes. *Phys Rev D* 95:043511. <https://doi.org/10.1103/PhysRevD.95.043511>. arXiv:1612.06264 [astro-ph.CO]
- Nakamura T, Sasaki M, Tanaka T, Thorne KS (1997) Gravitational waves from coalescing black hole MACHO binaries. *Astrophys J Lett* 487:L139–L142. <https://doi.org/10.1086/310886>. arXiv:astro-ph/9708060
- Narain G, Schaffner-Bielich J, Mishustin IN (2006) Compact stars made of fermionic dark matter. *Phys Rev D* 74. <https://doi.org/10.1103/physrevd.74.063003>
- Navarro JF, Frenk CS, White SDM (1996) The Structure of cold dark matter halos. *Astrophys J* 462:563–575. <https://doi.org/10.1086/177173>. arXiv:astro-ph/9508025
- Navarro JF, Frenk CS, White SDM (1997) A Universal density profile from hierarchical clustering. *Astrophys J* 490:493–508. <https://doi.org/10.1086/304888>. arXiv:astro-ph/9611107
- Navarro P, Gimeno B, Monzó-Cabrera J, Díaz-Morcillo A, Blas D (2024) Study of a cubic cavity resonator for gravitational waves detection in the microwave frequency range. *Phys Rev D* 109(10):104048. <https://doi.org/10.1103/PhysRevD.109.104048>. arXiv:2312.02270 [hep-ph]
- Nazari Z, Cicoli M, Clough K, Muia F (2021) Oscillon collapse to black holes. *JCAP* 2021(5):027. <https://doi.org/10.1088/1475-7516/2021/05/027>. arXiv:2010.05933 [gr-qc]
- Niikura H, Takada M, Yokoyama S, Sumi T, Masaki S (2019) Constraints on Earth-mass primordial black holes from OGLE 5-year microlensing events. *Phys Rev D* 99:083503. <https://doi.org/10.1103/PhysRevD.99.083503>. arXiv:1901.07120 [astro-ph.CO]
- Nishizawa A, Kawamura S, Akutsu T, Arai K, Yamamoto K, Tatsumi D, Nishida E, Sakagami MA, Chiba T, Takahashi R, Sugiyama N (2008) Laser-interferometric detectors for gravitational wave backgrounds at 100 MHz. *Phys Rev D* 77:022002. <https://doi.org/10.1103/PhysRevD.77.022002>
- Nishizawa A et al (2008) Laser-interferometric detectors for gravitational wave background at 100 MHz: detector design and sensitivity. *Phys Rev D* 77:022002. <https://doi.org/10.1103/PhysRevD.77.022002>. arXiv:0710.1944 [gr-qc]
- O’Leary RM, Kocsis B, Loeb A (2009) Gravitational waves from scattering of stellar-mass black holes in galactic nuclei. *Mon Not R Astron Soc* 395(4):2127–2146. <https://doi.org/10.1111/j.1365-2966.2009.14653.x>. arXiv:0807.2638 [astro-ph]
- Oliveira NF, Aguiar OD (2016) The Mario Schenberg gravitational wave antenna. *Braz J Phys* 46(5):596–603. <https://doi.org/10.1007/s13538-016-0436-1>

- Pagano L, Salvati L, Melchiorri A (2016) New constraints on primordial gravitational waves from Planck 2015. *Phys Lett B* 760:823–825. <https://doi.org/10.1016/j.physletb.2016.07.078>. arXiv:1508.02393 [astro-ph.CO]
- Palenzuela C, Pani P, Bezares M, Cardoso V, Lehner L, Liebling S (2017) Gravitational wave signatures of highly compact boson star binaries. *Phys Rev D* 96(10). <https://doi.org/10.1103/physrevd.96.104058>
- Pankratov AL, Gordeeva AV, Chiginev AV, Revin LS, Blagodatkin AV, Crescini N, Kuzmin LS (2025) Observation of thermal microwave photons with a Josephson junction detector. *Nat Commun* 16:3457. <https://doi.org/10.1038/s41467-025-56040-4>. arXiv:2404.10434 [quant-ph]
- Pappas KMW et al (2025) High-frequency gravitational wave search with ABRACADABRA-10 cm. arXiv e-prints arXiv:2505.02821 [hep-ex]
- Patra A et al (2025) Broadband limits on stochastic length fluctuations from a pair of table-top Interferometers. *Phys Rev Lett* 135:101402. <https://doi.org/10.1103/61j9-cjkk>. arXiv:2410.09175 [gr-qc]
- Peebles PJE, Vilenkin A (1999) Quintessential inflation. *Phys Rev D* 59:063505. <https://doi.org/10.1103/PhysRevD.59.063505>. arXiv:astro-ph/9810509
- Pegoraro F, Picasso E, Radicati LA (1978a) On the operation of a tunable electromagnetic detector for gravitational waves. *J Phys A* 11:1949–1962. <https://doi.org/10.1088/0305-4470/11/10/013>
- Pegoraro F, Radicati L, Bernard P, Picasso E (1978b) Electromagnetic detector for gravitational waves. *Phys Lett* 68:165–168. [https://doi.org/10.1016/0375-9601\(78\)90792-2](https://doi.org/10.1016/0375-9601(78)90792-2)
- Peloso M, Unal C (2015) Trajectories with suppressed tensor-to-scalar ratio in Aligned Natural Inflation. *JCAP* 1506:040. <https://doi.org/10.1088/1475-7516/2015/06/040>. arXiv:1504.02784 [astro-ph.CO]
- Peloso M, Sorbo L, Unal C (2016) Rolling axions during inflation: perturbativity and signatures. *JCAP* 1609:001. <https://doi.org/10.1088/1475-7516/2016/09/001>. arXiv:1606.00459 [astro-ph.CO]
- Phinney ES et al (2003) The Big Bang Observer: Direct detection of gravitational waves from the birth of the universe to the present. NASA Mission Concept Study
- Pollney D, Reisswig C (2011) Gravitational memory in binary black hole mergers. *Astrophys J Lett* 732:L13. <https://doi.org/10.1088/2041-8205/732/1/L13>. arXiv:1004.4209 [gr-qc]
- Pontin A, Mourounas LS, Geraci AA, Barker PF (2018) Levitated optomechanics with a fiber Fabry–Perot interferometer. *New J Phys* 20:023017. <https://doi.org/10.1088/1367-2630/aaa71c>
- Posen S (2021) Efforts towards first applications of Nb<sub>3</sub>Sn SRF cavities. [https://indico.frib.msu.edu/event/38/attachments/160/1305/FROFDV05\\_TALK\\_Posen.pdf](https://indico.frib.msu.edu/event/38/attachments/160/1305/FROFDV05_TALK_Posen.pdf), presented at SRF21
- Prokopec T, Roos TG (1997) Lattice study of classical inflaton decay. *Phys Rev D* 55:3768–3775. <https://doi.org/10.1103/PhysRevD.55.3768>. arXiv:hep-ph/9610400
- Pshirkov MS, Baskaran D (2009) Limits on high-frequency gravitational wave background from its interplay with large scale magnetic fields. *Phys Rev D* 80:042002. <https://doi.org/10.1103/PhysRevD.80.042002>. arXiv:0903.4160 [gr-qc]
- Pshirkov MS, Popov SB (2009) Conversion of Dark matter axions to photons in magnetospheres of neutron stars. *J Exp Theor Phys* 108:384–388. <https://doi.org/10.1134/S1063776109030030>. arXiv:0711.1264 [astro-ph]
- Pujolas O, Vaskonen V, Veermäe H (2021) Prospects for probing gravitational waves from primordial black hole binaries. *Phys Rev D* 104(8):083521. <https://doi.org/10.1103/PhysRevD.104.083521>. arXiv:2107.03379 [astro-ph.CO]
- Punturo M et al (2010) The Einstein telescope: a third-generation gravitational wave observatory. *Class Quantum Grav* 27:194002. <https://doi.org/10.1088/0264-9381/27/19/194002>
- Quiskamp A, McAllister BT, Altin P, Ivanov EN, Goryachev M, Tobar ME (2024) Exclusion of axionlike-particleogenesis dark matter in a mass window above 100  $\mu\text{eV}$ . *Phys Rev Lett* 132(3):031601. <https://doi.org/10.1103/PhysRevLett.132.031601>. arXiv:2310.00904 [hep-ex]
- Quiskamp AP, McAllister BT, Altin P, Ivanov EN, Goryachev M, Tobar ME (2022) Direct search for dark matter axions excluding ALPogenesis in the 63- to 67- $\mu\text{eV}$  range with the ORGAN experiment. *Sci Adv* 8(27):abq3765. <https://doi.org/10.1126/sciadv.abq3765>. arXiv:2203.12152 [hep-ex]
- Radice D, Morozova V, Burrows A, Vartanyan D, Nagakura H (2019) Characterizing the gravitational wave signal from core-collapse supernovae. *Astrophys J Lett* 876(1):L9. <https://doi.org/10.3847/2041-8213/ab191a>. arXiv:1812.07703 [astro-ph.HE]
- Raffelt G, Stodolsky L (1988) Mixing of the photon with low mass particles. *Phys Rev D* 37:1237. <https://doi.org/10.1103/PhysRevD.37.1237>

- Raidal M, Spethmann C, Vaskonen V, Veermäe H (2019) Formation and evolution of primordial black hole binaries in the early universe. *JCAP* 1902:018. <https://doi.org/10.1088/1475-7516/2019/02/018>. [arXiv:1812.01930](https://arxiv.org/abs/1812.01930) [astro-ph.CO]
- Raidal M, Vaskonen V, Veermäe H (2025) Formation of primordial black hole binaries and their merger rates. In: Byrnes C et al (eds) *Primordial Black Holes*. Springer Series in Astrophysics and Cosmology. Springer, Singapore, pp 393–427. [https://doi.org/10.1007/978-981-97-8887-3\\_16](https://doi.org/10.1007/978-981-97-8887-3_16). [arXiv:2404.08416](https://arxiv.org/abs/2404.08416) [astro-ph.CO]
- Rakhmanov M (2005) Response of test masses to gravitational waves in the local Lorentz gauge. *Phys Rev D* 71:084003. <https://doi.org/10.1103/PhysRevD.71.084003>. [arXiv:gr-qc/0406009](https://arxiv.org/abs/gr-qc/0406009)
- Rakhmanov M (2014) Fermi-normal, optical, and wave-synchronous coordinates for spacetime with a plane gravitational wave. *Class Quantum Grav* 31:085006. <https://doi.org/10.1088/0264-9381/31/8/085006>. [arXiv:1409.4648](https://arxiv.org/abs/1409.4648) [gr-qc]
- Ramazano S, Samanta R, Trenkler G, Urban FR (2023) Shimmering gravitons in the gamma-ray sky. *JCAP* 06:019. <https://doi.org/10.1088/1475-7516/2023/06/019>. [arXiv:2304.11222](https://arxiv.org/abs/2304.11222) [astro-ph.HE]
- Randall L, Sundrum R (1999) Out of this world supersymmetry breaking. *Nucl Phys B* 557:79–118. [https://doi.org/10.1016/S0550-3213\(99\)00359-4](https://doi.org/10.1016/S0550-3213(99)00359-4). [arXiv:hep-th/9810155](https://arxiv.org/abs/hep-th/9810155)
- Ranjit G, Cunningham M, Casey K, Geraci AA (2016) Zeptonewton force sensing with nanospheres in an optical lattice. *Phys Rev A* 93:053801. <https://doi.org/10.1103/PhysRevA.93.053801>
- Raposo G, Pani P, Bezares M, Palenzuela C, Cardoso V (2019) Anisotropic stars as ultracompact objects in General Relativity. *Phys Rev D* 99(10):104072. <https://doi.org/10.1103/PhysRevD.99.104072>. [arXiv:1811.07917](https://arxiv.org/abs/1811.07917) [gr-qc]
- Ratzinger W, Schwaller P, Stefanek BA (2021) Gravitational waves from an axion-dark photon system: a lattice study. *SciPost Phys* 11:001. <https://doi.org/10.21468/SciPostPhys.11.1.001>. [arXiv:2012.11584](https://arxiv.org/abs/2012.11584) [astro-ph.CO]
- Ratzinger W, Schenk S, Schwaller P (2024) A coordinate-independent formalism for detecting high-frequency gravitational waves. *JHEP* 08:195. [https://doi.org/10.1007/JHEP08\(2024\)195](https://doi.org/10.1007/JHEP08(2024)195). [arXiv:2404.08572](https://arxiv.org/abs/2404.08572) [gr-qc]
- Read JS, Baiotti L, Creighton JDE, Friedman JL, Giacomazzo B, Kyutoku K, Markakis C, Rezzolla L, Shibata M, Taniguchi K (2013) Matter effects on binary neutron star waveforms. *Phys Rev D* 88:044042. <https://doi.org/10.1103/PhysRevD.88.044042>. [arXiv:1306.4065](https://arxiv.org/abs/1306.4065) [gr-qc]
- Reardon DJ et al (2023) Search for an isotropic gravitational-wave background with the Parkes Pulsar Timing Array. *Astrophys J Lett* 951(1):L6. <https://doi.org/10.3847/2041-8213/acdd02>. [arXiv:2306.16215](https://arxiv.org/abs/2306.16215) [astro-ph.HE]
- Reece CE, Reiner PJ, Melissinos AC (1982) A detector for high frequency gravitational effects based on parametric conversion at 10 GHz. *eConf C8206282*:394–402
- Reece CE, Reiner PJ, Melissinos AC (1984) Observation of  $4 \times 10^{-17}$  cm harmonic displacement using a 10 ghz superconducting parametric converter. *Phys Lett* 104:341–344. [https://doi.org/10.1016/0375-9601\(84\)90811-9](https://doi.org/10.1016/0375-9601(84)90811-9)
- Reina-Valero J, Madrid JRN, Blas D, Morcillo AD, Irastorza IG, Gimeno B, Cabrera JM (2025) High-frequency gravitational waves detection with the BabyIAXO haloscopes. *Phys Rev D* 111:043024. <https://doi.org/10.1103/PhysRevD.111.043024>. [arXiv:2407.20482](https://arxiv.org/abs/2407.20482) [hep-ex]
- Reinhardt C, Masalehdan H, Croatto S, Franke A, Kunze MBK, Schaffran J, Sülthmann N, Lindner A, Schnabel R (2024) Self-calibrating gas pressure sensor with a 10-decade measurement range. *ACS Photonics* 11(4):1438–1446. <https://doi.org/10.1021/acsp Photonics.3c01488>. [arXiv:2309.12044](https://arxiv.org/abs/2309.12044) [physics.app-ph]
- Ricciardone A, Tasinato G (2017) Primordial gravitational waves in supersolid inflation. *Phys Rev D* 96:023508. <https://doi.org/10.1103/PhysRevD.96.023508>. [arXiv:1611.04516](https://arxiv.org/abs/1611.04516) [astro-ph.CO]
- Ricotti M, Ostriker JP, Mack KJ (2008) Effect of primordial black holes on the cosmic microwave background and cosmological parameter estimates. *Astrophys J* 680:829. <https://doi.org/10.1086/587831>. [arXiv:0709.0524](https://arxiv.org/abs/0709.0524) [astro-ph]
- Ringwald A, Tamarit C (2022) Revealing the cosmic history with gravitational waves. *Phys Rev D* 106(6):063027. <https://doi.org/10.1103/PhysRevD.106.063027>. [arXiv:2203.00621](https://arxiv.org/abs/2203.00621) [hep-ph]
- Ringwald A, Schütte-Engel J, Tamarit C (2021) Gravitational waves as a big bang thermometer. *JCAP* 2021(03):054. <https://doi.org/10.1088/1475-7516/2021/03/054>. [arXiv:2011.04731](https://arxiv.org/abs/2011.04731) [hep-ph]
- Rubakov VA, Shaposhnikov ME (1983) Do we live inside a domain wall? *Phys Lett B* 125:136–138. [https://doi.org/10.1016/0370-2693\(83\)91253-4](https://doi.org/10.1016/0370-2693(83)91253-4)



- Saffin PM, Tognarelli P, Tranberg A (2014) Oscillon lifetime in the presence of quantum fluctuations. *JHEP* 08:125. [https://doi.org/10.1007/JHEP08\(2014\)125](https://doi.org/10.1007/JHEP08(2014)125). arXiv:1401.6168 [hep-ph]
- Saito K, Soda J, Yoshino H (2021) Universal 1020 Hz stochastic gravitational waves from photon spheres of black holes. *Phys Rev D* 104(6):063040. <https://doi.org/10.1103/PhysRevD.104.063040>. arXiv:2106.05552 [gr-qc]
- Salemi CP et al (2021) Search for low-mass axion dark matter with ABRACADABRA-10 cm. *Phys Rev Lett* 127(8):081801. <https://doi.org/10.1103/PhysRevLett.127.081801>. arXiv:2102.06722 [hep-ex]
- Salmi P, Hindmarsh M (2012) Radiation and relaxation of oscillons. *Phys Rev D* 85:085033. <https://doi.org/10.1103/PhysRevD.85.085033>. arXiv:1201.1934 [hep-th]
- Sanchez-Garitaonandia M, van de Vis J (2024) Prediction of the bubble wall velocity for a large jump in degrees of freedom. *Phys Rev D* 110(2):023509. <https://doi.org/10.1103/PhysRevD.110.023509>. arXiv:2312.09964 [hep-ph]
- Sang Y, Huang QG (2019) Stochastic gravitational-wave background from axion-monodromy oscillons in string theory during preheating. *Phys Rev D* 100:063516. <https://doi.org/10.1103/PhysRevD.100.063516>. arXiv:1905.00371 [astro-ph.CO]
- Sarin N, Lasky PD (2021) The evolution of binary neutron star post-merger remnants: a review. *Gen Relativ Gravit* 53(6):59. <https://doi.org/10.1007/s10714-021-02831-1>. arXiv:2012.08172 [astro-ph.HE]
- Sasaki M, Suyama T, Tanaka T, Yokoyama S (2016) Primordial black hole scenario for the gravitational-wave event GW150914. *Phys Rev Lett* 117:061101. <https://doi.org/10.1103/PhysRevLett.117.061101>. erratum: *Phys Rev Lett* 121:059901 (2018). arXiv:1603.08338 [astro-ph.CO]
- Schnabel R, Korobko M (2025) Optical sensitivities of current gravitational wave observatories at higher kHz, MHz and GHz frequencies. *Sci Rep* 15(1):25733. <https://doi.org/10.1038/s41598-025-08668-x>. arXiv:2409.03019 [astro-ph.IM]
- Seahra SS, Clarkson C, Maartens R (2007) Detecting extra dimensions with gravity wave spectroscopy: the black string brane worlds. *Phys Rev Lett* 94:121302
- Segur H, Kruskal MD (1987) Nonexistence of small amplitude breather solutions in  $\phi^4$  theory. *Phys Rev Lett* 58:747–750. <https://doi.org/10.1103/PhysRevLett.58.747>
- Seidel E, Suen WM (1991) Oscillating soliton stars. *Phys Rev Lett* 66:1659–1662. <https://doi.org/10.1103/PhysRevLett.66.1659>
- Sendra I, Smith TL (2012) Improved limits on short-wavelength gravitational waves from the cosmic microwave background. *Phys Rev D* 85:123002. <https://doi.org/10.1103/PhysRevD.85.123002>. arXiv:1203.4232 [astro-ph.CO]
- Servin M, Brodin G (2003) Resonant interaction between gravitational waves, electromagnetic waves and plasma flows. *Phys Rev D* 68:044017. <https://doi.org/10.1103/PhysRevD.68.044017>. arXiv:gr-qc/0302039
- Seto N, Kawamura S, Nakamura T (2001) Possibility of direct measurement of the acceleration of the universe using 0.1-Hz band laser interferometer gravitational wave antenna in space. *Phys Rev Lett* 87:221103. <https://doi.org/10.1103/PhysRevLett.87.221103>. arXiv:astro-ph/0108011
- Shibagaki S, Kuroda T, Kotake K, Takiwaki T (2020) A new gravitational wave signature of low- $T/|W|$  instability in rapidly rotating stellar core collapse. *Mon Not R Astron Soc* 493(1):L138–L142. <https://doi.org/10.1093/mnras/llaa021>. arXiv:1909.09730 [astro-ph.HE]
- Shtanov Y, Traschen JH, Brandenberger RH (1995) Universe reheating after inflation. *Phys Rev D* 51:5438–5455. <https://doi.org/10.1103/PhysRevD.51.5438>. arXiv:hep-ph/9407247
- Smith TL, Pierpaoli E, Kamionkowski M (2006) A new cosmic microwave background constraint to primordial gravitational waves. *Phys Rev Lett* 97:021301. <https://doi.org/10.1103/PhysRevLett.97.021301>. arXiv:astro-ph/0603144 [astro-ph]
- Somiya K, Kataoka Y, Kato J, Saito N, Yano K (2016) Parametric signal amplification to create a stiff optical bar. *Phys Lett A* 380:521–524. <https://doi.org/10.1016/j.physleta.2015.11.010>. arXiv:1403.1222 [physics.optics]
- Soni S et al (2025) LIGO Detector Characterization in the first half of the fourth Observing run. *Class Quantum Grav* 42:085016. <https://doi.org/10.1088/1361-6382/adc4b6>. arXiv:2409.02831 [astro-ph.IM]
- Sorbo L (2011) Parity violation in the Cosmic Microwave Background from a pseudoscalar inflaton. *JCAP* 1106:003. <https://doi.org/10.1088/1475-7516/2011/06/003>. arXiv:1101.1525 [astro-ph.CO]

- Sprague JR et al (2024) Simulating the Galactic population of axion clouds around stellar-origin black holes: Gravitational wave signals in the 10–100 kHz band. *Phys Rev D* 110:123025. <https://doi.org/10.1103/PhysRevD.110.123025>. arXiv:2409.03714 [astro-ph.HE]
- Steinhardt PJ (1982) Relativistic detonation waves and bubble growth in false vacuum decay. *Phys Rev D* 25:2074. <https://doi.org/10.1103/PhysRevD.25.2074>
- Takami K, Rezzolla L, Baiotti L (2014) Constraining the equation of state of neutron stars from binary mergers. *Phys Rev Lett* 113(9):091104. <https://doi.org/10.1103/PhysRevLett.113.091104>. arXiv:1403.5672 [gr-qc]
- Takhistov V, Fuller GM, Kusenkov A (2021) Test for the origin of solar mass black holes. *Phys Rev Lett* 126(7):071101. <https://doi.org/10.1103/PhysRevLett.126.071101>. arXiv:2008.12780 [astro-ph.HE]
- Ternov IM, Khalilov VR, Chizhov GA, Gaina AB (1978) Finite movement of massive particles in Kerr and Schwarzschild fields. *Sov Phys J* 21:1200–1204. <https://doi.org/10.1007/BF00894575>. (Izv. Vuz. Fiz.21N9,109(1978))
- Teuscher M, Barrau A, Martineau K (2024) Elementary considerations on gravitational waves from hyperbolic encounters. *Gen Relativ Gravit* 56(8):89. <https://doi.org/10.1007/s10714-024-03276-y>. arXiv:2402.10706 [gr-qc]
- Thrane E, Romano JD (2013) Sensitivity curves for searches for gravitational-wave backgrounds. *Phys Rev D* 88:124032. <https://doi.org/10.1103/PhysRevD.88.124032>. arXiv:1310.5300 [astro-ph.IM]
- Tobar G, Manikandan SK, Beitel T, Pikovski I (2024) Detecting single gravitons with quantum sensing. *Nat Commun* 15(1):7229. <https://doi.org/10.1038/s41467-024-51420-8>. arXiv:2308.15440 [quant-ph]
- Tobar G, Pikovski I, Tobar ME (2025) Detecting kHz gravitons from a neutron star merger with a multi-mode resonant bar. *Class Quantum Grav* 42:055017. <https://doi.org/10.1088/1361-6382/adae4a>. arXiv:2406.16898 [astro-ph.IM]
- Tobar ME (1995) Characterizing multi-mode resonant-mass gravitational wave detectors. *J Phys D Appl Phys* 28(8):1729. <https://doi.org/10.1088/0022-3727/28/8/025>
- Tobar ME, Ivanov EN, Blair DG (2000) Parametric transducers for the advanced cryogenic resonant-mass gravitational wave detectors. *Gen Relativ Gravit* 32:1799–1821. <https://doi.org/10.1023/A:1001932614183>
- Tobar ME, Thomson CA, Campbell WM, Quiskamp A, Bourhill JF, McAllister BT, Ivanov EN, Goryachev M (2022) Comparing instrument spectral sensitivity of dissimilar electromagnetic haloscopes to axion dark matter and high frequency gravitational waves. *Symmetry* 14(10):2165. <https://doi.org/10.3390/sym14102165>. arXiv:2209.03004 [physics.ins-det]
- Tomita K (1975) Evolution of irregularities in a chaotic early universe. *Prog Theor Phys* 54:730. <https://doi.org/10.1143/PTP.54.730>
- Tootle S, Ecker C, Topolski K, Demircik T, Järvinen M, Rezzolla L (2022) Quark formation and phenomenology in binary neutron-star mergers using V-QCD. *SciPost Phys* 13:109. <https://doi.org/10.21468/SciPostPhys.13.5.109>. arXiv:2205.05691 [astro-ph.HE]
- Tranberg A, Tähtinen S, Weir DJ (2018) Gravitational waves from non-Abelian gauge fields at a tachyonic transition. *JCAP* 1804:012. <https://doi.org/10.1088/1475-7516/2018/04/012>. arXiv:1706.02365 [hep-ph]
- Traschen JH, Brandenberger RH (1990) Particle production during out-of-equilibrium phase transitions. *Phys Rev D* 42:2491–2504. <https://doi.org/10.1103/PhysRevD.42.2491>
- Tse M, Yu H, Kijbunchoo N, Fernandez-Galiana A, Dupej P, Barsotti L, Blair CD, Brown DD, Dwyer SE, Effler A et al (2019) Quantum-enhanced Advanced LIGO detectors in the era of gravitational-wave astronomy. *Phys Rev Lett* 123:231107. <https://doi.org/10.1103/PhysRevLett.123.231107>
- Turner M (1977) Gravitational radiation from point-masses in unbound orbits: Newtonian results. *ApJ* 216:610–619. <https://doi.org/10.1086/155501>
- Turner MS (1983) Coherent scalar field oscillations in an expanding universe. *Phys Rev D* 28:1243. <https://doi.org/10.1103/PhysRevD.28.1243>
- Turner MS, Weinberg EJ, Widrow LM (1992) Bubble nucleation in first order inflation and other cosmological phase transitions. *Phys Rev D* 46:2384–2403. <https://doi.org/10.1103/PhysRevD.46.2384>
- Turok N (1984) Grand unified strings and galaxy formation. *Nucl Phys B* 242:520–541. [https://doi.org/10.1016/0550-3213\(84\)90407-3](https://doi.org/10.1016/0550-3213(84)90407-3)

- Unal C (2019) Imprints of primordial non-Gaussianity on gravitational wave spectrum. *Phys Rev D* 99:041301. <https://doi.org/10.1103/PhysRevD.99.041301>. [arXiv:1811.09151](https://arxiv.org/abs/1811.09151) [astro-ph.CO]
- Urena-Lopez LA, Matos T, Becerril R (2002) Inside oscillatons. *Class Quantum Grav* 19:6259–6277. <https://doi.org/10.1088/0264-9381/19/23/320>
- Vacalis G, Marocco G, Bamber J, Bingham R, Gregori G (2023) Detection of high-frequency gravitational waves using high-energy pulsed lasers. *Class Quantum Grav* 40(15):155006. <https://doi.org/10.1088/1361-6382/acd517>. [arXiv:2301.08163](https://arxiv.org/abs/2301.08163) [gr-qc]
- Vachaspati T, Vilenkin A (1985) Gravitational Radiation from Cosmic Strings. *Phys Rev D* 31:3052. <https://doi.org/10.1103/PhysRevD.31.3052>
- Vadakkumbatt V, Hirschel M, Manley J, Clark TJ, Singh S, Davis JP (2021) Prototype superfluid gravitational wave detector. *Phys Rev D* 104(8):082001. <https://doi.org/10.1103/PhysRevD.104.082001>. [arXiv:2107.00120](https://arxiv.org/abs/2107.00120) [gr-qc]
- Vartanyan D, Burrows A, Wang T, Coleman MSB, White CJ (2023) Gravitational-wave signature of core-collapse supernovae. *Phys Rev D* 107(10):103015. <https://doi.org/10.1103/PhysRevD.107.103015>. [arXiv:2302.07092](https://arxiv.org/abs/2302.07092) [astro-ph.HE]
- Vermeulen SM, Aiello L, Ejlli A, Griffiths WL, James AL, Dooley KL, Grote H (2021) An experiment for observing quantum gravity phenomena using twin table-top 3D interferometers. *Class Quantum Grav* 38:085008. <https://doi.org/10.1088/1361-6382/abe757>. [arXiv:2008.04957](https://arxiv.org/abs/2008.04957) [gr-qc]
- Vilenkin A (1982) Cosmological evolution of monopoles connected by strings. *Nucl Phys B* 196:240–258. [https://doi.org/10.1016/0550-3213\(82\)90037-2](https://doi.org/10.1016/0550-3213(82)90037-2)
- Vilenkin A, Shellard EPS (2000) Cosmic strings and other topological defects. Cambridge University Press, Cambridge
- Vinante A (2006) Present performance and future upgrades of the AURIGA capacitive readout. *Class Quantum Grav* 23:S103–S110. <https://doi.org/10.1088/0264-9381/23/8/S14>
- Vincent G, Antunes ND, Hindmarsh M (1998) Numerical simulations of string networks in the Abelian Higgs model. *Phys Rev Lett* 80:2277–2280. <https://doi.org/10.1103/PhysRevLett.80.2277>. [arXiv:hep-ph/9708427](https://arxiv.org/abs/hep-ph/9708427) [hep-ph]
- Wagoner RV, Paik HJ (1977) Multimode detection of gravitational waves by a sphere. In: *Experimental gravitation*. Accademia Nazionale dei Lincei Rome, pp 257–265
- Weber J (1960) Detection and generation of gravitational waves. *Phys Rev* 117:306–313. <https://doi.org/10.1103/PhysRev.117.306>
- Weinberg S (1972) *Gravitation and cosmology: principles and applications of the general theory of relativity*. Wiley, New York
- Wen H, Li FY, Li J, Fang ZY, Beckwith A (2017) Very high-frequency gravitational waves from magnetars and gamma-ray bursts. *Chin Phys C* 41:125101. <https://doi.org/10.1088/1674-1137/41/12/125101>. [arXiv:1608.03186](https://arxiv.org/abs/1608.03186) [physics.gen-ph]
- Winstone G, Bhattacharya M, Geraci AA, Li T, Pauzauskie PJ, Vamivakas N (2023) Levitated optomechanics: a tutorial and perspective. *arXiv e-prints* [arXiv:2307.11858](https://arxiv.org/abs/2307.11858) [quant-ph]
- Winstone G et al (2022) Optical trapping of high-aspect-ratio NaYF hexagonal prisms for kHz-MHz gravitational wave detectors. *Phys Rev Lett* 129(5):053604. <https://doi.org/10.1103/PhysRevLett.129.053604>. [arXiv:2204.10843](https://arxiv.org/abs/2204.10843) [physics.optics]
- Wiseman AG, Will CM (1991) Christodoulou's nonlinear gravitational-wave memory: evaluation in the quadrupole approximation. *Phys Rev D* 44:R2945–R2949. <https://doi.org/10.1103/PhysRevD.44.R2945>
- Witten E (1984) Cosmic separation of phases. *Phys Rev D* 30:272–285. <https://doi.org/10.1103/physrevd.30.272>
- Woods RC (2012) Diffraction from embedded reflectors in Li-Baker HFGW detector. *Phys Procedia* 38:66–76. <https://doi.org/10.1016/j.phpro.2012.08.012>
- Xu H et al (2023) Searching for the nano-Hertz stochastic gravitational wave background with the chinese pulsar timing array data release I. *Res Astron Astrophys* 23(7):075024. <https://doi.org/10.1088/1674-4527/acdfa5>. [arXiv:2306.16216](https://arxiv.org/abs/2306.16216) [astro-ph.HE]
- Yeh TH, Shelton J, Olive KA, Fields BD (2022) Probing physics beyond the standard model: limits from BBN and the CMB independently and combined. *JCAP* 10:046. <https://doi.org/10.1088/1475-7516/2022/10/046>. [arXiv:2207.13133](https://arxiv.org/abs/2207.13133) [astro-ph.CO]

- Yoshino H, Kodama H (2014) Gravitational radiation from an axion cloud around a black hole: Superradiant phase. PTEP 2014:043E02. <https://doi.org/10.1093/ptep/ptu029>. arXiv:1312.2326 [gr-qc]
- Zel'dovich YB, Polnarev AG (1974) Radiation of gravitational waves by a cluster of superdense stars. Sov Astron 18:17
- Zha S, O'Connor EP, Mc C, Lin LM, Couch SM (2020) Gravitational-wave signature of a first-order quantum chromodynamics phase transition in core-collapse supernovae. Phys Rev Lett 125(5):051102. <https://doi.org/10.1103/PhysRevLett.127.219901>. [Erratum: Phys. Rev. Lett. 127, 219901 (2021)]. arXiv:2007.04716 [astro-ph.HE]
- Zhang HY, Amin MA, Copeland EJ, Saffin PM, Lozanov KD (2020) Classical decay rates of oscillons. JCAP 07:055. <https://doi.org/10.1088/1475-7516/2020/07/055>. arXiv:2004.01202 [hep-th]
- Zhang Z, Horns D, Ghosh O (2022) Search for dark matter with an LC circuit. Phys Rev D 106(2):023003. <https://doi.org/10.1103/PhysRevD.106.023003>. arXiv:2111.04541 [hep-ex]
- Zhao ZC, Liu X, Cao Z, He X (2021) Gravitational wave memory of the binary black hole events in GWTC-2. Phys Rev D 104(6):064056. <https://doi.org/10.1103/PhysRevD.104.064056>. arXiv:2111.13882 [gr-qc]
- Zheng X, Dolde J, Lochab V, Merriman BN, Li H, Kolkowitz S (2022) High precision differential clock comparisons with a multiplexed optical lattice clock. Nature 602:425–430. <https://doi.org/10.1038/s41586-021-04344-y>. arXiv:2109.12237 [physics.atom-ph]
- Zhong L et al (2018) Results from phase 1 of the HAYSTAC microwave cavity axion experiment. Phys Rev D 97(9):092001. <https://doi.org/10.1103/PhysRevD.97.092001>. arXiv:1803.03690 [hep-ex]
- Zhou SY, Copeland EJ, Easther R, Finkel H, Mou ZG, Saffin PM (2013) Gravitational waves from oscillon preheating. JHEP 10:026. [https://doi.org/10.1007/JHEP10\(2013\)026](https://doi.org/10.1007/JHEP10(2013)026). arXiv:1304.6094 [astro-ph.CO]
- Zhu XJ, Howell E, Regimbau T, Blair D, Zhu ZH (2011) Stochastic gravitational wave background from coalescing binary black holes. Astrophys J 739:86. <https://doi.org/10.1088/0004-637X/739/2/86>. arXiv:1104.3565 [gr-qc]
- Zouros TJM, Eardley DM (1979) Instabilities of massive scalar perturbations of a rotating black hole. Ann Phys 118:139–155. [https://doi.org/10.1016/0003-4916\(79\)90237-9](https://doi.org/10.1016/0003-4916(79)90237-9)

**Publisher's Note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

## Authors and Affiliations

Nancy Aggarwal<sup>1</sup> · Odylio D. Aguiar<sup>2</sup> · Diego Blas<sup>3,4</sup> · Andreas Bauswein<sup>5</sup> · Giancarlo Cella<sup>6</sup> · Sebastian Clesse<sup>7</sup> · Adrian Michael Cruise<sup>8</sup> · Valerie Domcke<sup>9</sup>  · Sebastian Ellis<sup>10</sup> · Daniel G. Figueroa<sup>11</sup> · Gabriele Franciolini<sup>9</sup> · Camilo García-Cely<sup>11</sup> · Andrew Geraci<sup>1</sup> · Maxim Goryachev<sup>12</sup> · Hartmut Grote<sup>13</sup> · Mark Hindmarsh<sup>14,15</sup> · Asuka Ito<sup>16,17</sup> · Joachim Kopp<sup>9,18</sup> · Sung Mook Lee<sup>9</sup> · Killian Martineau<sup>19</sup> · Jamie McDonald<sup>20</sup> · Francesco Muia<sup>21</sup> · Nikhil Mukund<sup>22</sup> · David Ottaway<sup>23</sup> · Marco Peloso<sup>24,25</sup> · Krisztian Peters<sup>26</sup> · Fernando Quevedo<sup>21,27</sup> · Angelo Ricciardone<sup>6,28</sup> · Andreas Ringwald<sup>26</sup> · Jessica Steinlechner<sup>29,30,31</sup> · Sebastian Steinlechner<sup>29,30</sup> · Sichun Sun<sup>32</sup> · Carlos Tamarit<sup>18</sup> · Michael E. Tobar<sup>12</sup> · Francisco Torrenti<sup>33</sup> · Caner Ünal<sup>34,35</sup> · Graham White<sup>36</sup>

- ✉ Valerie Domcke  
valerie.domcke@cern.ch
- ✉ Sebastian Ellis  
Sebastian.Ellis@unige.ch
- ✉ Gabriele Franciolini  
gabriele.franciolini@cern.ch
- ✉ Joachim Kopp  
jkopp@uni-mainz.de
- ✉ Sung Mook Lee  
sungmook.lee@cern.ch

- <sup>1</sup> Department of Physics and Astronomy, Northwestern University, Evanston, IL, USA
- <sup>2</sup> Instituto Nacional de Pesquisas Espaciais (INPE), São José dos Campos, São Paulo, Brazil
- <sup>3</sup> IFAE, The Barcelona Institute of Science and Technology, Bellaterra, Barcelona, Spain
- <sup>4</sup> Institució Catalana de Recerca i Estudis Avançats (ICREA), Barcelona, Spain
- <sup>5</sup> GSI Helmholtzzentrum für Schwerionenforschung, Darmstadt, Germany
- <sup>6</sup> Istituto Nazionale di Fisica Nucleare, Sezione di Pisa, Pisa, Italy
- <sup>7</sup> Service de Physique Théorique, Université Libre de Bruxelles, Brussels, Belgium
- <sup>8</sup> School of Physics and Astronomy, University of Birmingham, Edgbaston, Birmingham, UK
- <sup>9</sup> Theoretical Physics Department, CERN, Geneva, Switzerland
- <sup>10</sup> Département de Physique Théorique, Université de Genève, Geneva, Switzerland
- <sup>11</sup> Instituto de Física Corpuscular (IFIC), CSIC-Universitat de València, Valencia, Spain
- <sup>12</sup> Department of Physics, University of Western Australia, Crawley, WA, Australia
- <sup>13</sup> Cardiff University, Cardiff, UK
- <sup>14</sup> Department of Physics and Helsinki Institute of Physics, University of Helsinki, Helsinki, Finland
- <sup>15</sup> Department of Physics and Astronomy, University of Sussex, Brighton, UK
- <sup>16</sup> Department of Physics, Kobe University, Kobe, Japan
- <sup>17</sup> QUP, KEK, Tsukuba, Japan
- <sup>18</sup> PRISMA+ Cluster of Excellence, Johannes Gutenberg University, Mainz, Germany
- <sup>19</sup> LPSC, Université Grenoble-Alpes, CNRS-IN2P3, Grenoble, France
- <sup>20</sup> Department of Physics and Astronomy, University of Manchester, Manchester, UK
- <sup>21</sup> DAMTP, Centre for Mathematical Sciences, Cambridge, UK
- <sup>22</sup> Massachusetts Institute of Technology, Cambridge, MA, USA
- <sup>23</sup> ARC Centre of Excellence OzGrav, The University of Adelaide, Adelaide, Australia
- <sup>24</sup> Dipartimento di Fisica e Astronomia ‘Galileo Galilei’ Università di Padova, Padua, Italy
- <sup>25</sup> INFN, Sezione di Padova, Padua, Italy
- <sup>26</sup> Deutsches Elektronen-Synchrotron DESY, Hamburg, Germany
- <sup>27</sup> New York University, Abu Dhabi, United Arab Emirates
- <sup>28</sup> Dipartimento di Fisica ‘Enrico Fermi’, Università di Pisa, Pisa, Italy
- <sup>29</sup> Maastricht University, Maastricht, The Netherlands

- <sup>30</sup> Nikhef, Amsterdam, The Netherlands
- <sup>31</sup> SUPA, School of Physics and Astronomy, University of Glasgow, Glasgow, Scotland, UK
- <sup>32</sup> School of Physics, Beijing Institute of Technology, Beijing, People's Republic of China
- <sup>33</sup> Departament de Física Quàntica i Astrofísica & ICCUB, Universitat de Barcelona, Barcelona, Spain
- <sup>34</sup> CEICO, Institute of Physics of the Czech Academy of Sciences, Prague, Czechia
- <sup>35</sup> Department of Physics, Ben-Gurion University of the Negev, Be'er Sheva, Israel
- <sup>36</sup> School of Physics and Astronomy, University of Southampton, Southampton, UK