## Neural-Network Extraction of Unpolarized Transverse-Momentum-Dependent **Distributions**

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We present the first extraction of transverse-momentum-dependent distributions of unpolarized quarks from experimental Drell-Yan data using neural networks to parametrize their nonperturbative part. We show that neural networks outperform traditional parametrizations providing a more accurate description of data. This Letter establishes the feasibility of using neural networks to explore the multidimensional partonic structure of hadrons and paves the way for more accurate determinations based on machinelearning techniques.

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Introduction—Transverse-momentum-dependent (TMD) distributions provide an important window to investigate the partonic structure of hadrons, enabling a deeper understanding of the three-dimensional dynamics of quarks and gluons within them. TMDs consist of both perturbative and nonperturbative components. While the perturbative part can be calculated from first principles using quantum chromodynamics (QCD), the nonperturbative part, which encapsulates long-distance physics, by definition cannot be evaluated using perturbative methods and must be extracted from experimental data. An accurate parametrization of the

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nonperturbative contribution to TMDs is therefore essential for reliable extractions. The abundance of experimental measurements and the development of a robust theoretical framework have favored a remarkable progress of TMD studies in recent years. Indeed, accurate phenomenological extractions for unpolarized quark TMDs in the proton are now available [1–9].

Despite this active research landscape, explorations of different parametrizations of the TMD nonperturbative part were limited to models based on a small set of functions, such as exponentials and (weighted) Gaussians. While these parametrizations are effective, they carry a significant bias that may limit the accuracy of the models. This rigidity can hinder the ability to fully capture the underlying physics and extract information from experimental data. To overcome these limitations, a promising alternative is given by neural networks (NNs).

In this Letter, we present the first extraction of the unpolarized quark TMD parton distribution functions (PDFs) in the proton using NNs to parametrize their nonperturbative component, achieving next-to-next-tonext-to-leading logarithmic (N<sup>3</sup>LL) accuracy. This constitutes a proof-of-concept extraction, as it is based on Drell-Yan (DY) production data only and neglects flavor dependence of the intrinsic transverse momentum of

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quarks. Nevertheless, it demonstrates that NN-based TMD extractions outperform traditional nonperturbative parametrizations. Indeed, we provide evidence that current experimental data encode complexities beyond the reach of traditional parametrizations. We remark that NNs have been used in the past to study other partonic distributions (see, e.g., Refs. [10–14]), but never unpolarized TMDs. Our Letter paves the way for improved TMD extractions, leveraging the flexibility of NNs to extract information on the multidimensional structure of hadrons using data from current and future experiments.

Formalism and parametrization—We consider the DY process  $h_A + h_B \rightarrow \ell^+ + \ell^- + X$ , where two hadrons with mass M and four-momenta  $P_A$  and  $P_B$  collide with center-of-mass energy squared  $s = (P_A + P_B)^2$ , and inclusively produce a lepton pair with total four-momentum q and invariant mass  $Q \gg M$ . If the transverse momentum component  $q_T$  with respect to the collision axis satisfies the condition  $|q_T| \equiv q_T \ll Q$ , the differential cross section can be written as

$$\begin{split} \frac{d\sigma^{\mathrm{DY}}}{dq_T dy dQ} &= \frac{8\pi\alpha^2 q_T}{9Q^3} \mathcal{P} x_A x_B \mathcal{H}^{\mathrm{DY}}(Q, \mu) \sum_a c_a(Q^2) \\ &\times \int_0^\infty db_T b_T J_0(b_T q_T) \hat{f}_1^a(x_A, b_T^2; \mu, \zeta_A) \\ &\times \hat{f}_1^{\bar{a}}(x_B, b_T^2; \mu, \zeta_B), \end{split} \tag{1}$$

where  $y = \ln \sqrt{(q_0 + q_z)/(q_0 - q_z)}$  is the lepton-pair rapidity,  $\alpha$  is the electromagnetic coupling,  $\mathcal{P}$  is a phase-space-reduction factor accounting for possible lepton cuts (see Appendix C of Ref. [5] for details),  $x_{A,B} = Qe^{\pm y}/\sqrt{s}$  are the longitudinal momentum fractions carried by the incoming quarks,  $\mathcal{H}^{\mathrm{DY}}$  is a perturbative hard factor encoding the virtual part of the scattering, and the sum runs over all active quark flavors a with  $c_a$  the quark electroweak charges.

In Eq. (1),  $\hat{f}_1^a$  is the Fourier transform of the unpolarized TMD PDF of quark flavor a. It depends on the quark longitudinal momentum fraction x and on the variable  $b_T = |\boldsymbol{b}_T|$ , where  $\boldsymbol{b}_T$  is Fourier-conjugated to the quark intrinsic transverse momentum  $\boldsymbol{k}_\perp$ . It also depends on the renormalization scale  $\mu$  and on the rapidity scale  $\zeta$  (with the constraint  $\zeta_A \zeta_B = Q^4$ ). Such dependence arises from the removal of ultraviolet and rapidity divergences [15] and is controlled by corresponding evolution equations. The complete set of equations (omitting unessential variables and indices) is given by

$$\frac{\partial \hat{f}_{1}}{\partial \ln \mu} = \gamma(\mu, \zeta), \frac{\partial \hat{f}_{1}}{\partial \ln \sqrt{\zeta}} = K(\mu), 
\frac{\partial K}{\partial \ln \mu} = \frac{\partial \gamma}{\partial \ln \sqrt{\zeta}} = -\gamma_{K}(\alpha_{s}(\mu)), \tag{2}$$

where  $\gamma$  and K are the anomalous dimensions of renormalization group and of Collins–Soper equations, respectively, and  $\gamma_K$  is the so-called cusp anomalous dimension which relates the cross derivatives of  $\hat{f}_1$ .

Given a set of initial scales  $(\mu_i, \zeta_i)$ , the solution to these differential equations allows us to determine the  $\hat{f}_1$  at any final scales  $(\mu_f, \zeta_f)$ . In addition, in the region of small transverse separations  $b_T$ , the TMD PDF  $\hat{f}_1$  can be matched onto unpolarized *collinear* PDFs  $f_1$  through a convolution with perturbatively calculable matching coefficients C.

The resulting expression for the TMD PDF at the final scales  $(\mu_f, \zeta_f)$  is

$$\begin{split} \hat{f}_{1}(x, b_{T}; \mu_{f}, \zeta_{f}) \\ &= [C \otimes f_{1}](x, b_{T}; \mu_{i}, \zeta_{i}) \exp \left\{ K(\mu_{i}) \ln \frac{\sqrt{\zeta_{f}}}{\sqrt{\zeta_{i}}} \right. \\ &\left. + \int_{\mu_{i}}^{\mu_{f}} \frac{d\mu}{\mu} \left[ \gamma_{F}(\alpha_{s}(\mu)) - \gamma_{K}(\alpha_{s}(\mu)) \ln \frac{\sqrt{\zeta_{f}}}{\mu} \right] \right\}, \quad (3) \end{split}$$

where  $\gamma_F(\alpha_s(\mu)) = \gamma(\mu, \mu^2)$  and  $\otimes$  indicates the Mellin convolution over the longitudinal momentum fraction x. A convenient choice for the initial scales is  $\mu_i = \sqrt{\zeta_i} \equiv \mu_b = 2e^{-\gamma_E}/b_T$ , with  $\gamma_E$  the Euler constant, in that it avoids the insurgence of large logarithms in the anomalous dimension K and in the matching coefficients C.

The TMD PDF in Eq. (3) includes the resummation of large logarithms of  $b_T$  to all orders in perturbation theory. A given logarithmic accuracy implies that each ingredient in Eq. (3) must be computed to the appropriate perturbative accuracy. The present extraction incorporates all the necessary ingredients to reach N<sup>3</sup>LL accuracy [3].

The introduction of the scale  $\mu_b \sim 1/b_T$  requires a prescription to avoid integrating in Eq. (1) over the QCD Landau pole ( $\Lambda_{\rm QCD}$ ) in the large- $b_T$  region. To this purpose, we adopt the same choice of Refs. [1,5,7,9,16] and replace  $\mu_b$  with  $\mu_{b_*} = 2e^{-\gamma_E}/b_*$ , where

$$b_*(b_T, b_{\min}, b_{\max}) = b_{\max} \left( \frac{1 - e^{-b_T^4/b_{\max}^4}}{1 - e^{-b_T^4/b_{\min}^4}} \right)^{1/4},$$
 (4)

with

$$b_{\rm max} = 2e^{-\gamma_{\rm E}}{\rm GeV^{-1}} b_{\rm min} = 2e^{-\gamma_{\rm E}}/\mu_f.$$
 (5)

This choice guarantees that the variable  $b_*$  rapidly saturates to  $b_{\rm max}$  at large values of  $b_T$ , preventing  $\mu_{b_*}$  from reaching  $\Lambda_{\rm QCD}$ . However,  $b_*$  also introduces spurious power corrections that scale like  $(\Lambda_{\rm QCD}/q_T)^k$  [17–20], with k>0. In the region  $q_T\simeq\Lambda_{\rm QCD}$ , these power corrections become sizeable and can be modeled by including in Eq. (3) the nonperturbative function  $f_{\rm NP}$  as follows:

$$\begin{split} \hat{f}_{1}(x, b_{T}; \mu_{f}, \zeta_{f}) \\ &= [C \otimes f_{1}] \left( x, b_{T}; \mu_{b_{*}}, \mu_{b_{*}}^{2} \right) \exp \left\{ K(b_{*}, \mu_{b_{*}}) \ln \frac{\sqrt{\zeta_{f}}}{\mu_{b_{*}}} \right. \\ &+ \int_{\mu_{b_{*}}}^{\mu_{f}} \frac{d\mu}{\mu} \left[ \gamma_{F} \left( \alpha_{s}(\mu) \right) - \gamma_{K} \left( \alpha_{s}(\mu) \right) \ln \frac{\sqrt{\zeta_{f}}}{\mu} \right] \right\} \\ &\times f_{\text{NP}}(x, b_{T}; \zeta_{f}). \end{split} \tag{6}$$

The nonperturbative function must satisfy the condition  $f_{\rm NP} \to 1$  for  $b_T \to 0$  in order to recover the perturbative regime. It must also grant that the TMD PDF is suppressed for large values of  $b_T$  and  $\zeta_f$ . We parametrize  $f_{\rm NP}$  using a NN but enforcing these physically required constraints. We explored several different NN parametrizations and will report on them in a future work. As a proof of concept, in this Letter we focus on the following model:

$$f_{\rm NP}(x, b_T; \zeta) = \frac{\mathbb{NN}(x, b_T)}{\mathbb{NN}(x, o)} \exp\left[-g_2^2 b_T^2 \log\left(\frac{\zeta}{Q_0^2}\right)\right], \quad (7)$$

where, as customary, we split  $f_{\rm NP}$  into an "intrinsic" non-perturbative part, entirely parametrized by the NN (denoted as NN), and the nonperturbative contribution to the rapidity evolution, encoded in the exponential function. The NN is taken with architecture [2, 10, 1], i.e., with two inputs corresponding to x and  $b_T$ , 10 hidden nodes, and one output node. The activation function associated to the nodes of the hidden layer is

$$\sigma(z) = \frac{1}{2} \left( 1 + \frac{z}{1 + |z|} \right),\tag{8}$$

which resembles the more traditional sigmoid function but offers a significant reduction of computational burden while granting an excellent quality of the final result. The activation function for the outer layer is instead chosen to be quadratic. The reference scale for the rapidity evolution is set to  $Q_0=1$  GeV. The parametrization of the function  $f_{\rm NP}$  in Eq. (7) is engineered to match the constraints mentioned above, namely,  $f_{\rm NP} \to 1$  for  $b_T \to 0$  and  $f_{\rm NP} \ll 1$  for large  $b_T$  and  $\zeta_f$ . With this setup, we have a total of 42 free parameters, 41 associated to the NN and one  $(g_2)$  to the evolution.

The values of the best-fit parameters are obtained by minimizing a  $\chi^2$  that accounts for all sources of experimental uncertainties. The minimization is performed using the Levenberg–Marquardt algorithm as implemented in the Ceres-Solver package [21]. An important aspect of our analysis is that the gradient of the  $\chi^2$  with respect to the free parameters is evaluated *analytically* by exploiting the ability to compute the derivatives of the NN with respect to its parameters in a closed form [22]. This feature is crucial to ensure a fast and stable convergence of the minimization procedure.

Finally, overfitting is a well-known problem of phenomenological analyses based on NNs [23,24]. We avoid it by using the cross-validation method [25]. Specifically, the data set is split into two subsets: one for training and one for validation. The training set is used to determine the best-fit parameters, while the validation set is used to monitor the quality of the fit. The best-fit set of parameters is determined by requiring the  $\chi^2$  of the validation set to be minimal. In our analysis, we divided the data set into validation and training sets of the same size.

Results—In this section, we discuss the results for the fit of  $f_{\rm NP}$  in Eq. (7) to the DY experimental data included in the most recent analyses of the MAP Collaboration (see Refs. [7,9] for more details). We consider fixed-target data from Fermilab (E605 [26], E288 [27], and E772 [28]) and collider data from Tevatron (CDF [29,30], D0 [31–33]), RHIC (STAR [34]) and the LHC (LHCb [35–37], CMS [38–40], ATLAS [41–43]).

The collinear PDFs  $f_1$  in Eq. (6) are taken from the MSHT2020 set [44] of the LHAPDF library [45] at next-to-next-to-leading order, which is necessary to achieve N<sup>3</sup>LL. The strong coupling  $\alpha_s$  is obtained from the same PDF set. We propagate the uncertainties of collinear PDFs into TMD PDFs as in Refs. [7,16]. In order to ensure applicability of TMD factorization, we impose the kinematic cut  $q_T/Q < 0.2$ . We exclude all experimental data in the energy range of the  $\Upsilon$  resonance (9 GeV < Q < 11 GeV). Moreover, we neglect the PHENIX data of Ref. [46], originally included in the analyses of Refs. [7,9], because only two data points survive the  $q_T/Q$  cut and their description is typically poor for any parametrization of  $f_{NP}$ .

The propagation of the experimental uncertainties into the TMD PDFs is achieved through Monte Carlo (MC) sampling: an ensemble of  $N_{\rm rep}=250$  fluctuations (replicas) of the experimental data set is generated accounting for correlated uncertainties, and each replica is used to extract  $f_{\rm NP}$ .

In order to estimate the performance of our NN-based fit, we performed an additional fit with the same settings (data set, perturbative order, etc.) but parametrizing  $f_{\rm NP}$  with the functional form used in Ref. [7], which features 12 free parameters. In Table I, we compare the quality of the NN-based fit with this latter fit referred to as MAP22 (see Ref. [47] for the full results). For each data subset (fixed-target, RHIC, Tevatron, ATLAS, CMS, and LHCb) we list the number of points included in the fit ( $N_{\rm dat}$ ) and the reduced  $\bar{\chi}^2$  (=  $\chi^2/N_{\rm dat}$ ) of the central replica, i.e., the fit to the experimental central values without MC fluctuations. The total  $\bar{\chi}^2$  is given in the bottom line. For each  $\bar{\chi}^2$  value, we also provide separately uncorrelated ( $\bar{\chi}_D^2$ ) and correlated ( $\bar{\chi}_D^2$ ) contributions (see Appendix B of Ref. [3] for more details).

It is evident that the NN fit achieves a better description of data than MAP22, not only at the level of the global  $\bar{\chi}^2$  (0.97 for NN vs 1.28 for MAP22), but also for almost all

TABLE I. Breakdown of the reduced  $\bar{\chi}^2 = \chi^2/N_{\rm dat}$  for each subset included in the fit and for the total data set. Results obtained with the parametrization in Eq. (7) (NN) and that of Ref. [7] (MAP22) are shown.  $\bar{\chi}_D^2$  and  $\bar{\chi}_\lambda^2$  correspond to uncorrelated and correlated contributions to  $\bar{\chi}^2$ , respectively [3].

		$ar{\chi}^2(ar{\chi}_D^2+ar{\chi}_\lambda^2)$	
Experiment	$N_{\rm dat}$	NN	MAP22
Fixed-target	233	1.08(0.98 + 0.10)	0.91(0.70 + 0.21)
RHIC	7	1.11(1.03 + 0.07)	1.45(1.37 + 0.08)
Tevatron	71	0.80(0.73 + 0.06)	1.20(1.17 + 0.04)
LHCb	21	0.98(0.88 + 0.10)	1.25(1.05 + 0.20)
CMS	78	0.40(0.38 + 0.02)	0.41(0.35 + 0.06)
ATLAS	72	1.38(1.09 + 0.29)	3.51(3.03 + 0.49)
Total	482	0.97(0.86 + 0.11)	1.28(1.09 + 0.20)

single subsets, with the only exception being fixed target. Indeed, the NN  $\bar{\chi}^2$  for this data set, despite still acceptable, is larger than the MAP22 one. This result can be ascribed to a possible tension between fixed-target and ATLAS data. In fact, when excluding the ATLAS data from the fit, we find that the quality of the NN fit is better than the MAP22 fit for *all* subsets, including the fixed-target ones [48].

Particularly significant is the improvement for ATLAS, for which the  $\bar{\chi}^2$  value drops from 3.51 for MAP22 to 1.38 for NN. As the ATLAS measurements are the most precise ones, this is a clear indication that the NN parametrization can better capture the information encoded in the data. We also note that the correlated contributions  $\bar{\chi}_{\lambda}^2$  for the NN fit are generally smaller than for MAP22, i.e., the NN fit is able to describe the data without relying on large correlated shifts.

A visual representation of this statement is given in Fig. 1, where we show a comparison between experimental data and results of the fit for a representative selection of data: a Q bin from the fixed-target E605 experiment (top plot) and the ATLAS measurements at 13 TeV (bottom plot). Blue and red bands correspond to one- $\sigma$  uncertainties of NN and MAP22 fits, respectively, while experimental data points are shown as black dots along with their uncorrelated uncertainties. The upper panel of each plot displays the absolute distributions while the lower panel displays the distributions normalized to the experimental central values. In order to facilitate visual comparison, systematic shifts were applied to predictions.

In Fig. 1, it is evident that uncertainty bands are significantly different between NN and MAP22 fits, with the former being generally smaller than the latter. This is a direct consequence of the larger systematic shifts that affect MAP22 (see Table I). This is especially evident for the E605 data where correlated uncertainties are particularly large. For the ATLAS data, the size of the bands is comparable because systematic shifts are bound to be small due to the small size of experimental uncertainties. We also

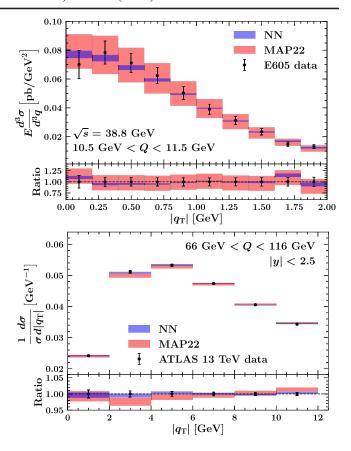


FIG. 1. Comparison between experimental data (black dots) and results obtained with NN (blue band) and MAP22 (red band) fits. The top plot displays the 10.5 GeV < Q < 11.5 GeV bin of the E605 data set, while the bottom plot displays the ATLAS measurements at 13 TeV. For each plot, upper and lower panels show the actual distributions and their ratios to the experimental central values, respectively. Theoretical uncertainty bands correspond to one- $\sigma$  uncertainties; error bars on experimental data display uncorrelated uncertainties only. Predictions include systematic shifts.

observe that the NN fit tends to better reproduce the shape of the ATLAS data distribution.

In Fig. 2, we show the unpolarized TMD PDF of the u quark in the proton at  $\mu=\sqrt{\zeta}=2$  GeV and x=0.01 as a function of the quark transverse momentum  $|{\pmb k}_\perp|$ . As before, blue and red bands correspond to NN and MAP22, respectively. The upper panel displays the actual TMD distributions, while in the lower panel they are normalized to the respective central values.

A generally good agreement between NN and MAP22 is observed, with the former featuring a larger relative uncertainty band. This is a direct consequence of the flexibility of the NN parametrization. In this respect, it is interesting to observe that the relative size of the NN uncertainty band remains fairly stable up to  $|{\bf k}_\perp| \sim 0.6$  GeV, while it tends to increase for larger values of  $|{\bf k}_\perp|$  because of the increasingly smaller central value. On the contrary, the MAP22 relative uncertainty band shrinks as  $|{\bf k}_\perp|$ 

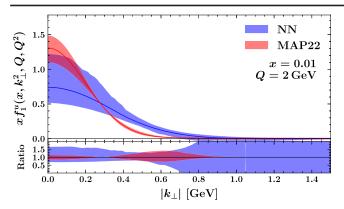


FIG. 2. The unpolarized TMD PDF of the u quark in the proton extracted using the NN (blue) and the MAP22 (red) parametrizations at  $\mu=\sqrt{\zeta}=2$  GeV and x=0.01 as functions of the quark transverse momentum  $|{\pmb k}_\perp|$ . The upper panel shows the actual distributions, while the bottom panel shows their ratios to the respective central values. Error bands represent one- $\sigma$  uncertainties.

increases. Moreover, it shows a node at intermediate values of  $|\mathbf{k}_{\perp}|$ . This behavior can be traced back to the rigidity of the parametrization.

The fact that the NN TMD PDF has larger uncertainties than the MAP22 one may seem to contrast with the results shown in Fig. 1, where cross sections computed with the NN model display smaller uncertainties than MAP22. This can be understood by noting that during the minimization process the greater flexibility of the NN model enables it to better adapt to the behavior of data. Consequently, the minimizer does not need to resort to large correlated shifts to minimize the  $\chi^2$ , avoiding an inflation of the uncertainty in the final outcome.

We conclude this section by noting that we have conducted preliminary closure tests [49], which, albeit not exhaustive, provide promising evidence supporting the robustness of our methodology [48]. We plan to produce a comprehensive documentation of closure testing results in a future publication.

Conclusions—In this Letter, we presented the first extraction of the unpolarized quark TMD PDFs in the proton from a comprehensive set of DY data using a parametrization for the nonperturbative part based on an NN. Our results employ state-of-the-art perturbative inputs reaching N<sup>3</sup>LL accuracy, and leverage modern numerical techniques, such as MC sampling for uncertainty propagation, analytic computation of the gradient of the  $\chi^2$  for a more accurate exploration of the parameter space, cross validation to avoid overfitting, and full treatment of correlated experimental uncertainties.

A key strength of the NN parametrization is its flexibility, which can accommodate tensions between data sets more effectively than simpler parametrizations, and allows for a more faithful statistical description of uncertainties. These advantages are reflected in our findings: we show

that the NN parametrization achieves better fit quality compared to the traditional functional form of Ref. [7], particularly for the ATLAS measurements, the most precise data sets included in the fit. We further showed that the NN approach improves control over correlated uncertainties. For data sets with large correlated systematics, such as the fixed-target measurements, this typically results in a significant reduction in uncertainties.

This Letter serves as a proof of concept, opening new and exciting possibilities for future high-precision and high-impact extractions. One of the main advantages of NNs is that they scale particularly well with the complexity of the task. More specifically, extending the data set to include semi-inclusive deep-inelastic scattering data (which in turn requires a simultaneous fit of TMD PDFs and TMD fragmentation functions) and introducing TMD flavor dependence is a relatively straightforward task when using NNs. We are currently working along these directions and plan to release a fully fledged TMD extraction based on NNs in the near future.

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Data availability—The data that support the findings of this Letter are openly available [47].

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