



Constraints on the Intergalactic Magnetic Field Using Fermi-LAT and H.E.S.S. Blazar Observations

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Abstract

Magnetic fields in galaxies and galaxy clusters are believed to be the result of the amplification of intergalactic seed fields during the formation of large-scale structures in the universe. However, the origin, strength, and morphology of this intergalactic magnetic field (IGMF) remain unknown. Lower limits on (or indirect detection of) the IGMF can be obtained from observations of high-energy gamma rays from distant blazars. Gamma rays interact with the extragalactic background light to produce electron–positron pairs, which can subsequently initiate electromagnetic cascades. The gamma-ray signature of the cascade depends on the IGMF since it deflects the pairs. Here we report on a new search for this cascade emission using a combined data set from the Fermi Large Area Telescope and the High Energy Stereoscopic System. Using state-of-the-art Monte Carlo predictions for the cascade signal, our results place a lower limit on the IGMF of $B > 7.1 \times 10^{-16}$ G for a coherence length of 1 Mpc even when blazar duty cycles as short as 10 yr are assumed. This improves on previous lower limits by a factor of 2. For longer duty cycles of 10^4 (10^7) yr, IGMF strengths below 1.8×10^{-14} G (3.9×10^{-14} G) are excluded, which rules out specific models for IGMF generation in the early universe.

Unified Astronomy Thesaurus concepts: Active galaxies (17); High energy astrophysics (739); Extragalactic magnetic fields (507)

1. Introduction

Astrophysical magnetic fields in galaxies and galaxy clusters are ubiquitously observed and believed to have been seeded by a turbulent intergalactic magnetic field (IGMF), which should still be present at its seed field value and coherence length in cosmic voids (see, e.g., Durrer & Neronov 2013; Alves Batista & Saveliev 2021, for reviews). Such a seed field should have a small field strength in the voids, making it extremely difficult to observe directly. Currently, only upper limits of the order of 10^{-9} G are known from Faraday rotation measurements (Pshirkov et al. 2016).

Detecting or constraining the IGMF would provide insight into many processes in the early universe; it might be possible to determine whether the IGMF was created during inflation or during phase transitions and to probe contributions of beyond-the-standard-model physics. Alternatively, the IGMF could be found to have an astrophysical origin.

Observations of blazars (active galactic nuclei (AGNs) with relativistic bulk outflows closely aligned with the line of sight (LOS)) at gamma-ray energies offer a unique alternative probe of the IGMF, with different systematics from other established methods (e.g., Durrer & Neronov 2013). During propagation, gamma rays interact with photons of background radiation fields, most notably the extragalactic background light (EBL), and produce electron–positron pairs. These pairs can inverse Compton (IC) scatter cosmic microwave background (CMB) photons up to gamma-ray energies, thereby initiating a cascade as these upscattered photons again pair-produce. The deflection of the pairs in the IGMF delays the arrival of the gamma rays produced in the cascades (compared to the primary gamma rays; Plaga 1995), which should appear as an extended halo around the blazar (Aharonian et al. 1994) and enhance its apparent brightness at lower gamma-ray energies (Neronov & Semikoz 2009).

The higher the value of the IGMF, the stronger the deflection of the pairs and, in turn, the larger the pair halos (with lower surface brightness), the lower the GeV excess of cascade photons, and the longer the time delays. The nonobservation of an excess of GeV photons in individual blazar observations with the Fermi Large Area Telescope (LAT) has thus been used to place lower limits on the IGMF of the order of $B \gtrsim 10^{-15}$ G (e.g., Neronov & Vovk 2010). Similarly, searches for a halo with imaging air Cherenkov telescopes (IACTs) have ruled out an IGMF strength between $\sim 10^{-16.5}$ and $\sim 10^{-15.5}$ G (H.E.S.S. Collaboration et al. 2014), as well as between $\sim 10^{-14.5}$ and $\sim 10^{-13.5}$ G (Archambault et al. 2017). The gamma-ray constraints are considerably relaxed when short activity times of blazars are considered (Dermer et al. 2011).⁴⁰ However, even if blazars have only been active for the past 10 yr, a joint analysis of Fermi-LAT and archival IACT spectra from several sources is still able to exclude $B \lesssim 3 \times 10^{-16}$ G for a coherence length of $\ell_B \gtrsim 10$ kpc (Ackermann et al. 2018). A comprehensive overview of current constraints is provided by Alves Batista & Saveliev (2021).

Here we perform an updated search for the cascade emission of hard-spectrum blazars. In contrast to previous cascade searches, we use a combination of Fermi-LAT data and observations carried out with the High Energy Stereoscopic System (H.E.S.S.) based on the full Poisson likelihood for gamma-ray event statistics and calculate pair halo templates with state-of-the-art Monte Carlo simulations.

2. Observations

2.1. Source Selection

Among the blazars observed with both H.E.S.S. and the LAT, we aim to select those for which the cascade emission is expected to be maximal. Extreme high-frequency-peaked BL Lac-type objects (EHLs) with an observed synchrotron peak $\gtrsim 1$ keV are the most promising for such searches. Their hard spectra are measured up to TeV energies without finding evidence for a

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⁴⁰ We define the activity time (duty cycle) as the length of the time during which the blazar has been emitting gamma rays. Throughout this work, we assume that a blazar has emitted a flux that is constant in time, which can be described with the average spectrum observed today.

Table 1
Selected Sources and Observation Summaries

Source	z	H.E.S.S.			Fermi-LAT	
		Live Time (hr)	Significance (σ)	Γ_{int}	$\sqrt{\text{TS}}$	Γ_{int}
1ES 0229+200	0.140	144.1	16.5	1.76 ± 0.12	14.2	1.73 ± 0.12
1ES 0347–121	0.188	59.2	16.1	2.12 ± 0.15	18.3	1.81 ± 0.11
PKS 0548–322	0.069	53.9	10.2	1.92 ± 0.12	11.7	2.06 ± 0.17
1ES 1101–232	0.186	71.9	18.7	1.66 ± 0.09	19.5	1.65 ± 0.09
H2356–309	0.165	150.5	23.4	2.10 ± 0.09	21.7	1.81 ± 0.09

Note. Second column: spectroscopic redshift, z , taken from (in order of increasing R.A.) Fosbury & Disney (1976), Remillard et al. (1989), Woo et al. (2005), Jones et al. (2009), and Peña-Herazo et al. (2021). Third column: total observation time taking data quality cuts and dead time into account. Fourth and sixth columns: detection significance in units of σ . Fifth and seventh columns: power-law indices for EBL-corrected spectra.

source-intrinsic spectral cutoff. Therefore, a lot of energy is potentially available for reprocessing into the cascade. To select EHLB sources, we start from the fourth catalog of AGNs observed with the LAT (4LAC; Lott et al. 2020). We select blazars that (i) follow a power-law spectrum in energy E , $dN/dE = N_0(E/E_0)^{-\Gamma}$, with spectral index $\Gamma < 2$ within statistical uncertainties; (ii) have a known spectroscopic redshift z ; and (iii) have a synchrotron peak $\nu_{\text{peak}} > 10^{17}$ Hz. Additionally, we demand that the flux have a chance probability of being variable at less than 99% in the LAT energy band on monthly timescales. This choice excludes sources that exhibit strong variability. Otherwise, the past temporal flux evolution would have to be taken into account to predict the time-delayed cascade emission. This selection results in five sources that have been previously detected with H.E.S.S. (Aharonian et al. 2006b, 2007a, 2007b, 2010). These are listed in Table 1. Except for PKS 0548–322, all of the selected sources are also included in the analysis of Ackermann et al. (2018). In addition, Ackermann et al. (2018) considered the H.E.S.S.-detected blazar 1ES 0414+009; however, this source fails our cuts on the synchrotron peak frequency and the probability for variability.

2.2. Fermi-LAT Observations

The Fermi-LAT is a pair-conversion telescope that detects gamma rays from 20 MeV to beyond 300 GeV (Atwood et al. 2009). For our five sources, we analyze 11.5 yr of LAT data between 1 GeV and 3 TeV extracted from a $6^\circ \times 6^\circ$ region of interest (ROI) centered on the nominal source position. The data selection closely follows Ackermann et al. (2018). Using events and instrumental response functions of the P8R3_SOURCE_V3 class, we find the optimal model for the ROI that includes all point sources listed in the second data release of the fourth LAT point-source catalog (4FGL-DR2; Ballet et al. 2020), as well as templates for the diffuse Galactic and isotropic backgrounds (see Appendix A for further details). All of our blazars are modeled with power laws in our initial ROI model. After an initial optimization of the model, we change the spectral model to a power law with index Γ_{int} that includes absorption on the EBL, given by $\exp(-\tau_{\gamma\gamma})$, where $\tau_{\gamma\gamma}$ is the optical depth. Throughout this article, the EBL absorption is taken from the model of Domínguez et al. (2011). The obtained spectral indices and source significances, expressed as the square root of the test statistic (TS),⁴¹ are listed in Table 1. In Figure 1, we show a sky map with TS values for our optimized ROI model for

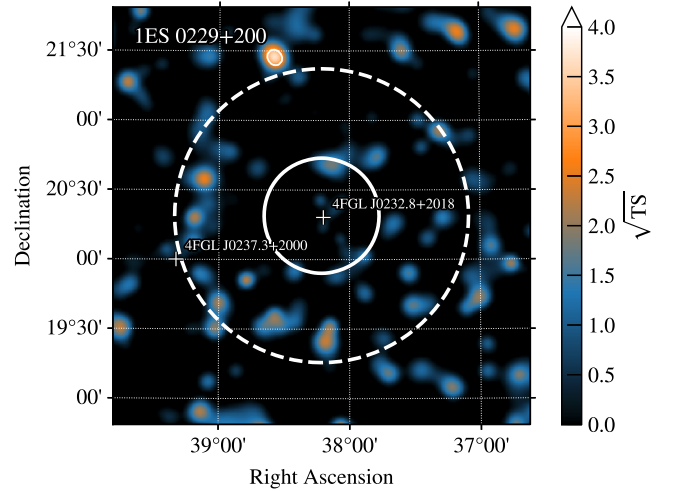


Figure 1. A TS map for the LAT analysis of the ROI around 1ES 0229+200. Point sources within the ROI are marked with plus signs. The 68% containment radii at 1 GeV for the LAT point-spread function for the events with the worst and best angular reconstruction are shown as a dashed and solid circle, respectively. The thin white contour indicates a region where $\sqrt{\text{TS}} = 3$.

1ES 0229+200. In each pixel, the significance of a putative source with a power-law index equal to 2 is calculated. A potential halo could reveal itself as a TS excess around the central source. This is, however, not observed for any of the studied sources (see also Appendix A).

2.3. H.E.S.S. Observations

H.E.S.S. is an array of five IACTs located in the Khomas highlands in Namibia. The array is composed of four telescopes with an effective mirror diameter of 12 m, called CT1–CT4, and one with an effective mirror diameter of 28 m, called CT5. New cameras were installed between 2015 and 2016 for CT1–CT4 and in 2019 for CT5. H.E.S.S. can detect very high energy gamma rays between ≈ 50 GeV and ≈ 100 TeV. All sources considered here have been detected with H.E.S.S. For all EHLBs except PKS 0548–322, additional data have been taken since the original publications during different phases of the experiment (with and without CT5, before and after the camera exchange campaigns). In order to have a data set with a hardware setup as homogeneous as possible, we restrict ourselves to runs⁴² with

⁴¹ The test statistic is defined as $\text{TS} = -2(\ln \mathcal{L}_1 - \ln \mathcal{L}_0)$, where $\mathcal{L}_1$ ($\mathcal{L}_0$) is the likelihood of the model including (excluding) a source.

⁴² One run is a consecutive observation of a source with a duration of approximately 28 minutes.

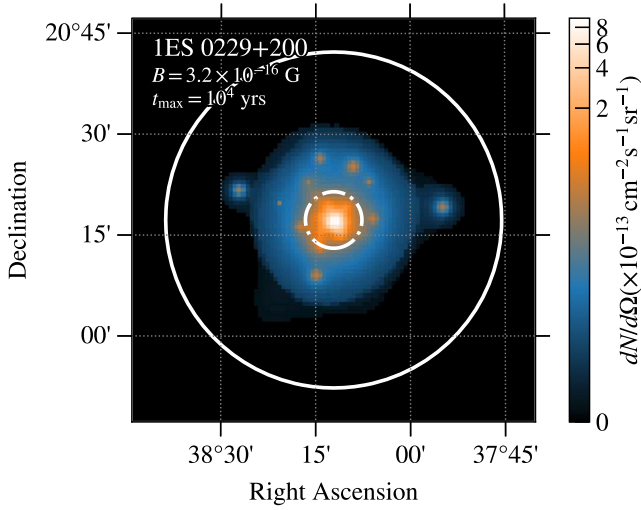


Figure 2. Simulated halo photon flux per solid angle, $dN/d\Omega$, integrated above 1 GeV for the best-fit spectrum (see Section 3.2) for IES 0229+200. An activity time of $t_{\max} = 10^4$ yr and a field strength of $B = 3.2 \times 10^{-16}$ G are assumed. The same 68% containment radius as in Figure 1 is shown for comparison, along with the On region for the H.E.S.S. observations (dotted–dashed circle). The hot spots correspond to individual simulated particles.

good data quality in which three or four of the smaller telescopes participated. For the same reason, we only use data taken with the cameras originally mounted on the 12 m telescopes. The energies of the recorded gamma-ray-like events are reconstructed using the *ImPACT* method and standard selection cuts (Parsons & Hinton 2014). The spectral analysis is performed using *gammapy* version 0.18.2 (Deil et al. 2017). Source counts are extracted from an “On” region of radius of $0^\circ.07$ centered on the source location, which corresponds to the 68% confidence radius of the point-spread function. The observed spectra are modeled with power laws with EBL attenuation; models with spectral curvature are not preferred. The resulting spectral indices are provided in Table 1, together with observation live times and detection significances. Further details on the analysis are provided in Appendix B.

3. Search for the Pair Halo and Constraints on the IGMF

3.1. Cascade Predictions

We generate templates for the pair halo for each redshift using the *CRPropa* Monte Carlo simulation package version 3.1.6⁴³ (Alves Batista et al. 2016a). In the simulation, we include all relevant particle interactions and consider cascade photons arriving with a time delay shorter than a maximum blazar activity time $t_{\max}$. Using a spectral reweighting (Ackermann et al. 2018) and parallel transport (Alves Batista et al. 2016b), the simulations are converted into energy-dependent sky maps for arbitrary input spectra and angles θ_{obs} between the jet axis and the LOS (see Appendix C for further details on the simulation).⁴⁴ These serve as input templates for our data analysis. For simplicity, $\theta_{\text{obs}} = 0^\circ$ is assumed throughout. For $0 < \theta_{\text{obs}} < \theta_{\text{jet}}/2$, the templates will be asymmetric. However, in the considered energy range, the asymmetry is small, and our results do not depend strongly on

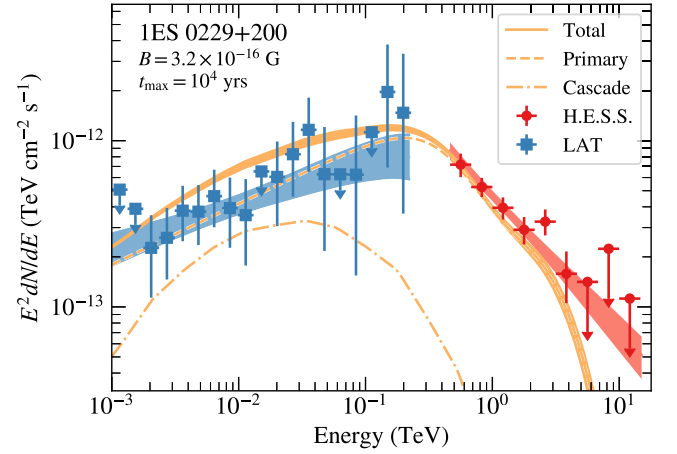


Figure 3. Observed LAT and H.E.S.S. spectra of IES 0229+200 (blue and red markers and lines, respectively), together with the total best-fit spectrum (orange solid band, including uncertainties) for a point-source model of the primary gamma-ray flux (dashed orange line) and the halo flux (dashed–dotted orange line). Spectral points are shown as upper limits if the detection significance is below 2σ . The same values for $t_{\max}$ and B are assumed as in Figure 2.

θ_{obs} and the orientation of the halo. The IGMF is modeled as cell-like; each cell has a side length of $\ell_B = 1$ Mpc, and the B -field orientation changes randomly from one cell to the next. The templates are generated for each source and for seven values of the field strength, $B = 10^{-16}, 10^{-15.5}, \dots, 10^{-13}$ G. For higher values of B , the pairs are quickly isotropized and the cascade emission would appear as an additional component to the isotropic gamma-ray background in the LAT energy band. An example of the simulated energy-integrated sky map is shown in Figure 2, and an output spectrum is shown in Figure 3. Spectra for all other sources and different choices of the IGMF are presented in Figure 6 in Appendix D.

3.2. Combined LAT and H.E.S.S. Analysis

We test for the presence of a halo for a given field strength using a likelihood ratio test. Different fixed values of $t_{\max} = 10, 10^4$, and 10^7 yr are assumed, which correspond to a conservative, intermediate, and optimistic scenario, respectively, in terms of the amount of cascade emission. Our model is the sum of the point-source flux $\phi_{\text{src}}(E, \theta_i)$ for central source i and spectral parameters θ_i and the diffuse halo flux $\phi_{\text{halo}}(E, \mathbf{p}, \theta_i, B)$, which also depends on the sky position $\mathbf{p}$ and the IGMF. In contrast to Section 2, the point-source spectra are now modeled with a power law with a cutoff at energy E_{cut} ,

$$\phi_{\text{src}} = N_0 (E/E_0)^{-\Gamma_{\text{int}}} \exp(-E/E_{\text{cut}} - \tau_{\gamma\gamma}), \quad (1)$$

i.e., $\theta = (N_0, \Gamma_{\text{int}}, E_{\text{cut}}, E_0)$. With this choice, we obtain plausible constraints on the IGMF since the high-energy cutoff reduces the number of gamma rays that can initiate the cascade. Assuming instead a simple power law as the intrinsic spectrum would bear the risk of overestimating the flux of primary gamma rays and thus of the cascade.

The likelihood of observing the data $\mathcal{D}_i$ given the model parameters is the product of the individual Poisson likelihoods for LAT and H.E.S.S. data, $\mathcal{L}_i \equiv \mathcal{L}(B, \theta_i | \mathcal{D}_i) = \mathcal{L}(B, \theta_i | \mathcal{D}_{\text{LAT}, i}) \mathcal{L}(B, \theta_i | \mathcal{D}_{\text{H.E.S.S.}, i})$. The log-likelihood ratio test

⁴³ <https://github.com/CRPropa/CRPropa3>

⁴⁴ A Python package performing these calculations is publicly available at <https://github.com/me-manu/simCRPropa>.

can then be written as

$$\lambda(B) = -2 \sum_i \ln \left(\frac{\mathcal{L}(B, \hat{\theta}_i | \mathcal{D}_i)}{\mathcal{L}(\hat{B}, \hat{\theta}_i | \mathcal{D}_i)} \right), \quad (2)$$

where $\hat{\theta}_i$ denotes the spectral parameters maximizing $\mathcal{L}_i$ for a fixed field strength, whereas $\hat{\theta}_i$ and $\hat{B}$ are the parameters that maximize $\mathcal{L}_i$ unconditionally. We first extract $\ln \mathcal{L}(B, \theta_i | \mathcal{D}_{\text{LAT},i})$ over a grid of IGMF values and spectral parameters by adding the reweighted cascade template to the ROI model (see Section 2.2) and reoptimizing the spectral parameters of the background sources (see Appendix A.2 for further details). In a second step, we determine the spectral parameters that maximize the total $\mathcal{L}_i$ for a given value of B using the MINUIT fit routine in *gammapy*. For the H.E.S.S. data, the model includes the point source and the pair halo intensity within the On region. In each step of the parameter optimization, the cascade template is reweighted to account for the changing spectrum, and the extracted value of $\ln \mathcal{L}(B, \theta_i | \mathcal{D}_{\text{LAT},i})$ is added to $\ln \mathcal{L}(B, \theta_i | \mathcal{D}_{\text{H.E.S.S.},i})$. In this way, for a given set of IGMF parameters, the best-fit spectrum of each source for both the LAT and H.E.S.S. energy ranges is determined. An example of the fit for 1ES 0229+200 is shown in Figure 3. Figures for other sources are shown in Appendix D.1, where we also report the best-fit parameters.⁴⁵

In general, high values of B provide a better fit to the data than low IGMF values, implying halos with large extensions and a low surface brightness. For low values of B , the fit prefers low values of E_{cut} to minimize the cascade contribution. For instance, for $t_{\text{max}} \geq 10^4$ yr and $B = 10^{-16}$ G the cutoff energy is below $E_{\text{cut}} \lesssim 3$ TeV for all sources except PKS 0548–322. However, even the fits assuming high IGMF values are not significantly preferred over the fit without cascade emission. The largest value for the log-likelihood ratio between the fit without and with a halo is found to be $\text{TS} \sim 0.9$ for $B = 10^{-13}$ G and $t_{\text{max}} = 10^4$ yr. Thus, we do not find any evidence for the presence of a halo and proceed to set lower limits on the IGMF strength. As the field strength constitutes one additional degree of freedom, we set 95% confidence limits when $\lambda > 2.71$. We find that we can rule out an IGMF with a field strength $B < 3.9 \times 10^{-14}$ G for $t_{\text{max}} = 10^7$ yr. For a more conservative choice of the blazar activity time, we exclude $B < 1.8 \times 10^{-14}$ G for $t_{\text{max}} = 10^4$ yr and $B < 7.1 \times 10^{-16}$ G for $t_{\text{max}} = 10$ yr. The strongest constraints are provided by 1ES 0229+200 and 1ES 1101–232 (see Appendix D.2 for the full likelihood profiles). These limits, together with previous constraints and theoretically motivated parameters, are shown in Figure 4.

4. Discussion

The analysis presented here improves on previous analyses of a combination of IACT and LAT data in two ways. First, we use the CRPropa code to generate predictions for the spectral and spatial shape of the halo. As the code traces the full trajectories of the particles, we are not limited by the assumption of, e.g., small deflections of the pairs in the IGMF, which limited the validity range of the results of

Ackermann et al. (2018). Second, we combine LAT and H.E.S.S. data on the likelihood level and self-consistently include the halo contribution. As a result, we are able to improve on the constraints found by Ackermann et al. (2018) by a factor of two for blazar activity times as short as 10 yr. To our knowledge, these are the tightest constraints on the IGMF from gamma-ray observations to date (compare Figure 4).

The assumed activity time of the sources poses the largest systematic uncertainty in our study. Changing t_{max} from 10 to 10^4 yr strengthens the constraint by almost a factor of 30 (activity times of 10^7 – 10^8 yr could be realistic; Parma et al. 2002). For $t_{\text{max}} = 10^7$, we cannot rule out as high IGMF values as Archambault et al. (2017). The likely reason is that we do not include the spatial halo extension in the H.E.S.S. energy range, as we only consider the cascade photons that arrive within the On region. We are instead able to probe low IGMF values thanks to the combination of LAT and H.E.S.S. data. We have deliberately selected sources that do not experience strong variability in the LAT data. However, at least H2356–309 and 1ES 0229+200 show flux variations by factors ~ 2 – 3 above 100 GeV on monthly and yearly timescales, respectively (H.E.S.S. Collaboration et al. 2010; Acciari et al. 2023). Our reweighting framework developed in Appendix C could in principle be extended to study how long-term variability affects the predictions for the cascade. This is left for future study. Additional systematic uncertainties with a smaller effect on the results compared to the change in activity time, such as the choice of the EBL model, the choice of θ_{jet} , and the different absolute energy scales of the LAT and H.E.S.S. (which can be treated self-consistently in our likelihood framework), are discussed in Appendix D.3.

Under the assumptions that (a) the sources have been active for $10 \text{ yr} \lesssim t_{\text{max}} \lesssim 10^4 \text{ yr}$ and (b) our constraints scale as $\ell_B^{-1/2}$ in the case when ℓ_B is shorter than the mean free path of the pairs for IC scattering (Neronov & Semikoz 2009; see, however, Caprini & Gabici 2015), our results challenge particular models for the IGMF generation. For example, we can rule out models where the seed fields are created through axion-driven magnetogenesis (which predicts a present-day IGMF with $B \sim 10^{-13}$ G and $\ell_B \sim 20$ pc; see Miniati et al. 2018) and the low end of allowed B -field values generated during or shortly after inflation with values $B \gtrsim 10^{-15}$ G on megaparsec scales (Kobayashi 2014).

It could be possible that the pairs predominantly lose their energy by heating the intergalactic medium through plasma instabilities, which would suppress the cascade (Broderick et al. 2012). Whether such instabilities develop is, however, still debated (see, e.g., Alves Batista & Saveliev 2021). We can introduce an additional normalization for our halo templates, $0 \leq N_{\text{halo}} \leq 1$, to mimic the possibility that the pairs lose part of their energy through this process ($N_{\text{halo}} = 1$ corresponds to the case discussed so far). The fit tends to select $N_{\text{halo}} \sim 0$, as the halo is not present in the data, i.e., no energy is dissipated through IC scattering. In this case, no limits on the IGMF are possible. We note, however, that our constraints for $t_{\text{max}} = 10$ yr are not affected, as the energy loss due to beam instabilities would only dominate over IC cooling after hundreds of years of blazar activity (Broderick et al. 2012).

In the future, observations with the upcoming Cherenkov Telescope Array (CTA) should be able to detect an IGMF as strong as 10^{-13} G for sufficiently long blazar activity times (see Figure 4) thanks to its improved angular resolution, point-

⁴⁵ We provide the Fermi-LAT and H.E.S.S. spectra, best-fit values, as well as the cascade simulation output electronically at [10.5281/zenodo.8014311](https://doi.org/10.5281/zenodo.8014311).

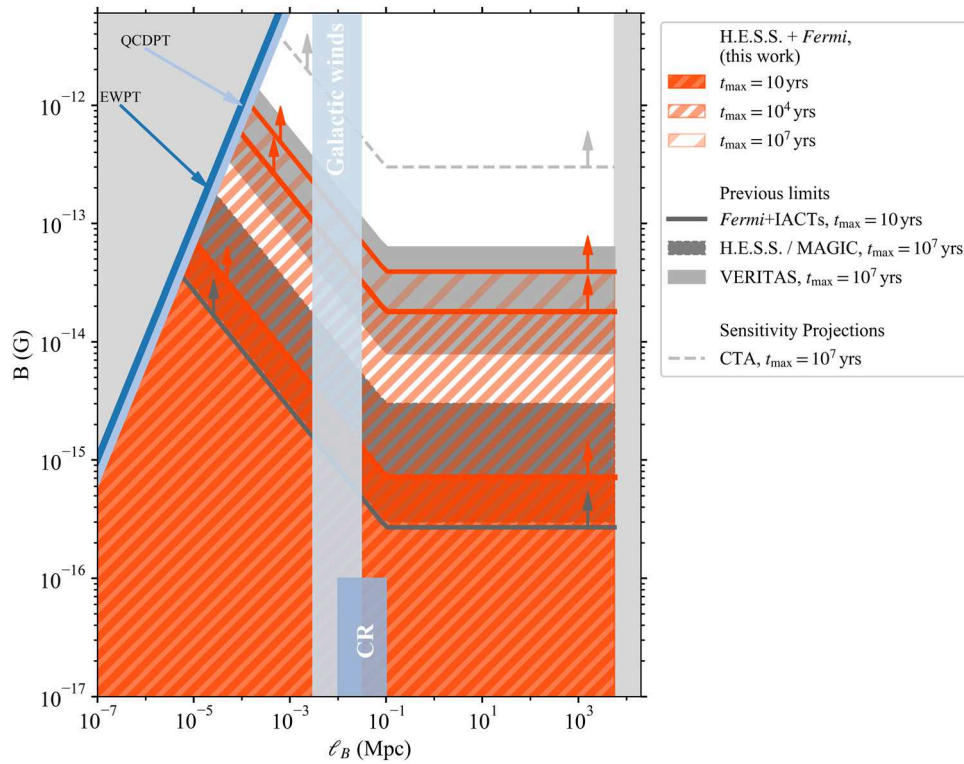


Figure 4. The IGMF parameter space probed with gamma-ray instruments. Lower limits at 95% confidence level on the IGMF derived from the combined Fermi-LAT and H.E.S.S. analysis for different assumed blazar activity times are shown as orange filled and hatched regions. A scaling of the limits with the coherence length as $\ell_B^{-1/2}$ is assumed. Exclusion regions from H.E.S.S., MAGIC, and VERITAS are shown as gray filled regions (Aleksić et al. 2010; H.E.S.S. Collaboration et al. 2014; Archambault et al. 2017). The CTA could exclude field strengths below the dashed gray line (Abdalla et al. 2021). The dark-gray line shows combined Fermi-LAT and IACT lower limits for $t_{\max} = 10$ yr (Ackermann et al. 2018). Light-gray shaded regions are disfavored by theory. Blue lines and regions indicate theoretically favored regions for the generation of the IGMF during either electro-weak phase transitions (EWPT) or QCD phase transitions (QCDPT), by Galactic winds or induced by cosmic-ray (CR) streaming (see Durrer & Neronov 2013, and references therein).

source sensitivity, and covered energy range (Meyer et al. 2016; Abdalla et al. 2021).

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Facilities: Fermi-LAT, H.E.S.S.

Software: astropy (Astropy Collaboration et al. 2013), numpy (Harris et al. 2020), scipy (Virtanen et al. 2020), CRPropa3 (Alves Batista et al. 2016a), fermipy (Wood et al. 2017), fermitools (Fermi Science Support Development Team 2019), gammapy (Deil et al. 2017).

Appendix A

Details on the Fermi-LAT Data Analysis

A.1. Data Selection and Initial Model Optimization

In this appendix, we provide further details on the Fermi-LAT data selection and analysis choices. Events of the P8R3_SOURCE_V3 class with arrival times between 2008 August 4 and 2020 January 4 are extracted from a $6^\circ \times 6^\circ$ sky region in the energy

range from 1 GeV to 3 TeV that arrived with a zenith angle $\leq 100^\circ$ in order to minimize contamination of our sample with gamma rays from the Earth limb. The standard data filter `DATA_QUAL > 0 && LAT_CONFIG == 1` is applied. Following Ackermann et al. (2018), the events are then binned using a spatial binning of 0.025 pixel^{-1} and a logarithmic binning in energy with 8 bins per decade. Furthermore, we split the data sample into two subsamples using the quality of the angular reconstruction (the so-called PSF event classes; see Atwood et al. 2013). The first subsample contains all events belonging to the PSF event classes 0–2 (event type 28), and the second sample contains the events with the best reconstructed arrival directions, PSF event class 3 (event type 32). A combined likelihood analysis is performed on these two subsamples using `fermipy`⁴⁶ (Wood et al. 2017) version 0.19.0 and the `fermitools` version 1.2.23⁴⁷ with the MINUIT optimizer.

For the initial optimization of the ROI model we include the point sources listed in the 4FGL-DR2 up to an angular distance of 10° from the ROI center. Templates for the galactic diffuse (`gll_iem_v07`) and isotropic diffuse (`iso_P8R3_SOURCE_V3_v1`) emission are added to the model as well.⁴⁸ All spectral parameters of sources up to a radius of 6° are left free to vary, and only spectral normalizations are free parameters for sources at larger distances. After an initial optimization using the `fermipy` `optimize` routine, we fix all spectral source parameters (spectral shape parameters, i.e., all parameters but the spectral normalization) for sources that are detected with a $\text{TS} < 5$ ($\text{TS} < 9$) or that have a predicted number of photons less than 10^{-2} . The flux normalization parameter of sources with $\text{TS} > 50$ that was originally frozen is also left free to vary during the fit. After a first fit to the data, a TS map is computed. Putative point sources (modeled with a power law) are added consecutively to the ROI to hot spots with $\text{TS} > 25$. This procedure could tentatively mask any additional unaccounted flux from the cascade halo. Only one additional source had to be added in the vicinity of 1ES 1101–232 at a distance of larger than 1° , which should not have an effect on the halo search. From this it appears unlikely that our analysis procedure could mask an additional halo contribution. The TS maps for 1ES 0229+200 are shown in Figure 1 and for all other sources in Figure 5. The above analysis choices result in generally flat spectral and spatial residuals.

The best-fit spectral parameters for a point-source analysis with and without EBL absorption are provided in Table 2. For the fit with EBL, we only provide the spectral index, Γ_{int} , which, for all sources, is compatible with the fit without absorption (with index Γ) within 1σ uncertainties. The reason is the limited number of observed gamma rays by the LAT in the energy range where the optical depth $\tau_{\gamma\gamma} \gtrsim 1$. The obtained point-source spectra for all sources are shown as blue squares and solid lines in Figure 6 in Appendix D.1. We note that the LAT spectrum of 1ES 0347-121 exhibits evidence for a detection ($\sqrt{\text{TS}} \gtrsim 4$) of the source above 1 TeV. This result is due to two photons detected above 1 TeV in the vicinity of the source.

A.2. Extracting Likelihood Values in the Presence of the Halo

In the presence of a halo, it is nontrivial to extract the likelihood values, $\mathcal{L}(\mathcal{B}, \theta_i | \mathcal{D}_{\text{LAT}, i})$, using the built-in functionality of `fermipy`. The reason is that the cascade flux depends on the intrinsic spectral parameters of the blazar. Therefore, we loop over the spectral parameters of the central blazar and fix them at each step. Then, we add the corresponding reweighted halo template and extract the likelihood values. More specifically, we start from the optimized ROI model of the LAT data for each source i as described in Section 2.2. We loop through values of the source-intrinsic spectral index, $\Gamma_{\text{int}} = \Gamma_{\text{int},0} + \Delta\Gamma_{\text{int}}$, where $\Gamma_{\text{int},0}$ denotes the best-fit value from LAT data (see Table 1) and $\Delta\Gamma_{\text{int}}$ ranges from -0.75 to 0.75 with a step size of 0.075 . We further sample the exponential cutoff energy of the spectrum, $E_{\text{cut}} = 1, 3, \dots, 13 \text{ TeV}$ (which itself is not constrained from LAT data) and the spectral normalization N_0 . The choice is motivated by the energy range of the H.E.S.S. spectra. For each combination of the spectral parameters, we reweight the cascade template, add it to the ROI, and extract the multidimensional profile likelihood cube for the model with the halo emission to describe the data. The normalizations of the other (diffuse) sources in the ROI are optimized in each step of the loop.

⁴⁶ <https://fermipy.readthedocs.io/en/latest/>

⁴⁷ <https://fermi.gsfc.nasa.gov/ssc/data/analysis/>

⁴⁸ See <https://fermi.gsfc.nasa.gov/ssc/data/access/lat/BackgroundModels.html>. For the isotropic diffuse emission, we calculate an average of the templates for the PSF classes 0–2.

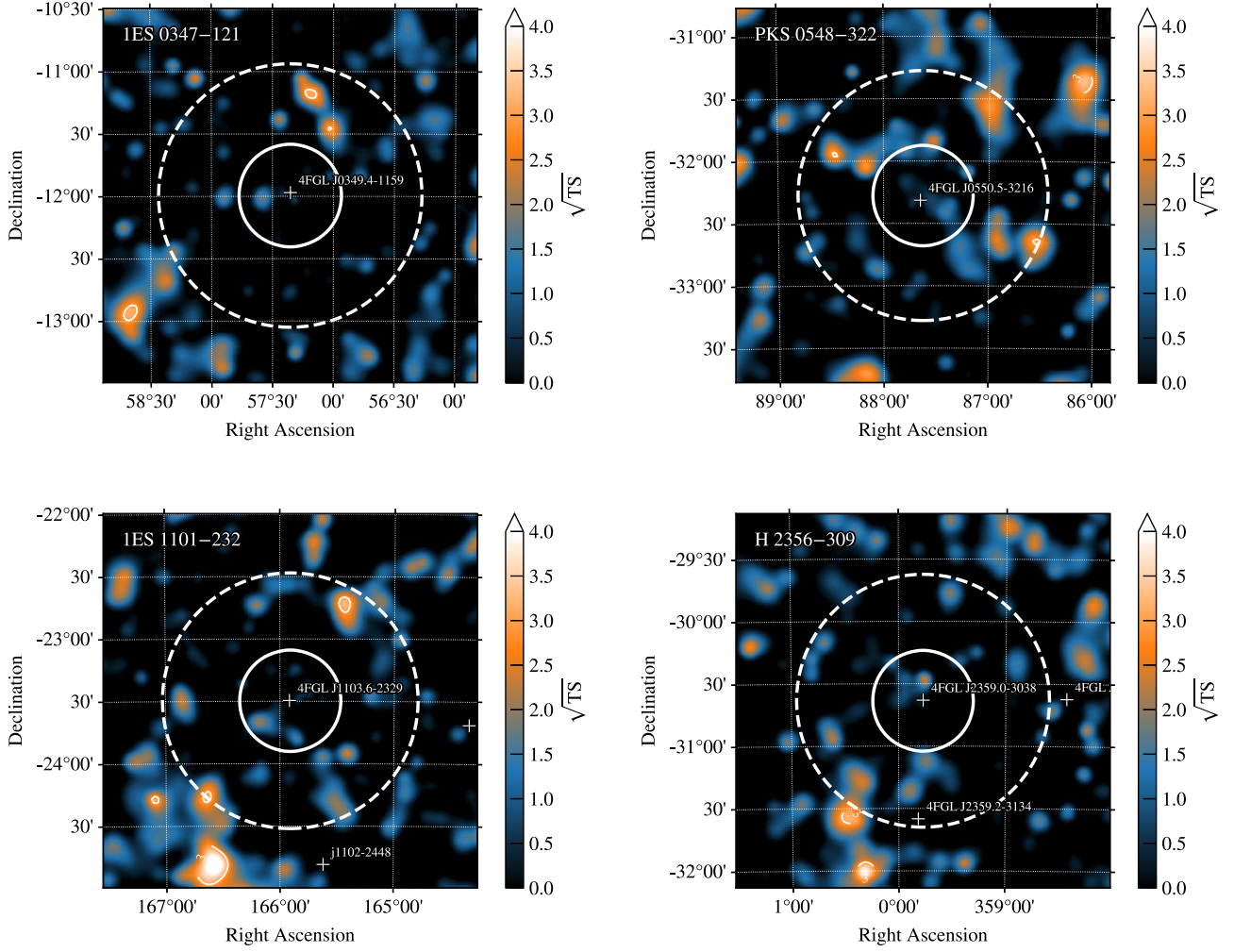


Figure 5. TS maps as in Figure 1 for all other considered sources. Again, no significant excess is observed close to any considered source. The additional source in the ROI of 1ES 1101–232 is marked with a lowercase j and its coordinates.

Table 2
Best-fit Parameters for the LAT Spectra of the Considered EBL Sources without a Halo Component

Source Name	N_0 (10^{-14} MeV $^{-1}$ cm $^{-2}$ s $^{-1}$)	E_0 (GeV)	Γ	Γ_{int}
1ES 0229+200	1.02 ± 0.14	5.80	1.77 ± 0.09	1.73 ± 0.12
1ES 0347–121	1.90 ± 0.21	4.82	1.81 ± 0.08	1.81 ± 0.11
PKS 0548–322	2.17 ± 0.32	3.29	1.99 ± 0.12	2.06 ± 0.17
1ES 1101–232	2.09 ± 0.23	4.84	1.68 ± 0.07	1.65 ± 0.09
H2356–309	3.49 ± 0.35	3.70	1.78 ± 0.07	1.81 ± 0.09

Appendix B

Details on the H.E.S.S. Data Analysis

In this appendix, details on the analysis choices for the H.E.S.S. observations are given in addition to the main selection criteria described in Section 2.3. For each source, the runs are stacked onto one data set per source for runs that pass our selection given in the main text in combination with an offset between telescope pointing and source direction of $\leq 2^\circ$ and a zenith angle of $Z \leq 60^\circ$. The background in the On region is estimated from multiple reflected “Off” regions of the same size that have a minimum separation to the source location of

0.2° (Aharonian et al. 2006a). The energy threshold E_{thr} of this stacked data set is computed from the condition that the energy bias of the energy dispersion matrix is below 10%. The median zenith angles $\langle Z \rangle$ and values of E_{thr} are provided in Table 3. We choose an energy binning of the recorded events of 24 bins per decade. Using the MINUIT back end in *gammapy*, we fit a simple power law without (with) EBL absorption to the observations. The best-fit parameters, N_0 ($N_{0,\text{int}}$) and Γ (Γ_{int}), are also provided in Table 3. The EBL absorption effect is clearly visible as $\Gamma_{\text{int}} < \Gamma$ for all sources. The energy normalization E_0 is determined from the fit without EBL absorption such that the off-diagonal terms of the covariance matrix are

Table 3Mean Zenith Angle $\langle Z \rangle$, Energy Threshold E_{thr} , and Best-fit Parameters for the H.E.S.S. Spectra of the Considered EHBL Sources without a Halo Component

Source Name	$\langle Z \rangle$ (deg)	E_{thr} (TeV)	N_0 ($10^{-12} \text{ TeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1}$)	$N_{0,\text{int}}$ ($10^{-12} \text{ TeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1}$)	E_0 (TeV)	Γ	Γ_{int}
1ES 0229+200	44.4	0.46	0.32 ± 0.02	1.64 ± 0.11	1.14	2.81 ± 0.11	1.76 ± 0.12
1ES 0347-121	16.1	0.22	4.70 ± 0.35	11.94 ± 0.09	0.43	3.40 ± 0.14	2.12 ± 0.15
PKS 0548-322	11.0	0.22	0.44 ± 0.05	0.85 ± 0.09	0.89	2.44 ± 0.11	1.92 ± 0.12
1ES 1101-232	21.3	0.16	2.75 ± 0.18	10.13 ± 0.64	0.54	2.93 ± 0.09	1.66 ± 0.09
H2356-309	13.5	0.22	3.60 ± 0.18	9.14 ± 0.46	0.46	3.21 ± 0.09	2.10 ± 0.09

minimal. The resulting point-source spectra are shown in Figure 6 in Appendix D.1 as a red bow tie and red points. For the spectral points, we use 9 bins between E_{thr} and $10^{1.25}$ TeV. A cross-check analysis with an independent analysis chain (de Naurois & Rolland 2009) yields consistent results.

Appendix C

Details on the Cascade Simulations with CRPropa

The CRPropa simulations are carried out in the large sphere observer framework, with the source placed at the origin of a sphere with radius equal to the comoving distance D to the source. We use a standard Λ CDM cosmology with $H_0 = 67.3 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and a matter density of $\Omega_m = 0.315$ (these are default CRPropa values). From the source, gamma rays are injected into a cone with opening angle $\theta_{\text{jet}} = 6^\circ$ (which is in the range of typically observed angles; e.g., Jorstad et al. 2017), with its central axis pointing along the negative x -axis in the simulation coordinate system. We include energy losses through pair production, IC scattering, synchrotron emission of electrons in the IGMF, and propagation of particles in an expanding universe. Within the propagation module of CRPropa, we set the tolerance parameter, which determines the numerical precision, to 10^{-9} and set the minimum step length of the simulation such that time delays τ down to 1 yr can be resolved. In order to reduce the computational time, we stop tracing particles if their energy drops below 0.1 GeV or if their total propagating distance becomes larger than 4 Gpc. We inject monochromatic gamma rays with energies ϵ equal to the central energies of bins $\Delta\epsilon$ between 1 GeV and ≈ 31.6 TeV using 4 bins per decade. The value of the maximum energy is limited by the available computational resources for the simulations. As shown in Section 3.2, the intrinsic blazar spectra will tend to have lower cutoff energies so that this choice does not affect our results. The time delay τ of the cascade gamma rays is calculated through $c\tau \approx (d - D)$, where c is the speed of light. To mitigate simulation noise introduced through a finite number of injected gamma rays, the sky maps are adaptively smoothed using the ASMOOTH algorithm (Ebeling et al. 2006). From the CRPropa simulation, we obtain a multidimensional histogram of photon counts $\mathcal{N}$. We can convert this histogram into the number of counts arriving per injected energy ϵ , observed energy E , solid angle Ω , time delay interval $d\tau$, and injected particle in the interval $\Delta\epsilon$ as

$$\frac{d\mathcal{N}}{d\epsilon dE d\tau d\Omega} = \frac{1}{N_{\text{inj}}(\Delta\epsilon)} \frac{\mathcal{N}}{\Delta\epsilon \Delta E \Delta\tau \Delta\Omega}, \quad (\text{C1})$$

where ΔX is the chosen bin width of the CRPropa histogram for quantity X . To speed up computations, the number of injected particles N_{inj} decreases for larger injected energies and thus depends on the injected energy. For a single simulation, $N_{\text{inj}} = 10$ for $\epsilon < 1$ TeV, $N_{\text{inj}} = 5$ for $1 \leq \epsilon < 10$ TeV, and

$N_{\text{inj}} = 3$ for $\epsilon \geq 10$ TeV. For magnetic fields $\log_{10}(B/G) \leq -15$, 1000 independent simulations are performed that are combined into a single spectrum. For higher B fields we run more simulations as more particles are deflected at large angles and discarded (see Section C.1), which increases the noise of the simulations. We increase the number of simulations by 200 for each tested IGMF, resulting in 1800 simulations for $\log_{10}(B/G) = -13$.

To obtain the cascade flux that arrives within some maximum time delay τ_{max} for an arbitrary injected (time-averaged) photon spectrum $dN/d\epsilon$ (e.g., in units $\text{s}^{-1} \text{ cm}^{-2} \text{ eV}^{-1}$), we need to convolve the initial cascade spectrum in Equation (C1) with the injected spectrum and integrate over the delay times,

$$\begin{aligned} \frac{d\mathcal{N}}{dE d\Omega} &= \int_0^\infty d\epsilon \int_0^\infty d\epsilon' \frac{dN}{d\epsilon'} \int_0^{\tau_{\text{max}}} d\tau \frac{d\mathcal{N}}{d\epsilon' dE d\tau d\Omega} \\ &\approx \sum_i \sum_j \Delta\epsilon_i \Delta\tau_j w_i \left(\frac{d\mathcal{N}}{d\epsilon dE d\tau d\Omega} \right)_{ij}. \end{aligned} \quad (\text{C2})$$

In the last step, we have discretized the two integrals and introduced the spectral weights w_i for the i th energy bin of the injected spectrum $\Delta\epsilon_i$,

$$w_i = \int_{\Delta\epsilon_i} \frac{dN}{d\epsilon} d\epsilon. \quad (\text{C3})$$

C.1. Applied Rotations in the Large Sphere Observer Framework

Each event is recorded when it hits the sphere at some position $\mathbf{x}$ in the global simulation coordinate system S_{sim} with Cartesian unit vectors $\hat{x}_{\text{sim}}$, $\hat{y}_{\text{sim}}$, and $\hat{z}_{\text{sim}}$. For each event the final (initial) unit momentum vector $\mathbf{p}$ ($\mathbf{p}_0$), final (initial) energy E (ϵ), and propagation length d are recorded. The sphere has a radius equal to the comoving distance D to the source, and the source is located at the center of the sphere with Cartesian coordinates $\mathbf{x}_0 = (0, 0, 0)$. For the simulation, we assume a source that emits particles uniformly into a cone with aperture θ_{jet} with the jet axis $\mathbf{j}$ pointing in the $(-1, 0, 0)$ direction.

We adopt the large sphere observer framework and follow the same method as in Alves Batista et al. (2016b), placing an observer at each hit position $\mathbf{x}$ on the surface of the sphere and defining a local coordinate system S_{obs} . In S_{obs} , the unit vector of the z_{obs} -axis points along the connection between the hit location and the source, i.e., the LOS, defined by the unit vector $\hat{\xi} = \xi_x \hat{x}_{\text{sim}} + \xi_y \hat{y}_{\text{sim}} + \xi_z \hat{z}_{\text{sim}} = (\mathbf{x} - \mathbf{x}_0)/|\mathbf{x} - \mathbf{x}_0|$. With this definition, we see that $\hat{z}_{\text{obs}} = -\hat{\xi}$. The $\hat{x}_{\text{obs}}$ and $\hat{y}_{\text{obs}}$ unit vectors are then defined in such a way that S_{obs} is a right-handed

coordinate system. Introducing the definitions,

$$\rho = \sqrt{\xi_x^2 + \xi_y^2} \quad (C4)$$

$$r = \sqrt{\xi_x^2 + \xi_y^2 + \xi_z^2} \quad (C5)$$

$$\cos \phi = \frac{\xi_x}{\rho} \quad (C6)$$

$$\sin \phi = \frac{\xi_y}{\rho} \quad (C7)$$

$$\cos \vartheta = \frac{\xi_z}{r} \quad (C8)$$

$$\sin \vartheta = \frac{\rho}{r}, \quad (C9)$$

the unit vectors $\hat{x}_{\text{obs}}$ and $\hat{y}_{\text{obs}}$ in S_{sim} are found to be

$$\hat{x}_{\text{obs}} = (-\sin \phi, \cos \phi, 0)^T, \quad (C10)$$

$$\hat{y}_{\text{obs}} = (\cos \phi \cos \vartheta, \sin \phi \cos \vartheta, -\sin \vartheta)^T. \quad (C11)$$

We proceed by projecting the momentum vectors $\mathbf{p}$ and $\mathbf{p}_0$ into the new basis,

$$\mathbf{p}_{\text{obs}} = \langle \mathbf{p}, \hat{x}_{\text{obs}} \rangle \hat{x}_{\text{obs}} + \langle \mathbf{p}, \hat{y}_{\text{obs}} \rangle \hat{y}_{\text{obs}} + \langle \mathbf{p}, \hat{z}_{\text{obs}} \rangle \hat{z}_{\text{obs}}, \quad (C12)$$

$$\mathbf{p}_{0,\text{obs}} = \langle \mathbf{p}_0, \hat{x}_{\text{obs}} \rangle \hat{x}_{\text{obs}} + \langle \mathbf{p}_0, \hat{y}_{\text{obs}} \rangle \hat{y}_{\text{obs}} + \langle \mathbf{p}_0, \hat{z}_{\text{obs}} \rangle \hat{z}_{\text{obs}}. \quad (C13)$$

We can now consider arbitrary orientations of the jet axis with respect to the LOS by defining the jet vector in S_{obs} to be

$$\mathbf{j}_{\text{obs}} = \cos \phi_{\text{jet}} \sin \vartheta_{\text{jet}} \hat{x}_{\text{obs}} + \sin \phi_{\text{jet}} \sin \vartheta_{\text{jet}} \hat{y}_{\text{obs}} + \cos \vartheta_{\text{jet}} \hat{z}_{\text{obs}}, \quad (C14)$$

with some values for ϕ_{jet} and ϑ_{jet} . The ϑ_{jet} angle is related to the angle θ_{obs} between the LOS and the jet axis through $\theta_{\text{obs}} = \pi/2 - \vartheta_{\text{jet}}$ (here we choose $\phi_{\text{jet}} = \pi$ and $\vartheta_{\text{jet}} = \pi/2$).

Only photons will be included in the cascade flux for which the angle α_{obs} between the initial photon momentum $\mathbf{p}_{0,\text{obs}}$ and the jet axis $\mathbf{j}_{\text{obs}}$ is smaller than the assumed half-opening angle of the jet, $\theta_{\text{jet}}/2$,

$$\cos \alpha_{\text{obs}} = \langle -\mathbf{j}_{\text{obs}}, \mathbf{p}_{0,\text{obs}} \rangle \geq \cos(\theta_{\text{jet}}/2). \quad (C15)$$

In this way, we can use the same simulation for arbitrary angles between the jet axis and the LOS.

Appendix D

Details on Fits with Halo Components

In this appendix, we provide additional details on the combined fits of LAT and H.E.S.S. data in the presence of a halo.

D.1. Best-fit Parameters

The best-fit parameters for the spectrum in Equation (1) for all sources for all tested values of the IGMF and t_{max} are reported in Table 4. For simplicity, E_0 is fixed to 1 TeV. Example spectra for all sources for three different values of the IGMF and $t_{\text{max}} = 10^7$ yr are shown in Figure 6 (same as

Figure 3 in the main text). From Figure 6 and the best-fit values of κ in the last column of Table 4, it becomes clear that exponential cutoffs at lower energies are preferred for low magnetic fields. This again shows the absence of a halo, as a lower-energy cutoff leads to fewer cascade photons. Figure 6 also illustrates that an increasing magnetic field leads to a suppression of the cascade at lower energies. Under the assumption that the coherence length of the magnetic field is much larger than the IC cooling length, the deflection of the pairs roughly scales as $E_e^{-2} B$, where E_e is the electron energy (Neronov & Semikoz 2009). As B increases, the low-energy pairs in particular will exhibit a large deflection and the upscattered cascade emission will not reach the observer. As a consequence, the peak of the cascade emission shifts toward higher energies as can be seen in each row of Figure 6.

D.2. Likelihood Profiles

In Figure 7, we show the likelihood ratios $\lambda(B)$ combined for all sources as defined in Equation (2) for our choice of different blazar activity times (black solid lines). In addition, we show the likelihood ratios $-2\Delta \ln \mathcal{L}_i$ for the individual sources as colored lines. It is evident that shorter activity times lead to weaker constraints on the IGMF, as the likelihood curves are consistently shifted toward lower values of B .

D.3. Additional Systematic Uncertainties

In the following, the effects of systematic uncertainties in addition to the unknown blazar activity time are discussed.

Increasing the jet opening angle θ_{jet} has a similar effect to increasing t_{max} . Larger jet opening angles will lead to larger halos and larger cascade fluxes as fewer gamma rays are rejected in our parallel transport prescription (see Section C.1). This makes sense, as photons emitted along the edge of the jet could be deflected toward the observer. However, given the observed spread of θ_{jet} (e.g., Jorstad et al. 2017), the uncertainty is subdominant compared to the uncertain activity time. Similarly, the choice of the EBL model introduces a negligible uncertainty, as it typically affects the number of generated pairs of the order of $\sim 5\%$ in the energy and redshift range under consideration (Meyer et al. 2016).

Another potentially important systematic uncertainty is the difference in the absolute energy scales of H.E.S.S. and the LAT. For the LAT, the error on the energy scale is of the order of a few percent (Ackermann et al. 2012), whereas the reconstructed energies of gamma rays observed by IACTs have an uncertainty of typically 10% (Hofmann et al. 2000). We can allow for a relative shift in energy between the two instruments by adding a scaling parameter s in our fitting procedure, such that the model fluxes fitted to H.E.S.S. data are changed to $\phi(E) \rightarrow \phi(E(1+s))$. We constrain s to lie within ± 0.2 . Repeating the fits for all sources, we find that for low magnetic fields s tends to its lowest allowed value. This minimizes the cascade emission, as the H.E.S.S. data are effectively shifted to lower fluxes. With this systematic term included, the limits on the magnetic field are weakened and $B < 5.3 \times 10^{-16}$ G is ruled out for $t_{\text{max}} = 10$ yr.

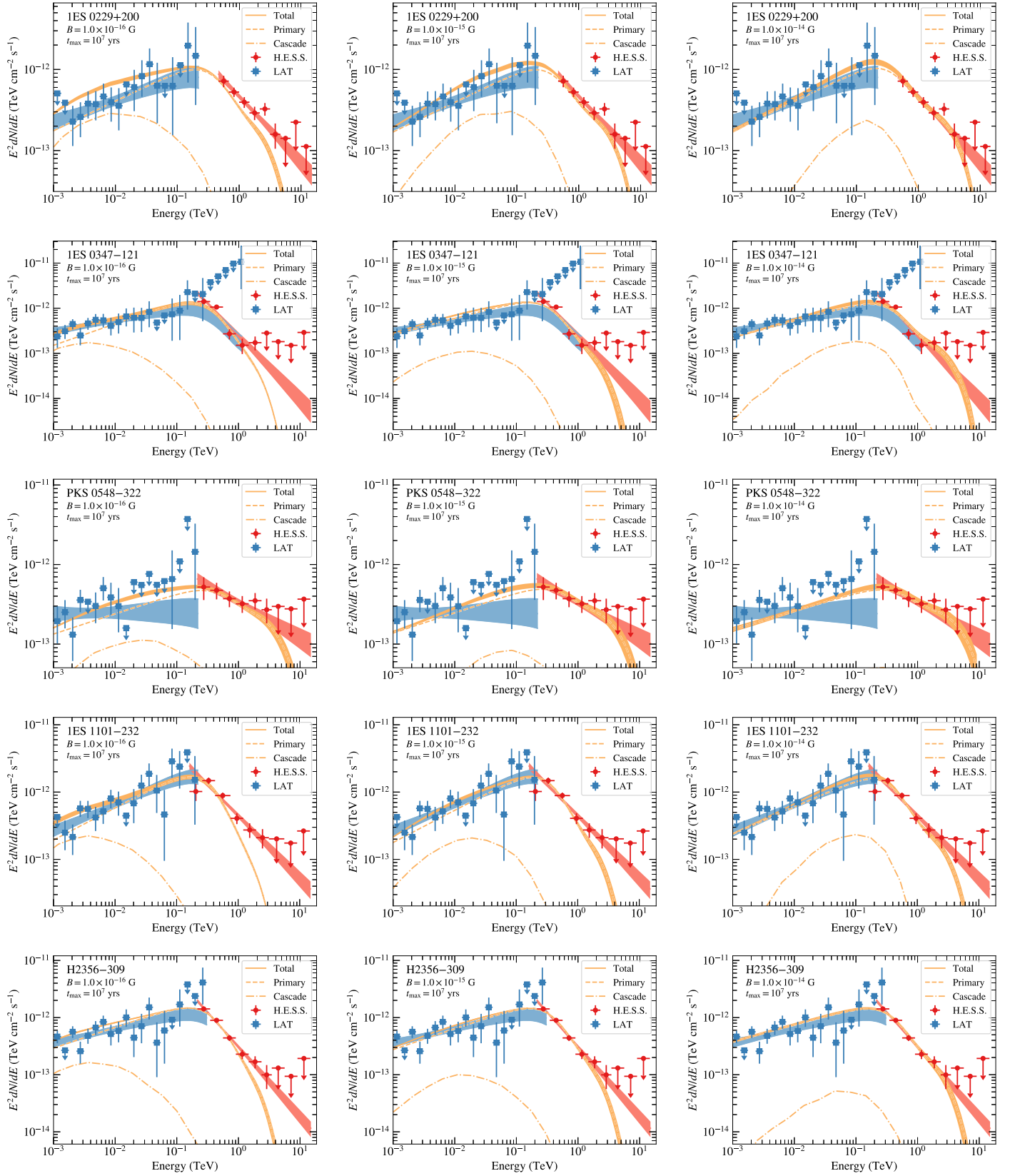


Figure 6. Best-fit spectra assuming a point-source model in addition to the halo flux templates for a combined LAT and H.E.S.S. analysis. An activity time of $t_{\max} = 10^7$ yr is assumed for all sources. The columns show different field strengths $B \in [10^{-16}, 10^{-15}, 10^{-14}]$ G, and each source is shown in one row. A coherence length of 1 Mpc is assumed throughout, together with the EBL model of Domínguez et al. (2011). Blue and red markers and lines show the point-source spectra measured with the LAT and H.E.S.S., respectively.

Table 4
Best-fit Parameters for the Combined LAT and H.E.S.S. Data in the Presence of a Halo

Source Name	IGMF Strength ($\log_{10}(B/G)$)	$N_{0,\text{int}}$ ($10^{-12} \text{ TeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1}$)	Γ_{int}	E_{cut} (TeV)
$t_{\text{max}} = 10 \text{ yr}$				
1ES 0229+200	−16.0	2.114 ± 0.223	1.632 ± 0.004	8.103 ± 3.022
1ES 0229+200	−15.5	2.160 ± 0.066	1.633 ± 0.003	8.865 ± 2.414
1ES 0229+200	−15.0	2.236 ± 6.016	1.639 ± 0.297	8.970 ± 10.878
1ES 0229+200	−14.5	2.260 ± 0.073	1.635 ± 0.007	10.031 ± 3.545
1ES 0229+200	−14.0	2.261 ± 0.085	1.639 ± 0.009	10.996 ± 0.500
1ES 0229+200	−13.5	2.300 ± 0.105	1.638 ± 0.011	11.000 ± 0.080
1ES 0229+200	−13.0	2.308 ± 0.092	1.638 ± 0.010	10.973 ± 1.487
1ES 0347−121	−16.0	2.945 ± 0.063	1.633 ± 0.005	3.970 ± 1.244
1ES 0347−121	−15.5	2.902 ± 0.119	1.633 ± 0.007	5.346 ± 2.173
1ES 0347−121	−15.0	2.907 ± 0.104	1.655 ± 0.007	5.901 ± 2.799
1ES 0347−121	−14.5	3.020 ± 0.093	1.633 ± 0.006	5.134 ± 2.421
1ES 0347−121	−14.0	3.137 ± 0.087	1.631 ± 0.005	4.019 ± 1.721
1ES 0347−121	−13.5	3.244 ± 0.066	1.633 ± 0.004	3.610 ± 1.410
1ES 0347−121	−13.0	2.797 ± 0.148	1.659 ± 0.012	11.000 ± 0.014
1ES 1101−232	−16.0	3.360 ± 0.111	1.632 ± 0.003	5.948 ± 1.609
1ES 1101−232	−15.5	3.109 ± 0.025	1.627 ± 0.002	10.906 ± 1.529
1ES 1101−232	−15.0	3.438 ± 0.056	1.633 ± 0.002	9.652 ± 3.680
1ES 1101−232	−14.5	3.625 ± 0.174	1.633 ± 0.008	9.517 ± 3.018
1ES 1101−232	−14.0	3.607 ± 0.184	1.627 ± 0.012	10.998 ± 0.315
1ES 1101−232	−13.5	3.706 ± 3.540	1.633 ± 0.010	10.777 ± 88.543
1ES 1101−232	−13.0	3.738 ± 0.540	1.632 ± 0.012	10.198 ± 14.941
H2356−309	−16.0	2.754 ± 0.075	1.717 ± 0.005	2.832 ± 0.573
H2356−309	−15.5	2.754 ± 0.690	1.726 ± 0.046	2.924 ± 0.895
H2356−309	−15.0	2.780 ± 0.591	1.727 ± 0.038	2.907 ± 1.988
H2356−309	−14.5	2.890 ± 0.024	1.710 ± 0.002	2.637 ± 0.503
H2356−309	−14.0	2.997 ± 0.049	1.707 ± 0.005	2.383 ± 0.437
H2356−309	−13.5	2.997 ± 0.046	1.697 ± 0.003	2.383 ± 0.436
H2356−309	−13.0	3.001 ± 0.058	1.696 ± 0.004	2.401 ± 0.450
PKS 0548−322	−16.0	7.520 ± 0.071	1.774 ± 0.008	7.621 ± 0.077
PKS 0548−322	−15.5	7.158 ± 0.161	1.803 ± 0.004	10.203 ± 4.209
PKS 0548−322	−15.0	7.449 ± 0.310	1.794 ± 0.008	9.973 ± 5.004
PKS 0548−322	−14.5	7.449 ± 0.294	1.789 ± 0.007	10.906 ± 3.623
PKS 0548−322	−14.0	7.853 ± 0.313	1.780 ± 0.008	9.150 ± 5.184
PKS 0548−322	−13.5	7.853 ± 0.306	1.780 ± 0.008	9.150 ± 5.177
PKS 0548−322	−13.0	7.853 ± 0.307	1.780 ± 0.009	9.150 ± 5.211
$t_{\text{max}} = 10^4 \text{ yr}$				
1ES 0229+200	−16.0	2.257 ± 0.061	1.633 ± 0.001	3.171 ± 0.456
1ES 0229+200	−15.5	2.274 ± 0.038	1.632 ± 0.002	4.106 ± 0.690
1ES 0229+200	−15.0	2.142 ± 0.046	1.633 ± 0.001	6.321 ± 1.301
1ES 0229+200	−14.5	2.146 ± 0.067	1.632 ± 0.004	8.070 ± 2.014
1ES 0229+200	−14.0	2.206 ± 0.083	1.633 ± 0.005	8.673 ± 2.458
1ES 0229+200	−13.5	2.217 ± 0.344	1.646 ± 0.013	9.921 ± 9.287
1ES 0229+200	−13.0	2.227 ± 0.106	1.644 ± 0.011	10.979 ± 1.248
1ES 0347−121	−16.0	4.398 ± 0.052	1.520 ± 0.003	1.000 ± 0.000
1ES 0347−121	−15.5	3.618 ± 0.041	1.626 ± 0.002	1.269 ± 0.210
1ES 0347−121	−15.0	2.997 ± 0.065	1.633 ± 0.002	2.976 ± 0.319
1ES 0347−121	−14.5	2.948 ± 0.009	1.637 ± 0.005	4.149 ± 0.013
1ES 0347−121	−14.0	2.965 ± 0.056	1.636 ± 0.004	5.046 ± 1.309
1ES 0347−121	−13.5	2.964 ± 0.042	1.644 ± 0.003	5.222 ± 1.402
1ES 0347−121	−13.0	2.960 ± 0.085	1.656 ± 0.006	5.022 ± 2.266
1ES 1101−232	−16.0	3.534 ± 0.087	1.633 ± 0.002	1.747 ± 0.258
1ES 1101−232	−15.5	3.366 ± 0.022	1.633 ± 0.001	2.897 ± 0.519
1ES 1101−232	−15.0	3.364 ± 0.059	1.632 ± 0.003	4.254 ± 0.951
1ES 1101−232	−14.5	3.378 ± 0.069	1.631 ± 0.004	6.024 ± 1.563
1ES 1101−232	−14.0	3.197 ± 0.024	1.625 ± 0.001	10.368 ± 2.810
1ES 1101−232	−13.5	3.365 ± 0.093	1.632 ± 0.005	10.964 ± 1.380
1ES 1101−232	−13.0	3.538 ± 0.084	1.631 ± 0.005	10.991 ± 0.715

Table 4
(Continued)

Source Name	IGMF Strength ($\log_{10}(B/G)$)	$N_{0,\text{int}}$ ($10^{-12} \text{ TeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1}$)	Γ_{int}	E_{cut} (TeV)
H2356–309	–16.0	3.555 ± 3.139	1.633 ± 0.002	1.255 ± 2.016
H2356–309	–15.5	3.696 ± 0.036	1.633 ± 0.002	1.328 ± 0.148
H2356–309	–15.0	3.494 ± 0.043	1.634 ± 0.002	1.640 ± 0.214
H2356–309	–14.5	2.789 ± 0.004	1.725 ± 0.006	2.704 ± 0.004
H2356–309	–14.0	2.795 ± 7.856	1.726 ± 0.159	2.770 ± 3.188
H2356–309	–13.5	2.841 ± 0.034	1.723 ± 0.002	2.703 ± 0.524
H2356–309	–13.0	2.900 ± 0.037	1.703 ± 0.003	2.638 ± 0.510
PKS 0548–322	–16.0	7.793 ± 0.080	1.745 ± 0.001	5.245 ± 1.428
PKS 0548–322	–15.5	7.877 ± 0.129	1.745 ± 0.002	5.870 ± 1.744
PKS 0548–322	–15.0	7.680 ± 0.250	1.768 ± 0.008	6.844 ± 2.431
PKS 0548–322	–14.5	7.610 ± 0.237	1.768 ± 0.006	8.011 ± 3.147
PKS 0548–322	–14.0	7.539 ± 0.284	1.783 ± 0.007	9.001 ± 4.146
PKS 0548–322	–13.5	7.543 ± 0.301	1.782 ± 0.009	10.057 ± 5.377
PKS 0548–322	–13.0	7.554 ± 0.407	1.786 ± 0.011	10.222 ± 5.494
$t_{\text{max}} = 10^7 \text{ yr}$				
1ES 0229+200	–16.0	2.217 ± 0.042	1.633 ± 0.001	2.880 ± 0.408
1ES 0229+200	–15.5	2.166 ± 0.030	1.633 ± 0.001	3.667 ± 0.552
1ES 0229+200	–15.0	2.144 ± 0.044	1.633 ± 0.001	5.209 ± 0.959
1ES 0229+200	–14.5	2.129 ± 0.165	1.633 ± 0.003	7.099 ± 2.412
1ES 0229+200	–14.0	2.201 ± 0.104	1.632 ± 0.005	7.814 ± 2.125
1ES 0229+200	–13.5	2.225 ± 0.124	1.635 ± 0.011	9.109 ± 3.505
1ES 0229+200	–13.0	2.225 ± 0.080	1.635 ± 0.008	10.584 ± 3.262
1ES 0347–121	–16.0	4.133 ± 0.418	1.520 ± 0.001	1.000 ± 0.000
1ES 0347–121	–15.5	4.462 ± 0.060	1.520 ± 0.002	1.000 ± 0.005
1ES 0347–121	–15.0	3.257 ± 0.055	1.632 ± 0.003	1.638 ± 0.324
1ES 0347–121	–14.5	2.960 ± 0.317	1.632 ± 0.004	3.020 ± 0.482
1ES 0347–121	–14.0	2.824 ± 0.117	1.632 ± 0.002	5.152 ± 2.231
1ES 0347–121	–13.5	2.655 ± 1.179	1.672 ± 0.088	8.368 ± 6.833
1ES 0347–121	–13.0	2.656 ± 0.241	1.672 ± 0.023	10.998 ± 0.100
1ES 1101–232	–16.0	5.335 ± 0.435	1.520 ± 0.002	1.001 ± 0.012
1ES 1101–232	–15.5	5.183 ± 0.081	1.520 ± 0.002	1.167 ± 0.139
1ES 1101–232	–15.0	4.893 ± 0.042	1.520 ± 0.001	1.766 ± 0.262
1ES 1101–232	–14.5	4.651 ± 0.149	1.553 ± 0.010	2.357 ± 0.224
1ES 1101–232	–14.0	3.810 ± 0.044	1.599 ± 0.002	4.753 ± 1.205
1ES 1101–232	–13.5	3.843 ± 0.080	1.600 ± 0.004	5.675 ± 1.756
1ES 1101–232	–13.0	3.858 ± 0.070	1.604 ± 0.004	6.623 ± 2.599
H2356–309	–16.0	3.709 ± 0.025	1.632 ± 0.001	1.085 ± 0.100
H2356–309	–15.5	3.411 ± 0.096	1.632 ± 0.003	1.421 ± 0.176
H2356–309	–15.0	3.486 ± 0.042	1.632 ± 0.002	1.527 ± 0.186
H2356–309	–14.5	3.331 ± 0.046	1.663 ± 0.003	1.739 ± 0.239
H2356–309	–14.0	2.875 ± 0.107	1.706 ± 0.007	2.571 ± 0.526
H2356–309	–13.5	2.877 ± 0.042	1.703 ± 0.003	2.642 ± 0.501
H2356–309	–13.0	2.878 ± 0.040	1.709 ± 0.003	2.646 ± 0.510
PKS 0548–322	–16.0	7.790 ± 0.097	1.745 ± 0.001	5.039 ± 1.201
PKS 0548–322	–15.5	7.781 ± 0.084	1.745 ± 0.001	5.821 ± 1.684
PKS 0548–322	–15.0	8.004 ± 0.249	1.745 ± 0.004	5.895 ± 1.845
PKS 0548–322	–14.5	7.836 ± 0.969	1.765 ± 0.023	7.142 ± 3.571
PKS 0548–322	–14.0	7.483 ± 0.336	1.769 ± 0.009	9.153 ± 4.287
PKS 0548–322	–13.5	7.482 ± 0.297	1.783 ± 0.008	10.372 ± 5.814
PKS 0548–322	–13.0	7.489 ± 0.412	1.792 ± 0.011	10.988 ± 2.337

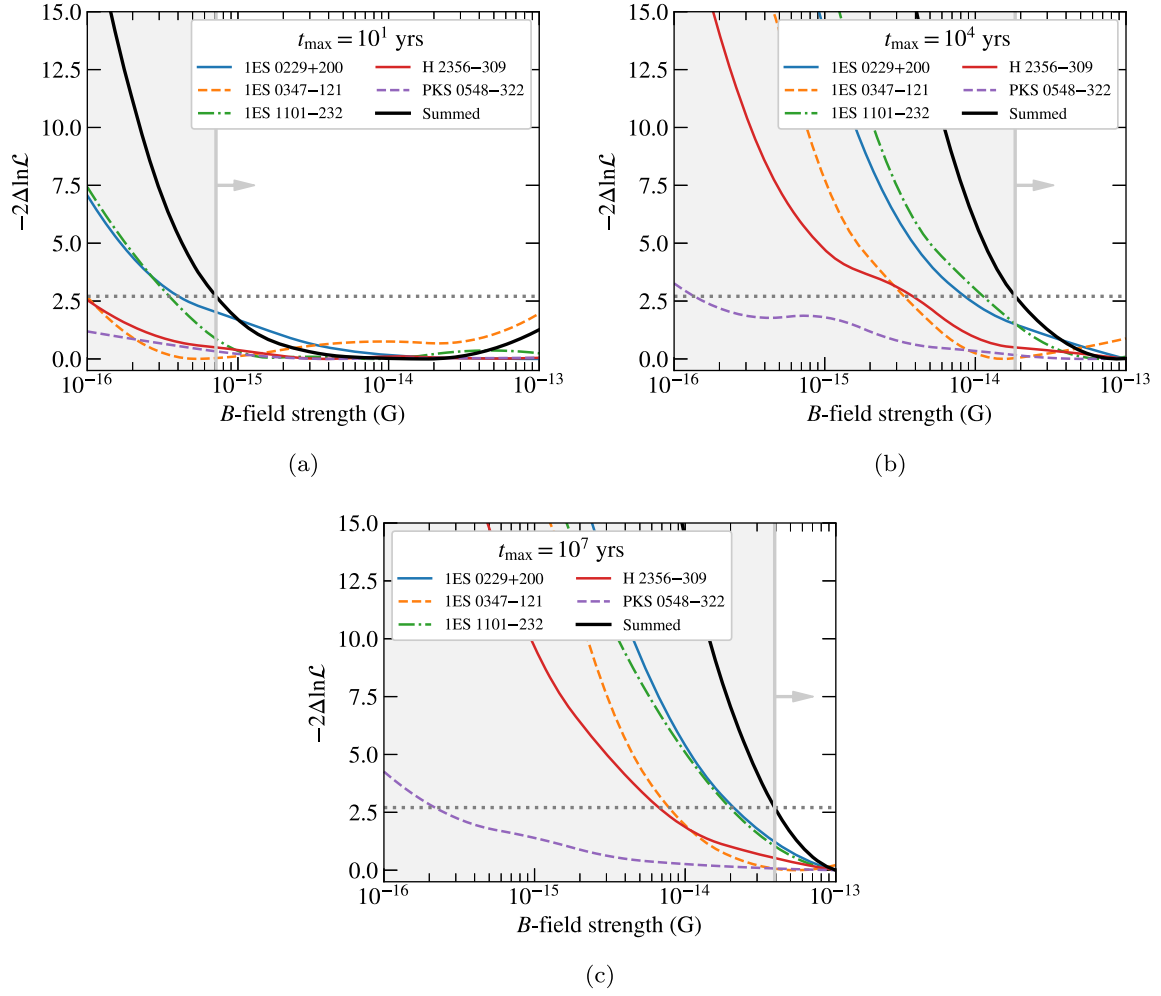


Figure 7. Likelihood profiles as a function of the IGMF strength for (a) $t_{\max} = 10$ yr, (b) $t_{\max} = 10^4$ yr, and (c) $t_{\max} = 10^7$ yr. Magnetic field values resulting in differences in the likelihood $-2\Delta \ln \mathcal{L} > 2.71$ (indicated by the gray dotted line) are ruled out at the 95% confidence level, which is shown by the gray shaded region and arrow. The likelihood curves are smoothed using a quadratic spline interpolation.

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