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Search for an invisible Z' in a final state with two muons and missing energy at Belle II

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The $L_\mu - L_\tau$ extension of the standard model predicts the existence of a lepton-flavor-universality-violating Z' boson that couples only to the heavier lepton families. We search for such a Z' through

its invisible decay in the process $e^+e^- \to \mu^+\mu^- Z'$. We use a sample of electron-positron collisions at a center-of-mass energy of 10.58 GeV collected by the Belle II experiment in 2019–2020, corresponding to an integrated luminosity of 79.7 fb^{-1}. We find no excess over the expected standard-model background. We set 90%-confidence-level upper limits on the cross section for this process as well as on the coupling of the model, which ranges from 3×10^{-3} at low Z' masses to 1 at Z' masses of 8 GeV/c^2.

Recent experimental observations are in tension with the standard model (SM) of particle physics. A notable example is the difference between the measured and expected values of the muon anomalous magnetic moment [1, 2]. In addition, the SM is known to provide an incomplete description of nature since, among other prominent issues, it does not address the phenomenology related to the existence of dark matter [3], specifically the prediction of the observed relic density. A simple way to explain both phenomena is the $L_\mu - L_\tau$ extension of the SM [4–6]. This model gauges the difference of the muon and tau lepton numbers, giving rise to a massive, electrically neutral, vector boson, the Z'. This particle would couple to the SM only through μ, τ, ν_μ, and ν_τ with coupling g'. The Z', with such a lepton-flavor-universality-violating coupling, would contribute to the muon magnetic moment and, for certain values of g' and $M_{Z'}$, would explain the observed anomaly [7]. This model also reproduces the observed dark-matter relic density, assuming dark matter is charged under $L_\mu - L_\tau$ [5, 8], and resolves the tensions in $b \to s\ell^+\ell^-$ ($\ell = e, \mu$) decays reported by the LHCb collaboration [9–12].

In this Letter, we report a search for the Z' in the process $e^+e^- \to \mu^+\mu^- Z'$ with $Z' \to$ invisible, where the Z' is radiated off a muon. If the Z' couples only to SM particles, a model henceforth referred to as the "vanilla" $L_\mu - L_\tau$ model, the branching fraction to neutrinos $\mathcal{B}(\mathrm{Z}' \to \nu\bar{\nu})$ varies between 33% and 100% depending on the Z' mass [13, 14].

If the Z' can decay directly into a pair of dark matter particles $\chi\bar{\chi}$ with a coupling constant $\alpha_\mathrm{D} = {g'_\mathrm{D}}^2/4\pi$ one expects $g'_\mathrm{D} \gg g'$, which implies $\mathcal{B}(\mathrm{Z}' \to \chi\bar{\chi}) \approx 1$: we henceforth refer to this possibility as the "fully invisible" $L_\mu - L_\tau$ model. We provide results for each scenario. In the vanilla model, the intrinsic width $\Gamma_{Z'}$ of the Z' is negligible compared to the experimental resolution. In the fully invisible model, $\Gamma_{Z'}$ depends on α_D: it is negligible for values of α_D smaller than 1 for $M_{Z'} \approx 1.5$ GeV/c^2, and smaller than 0.1 for $M_{Z'} \approx 4.5$ GeV/c^2. We focus our analysis on the case in which $\mathcal{B}(\mathrm{Z}' \to \chi\bar{\chi}) \approx 1$ and $\Gamma_{Z'}$ is negligible. We study separately one example in which $\Gamma_{Z'}$ is not negligible and assume one benchmark value such that $\Gamma_{Z'} = 0.1 M_{Z'}$, corresponding to $\alpha_\mathrm{D} = 2.9$.

Searches for a Z' decaying to muons have been performed by the *BABAR* [15], Belle [16], and CMS [17] experiments, and for low-mass invisible Z' decays by the NA64-e experiment [18]. Belle II has previously conducted a search for a Z' decaying invisibly using data collected during the commissioning run in 2018, with a luminosity of 0.276 fb^{-1} [19].

We use a sample of e^+e^- collisions collected by Belle II at the center-of-mass (c.m.) energy of the $\Upsilon(4\mathrm{S})$ resonance, 10.58 GeV, in 2019–2020, corresponding to a total integrated luminosity of 79.7 fb^{-1} [20]. This search supersedes that in Ref. [19], with an integrated luminosity nearly 300 times larger, improved muon identification, and the use of refined analysis algorithms.

The invisible-Z' signature is a narrow enhancement in the distribution of the mass M_recoil of the system recoiling against a muon pair. In the following, recoil quantities are computed against the two muons. These quantities coincide with Z' properties for signal events and typically correspond to undetected SM particles for background. In the analysis, we use the recoil mass squared M^2_recoil since this quantity is smoother than M_recoil for low masses, where negative M^2_recoil values may be observed due to resolution effects. We select events with exactly two charged particles identified as muons, and negligible additional activity in the detector. The dominant backgrounds are final states with two muons and missing energy. These are primarily $e^+e^- \to \mu^+\mu^-(\gamma)$ events with one or more undetected photons, $e^+e^- \to \tau^+\tau^-(\gamma)$ events with both τ leptons decaying to muons and neutrinos, and $e^+e^- \to e^+e^-\mu^+\mu^-$ events with electrons outside the detector acceptance.

We extract the signal yield from a fit to the two-dimensional distribution of the polar angle of the recoil momentum θ_recoil and M^2_recoil. Control samples are used to check simulation predictions and to infer correction factors. Selections are optimized using simulated events prior to examining data. However, once data were examined, we found an unexpected background source in the signal region that was taken into account with a rescaling procedure.

The Belle II detector [21] operates at the interaction region of the SuperKEKB electron-positron collider [22], located at KEK in Tsukuba, Japan. The energies of the electron and positron beams are 7 GeV and 4 GeV with a boost of the c.m. frame $\beta\gamma = 0.28$ relative to the laboratory frame. The detector consists of several subdetectors arranged around the beam pipe in a cylindrical structure. Subdetectors relevant for this analysis are briefly described here in order from innermost out; more details are given in Ref. [21, 23]. The innermost component is the vertex detector, consisting of two inner layers of silicon pixels and four outer layers of silicon strips. The second pixel layer is partially installed, covering one sixth of the azimuthal angle. The main tracking subdetector

is a large helium-based small-cell drift chamber. An electromagnetic calorimeter (ECL) consists of a barrel and two endcaps made of CsI(Tl) crystals. A superconducting solenoid provides a 1.5 T magnetic field. A K_L^0 and muon subdetector is made of iron plates providing the magnetic flux-return yoke, alternated with resistive-plate chambers and plastic scintillators in the barrel, and with plastic scintillators only in the endcaps. The longitudinal and transverse directions, and polar angle θ are defined with respect to the detector's cylindrical axis in the direction of the electron beam. In the following, quantities are defined in the laboratory frame unless otherwise specified.

Identification of muons relies mostly on charged-particle penetration depth in the muon detector for momenta larger than 0.7 GeV/c and on information from the drift chamber and ECL otherwise. The ratio between the muon likelihood and the sum of the likelihoods of all particle hypotheses is required to be greater than 0.5. This retains 93–99% of muons, and rejects 80–97% of pions, depending on their momenta. Electrons, used in control-sample studies, are identified primarily by comparing momenta with energies of associated ECL depositions, with a similar likelihood-ratio method. Photons are reconstructed from ECL depositions with energy greater than 100 MeV that are not associated with any track.

Signal events are simulated using `MadGraph 5` [24] with initial state radiation. The signal $M^2_{\rm recoil}$ resolution ranges from a minimum of 0.06 GeV$^2/c^4$ at 80 GeV$^2/c^4$ to a maximum of 0.23 GeV$^2/c^4$ at 9 GeV$^2/c^4$. We generate 582 Z' samples, with negligible $\Gamma_{Z'}$, corresponding to mass hypotheses ranging from 0.01 to 8.5 GeV/c^2 in steps of 3 to 202 MeV/c^2, following the resolution. Background events are simulated using the following generators: $e^+e^- \to \mu^+\mu^-(\gamma)$ with `KKMC` [25], $e^+e^- \to \tau^+\tau^-(\gamma)$ with `KKMC` [25] in combination with `TAUOLA` [26], $e^+e^- \to e^+e^-\mu^+\mu^-$ and $e^+e^- \to e^+e^-e^+e^-$ with `AAFH` [27], $e^+e^- \to \pi^+\pi^-(\gamma)$ with `PHOKHARA` [28], and $e^+e^- \to e^+e^-(\gamma)$ with `BabaYaga@NLO` [29]. Backgrounds coming from the final states $q\bar{q}$ ($q = u, d, s, c, b$), $J/\psi\gamma$ and $\psi(2S)\gamma$ with $J/\psi, \psi(2S) \to \mu^+\mu^-$, and $\mu^+\mu^-\nu\bar{\nu}$ are found to be negligible. Detector geometry and interactions of final-state particles with the detector material are simulated using `GEANT4` [30] and the Belle II Analysis Software Framework [31, 32].

The search uses an online event selection (trigger) that requires events with at least one pair of tracks in a restricted polar-angle acceptance, $\theta \in [37, 120]^\circ$, and an azimuthal opening angle larger than 90° or 30° for data collected in 2019 and 2020, respectively (two-track trigger). Events consistent with Bhabha scattering are rejected by a dedicated trigger veto.

In the offline analysis, we require that tracks originate from the interaction point, with transverse and longitudinal projections of their distance of closest approach smaller than 0.5 and 2.0 cm, respectively, to reject spurious and beam-induced background tracks. We require events to have exactly two oppositely charged particles identified as muons, that pass the trigger requirements and have transverse momenta larger than 0.4 GeV/c. We reject events with opening angles between the muons in the c.m. frame larger than 179°, to suppress $\mu^+\mu^-(\gamma)$ backgrounds. For $M^2_{\rm recoil} < 4$ GeV$^2/c^4$, most of the background comes from $\mu^+\mu^-(\gamma)$ events with single-photon emission: we require $\theta_{\rm recoil}$ to be within the ECL barrel acceptance $[34, 123]^\circ$ so as to exclude regions where photons can escape undetected. Additionally, we reject events with $\theta_{\rm recoil} \in [89, 91]^\circ$, where there is a 1.5 mm-wide gap in the ECL instrumentation. For $M^2_{\rm recoil} > 4$ GeV$^2/c^4$, most of the background comes from $\mu^+\mu^-(\gamma)$ events with multiple photon emission and the correlation between the photon direction and $\theta_{\rm recoil}$ is lost: we require $\theta_{\rm recoil} < 123^\circ$ because the signal is dominantly produced in the forward direction due to the c.m. boost. To suppress $\mu^+\mu^-(\gamma)$ backgrounds, we impose a photon veto: we require the total energy of all photons to be less than 0.5 GeV and no photon be within 15° of the recoil momentum. To suppress $\mu^+\mu^-(\gamma)$ and $e^+e^-\mu^+\mu^-$ backgrounds, we require that the transverse recoil momentum in the c.m. frame exceed 0.5 GeV/c.

The remaining background comes dominantly from $\tau^+\tau^-(\gamma)$ events with τ leptons decaying to muons or pions misidentified as muons in the region $M^2_{\rm recoil} < 50$ GeV$^2/c^4$ and from $e^+e^-\mu^+\mu^-$ events elsewhere. The background from $e^+e^- \to \mu^+\mu^-(\gamma)$ is subleading across the entire mass range.

The final selection uses an artificial neural network, denoted as Punzi-net [33], trained on simulated signal and background events, and specifically designed to optimize a figure of merit [34] for all Z' mass hypotheses simultaneously. We use as inputs the four kinematic variables, all defined in the c.m. frame, with the highest discriminating power: the transverse momentum of a muon with respect to the dimuon thrust axis [35, 36]; the transverse momentum of the higher-energy muon with respect to the momentum direction of the lower-energy muon; the longitudinal momentum of the higher-energy muon with respect to the momentum direction of the lower-energy muon; and the transverse momentum of the dimuon system. The first three variables exploit mostly the kinematic properties of Z' production through radiation from a final state muon, compared to $\tau^+\tau^-(\gamma)$ events, in which the recoil momentum arises from neutrinos from τ decays. The fourth variable exploits the kinematic features of $\mu^+\mu^-(\gamma)$ and $e^+e^-\mu^+\mu^-$ backgrounds, typically produced with low transverse momenta. Additional details are given in Ref. [33].

The resulting signal efficiency is typically 5%, nearly uniform as a function of $M^2_{\rm recoil}$. The Punzi-net selection removes nearly all $\tau^+\tau^-(\gamma)$ background, except for a small contribution in the region $M^2_{\rm recoil} > 50$ GeV$^2/c^4$. The residual background comes dominantly

from $\mu^+\mu^-(\gamma)$ in the region $M^2_{\rm recoil} < 50$ GeV$^2/c^4$ and from a large contribution of $e^+e^-\mu^+\mu^-$ elsewhere. In particular, the region $M^2_{\rm recoil} < 1$ GeV$^2/c^4$ is dominated by the $\mu^+\mu^-(\gamma)$ process with a single photon emission. Above 1 GeV$^2/c^4$ the $\mu^+\mu^-(\gamma)$ process contributes mostly with events containing two radiated photons. Typically, one photon is collinear with the beams and outside the acceptance, while the other is emitted in the direction of one of the gaps between the barrel and the forward or backward ECL endcaps. For $M^2_{\rm recoil}$ in the 1–50 GeV$^2/c^4$ range, this produces two distinctive bands in the $\theta^{\rm c.m.}_{\rm recoil}$–$M^2_{\rm recoil}$ plane, where $\theta^{\rm c.m.}_{\rm recoil}$ is the polar angle of the recoil momentum in the c.m. frame. This feature is exploited in a two-dimensional fitting procedure, which incorporates the expected background shapes due to $\mu^+\mu^-(\gamma)$ events, doubling the sensitivity as compared to one-dimensional fitting.

We fit to data by maximizing a binned likelihood based on signal and background two-dimensional templates obtained from simulation. The parameter of interest is the signal cross section while the background normalization is determined by the fit. The $M^2_{\rm recoil}$ bin widths vary across the spectrum and are set to the signal $M^2_{\rm recoil}$ resolution. The binning in $\theta^{\rm c.m.}_{\rm recoil}$ reflects the distribution of $\mu^+\mu^-(\gamma)$ events, which depends on $M^2_{\rm recoil}$. The number of bins varies from one (for high $M^2_{\rm recoil}$) to five (for low $M^2_{\rm recoil}$). We perform a squared-mass scan in steps corresponding to one unit of signal $M^2_{\rm recoil}$ resolution, testing all simulated mass hypotheses. Each fit is performed in search windows of 20 $M^2_{\rm recoil}$ bins centered around each hypothesis. Uncorrelated systematic uncertainties on the signal and background shapes (see below) are included in the respective templates by introducing in each bin of the template Gaussian nuisance parameters constrained by the corresponding uncertainties. A frequentist procedure based on the profile-likelihood ratio $\tilde{t}_\mu$ [37] is used to obtain 90% confidence-level (CL) intervals on the cross section. We use the `pyhf` software package [38] for inference and check the consistency of our results with simplified simulated samples.

We also consider the scenario in which $\Gamma_{Z'}$ is not negligible, as expected for large $\alpha_{\rm D}$ values [9, 39], and study one benchmark case that assumes $\Gamma_{Z'} = 0.1 M_{Z'}$. We account for the non-zero width in the fitting procedure by changing the shape of the signal templates to Breit-Wigner distributions with the widths $\Gamma_{Z'}$ convolved with Gaussian resolution functions. We use only one-dimensional $M^2_{\rm recoil}$ templates and enlarge the search windows to cover the sizable signal width.

Three control samples are used to validate the analysis and estimate systematic uncertainties. The $\mu\mu\gamma$ control sample is obtained by reversing the photon-veto criteria thus requiring a photon of energy greater than 1 GeV within 15° of the recoil momentum direction. The $e\mu$ and ee control samples are obtained by requiring one or both tracks to be identified as electrons and then applying all the other selection criteria.

The efficiency of the two-track trigger is studied with the $e\mu$ control sample with events collected by an ECL-based trigger, which is used as a reference. This requires that the total energy deposition in the barrel and forward endcap exceed 1 GeV. The two-track trigger efficiency increases from 89 to 93% as a function of $M^2_{\rm recoil}$.

We use the ee control sample to study the photon-veto performance. We select events with $M^2_{\rm recoil} < 1$ GeV$^2/c^4$, since they come dominantly from Bhabha scattering with a single radiated photon. The results indicate that the photon-veto inefficiency in the backward barrel ECL is larger than that estimated in simulation. This study was performed after observing a large data-simulation disagreement in the signal region compatible with photon-veto inefficiency. The photon-veto inefficiencies measured with the ee control sample are used to correct the expected $\mu\mu$ background.

We estimate systematic uncertainties on the signal efficiency and on the signal and background template shapes. The uncertainties on the template shapes independently affect each of the bins contained within the templates.

Uncertainties in selection efficiencies due to data-simulation mismodeling are studied by comparing data and simulation in the $\mu\mu\gamma$ and $e\mu$ control samples in three $M^2_{\rm recoil}$ ranges: $[-0.5, 9]$, $[9, 36]$, $[36, 81]$ GeV$^2/c^4$. The two control samples provide complementary coverage of the $M^2_{\rm recoil}$ range, with $\mu\mu\gamma$ addressing the lower region and $e\mu$ covering the higher. Systematic uncertainties due to data-simulation mismodeling in the trigger, luminosity, tracking efficiency, muon identification, background cross sections, and effect of the selections are collectively evaluated through data-simulation comparison before the application of the Punzi-net. Systematic uncertainties due to the Punzi-net are evaluated by studying its efficiencies, as they are indicators of the performances for the signal-like background component. The differences from unity of the data-to-simulation ratios of event yields before the Punzi-net application, and between the Punzi-net efficiencies in the three $M^2_{\rm recoil}$ ranges are summed in quadrature and found to be 2.7%, 6.5%, and 8.3%, respectively. These differences are assigned as systematic uncertainties on the signal efficiency.

The recoil mass resolution is studied using the $\mu\mu\gamma$ sample. The width of the $M^2_{\rm recoil}$ distribution is 8% larger in data than in simulation. This translates to a systematic uncertainty of 10% on the signal template shape.

Systematic uncertainties due to background shapes are evaluated on the $\mu\mu\gamma$ and $e\mu$ samples. We compute the average data-to-simulation ratios for the number of events in each search window. We assign twice the largest standard deviation on these averages in each of the three $M^2_{\rm recoil}$ ranges as an uncertainty for the shape in the respective $M^2_{\rm recoil}$ ranges. We use the $\mu\mu\gamma$ control sample for $M^2_{\rm recoil}$ up to 56 GeV$^2/c^4$ and the $e\mu$ control sample

above. The resulting uncertainties are 3.2%, 8.6%, and 25% in the three $M^2_{\rm recoil}$ ranges.

Uncertainties on the background template shape from the photon-veto inefficiency are studied on the ee control sample and are on average 34% for $M^2_{\rm recoil} < 1$ GeV$^2/c^4$ decreasing to 5% above 1 GeV$^2/c^4$. We assign a systematic uncertainty of 1% to the measured integrated luminosity [20].

The observed and expected $M^2_{\rm recoil}$ distributions are shown in Fig. 1. We find no significant excess of data above the expected background. The χ^2 value describing the goodness of the two-dimensional fit is acceptable for each test Z' mass with the largest incompatibility corresponding to a p-value of 0.05. The largest local significance is 2.8σ for $M_{Z'} = 2.352$ GeV$/c^2$. The global significance of this excess after correcting for the look-elsewhere effect [40] is 0.7σ.

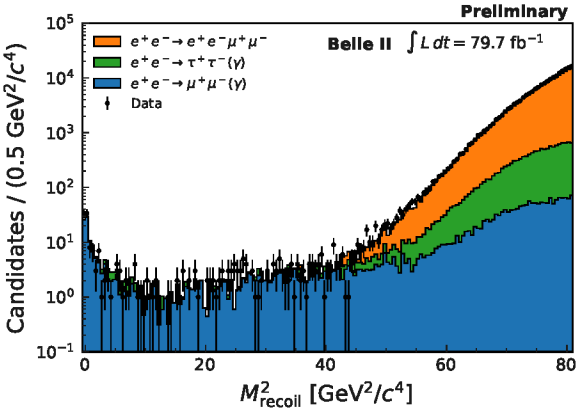

FIG. 1: Squared recoil mass spectrum of the $\mu^+\mu^-$ sample, compared with the stacked contributions from the various simulated background samples normalized to the integrated luminosity.

The 90% CL upper limits on the cross section for the process $e^+e^- \to \mu^+\mu^- Z'$ with Z' invisible, $\sigma(e^+e^- \to \mu^+\mu^- Z',\ Z' \to \text{invisible}) = \sigma(e^+e^- \to \mu^+\mu^- Z') \times \mathcal{B}(Z' \to \text{invisible})$, are shown in Fig. 2 as functions of $M_{Z'}$, along with the expected 1σ and 2σ bands of expected limits (median limits from background-only simulated samples). We set upper limits as small as 0.2 fb. In addition, we show upper limits for the benchmark scenario in which we assume non-negligible $\Gamma_{Z'}$.

Cross section results are translated into 90% CL upper limits on the coupling g' and shown in Fig. 3 in the fully invisible $L_\mu - L_\tau$ model for the cases of negligible and non-negligible $\Gamma_{Z'}$. For the case of negligible $\Gamma_{Z'}$, these constraints hold for $M_{Z'} \lesssim 6.5$ GeV$/c^2$. For $M_{Z'} > 6.5$ GeV$/c^2$, the assumption $\mathcal{B}(Z' \to \chi\bar{\chi}) \approx 1$ is not valid: numerical values in Fig. 3 can still be used, but need to be rescaled by $1/\sqrt{\mathcal{B}(Z' \to \chi\bar{\chi})}$, which depends on $\alpha_{\rm D}$. We also show limits from NA64-e [18] and the previous Belle II search [19]. Figure 4 presents limits in the vanilla $L_\mu - L_\tau$ model, together with limits from Belle [16], *BABAR* [15], and CMS [17] searches for $Z' \to \mu^+\mu^-$ and the constraints from NA64-e and Belle II [19]. In both fully invisible and vanilla models, we focus on the direct-search results and do not show constraints obtained from reanalyses of data from neutrino experiments [7, 41, 42]. Additional plots, including indirect constraints from neutrino experiments and detailed numerical results, are provided in the supplemental material [43].

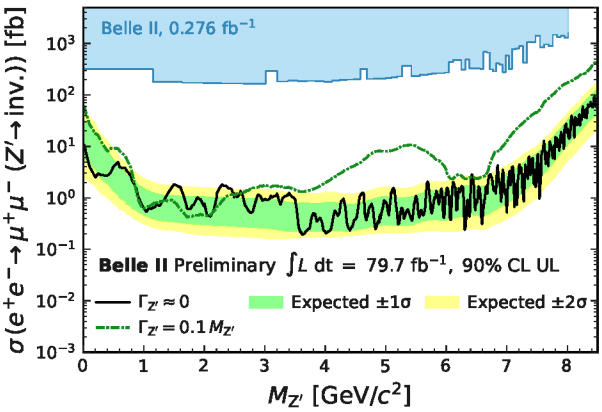

FIG. 2: Observed 90% CL upper limits on the cross section $\sigma(e^+e^- \to \mu^+\mu^- Z',\ Z' \to \text{invisible})$ as functions of the Z' mass for the cases of negligible $\Gamma_{Z'}$ and for $\Gamma_{Z'} = 0.1 M_{Z'}$. Also shown are previous limits from Belle II [19].

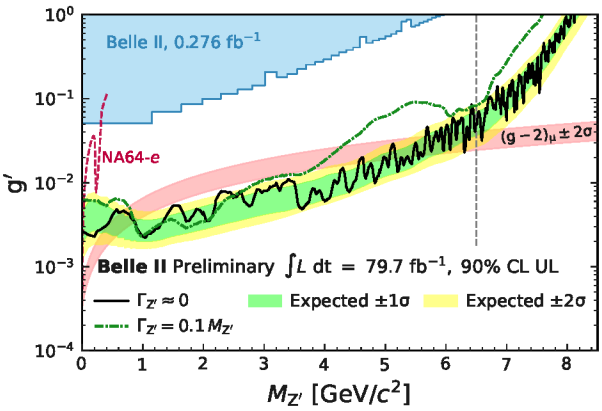

FIG. 3: Observed 90% CL upper limits on the coupling g' for the fully invisible $L_\mu - L_\tau$ model as functions of the Z' mass for the cases of negligible $\Gamma_{Z'}$ and for $\Gamma_{Z'} = 0.1 M_{Z'}$. Also shown are previous limits from NA64-e [18] and Belle II [19] searches. The red band shows the region that explains the muon anomalous magnetic moment $(g-2)_\mu \pm 2\sigma$ [2]. The vertical dashed line indicates the limit beyond which the hypothesis $\mathcal{B}(Z' \to \chi\bar{\chi}) \approx 1$ is not respected in the negligible $\Gamma_{Z'}$ case.

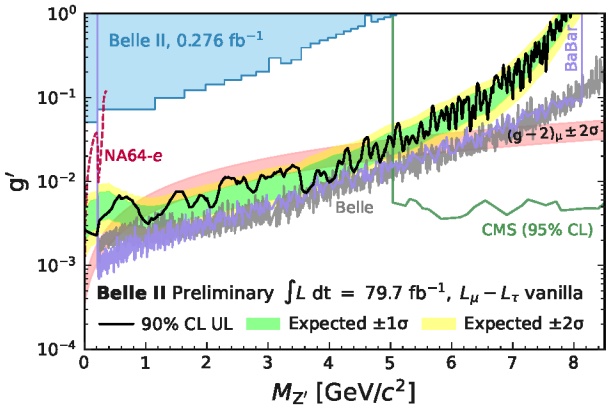

FIG. 4: Observed 90% CL upper limits on the coupling g' for the vanilla $L_\mu - L_\tau$ model as functions of the Z' mass. Also shown are previous limits from Belle II [19] and NA64-e [18] searches for invisible Z' decays, and from Belle [16], BaBar [15], and CMS [17] searches for Z' decays to muons (at 95% CL). The red band shows the region that explains the muon anomalous magnetic moment $(g-2)_\mu \pm 2\sigma$ [2].

In summary, we search for an invisibly decaying Z' boson in the process $e^+e^- \to \mu^+\mu^- Z'$ using data corresponding to 79.7 fb^{-1} collected by Belle II at SuperKEKB in 2019–2020. We find no significant excess above the expected background and set 90% CL upper limits on the coupling g' ranging from 3×10^{-3} at low Z' masses to 1 for masses at 8 GeV/c^2. These are world-leading direct-search results for Z' masses above 11.5 MeV/c^2 in the fully invisible $L_\mu - L_\tau$ model and for masses in the range 11.5 to 211 MeV/c^2 in the vanilla $L_\mu - L_\tau$ model. These limits are the first direct-search results that exclude at 90% CL a fully invisible Z' boson as an explanation of the $(g-2)_\mu$ anomaly for $0.8 < M_{Z'} < 5.0$ GeV/c^2.

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and Generalitat Valenciana, Spain Grant No. CIDEGENT/2018/020 Ministry of Science and Technology and research Grants No. MOST106-2112-M-002-005-MY3 and No. MOST107-2119-M-002-035-MY3, and the Ministry of Education (Taiwan); Thailand Center of Excellence in Physics; TUBITAK ULAKBIM (Turkey); National Research Foundation of Ukraine, project No. 2020.02/0257, and Ministry of Education and Science of Ukraine; the U.S. National Science Foundation and research Grants No. PHY-1913789 and No. PHY-2111604, and the U.S. Department of Energy and research Awards No. DE-AC06-76RLO1830, No. DE-SC0007983, No. DE-SC0009824, No. DE-SC0009973, No. DE-SC0010007, No. DE-SC0010073, No. DE-SC0010118, No. DE-SC0010504, No. DE-SC0011784, No. DE-SC0012704, No. DE-SC0019230, No. DE-SC0021274, No. DE-SC0022350; and the Vietnam Academy of Science and Technology (VAST) under Grant No. DL0000.05/21-23.

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[43] See Supplemental Material at `http://XYZ` for additional plots.

Search for an invisible Z' in a final state with two muons and missing energy at Belle II

Belle II Collaboration

arXiv:2212.03066v1 [hep-ex] 6 Dec 2022

This material is submitted as supplementary information for the Electronic Physics Auxiliary Publication Service

We provide a text file with numerical results for the observed 90% CL upper limit on the cross section of $e^+e^- \to \mu^+\mu^- Z'$, with $Z' \to$ invisible as well as of the observed 90% CL upper limit on g' as functions of $M_{Z'}$.

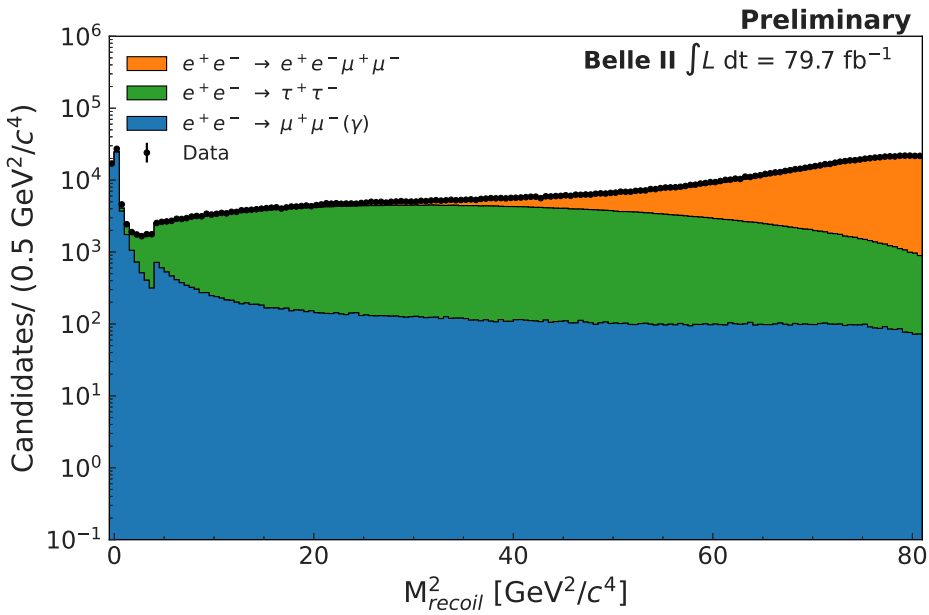

FIG. S1: Squared recoil mass spectrum for the $\mu^+\mu^-$ sample before the Punzi-net selection, compared with the stacked contributions from the various simulated background samples normalized to the integrated luminosity.

We also show the limits on g' as functions of $M_{Z'}$ on a logarithmic scale in Fig. S3 for the $L_\mu - L_\tau$ vanilla model and in Fig. S5 for the $L_\mu - L_\tau$ fully invisible model.

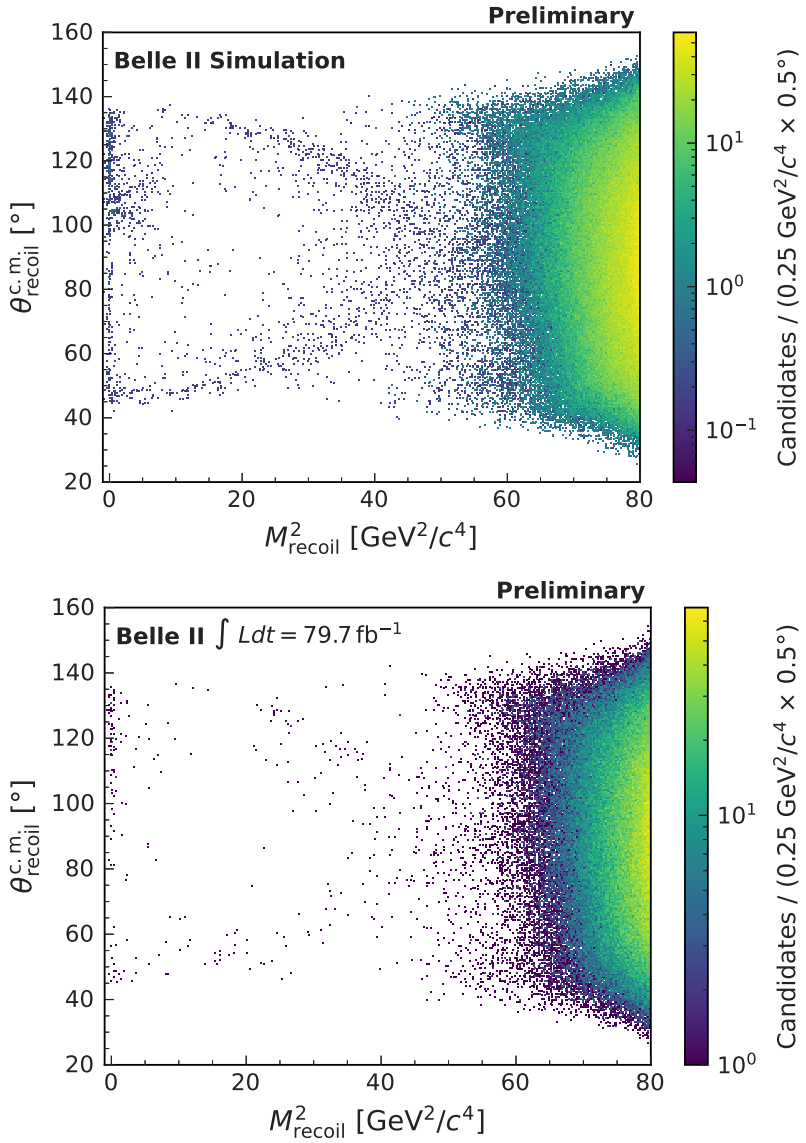

FIG. S2: Distribution of (top) expected background events and (bottom) data across the $\theta^{\mathrm{c.m.}}_{\mathrm{recoil}}$ versus M^2_{recoil} plane after all the analysis selections.

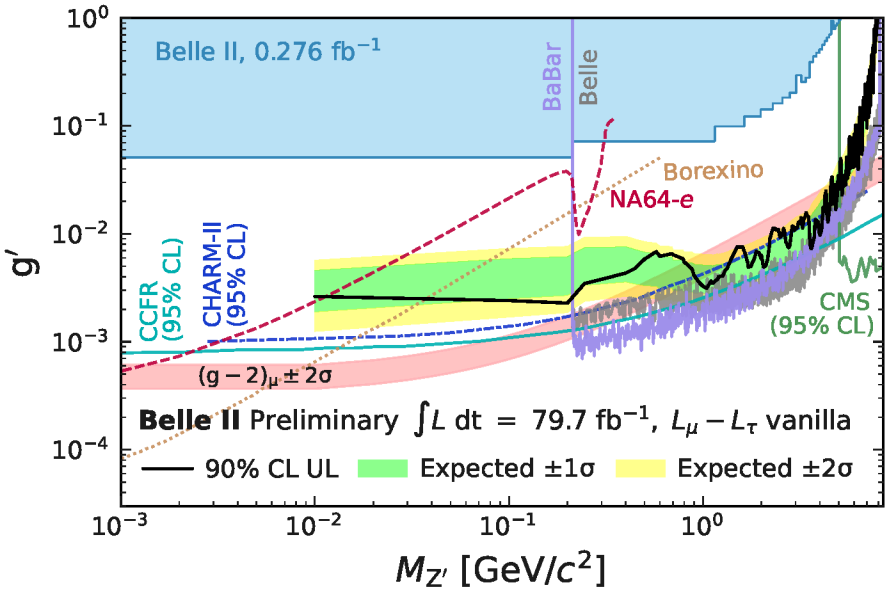

FIG. S3: Observed 90% CL upper limits on the coupling g' for the $L_\mu - L_\tau$ vanilla model as functions of $M_{Z'}$ on a logarithmic scale. Existing limits from BaBar [1], Belle [2], CMS [3] (95% CL), NA64-e [4], and Belle II [5] are shown, along with constraints (95% CL) derived from the trident production in neutrino experiments [6–8]. The red band shows the region that could explain the muon anomalous magnetic moment $(g-2)_\mu \pm 2\sigma$ [9].

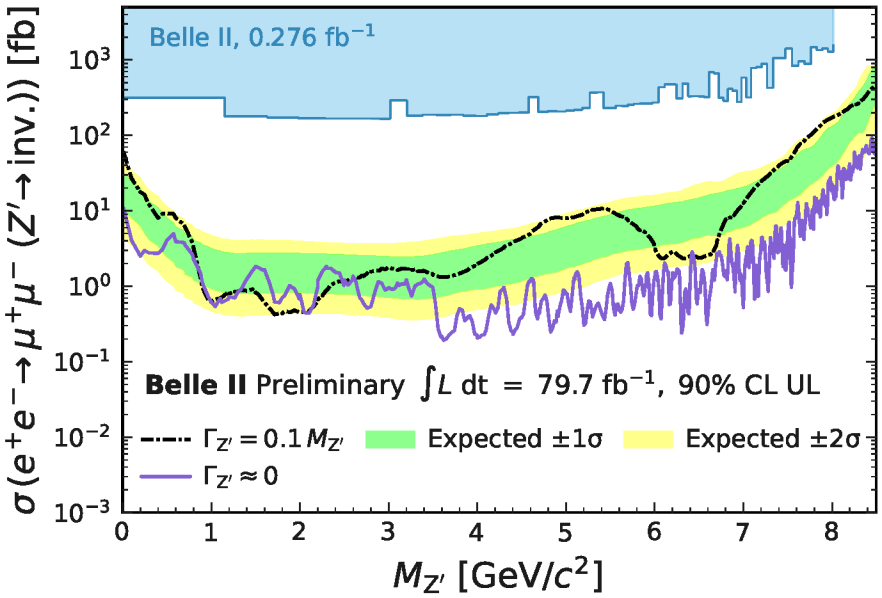

FIG. S4: Observed 90% CL upper limits on the cross section $\sigma(e^+e^- \to \mu^+\mu^- Z',\ Z' \to \text{invisible})$ as functions of the Z' mass for $\Gamma_{Z'} = 0.1 M_{Z'}$, including the ± 1 and $\pm 2\sigma$ bands around the expected limits. Also shown are previous limits from Belle II [5] and the observed limits for the negligible width case.

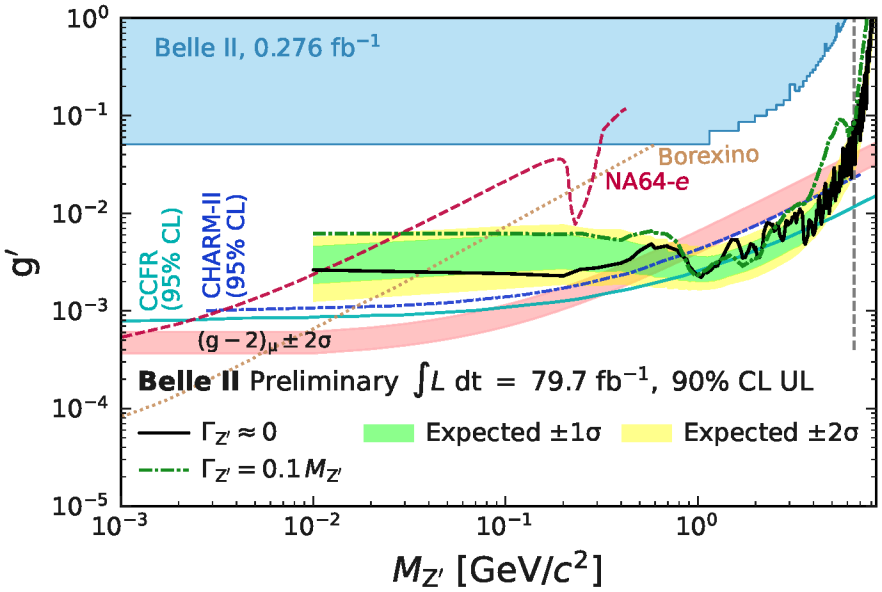

FIG. S5: Observed 90% CL upper limits on the coupling g' for the $L_\mu - L_\tau$ fully invisible model as functions of $M_{Z'}$ in logarithmic scale. Existing limits from NA64-e [4] and Belle II [5] are shown, along with constraints (95% CL) derived from the trident production in neutrino experiments [6–8]. The vertical dashed line indicates the limit beyond which the hypothesis $\mathcal{B}(Z' \to \chi\bar{\chi}) \approx 1$ is not valid in the negligible $\Gamma_{Z'}$ case. The red band shows the region that could explain the muon anomalous magnetic moment $(g-2)_\mu \pm 2\sigma$ [9].

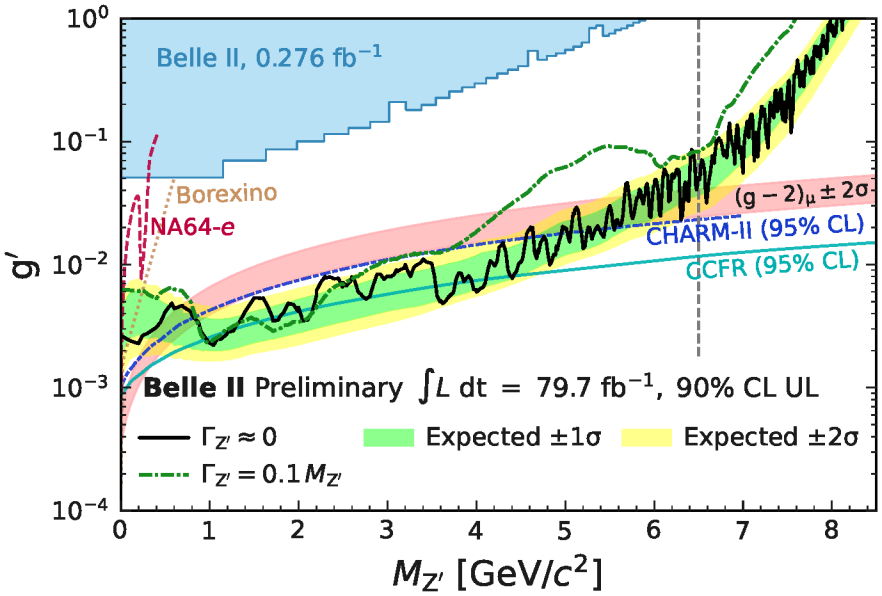

FIG. S6: Observed 90% CL upper limits on the coupling g' for the $L_\mu - L_\tau$ fully invisible model as functions of $M_{Z'}$. Existing limits from NA64-e [4] and Belle II [5] are shown, along with constraints (95% CL) derived from the trident production in neutrino experiments [6–8]. The vertical dashed line indicates the limit beyond which the hypothesis $\mathcal{B}(Z' \to \chi\bar{\chi}) \approx 1$ is not valid in the negligible $\Gamma_{Z'}$ case. The red band shows the region that could explain the muon anomalous magnetic moment $(g-2)_\mu \pm 2\sigma$ [9].

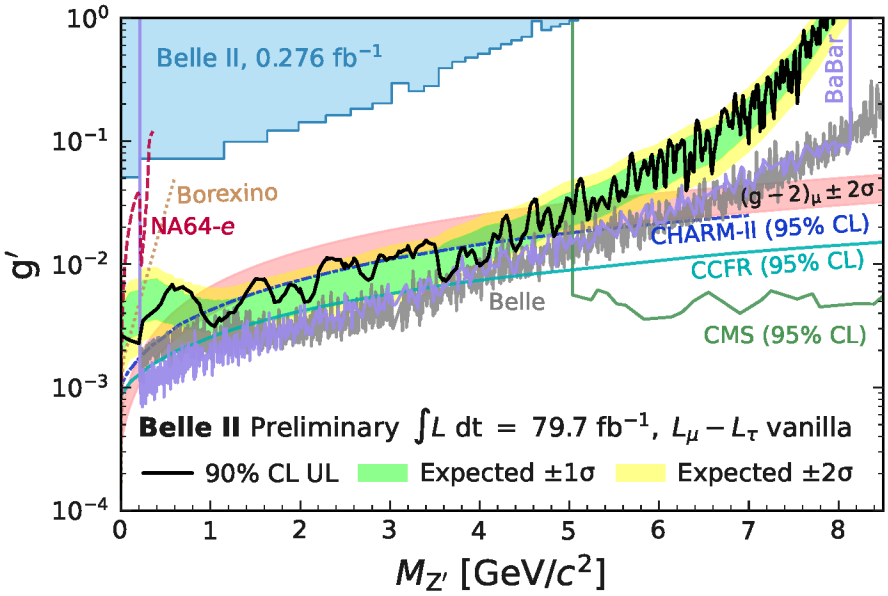

FIG. S7: Observed 90% CL upper limits on the coupling g' for the $L_\mu - L_\tau$ vanilla model as functions of $M_{Z'}$. Existing limits from BaBar [1], Belle [2], CMS [3] (95% CL), NA64-e [4], and Belle II [5] are shown, along with constraints (95% CL) derived from the trident production in neutrino experiments [6–8]. The red band shows the region that could explain the muon anomalous magnetic moment $(g-2)_\mu \pm 2\sigma$ [9].

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