Machine learning 3D-resolved prediction of electrolyte infiltration in battery porous electrodes

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HIGHLIGHTS

- A 3D Lattice Boltzmann method was used to simulate electrolyte infiltration.
- Simulation data was used to train a machine learning model.
- The machine learning model was able to predict electrolyte infiltration in 3D.
- Predictions can be performed in less than 1 s with high accuracies.
- The model can screen different conditions to optimize the infiltration process.

GRAPHICAL ABSTRACT

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ABSTRACT

Electrolyte infiltration is one of the critical steps of the manufacturing process of lithium ion batteries (LIB). We present here an innovative machine learning (ML) model, based on the multi-layers perceptron (MLP) approach, to fast and accurately predict electrolyte flow in three dimensions, as well as wetting degree and time for LIB electrodes. The ML model is trained on a database generated using a 3D-resolved physical model based on the Lattice Boltzmann Method (LBM) and a NMC electrode mesostructure obtained by X-ray micro-computer tomography. The trained ML model is able to predict the electrode filling process, with ultralow computational cost and with high accuracy. Also, systematic sensitivity analysis was carried out to unravel the spatial relationship between electrode mesostructure parameters and predicted infiltration process characteristics. This paves the way towards massive computational screening of electrode mesostructures/electrolyte pairs to unravel their impact on the cell wetting and optimize the infiltration conditions.

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Lithium ion batteries (LIBs) can provide high energy and power densities with long cycle life, constituting the technology of choice nowadays for electronic gadgets and electric vehicles [1]. Therefore, the demand for LIB increases rapidly and its cost becomes one of the critical issues to overcome. Generally, the price depends on the battery's cell chemistry and manufacturing process [2]. And the electrolyte infiltration in the battery cell is one of the bottlenecks in the manufacturing process [3]. It is crucial to optimize the electrolyte infiltration as it takes a relatively long time compared to the other manufacturing steps [4]. Moreover, a poor electrolyte impregnation decreases the active surface area (active material/electrolyte interface), and creates an inhomogeneous SEI layer in LIB negative electrodes. All these effects strongly depend on the mesostructural organization of the internal components of the electrodes themselves, and may lead to low energy and power densities, and shorter cycle life [5–9].

Despite its importance, it is experimentally challenging to analyze electrolyte flow through the porous electrodes. Several attempts were made to capture the dynamic path of the infiltrating electrolyte by using 2D in-plane imbibition, transmission neutron and X-ray imaging [10–12]. Nevertheless, these studies lack appropriate resolution and detailed information due to the limitations of the techniques. In addition, the experimental results constitute average values, making very challenging the differentiation of the effect of various manufacturing conditions on electrolyte wetting. Moreover, performing high throughput experimental characterizations to unravel parameters interdependencies in the infiltration process is not a trivial task [12,13], since the experimental techniques reported in the literature are costly and require sophisticated tools [14].

On the other side, a recent increase in computational power enables performing three-dimensional (3D) fluid flow computational simulations to quantify the permeability of complex porous materials and electrolyte penetration at the mesoscale, which can be carried out in electrode images obtained by micro-computer tomography (CT). One of the most prominent tools to evaluate the permeability of realistic 3D-resolved electrode mesostructures is the Lattice-Boltzmann Method (LBM) [6]. Typically, LBM simulations are performed in representative elementary volumes (REV), where relatively small sub-volumes of the bigger mesostructure are selected, such that the global mesostructural properties are preserved [15,16]. For the first time, we recently reported this approach to simulate electrolyte infiltration into LIB electrode mesostructures in 3D [6]. Results arising from LBM simulations are generally accurate, reliable and allow deep physical interpretation of the electrolyte infiltration process.

Nevertheless, performing routine calculations with LBM remains computationally expensive and time-consuming: typically, 48–120 h are needed for simulating electrolyte infiltration in one electrode, running the code in a supercomputer. Still, LBM constitutes a great tool to produce big data for further analysis (100–300 Gigabytes per electrode), something which is not possible with current dedicated experimental tools. The bottleneck of the LBM model is the inability to quickly screen a massive amount of electrode architectures and electrolyte types. Consequently, it remains crucial to speed up the simulation of the electrolyte infiltration process to pave the way towards the computational screening of the impact of electrolyte and electrode properties on the electrolyte infiltration dynamics and therefore envisage autonomous algorithms able to optimize the electrolyte infiltration for low required times.

Meanwhile, Artificial Intelligence (AI) has seen a tremendous rise in the last decade. In LIBs, machine learning (ML) techniques have enabled tools that significantly reduce the slow time frames related to trial-and-error approaches or physics-based simulations for faster and more efficient data assessment [17–23]. Such techniques have also been applied to datasets produced from LBM calculations in the geology domain through images-based prediction to obtain fluid flow properties in porous media [15,24,25].

Our aim in this study is to report, for the first time to our knowledge,

a ML model based on a multi-layers perceptron (MLP) approach that can describe the dynamics of the electrolyte infiltration process in 3D, given a particular mesostructure of a LIB electrode and its associated pore-network, while accounting for different external infiltration pressure conditions.

Extraction of REV: From the full tomography dataset of the NMC 94 % - CBD 6 % electrode, eleven $100 \times 100 \times 75 \mu\text{m}^3$ [3] sub-volumes of similar porosities were extracted with a maximal relative error of 5%. The carbon binder domain (CBD) location in the REV was resolved using an *in house* stochastic algorithm [21].

Individual pore identification: An accurate reconstruction of the three-dimensional pore spaces and the subsequent identification of individual pores was done by the PoroDict library within the GeoDict® software using the watershed algorithm. The interface threshold value for pore reconnection is kept constant at 10% for each of the representative sub-volumes that were extracted and analyzed. Then, their volume, surface area, and surface area of contact with other pores were calculated based on a six neighbors approach [26]. Compared to other pore-network modelling approaches [27], [–] [29] where the pores are approximated as spheres and cylindrical throats, the watershed algorithm identifies individual pores by labeling every voxel in the pore phase. This is especially useful when setting a one-to-one correspondence between the pore-wise labeled volumes and other voxel-based volumetric data coming from LBM simulations.

LBM simulations: Simulations were carried out using the open-source Palabos library version 1.0 [30]. All the simulations are in the laminar flow regime. The Navier-Stokes macroscopic kinetic theory was applied to describe fluid in the bulk flow at the mesoscopic level. Further details of the model and its description can be found in our previous LBM publication [6]. All the input parameters such as the density, the fluid contact angle with the solid phase, the viscosity, the surface tension and the sizes of simulation boxes are given in Table 1. After, the outputs from the Palabos library were further treated using NumPy [31] with the PyVista library [32] in order to obtain the individual pore-resolved saturation curves.

ML model: In this study, a sequential architecture is implemented to model the saturation curve values $\bar{S}$ and the times of filling (T_{f0} and T_{f1}) as seen in Scheme 1D) for every pore in the tomographic REV. The developed architecture follows a neural network-based model known as a MLP. The Python libraries, Tensorflow and Keras, are used in the backend to complete the architecture within a 3.7 version of Python. After training the modeling function, a sensitivity analysis is applied to analyze the effect of the input parameters on the uncertainty of the outputs. The architecture of the MLP comprises five hidden layers, with 80 nodes each, and one output layer containing 7 nodes. While no specific rule exists for selecting DNN hyperparameters [33], this architecture was sufficient to fit the training data correctly and to obtain trustable predictions as shown in the results section.

Table 1
List of input parameters for the LBM simulations.

AM 96%-CBD 4% un-calendered tomography	$100 \times 100 \times 75$ voxels	$100 \times 100 \times 75 \mu\text{m}^3$ [3]
Electrolyte density	10	$1300 \frac{\text{kg}}{\text{m}^3}$
Gas density	1	$1.18 \frac{\text{kg}}{\text{m}^3}$
Contact angle	0.357/1.643	90° [12]
Surface force (gas-liquid)	0.1	7.28×10^{-2}
t_0	1 μs	$1 \times 10^{-6} \text{s}$
Reynolds number	10^{-3}	10^{-3}
Capillary number	10^{-5}	10^{-5}
Pressure	p0.5	151 988 Pascal
Pressure	p1	202 650 Pascal
Pressure	p2	405 300 Pascal
Pressure	p4	810 600 Pascal
Pressure	p8	1 621 200 Pascal

Scheme 1. Summary of the data processing steps to be used as inputs in the ML model. (A) 3D micro-CT X-ray tomography data, colored rectangular parallelepipeds represent two examples of the different REVs that were extracted. (B) (left) Results from the watershed segmentation process, (C) (middle) volume data from LBM simulations with voxels labeled as liquid (orange), void (blue), and solid (white). (D) (right) Individual pore-resolved saturation curves. For clarity, two pores (blue and red) were highlighted, spanning the same spatial regions between the watershed and LBM voxel data. The respective pore-resolved saturation curves are also shown, alongside their relevant features ($\bar{S}$, T_{f0} , and T_{f1}). (E) Structure of the data used for the training of the NN, columns enumerate each pore, while rows are divided into the inputs (X_i) $_{(i \leq 6)}$ (blue shaded region) and outputs (Y_i) $_{(i \leq 7)}$ (red shaded region). (F) Architecture of the neural network used for training, nodes in blue (red) represent the input (output) layers, respectively. Nodes in yellow represent the hidden layer nodes $S_{j,k}$ where k is the layer index, and j is the node index. Nodes in green represent the bias that is applied to each hidden layer.

Scheme 1 illustrates the workflow that was used in this work. The details of the data extraction procedure of pore-resolved saturation curves and the ML model are given in the supporting information.

ML training and prediction: The evaluation of the electrolyte infiltration dynamics was done by extracting the relevant features of pore resolved saturation curves as shown in **Scheme 1D**. Specifically, we extracted the values of the times at which the pore filling starts (T_{f0}) and stops (T_{f1}), as well as the saturation values associated to ten in-between evenly spaced time steps, as the outputs of the MLP. The set of saturation points are defined as $\bar{S} = \{S_1, S_2, S_3, S_4, S_5, S_6, S_7, S_8, S_9, S_{10}\}$.

Fig. 1 displays the critical features for the training and validation of the MLP. The complete dataset is randomly split into the training and testing dataset containing 80 % and 20 % of the total data, respectively. **Fig. 1A** represents the evolution of the loss values (MSE) for the training data (80 % of the total amount of data) and the validation data (the remaining 20 %) during the training step of the MLP over 1000 training cycles. **Fig. 1B** shows the average R^2 scores for the model compared with the mean square error (MSE) between the initial saturation curve and its discretization to define the saturation values outputs. In order to obtain a compromise between the global accuracy of the MLP and the error between the saturation curves and their associated discretized values, we successively retrained the MLP model after removing those saturation value outputs that were not properly fitted, thus reducing the number of outputs in the model. Particularly, this compromise is met by selecting $\bar{S}_{3-7} = \{S_1, S_2, S_8, S_9, S_{10}\}$ as the outputs of the MLP, along with T_{f0} and T_{f1} (as shown in **Scheme 1E-F**). **Fig. 1C** and **D** display

regression plots comparing the predicted values from the MLP model and the actual values from the LBM simulations for the testing dataset, for the time at which the pore-filling starts (T_{f0}) and stops (T_{f1}), respectively.

Comparison of LBM simulation and prediction based on ML: As mentioned above, our trained MLP can accurately predict the saturation, initial electrolyte entering and fully wetting time at an individual pore in the structure for the test dataset. In order to further compare and contrast our model, an additional REV was used, whose pore-network was not part of neither the training nor testing datasets. After inputting the parameters of the brand-new pore-network in our MLP, the overall saturation curves were reconstructed from the obtained outputs, as shown in **Fig. 2**. The obtained results closely match the saturation curves obtained with LBM, which gives a hint of the ability our ML model to perform well in a variety of electrode mesostructures.

Five different applied pressures were also used as input parameters to study and predict their effect on electrolyte penetration. Again, **Fig. 2** shows the overall saturation curves simulated by LBM, and predicted by our MLP for different applied pressures. Generally, all saturation curves for both real and predicted cases show an asymptotic growth rate where the saturation curve increases steeply and slows down while it reaches the convergence point. Also, the wetting time for the electrode increases as applied pressure decreases for both real and predicted cases. Furthermore, the lower the applied pressure, the lower the overall saturation will be and the longer it will take to reach the convergence point. The saturation curves for real (LBM simulated) cases under the

Fig. 1. (A) MSE of the training and validation of the neural network, (B) R^2 scores (blue) and the MSE of the saturation curve reconstruction (garnet) as function of the set of saturation value ($\bar{S}$) outputs predicted by the model, (C) Prediction of the logarithm of the starting times for electrolyte filling of individual pores (T_{f0}) and (D) Prediction of the logarithm of the full wetting times (T_{f1}). (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)

Fig. 2. Saturation profile of liquid electrolyte from real (LBM simulated) and predicted (NN based) in the NMC 94% - CBD 6% cathode with various applied pressures.

applied pressures p_8 , p_4 and p_2 tend to rise monotonically and reach complete wetted conditions. For the lower pressure values (p_1 and $p_{0.5}$), the electrode wetting degrees are only 60 % and 25 %, respectively. In addition, the penetration rate, *i.e.* the rate at which the saturation will reach its convergence point, is slower for p_1 and $p_{0.5}$ compared to higher applied pressures. The predicted (MLP based) saturation curves agree with those from LBM simulated results, especially at high applied pressures where the predictions are extremely precise. In essence, the vital part is that the MLP can closely match the general simulation trends and is also able to precisely predict converging points, where the saturation degrees predicted by our MLP closely match those obtained by LBM simulations for high applied pressure inputs.

Our model also allows following the electrolyte wetting process in 3D, since its outputs depend on spatially resolved pore-networks. **Fig. 3**

shows the temporal evolution of the saturation degree of individual pores in the electrode mesostructure. It is known that electrolyte flows through the porous electrode due to the pressure difference between the electrolyte and air phases, known as capillary forces, while local resistance forces drive the electrolytes path within the porous electrode. Usually, the electrolyte is always directed towards larger pores, as shown in our previous LBM simulations [6]. **Fig. 3** shows an excellent agreement between the MLP prediction and physical-based LBM model, in the path that the electrolyte takes within the porous electrode. There is a slight deviation at time step 1×10^4 [4]lu, but the difference disappears at the converging point.

Parameters influencing the saturation and their physical interpretation: Performing a sensitivity analysis of computational models is a clear and straightforward way to assess how the calculated outputs as a function of the used inputs. In this work the Sobol indexes were extracted in order to evince the individual and total impacts that the input parameters of the MLP model have on the seven outputs that we aim to predict, *i.e.* T_{f0} , T_{f1} and the saturation values $\bar{S}$. Additionally, the Sobol indexes corresponding to the initial ($S_{f0} = \{S_1, S_2\}$) and final ($S_{f1} = \{S_8, S_9, S_{10}\}$) saturation values are averaged out, which allows condensing the results in order to facilitate their physical interpretation (**Fig. 4**).

Fig. 4 shows the 1st order Sobol indexes regarding all possible combinations between inputs (geometrical properties of the pores and applied pressures) and outputs (T_{f0} , T_{f1} , S_{f0} and S_{f1}) in this study. We can see that the initial pore filling time (T_{f0}) highly depends on the pore volume with a Sobol index of 0.7 followed by the pore total surface area and its location with Sobol indexes of 0.3. The total wetting time of the pore (T_{f1}) is also influenced mainly by these three parameters. The pore volume has a major effect with a Sobol index of 0.6 and the second biggest factor is the pore surface area with Sobol index 0.4. It is intuitive that the bigger the pore size, the easier it is for the electrolyte to occupy its volume. Also, other geometrical attributes such as pore location and pore surface area play a significant role in the pore filling start time (T_{f0}). Additionally, it is important to mention that all the input parameters

Fig. 3. The wetting process visualization (electrolyte in red color) from real (LBM simulated) and predicted (MLP based) for the NMC 94% - CBD 6% electrode (blue) at different time steps. The electrolyte inlet is the yz plane at $x = 0$. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)

Fig. 4. (A) Sobol indexes of the geometrical properties of individual pores and applied pressures, on the outputs T_{f0} , T_{f1} , S_{f0} , and S_{f1} . (B) Slice of the REV illustrating the geometrical properties of individual pores. The zoom region (black circle) illustrates the pore volume (grey zone), pore surface area (blue outline), pore contact surface area (red outline) and pore location (dotted turquoise arrow) of a given identified pore inside the REV. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)

have almost the same effect on the saturation values at the end of the pore filling (S_{f1}) with Sobol indexes about 0.45. The onset of saturation S_{f0} is, on the contrary, strongly influenced by the pore location with Sobol index around 0.7.

Thus, to have optimal electrode mesostructures to reach complete wetting at the shortest possible time, pore size distribution and inter-connectivity of the pores must be well designed during the manufacturing. This can be a challenging task with traditional manufacturing process, still it is achievable with alternative techniques such as SPS sintering and 3D printing [34,35].

In conclusion, we present an innovative ML model based on a multi-layers perceptron (MLP) architecture, to predict electrolyte infiltration in porous NMC electrodes. The host structure of the NMC porous electrode was obtained experimentally by (micro-CT) X-ray tomographic measurements. The MLP was trained with data coming from physics-based 3D LBM model and extracted pore networks from (micro-CT) X-ray tomography. The neural network prediction results were compared and validated by 3D LBM simulations.

The trained MLP can generalize the flow problems to predict the rate of saturation and filling time in porous electrodes. Moreover, it can predict the direction of the electrolyte flow, total saturation, and filling time of the electrode accurately. Additionally, a systematic sensitivity analysis was carried out to unravel the spatial relationship between complex electrode pore shape, pore location, pore volume, the connection between other pores and applied external pressure on the overall predicted electrolyte infiltration process characteristics, such as saturation degrees and filling times, among others.

Besides, the trained MLP accurately predicted scenarios with different geometries and applied pressures in less than 1 s of computation on a desktop computer, while physics-based LBM simulations took several days (2–5) on a server with high computational power. Additionally, our ML model generates only around 10 Mb of data to be compared with the 50–200 Gb generated during the LBM simulations, saving data storage space and making post-processing fast and affordable. All the advantages mentioned above allow the model to quickly screen different electrode architectures and electrolyte properties paving the way towards a fast and efficient tool for the optimization of the electrolyte infiltration process. On top of that, the simulation tool reported in this work is devoted to be integrated in the overall computational workflow of the ARTISTIC project, which aims at simulating a digital-twin of the LIB electrode manufacturing process, including the electrode slurry, the coating, the drying, the calendaring, the electrolyte infiltration and the resulting electrochemical performance. Thus, the model has the potential to become an invaluable asset for the project to fastly screen the effect of the electrode wetting on different electrolytes across the LIB fabrication process and their final electrochemical performances. Finally, this approach could be used in other electrochemical

energy devices (e.g. polymer electrolyte membrane fuel cells, redox flow batteries, flow capacitors) where fluid flow through porous media takes part.

Contributions

A.S., O.A., M.D. and A.A.F. had the original idea and designed the work plan. A.S., M.D., carried out the modeling. O.A., performed data management. A.S., O.A., M.C. provided inputs. A.S., M.D., O.A., J.L. and A.A.F. interpreted the results. A.S., O.A. and M.D. wrote the first version of the manuscript. All the authors edited and reviewed the manuscript. A.A.F. obtained the funding for this research and supervised the work.

Data and code availability

All the data and the codes used in the scope of this work will be publicly available on the ERC-ARTISTIC project's website [ARTISTIC-ERC/ElectrolytePenetration-ML](https://artistic-erc.eu/electrolyte-penetration-ml).

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.jpowsour.2021.230384>.

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