

Planck 2019 Granada, 3 June 2019

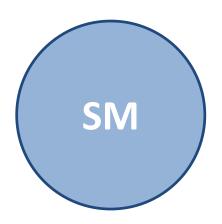


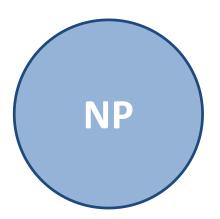


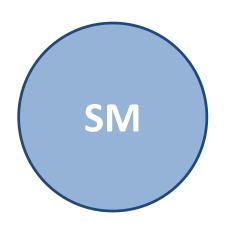
# The Minimal Simple Composite Higgs Model

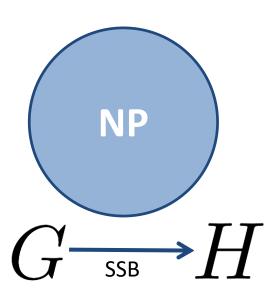
Alejo Nahuel Rossia DESY, IB & HU

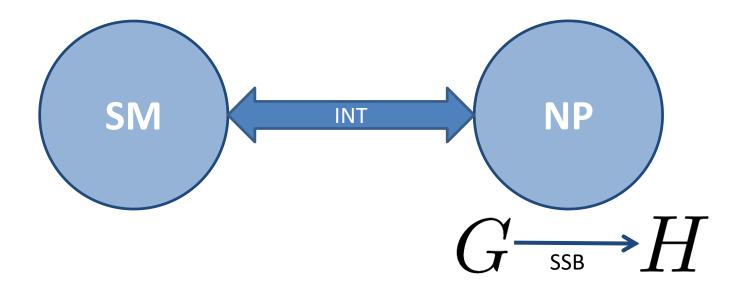
Based on arXiv: 1904.02560 [hep-ph], w/ L. Da Rold

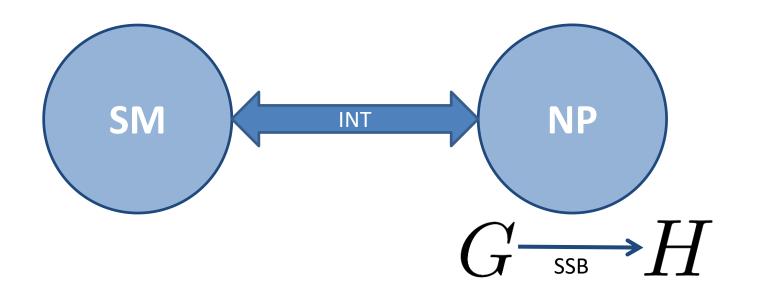




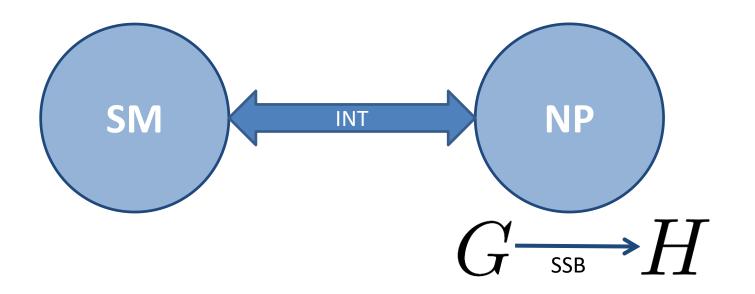






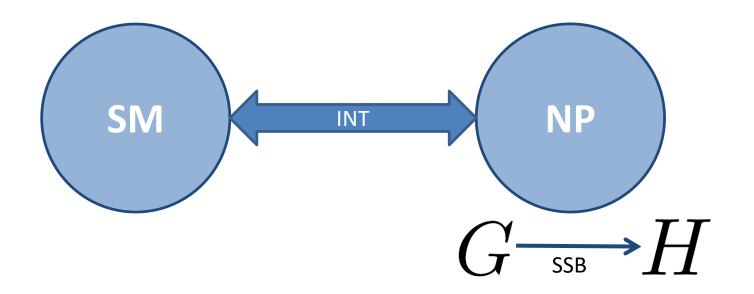


# Why a non-minimal CHM?



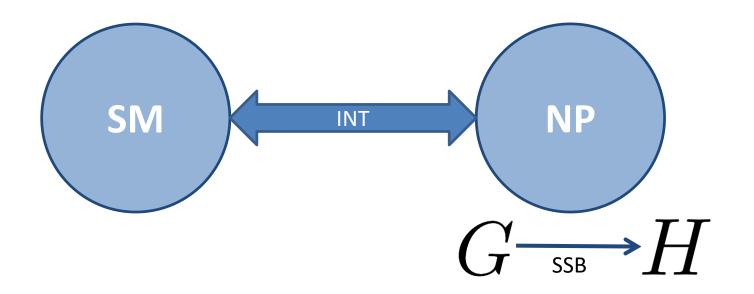
# Why a non-minimal CHM?

LHC results constrain severely the MCHM.



# Why a non-minimal CHIM?

- LHC results constrain severely the MCHM.
- Non-minimal CHMs satisfy the bounds better.



# Why a non-minimal CHM?

- LHC results constrain severely the MCHM
- Non-minimal CHMs satisfy the bounds better
- Different and rich phenomenology, less explored.

1

$$\mathbf{SO}(5) \times \mathbf{U}(1)_X / \mathbf{SO}(4) \times \mathbf{U}(1)_X$$

Agashe et al (hep-ph/0412089)

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Agashe et al (hep-ph/0412089)

#### Next to MCHM

$$\mathbf{SO}(6) \times \mathbf{U}(1)_X / \mathbf{SO}(5) \times \mathbf{U}(1)_X$$

Gripaios et al (0902.1483)

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### SO(7) CHM

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Chala et al (1605.08663), Balkin et al (1707.07685, 1809.09106)

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### **SO(7) CHIM**

$$\mathbf{SO}(7) \times \mathbf{U}(1)_X / \mathbf{SO}(6) \times \mathbf{U}(1)_X$$

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### Nevertheless...

### $\mathbf{SO}(7) \supset \mathbf{SO}(6) \supset \mathbf{SO}(4) \times \mathbf{U}(1)$

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 $\mathbf{SO}(7) / \mathbf{SO}(6)$ 

✓ Simple Lie groups

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 $\mathbf{SO}(7) / \mathbf{SO}(6)$ 

- Simple Lie groups
- Higgs doublet

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- ✓ Simple Lie groups
- Higgs doublet
- Custodial Symmetry

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$$\mathbf{SO}(7) \times \mathbf{U}(4)_X / \mathbf{SO}(6) \times \mathbf{U}(4)_X$$
  
 $\mathbf{SO}(7) / \mathbf{SO}(6)$ 

- ✓ Simple Lie groups
- Higgs doublet
- Custodial Symmetry
- Unifies EW group

$$egin{array}{ll} {
m SO}(6) & {}^{({
m SU}\,(2)_L,\,{
m SU}\,(2)_R)_X} \ {f 6} \sim ({f 2},{f 2})_0 + ({f 1},{f 1})_{\pm 1/\sqrt{2}} \end{array}$$

### EW embedding

$$egin{array}{lll} \mathrm{SO}(6) & ^{(\mathrm{SU}\,(2)_L,\,\mathrm{SU}\,(2)_R)_X} \\ \mathbf{6} \sim (\mathbf{2},\mathbf{2})_0 + (\mathbf{1},\mathbf{1})_{\pm 1/\sqrt{2}} \\ \downarrow & \downarrow & \downarrow \\ \mathrm{Higgs \ boson} & \chi \ \mathrm{boson} \end{array}$$

### EW embedding

$$Y = T_R^3 + \frac{2\sqrt{2}}{3}X$$
$$Q = T_L^3 + Y$$

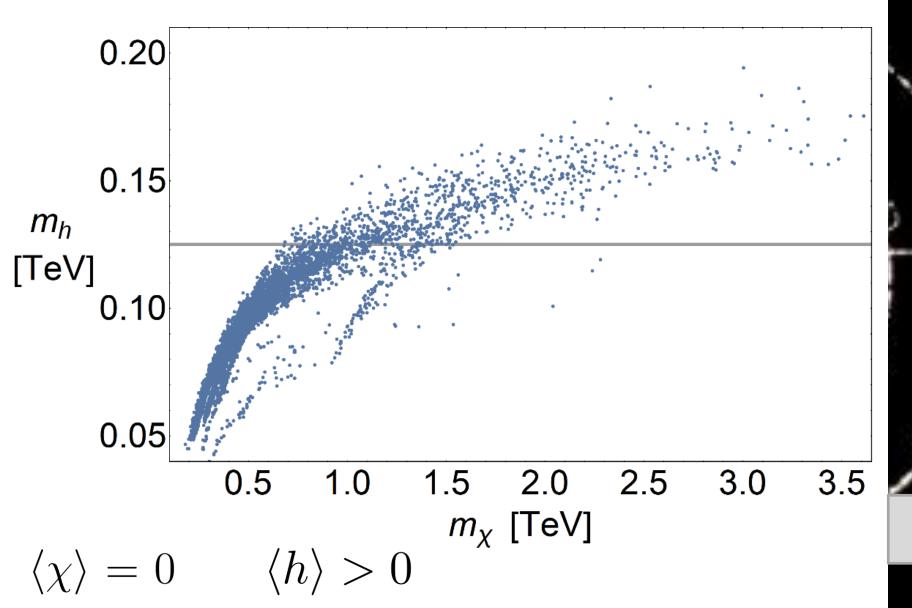
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### EW embedding

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 H:  $\mathbf{2}_{rac{1}{2}}$   $SU\left(2
ight)_L imes U\left(1
ight)_Y$   $Q=T_L^3+Y$   $\chi$ :  $\mathbf{1}_{rac{2}{3}}$ 

4

#### Parameter space scan



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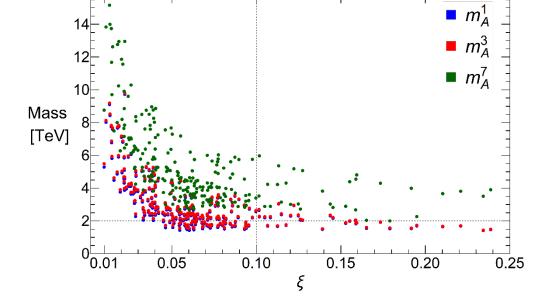
#### Resonances

#### **Vector bosons**

#### Dirac fermions

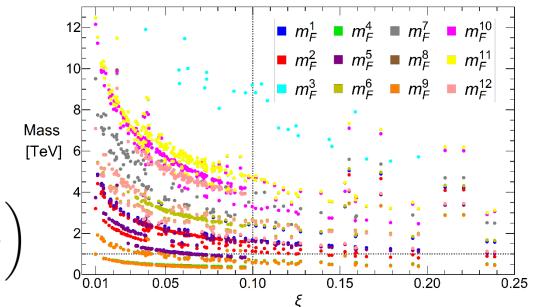
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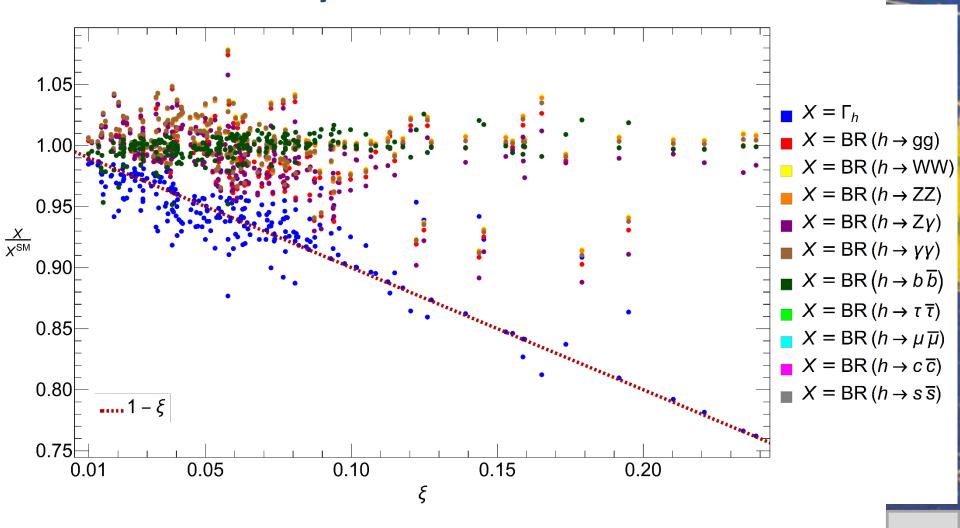
#### **Dirac fermions**

$$\xi = \left(\frac{v}{f}\right)^2 = \sin^2\left(\frac{\langle h \rangle}{f}\right)$$



6

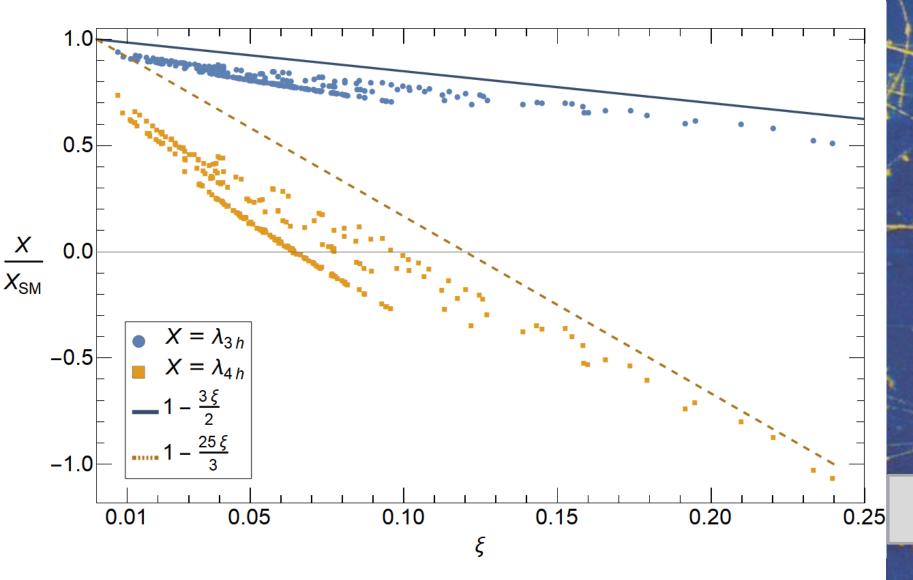
#### Decay width and BRs



$$\xi = \left(\frac{v}{f}\right)^2 = \sin^2\left(\frac{\langle h \rangle}{f}\right)$$



### Higgs self-couplings



8

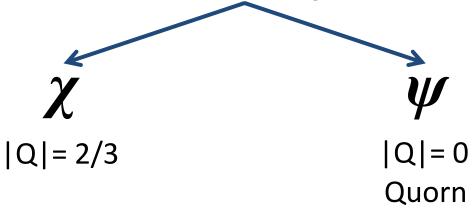
### Exotic stable particle

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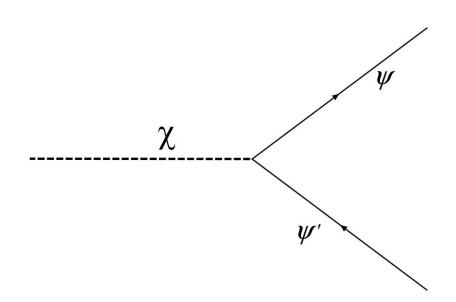


$$|Q| = 2/3$$

### Exotic stable particle



De Luca et al (1801.01135) Gross et al (1811.08418)





#### Conclusions

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- 5. Stronger suppression in Higgs self couplings.

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- 3. New particles with exotic charges appear.
- 4. Suppression in Higgs couplings, decay and production amplitudes of order 5-10%.
- 5. Stronger suppression in Higgs self couplings.
- 6. There is an exotic stable particle, which might be a DM candidate.





# SO(7) irreps decomposed... ...into SO(6)

$$7\sim 6+1 \hspace{0.5cm} 21\sim 15+6 \hspace{0.5cm} 35\sim 15+10+\overline{10}$$

# ...into SU(2)xSU(2)xU(1)

$$\mathbf{10} \sim (\mathbf{2},\mathbf{2})_0 + (\mathbf{3},\mathbf{1})_{1/\sqrt{2}} + (\mathbf{1},\mathbf{3})_{-1/\sqrt{2}}$$

$$\mathbf{15} \sim (\mathbf{2},\mathbf{2})_{\pm 1/\sqrt{2}} + (\mathbf{3},\mathbf{1})_0 + (\mathbf{1},\mathbf{3})_0 + (\mathbf{1},\mathbf{1})_0$$

$$\begin{aligned} 2\mathbf{1}_{SO(7)} &= (3,1)_0 \oplus (1,3)_0 \oplus (1,1)_0 \oplus (2,2)_{\frac{1}{\sqrt{2}}} \\ &\oplus (2,2)_{-\frac{1}{\sqrt{2}}} \oplus (2,2)_0 \oplus (1,1)_{\frac{1}{\sqrt{2}}} \oplus (1,1)_{-\frac{1}{\sqrt{2}}} \end{aligned}$$

#### SM fermions embedding and Partial compositeness

Field	$T_R^3$	$SO(4) \times U(1)_X$	SO(6)	SO(7)
q	-1/2	$({f 2},{f 2})_{1/\sqrt{2}}$	15	21
u	0	$({f 1},{f 3})_{1/\sqrt{2}}$	10	35
d	-1	$({f 1},{f 3})_{1/\sqrt{2}}$	10	35
$\ell$	-1/2	$({f 2},{f 2})_0$	6	7
e	-1	$({f 1},{f 3})_0$	15	21

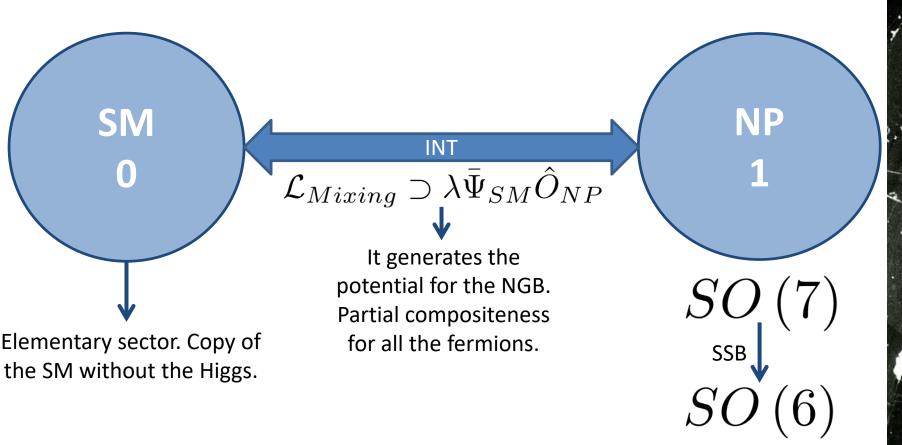
$$ME_{\psi} = \cos(\theta_{\psi}) \psi + \sin(\theta_{\psi}) C_{\psi}$$

$$y_{\psi} \sim y_{\hat{\Psi}\mathbf{r}} \sin(\theta_{\psi}) \sin(\theta_{\hat{\psi}}) \quad m_{\psi} \sim y_{\psi} v$$

$$\tan(\theta_{\psi}) = \frac{f_0 \lambda_{\psi}}{m_{\psi}}$$

Α

#### 2-site model



$$\xi = \left(\frac{v}{f}\right)^2 = \sin^2\left(\frac{\langle h \rangle}{f}\right)$$



#### Site 1, mixing and pNGBs

$$\mathcal{L}_{1} = -\frac{1}{4g_{1}^{2}}F_{\mu\nu}^{a}F^{a,\mu\nu} + \frac{f_{1}^{2}}{4}d_{\mu}^{\hat{a}}d^{\hat{a},\mu} + \bar{Q}(\not D - m_{Q})Q + \bar{U}(\not D - m_{U})U + \bar{D}(\not D - m_{D})D$$

$$+ \bar{L}(\not D - m_{L})L + \bar{E}(\not D - m_{E})E + f_{1}y_{U}[(\bar{Q}_{L}U_{1})_{15}(U_{1}^{\dagger}U_{R})_{15}]_{1}$$

$$+ f_{1}y_{D}[(\bar{Q}_{L}U_{1})_{15}(U_{1}^{\dagger}D_{R})_{15}]_{1} + f_{1}y_{E}[(\bar{L}_{L}U_{1})_{6}(U_{1}^{\dagger}E_{R})_{6}]_{1} + \text{h.c.}$$

$$\mathcal{L}_{\text{mix}} = \frac{f_0^2}{4} |D_{\mu}\Omega|^2 + f_0 \sum_{i} \lambda_i \bar{\psi}_i \Omega \Psi_i + \text{h.c.}$$

$$\psi_i = q, u, d, \ell, e$$
,  $\Psi_i = Q, U, D, L, E$ ,

$$\Gamma_1^2 = \sum (\Pi_1^{\hat{a}})^2 \quad U_1^{\dagger} D_{\mu} U_1 = i e_{\mu}^a T^a + i d_{\mu}^{\hat{a}} T^{\hat{a}}$$

$$\Omega = e^{i\sqrt{2}\Pi_0/f_0} U_1 = e^{i\sqrt{2}\Pi_1/f_1} , \qquad \Pi_1 = \Pi_1^{\hat{a}} T^{\hat{a}}$$

$$U_1 = I + i \frac{\sin(\Gamma_1/f_1)}{\Gamma_1} \Pi_1 + 2 \frac{\cos(\Gamma_1/f_1) - 1}{\Gamma_1^2} \Pi_1^2$$

#### Physical pNGBs and EW bosons identification

$$U = e^{i\sqrt{2}\Pi/f} , \qquad \Pi = \Pi^{\hat{a}}T^{\hat{a}} , \qquad \frac{1}{f^2} = \frac{1}{f_0^2} + \frac{1}{f_1^2}$$
$$\frac{1}{g^2} = \frac{1}{g_0^2} + \frac{1}{g_1^2} \qquad \frac{1}{g'^2} = \frac{17}{9} \left( \frac{1}{g_0'^2} + \frac{1}{g_1^2} \right)$$

$$W_{\mu}^{i} = \cos(\varphi) w_{\mu}^{i} + \sin(\varphi) A_{\mu}^{L,i}$$

$$B_{\mu} = \cos(\omega) b_{\mu} + \sin(\omega) \left[\cos(\theta_Y) A_{\mu}^{R,3} + \sin(\theta_Y) A_{\mu}^{X}\right]$$

$$\tan(\varphi) = \frac{g_0}{g_1} \qquad \tan(\omega) = \frac{g_0'}{g_1} \qquad \tan(\theta_Y) = \alpha = \frac{2\sqrt{2}}{3}$$

$$D_{\mu}\Omega = \partial_{\mu}\Omega - iA_{\mu}^{0,A}T^{A}\Omega + iA_{\mu}^{1,A}\Omega T^{A}$$



Name	Mass	$ Q_{em} $	Multiplicity
$m_A^1$	$\frac{f_0g_1}{\sqrt{2}}$	$\{0, 1/3, 2/3, 1, 5/3\}$	{1,2,4,2,2}
$m_A^2$	$f_0\sqrt{\frac{{g_0'}^2+{g_1^2}}{2}}+\epsilon$	0	1
$m_A^3$	$f_0\sqrt{\frac{g_0^2+g_1^2}{2}}+\eta$	1	2
$m_A^4$	$f_0\sqrt{\frac{g_0^2+g_1^2}{2}} + \Delta$	0	1
$m_A^5$	$g_1\sqrt{rac{f_0^2+f_1^2}{2}}$	{2/3,0}	{2,1}
$m_A^6$	$g_1\sqrt{\frac{f_0^2+f_1^2}{2}}+\delta$	1	2
$m_A^7$	$g_1\sqrt{\frac{f_0^2+f_1^2}{2}}+\alpha$	0	1

# Fermion resonances spectrum

Name	$Q_{em}$	Number of Dirac fermions
$m_F^1$	$\{0, \pm 1, -2/3\}$	$\{2, 2, 1\}$
$m_F^2$	$\{0, \pm 1/3, 2/3, -2/3, \pm 1, \pm 5/3\}$	$\{4,4,1,2,4,4\}$
$m_F^3$	2/3	1
$m_F^4$	2/3	1
$m_F^5$	2/3	1
$m_F^6$	2/3	1
$m_F^7$	2/3	1
$m_F^8$	2/3	1
$m_F^9$	$\{0, 1/3, -2/3, \pm 1, \pm 5/3\}$	$\{3, 1, 2, 4, 2\}$
$m_F^{10}$	$\{0, 1/3, -2/3, \pm 1, \pm 5/3\}$	$\{3, 1, 2, 4, 2\}$
$m_F^{11}$	$-\frac{1}{3}$	1
$m_F^{12}$	$-\frac{1}{3}$	1

# Effective theory

$$\mathcal{L}_{\text{eff}} \supset \frac{f^{2}}{4} d_{\mu}^{\hat{a}} d^{\hat{a},\mu} + \sum_{\mathbf{r}=\mathbf{6},\mathbf{15}} \Pi_{\mathbf{r}}(p^{2}) (U^{\dagger} a_{\mu})_{\mathbf{r}} (U^{\dagger} a^{\mu})_{\mathbf{r}} + \sum_{i=q,u,d,\ell,e} \sum_{\mathbf{r}} \Pi_{\mathbf{r}}^{i}(p^{2}) \overline{(U^{\dagger} \psi_{i})_{\mathbf{r}}} \not p (U^{\dagger} \psi_{i})_{\mathbf{r}}$$

$$+ \sum_{i=u,d} \sum_{\mathbf{r}} M_{\mathbf{r}}^{i}(p^{2}) \overline{(U^{\dagger} \psi_{q})_{\mathbf{r}}} (U^{\dagger} \psi_{i})_{\mathbf{r}} + \sum_{\mathbf{r}} M_{\mathbf{r}}^{e}(p^{2}) \overline{(U^{\dagger} \psi_{\ell})_{\mathbf{r}}} (U^{\dagger} \psi_{e})_{\mathbf{r}} .$$

$$\mathcal{L}_{\text{eff}} \supset \frac{1}{2} [Z_w + \Pi_w(p^2)] w_{\mu}^i w^{\mu i} + \frac{1}{2} [Z_b + \Pi_b(p^2)] b_{\mu} b^{\mu} + \Pi_{ib}(p^2) w_{\mu}^i b^{\mu}$$

$$+ \bar{q}_L \not p (Z_q + \Pi_q) q_L + \sum [\bar{\psi}_R \not p (Z_\psi + \Pi_\psi) \psi_R + \bar{q}_L M_{q\psi} \psi_R + \text{h.c.}]$$

# **CW** potential

$$V = \int \frac{d^4p}{(2\pi)^4} \left( -2N_c \ln \left[ \frac{\det \left[ \mathcal{A}_{\mathcal{F}} \right]}{\det \left[ \mathcal{A}_{\mathcal{F}} \right]_0} \right] + \frac{3}{2} \ln \left[ \frac{\det \left[ \mathcal{A}_{\mathcal{B}} \right]}{\det \left[ \mathcal{A}_{\mathcal{B}} \right]_0} \right] \right)$$

$$V = m_H^2 H^2 + m_\chi^2 \chi^2 + \lambda_H H^4 + \lambda_{H\chi} H^2 \chi^2 + \lambda_\chi \chi^4 + \mathcal{O}(\phi^6)$$

#### Parameter space scan

$$f_{0,1} \sim 1 \text{ TeV}$$
  $m_{U,Q} \in (0.5, 10) \text{ TeV}$   
 $\theta_{q,u} \in (0.4, \pi/2)$   $y_U \in (0.1, 3)$   $g_1 \in (1, 6)$   
 $g = 0.65$   $g' = 0.35$   $\langle \chi \rangle = 0$   $0 < \xi < 1$ 

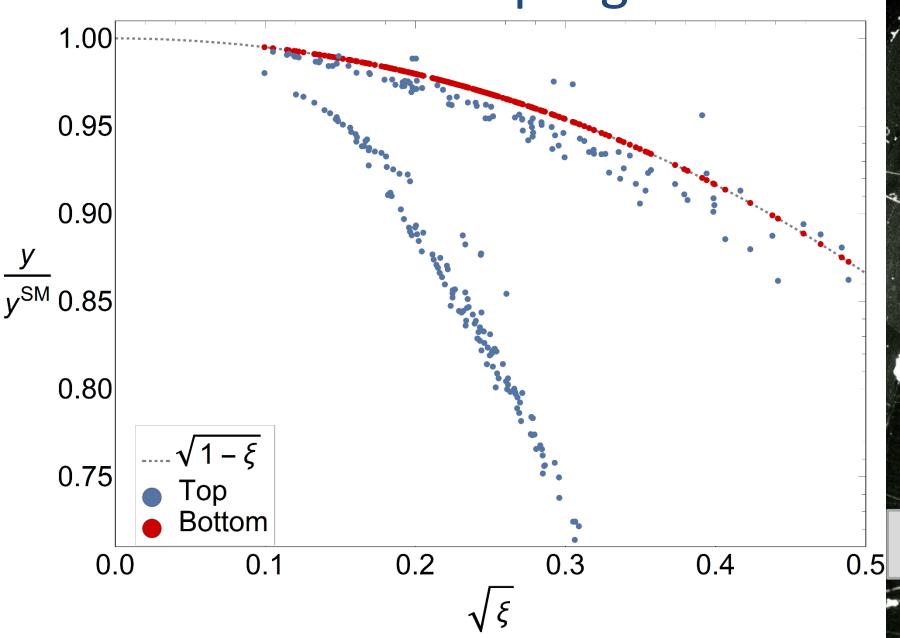
# Benchmark points criteria

$$v = 246 \text{ GeV}$$
  $f_0 g_1 > 2 \text{ TeV}$  100 GeV  $< m_H < 145 \text{ GeV}$   
140 GeV  $< m_t < 175 \text{ GeV}$   $\xi < 0.25$ 

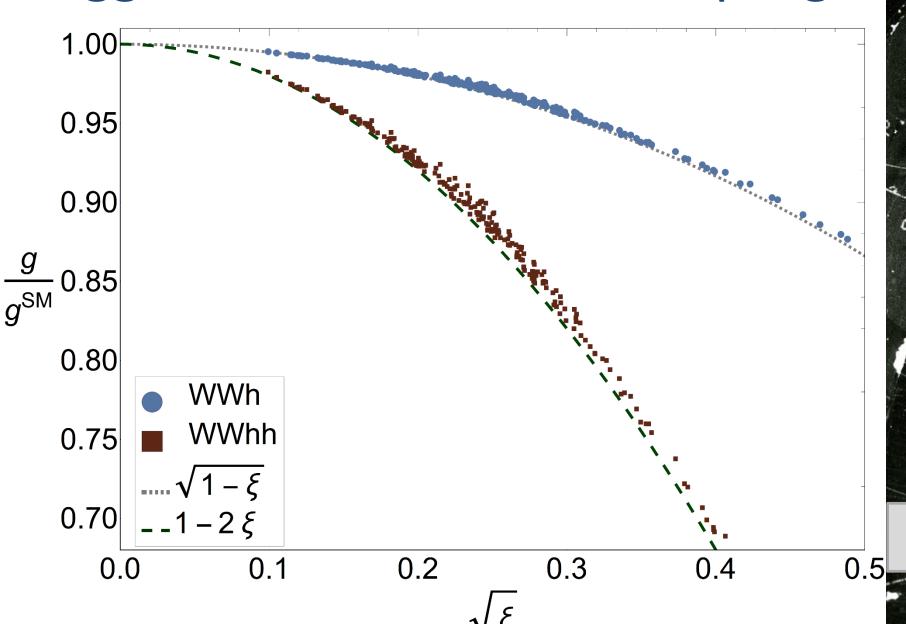
### Point for systematic scan

$$f_0 = 1.47 \text{ TeV}$$
  $f_1 = 2.34 \text{ TeV}$   $m_U = 2.44 \text{ TeV}$   
 $m_Q = 1.26 \text{ TeV}$   $\theta_u = 0.79$   $\theta_q = 1.37$   
 $g_1 = 1.95$   $y_U = 2.52$ 

### Yukawa couplings



### Higgs- EW vector bosons couplings



# Corrections w.r.t. the SM couplings

$$\frac{y_{\psi}^{(0)}}{m_{\psi}^{(0)}} \simeq \frac{F_{\psi}(\xi)}{\sqrt{\xi}f} \left[ 1 + \mathcal{O}\left(\xi \frac{\lambda_{\psi_L}^2 f^2}{m_{\Psi}^2}, \xi \frac{\lambda_{\psi_R}^2 f^2}{m_{\Psi}^2}\right) \right]$$

$$F_u = F_d = F_e = \sqrt{1 - \xi}$$

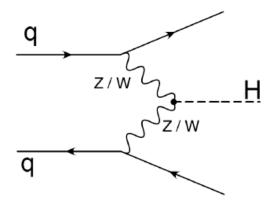
$$\frac{y_d}{m_d} \simeq \frac{F_d}{\sqrt{\xi} f} \left[ 1 - \xi \frac{f_1^2 y_D^2}{4} \frac{\sin^2(\theta_d)}{m_Q^2} + \mathcal{O}\left(\sin^4(\theta_{q,d})\right) \right]$$

$$\frac{y_u}{m_u} \simeq \frac{F_u}{\sqrt{\xi} f} \left[ 1 + \xi \frac{f_1^2 y_U^2}{4} \left( \frac{\sin^2(\theta_q)}{m_U^2} - \frac{\sin^2(\theta_u)}{m_Q^2} \right) + \mathcal{O}\left( \sin^4(\theta_{q,u}) \right) \right]$$

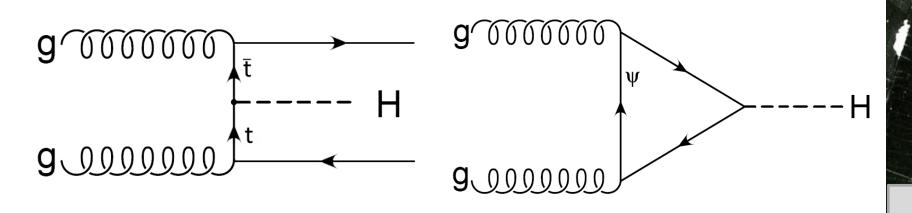
$$\frac{g_{WWh}}{g_{WWh}^{SM}} \simeq \sqrt{1-\xi} \left\{ 1 + \xi \frac{3}{4} \frac{g_0^2}{(g_0^2 + g_1^2)^2} \frac{f^4}{f_0^4 f_1^2} \left[ f_1^2 g_1^2 + f_0^2 \left( g_0^2 + 2g_1^2 \right) \right] \right\}$$

$$\frac{g_{WWhh}}{g_{WWhh}^{SM}} \simeq 1 - 2\xi + \xi(3 - 4\xi) \frac{g_0^2}{g_0^2 + g_1^2} \frac{g_1^2 f_1^2 + f^2}{f_0^2 + f_1^2}$$

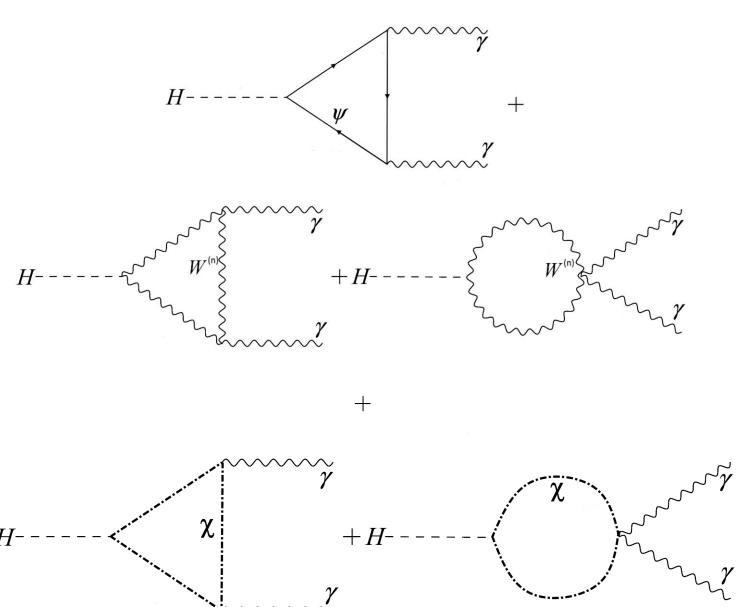
#### Vector boson fusion



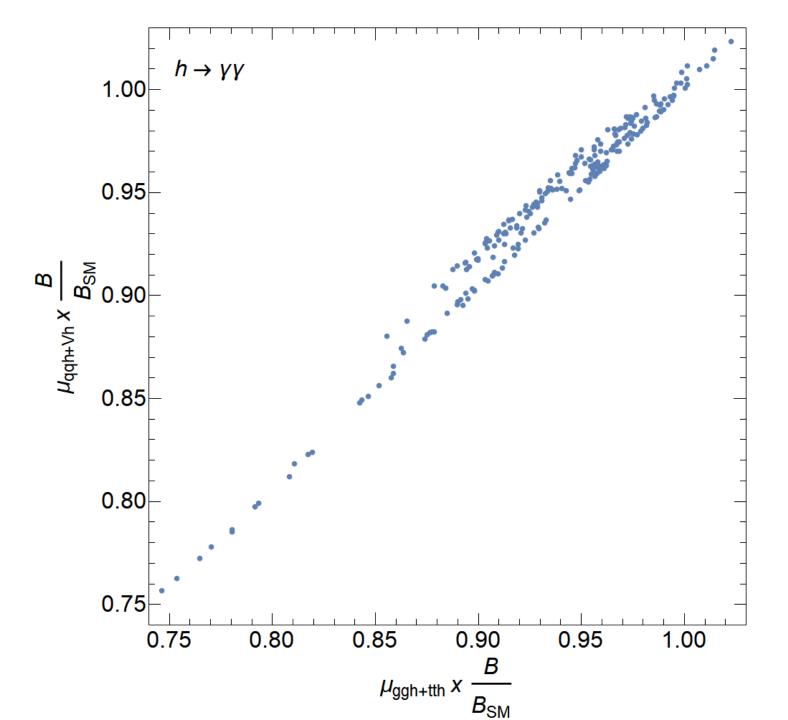
#### ttH and gluon fusion



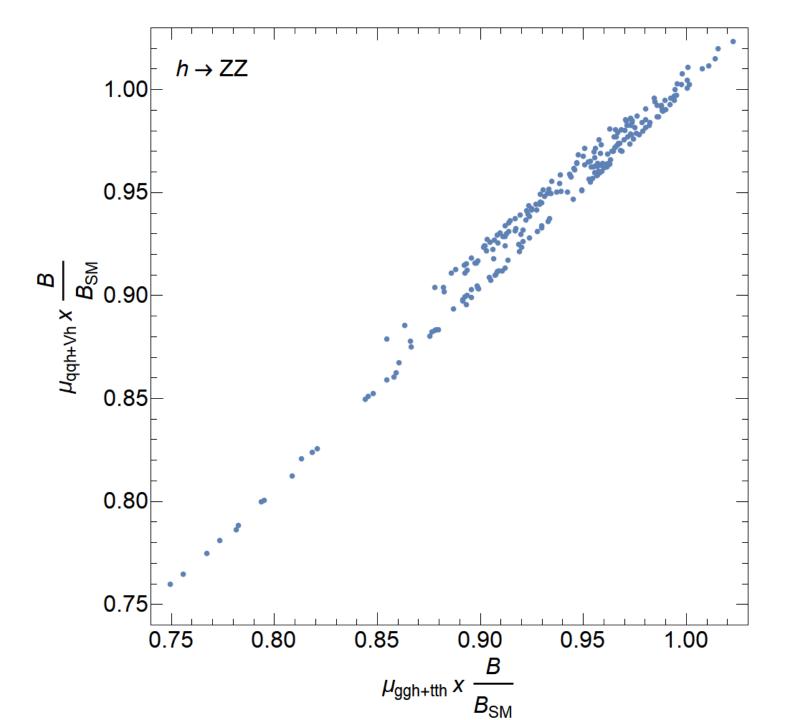
# Decay to photons



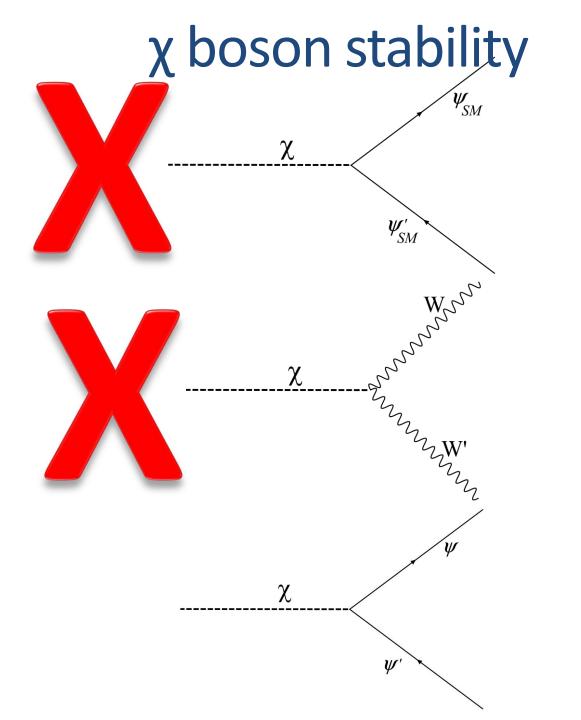
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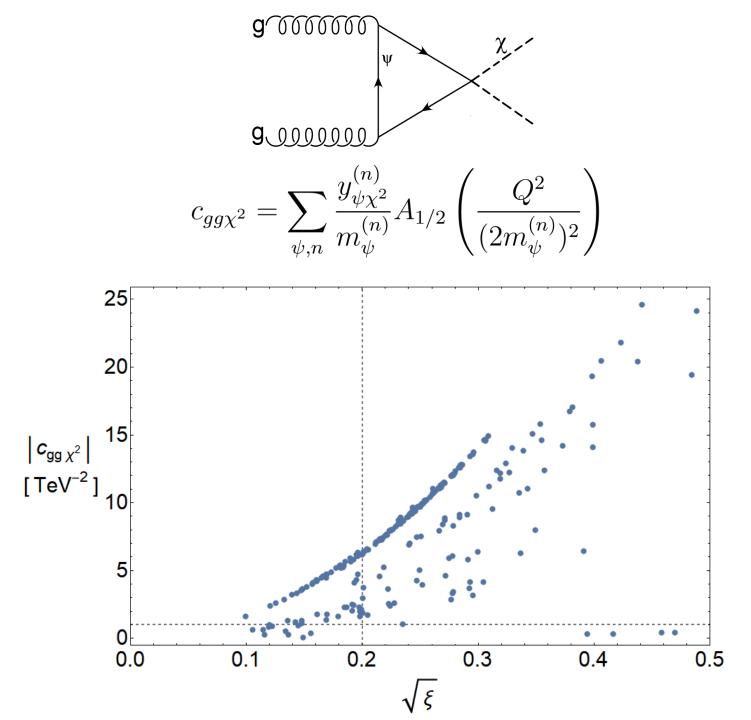


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# Dipole operator

$$\Gamma_{\mathbf{rst}}(p^2) \left[ \overline{(U^{\dagger}\psi_L)}_{\mathbf{r}} (U^{\dagger}a_{\mu\nu})_{\mathbf{s}} \sigma^{\mu\nu} (U^{\dagger}\psi_R)_{\mathbf{t}} \right]_{\mathbf{1}}$$

# SO(7) generators

$$(T_{ij})_{k\ell} = \frac{i}{\sqrt{2}} (\delta_{ik}\delta_{j\ell} - \delta_{i\ell}\delta_{jk}) , \qquad i < j, , i = 1, \dots 6, j = 2, \dots 7$$

$$T_1^L = -\frac{1}{\sqrt{2}} (T_{23} + T_{14}) T_2^L \qquad = \frac{1}{\sqrt{2}} (T_{13} - T_{24}) \qquad T_3^L = -\frac{1}{\sqrt{2}} (T_{12} + T_{34})$$

$$T_1^R = -\frac{1}{\sqrt{2}} (T_{23} - T_{14}) T_2^R \qquad = \frac{1}{\sqrt{2}} (T_{13} + T_{24}) \qquad T_3^R = -\frac{1}{\sqrt{2}} (T_{12} - T_{34})$$

 $7\otimes 21\sim 7\oplus 35\oplus 105$ 

 $X = T_{67}$ .