

On self-interacting dark matter: Current status and perspectives

Kai Schmidt-Hoberg

Task:

kindly ask you to talk about (one of) the **following topics**:

**Overview of SIDM including astroparticle probes,
structure formation and laboratory probes.**

With best regards,
Claudia and Mads
(local organizers of DAVCo)

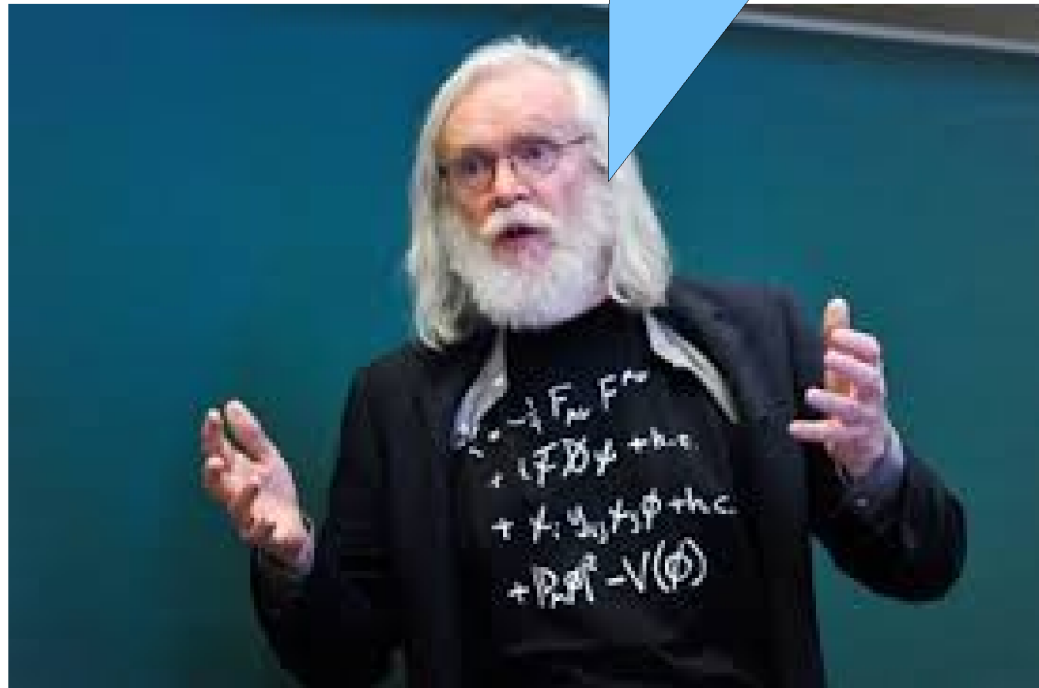
partially based on work with

T Bringmann, M Frandsen, F Kahlhoefer, J Kummer, S. Sarkar, P Walia, S Wild

Prelude: Thoughts about the SUSY WIMP

but being in Odense...

“SUSY anywhere is better than SUSY nowhere!”



Why we like(d) SUSY

- > **Hierarchy problem:** stabilizes the weak against the Planck scale
- > **Dark matter:** If lightest SUSY particle stable \rightarrow dark matter candidate
- > **Gauge coupling unification:**
- > **A 125 GeV Higgs boson:** Additional hint for SUSY?

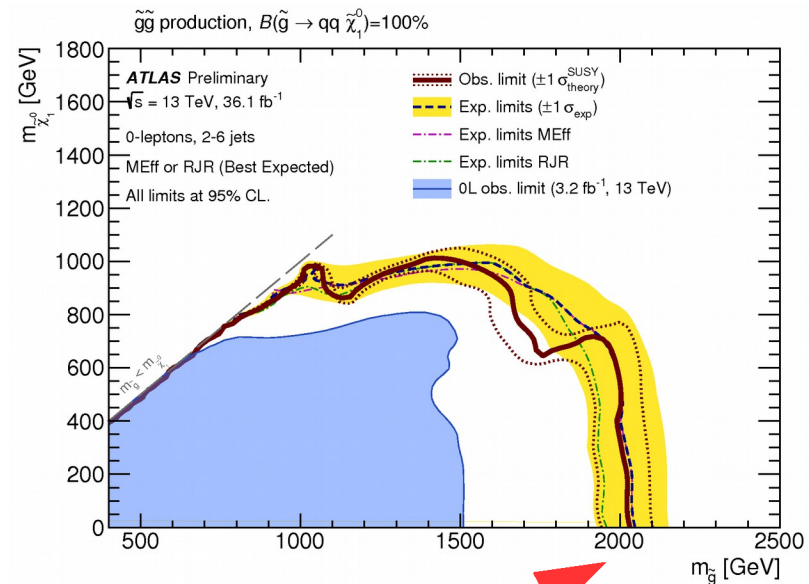
...someone from Odense still owes me...



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> So why do people get worried?



$\sim 2 \text{ TeV}$

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- > So why do people get worried?

NATURALNESS!



But nature doesn't always do what one might expect...

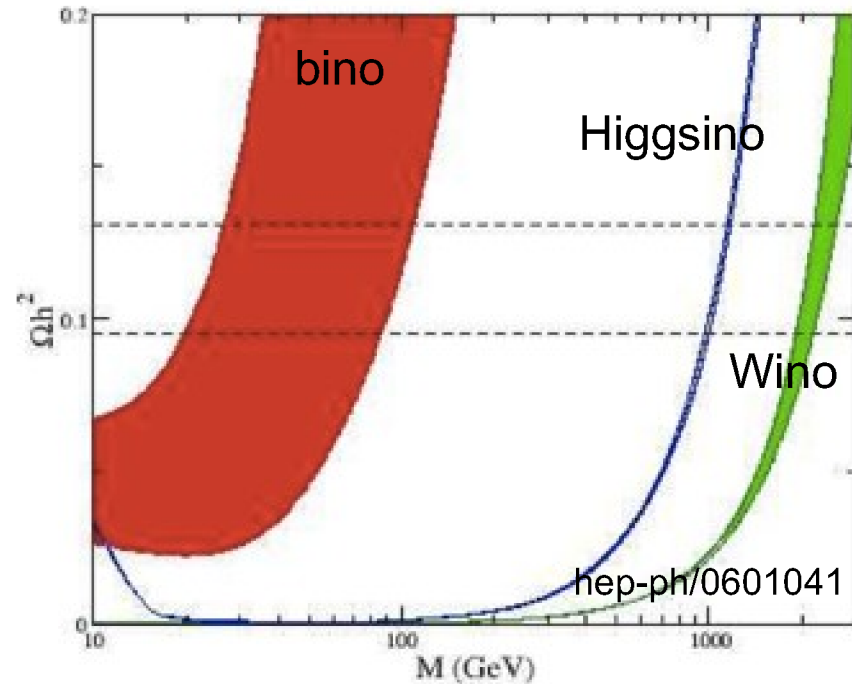
DM naturalness in the MSSM

- MSSM neutralino - the prototypical WIMP
- How naturally can the dark matter relic abundance be achieved?

Bino: Typically need to finely tune relic density via coannihilations or resonances :-)

2-3 TeV Wino challenged by ID
Lisanti et al [1307.4082](#)

1 TeV Higgsino looking good :-)



EW naturalness in the MSSM

- > Electroweak vev (or m_Z) determined by SUSY parameters

$$m_Z^2 = -2(m_{H_u}^2 + |\mu|^2) + \dots$$

- > Cancellation (tuning) needed for large SUSY masses $\rightarrow \Delta_p \equiv \frac{\partial \ln v^2}{\partial \ln p} = \frac{p}{v^2} \frac{\partial v^2}{\partial p}$

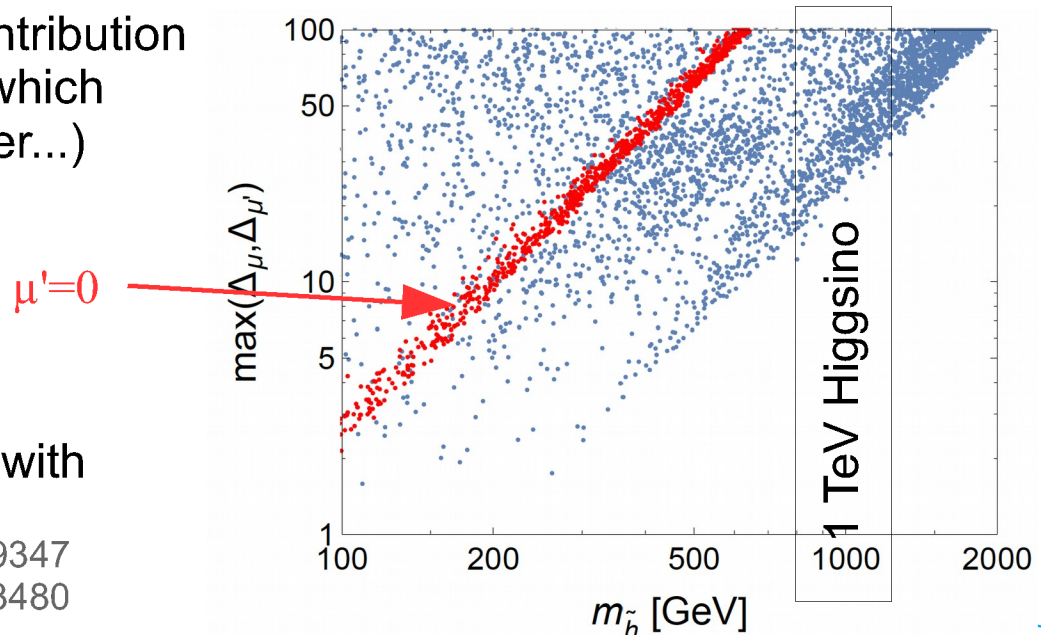
Higgsino mass $\sim \mu \sim 1 \text{ TeV} \rightarrow \Delta_\mu \sim \frac{2\mu^2}{M_Z^2} \sim 250$

- > However: possible soft contribution μ' to the Higgsino mass (which most people never consider...)

$$m_h \sim \mu + \mu'$$

- > Allows for 1 TeV Higgsino with moderate FT!

1603.09347
1701.03480



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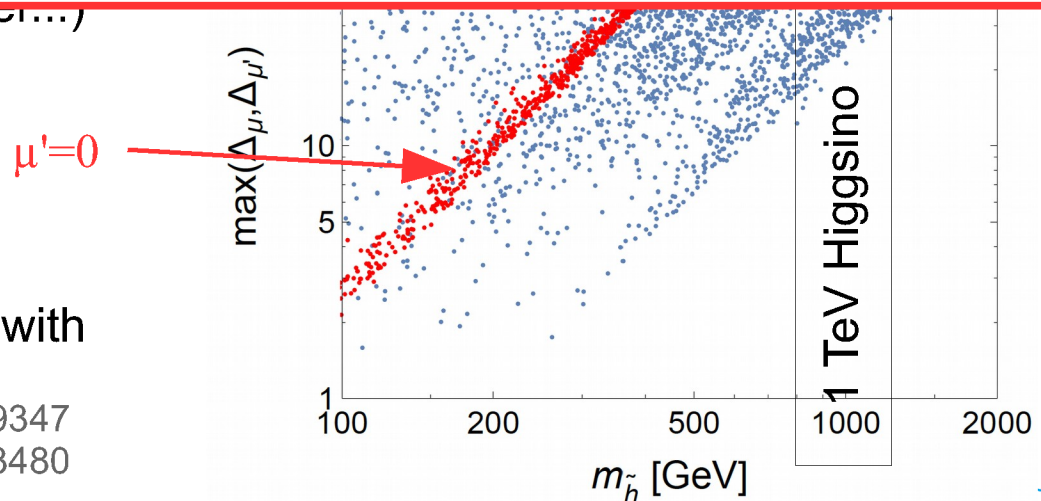
- > How μ' t...
most people never consider...)

...and now to the 'real' talk

$$m_h \sim \mu + \mu'$$

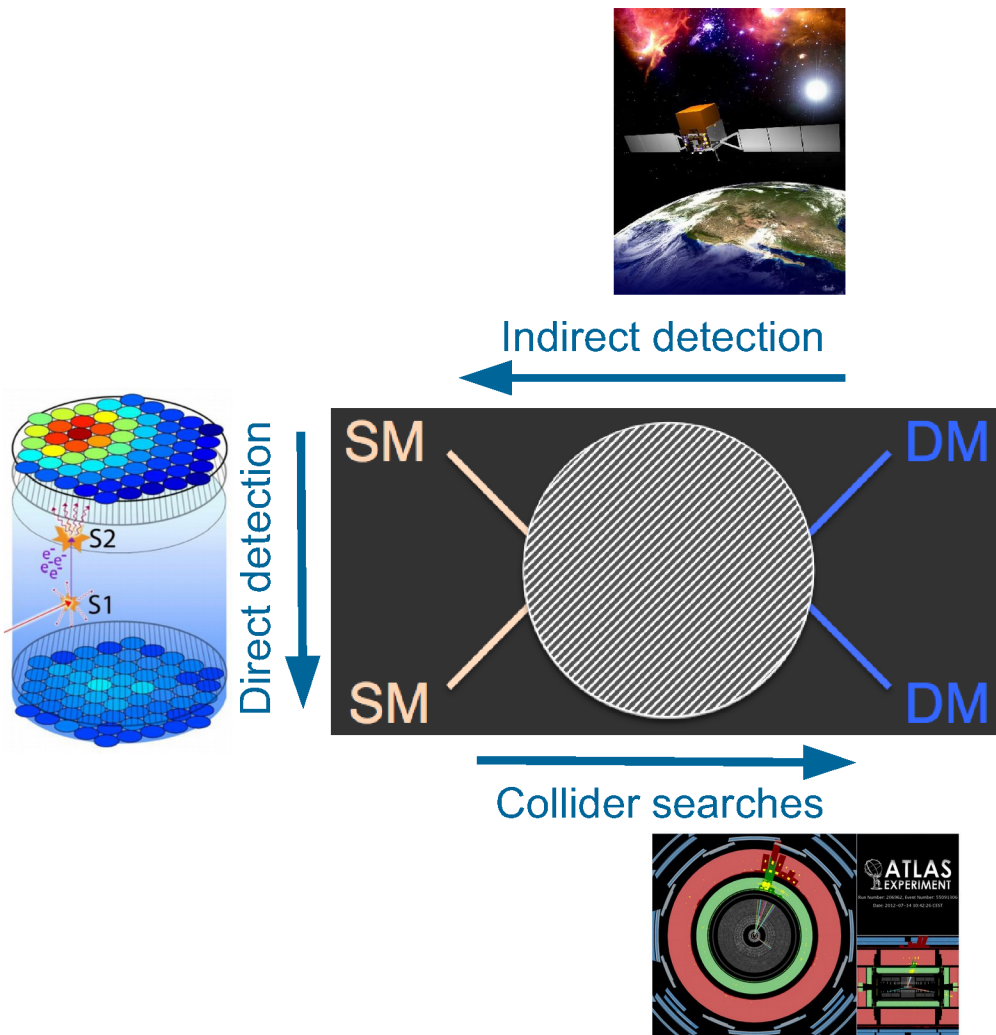
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How to constrain the properties of dark matter?

- > Our 'usual way' to search for dark matter

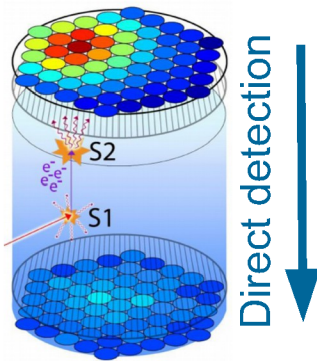


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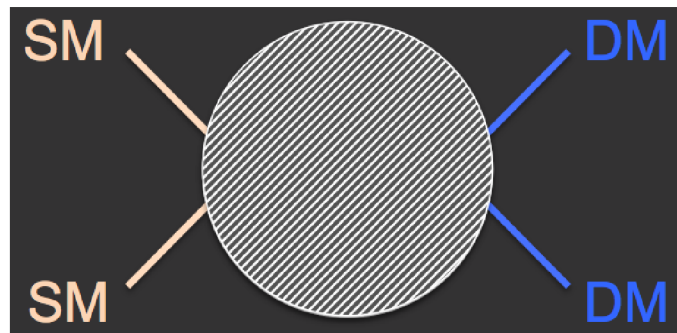
- > Our 'usual way' to search for dark matter
- > A fourth way...



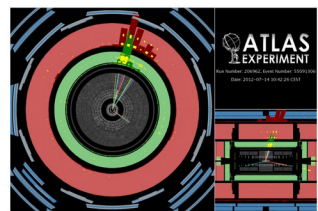
Indirect detection



Direct detection

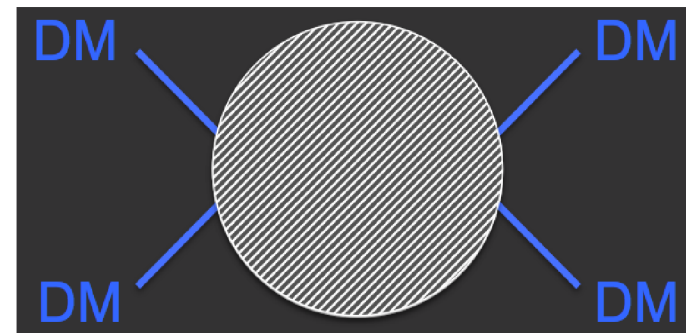


Collider searches



See also talks by
T Bringmann and F Kahlhoefer

This Talk:

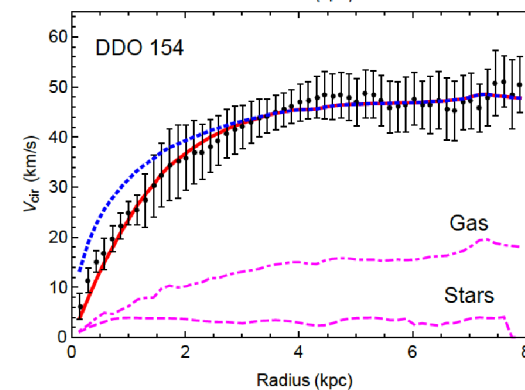
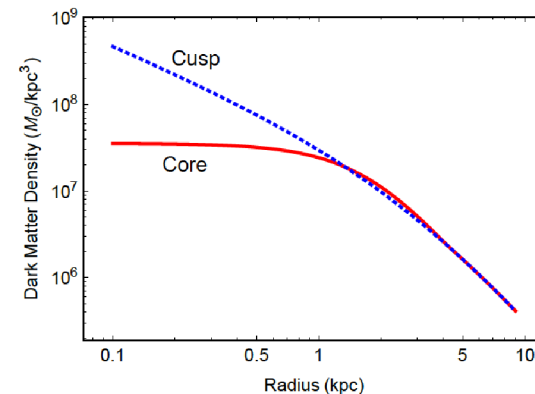


DM self-interactions

Motivation: Cosmology

- The collisionless cold dark matter paradigm fits perfectly at large scales
- There are however various discrepancies between N-body simulations of collisionless cold DM and astrophysical observations on galactic scales:

- Cusp-vs-core problem

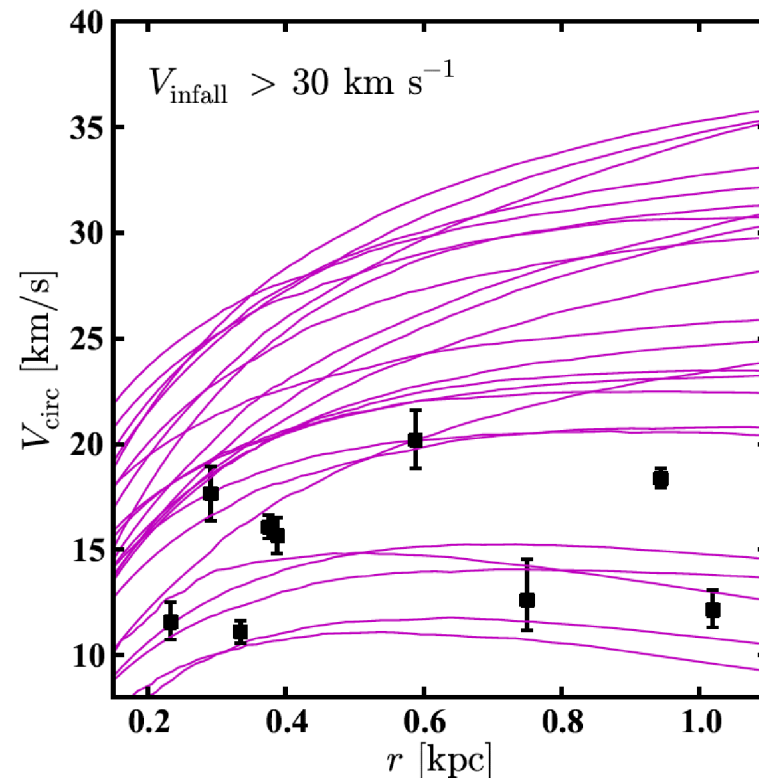


Tulin, Yu: 1705.02358

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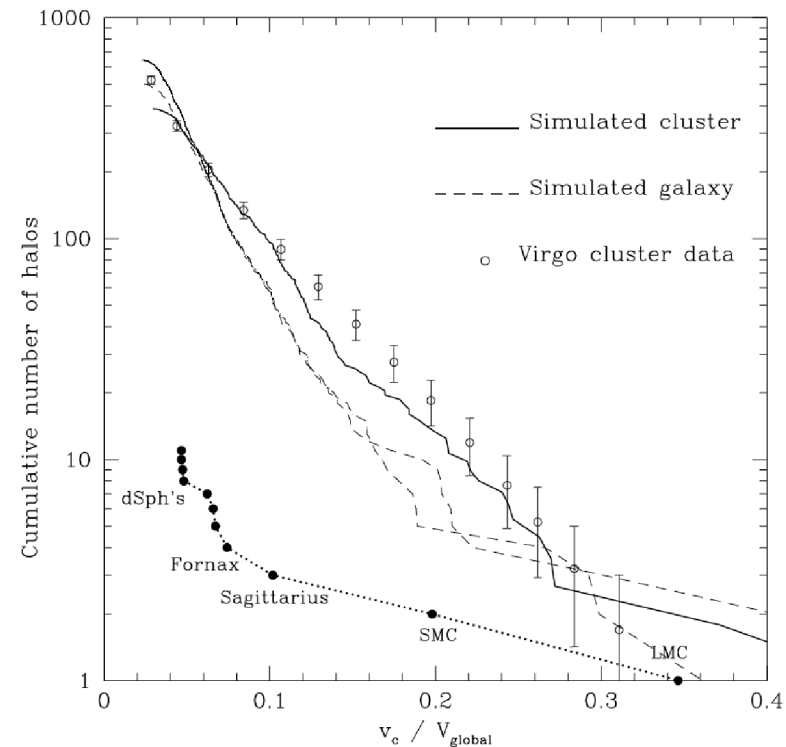


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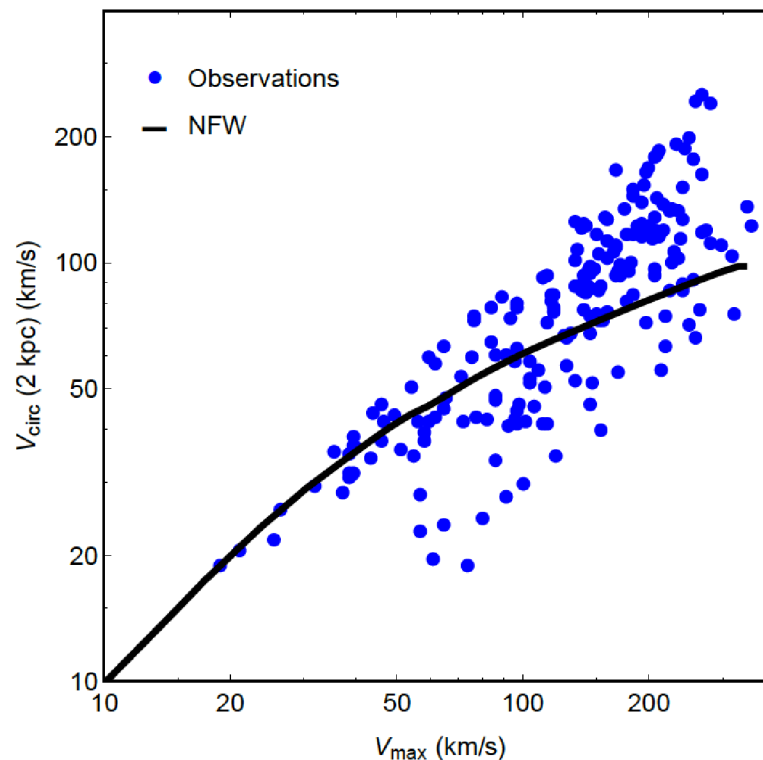


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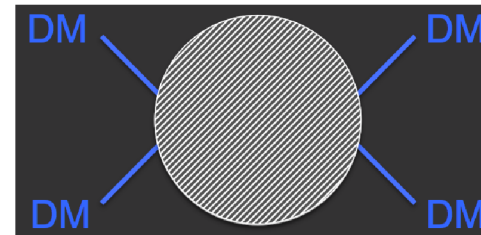


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DM self-interactions may solve some (or all) of these problems



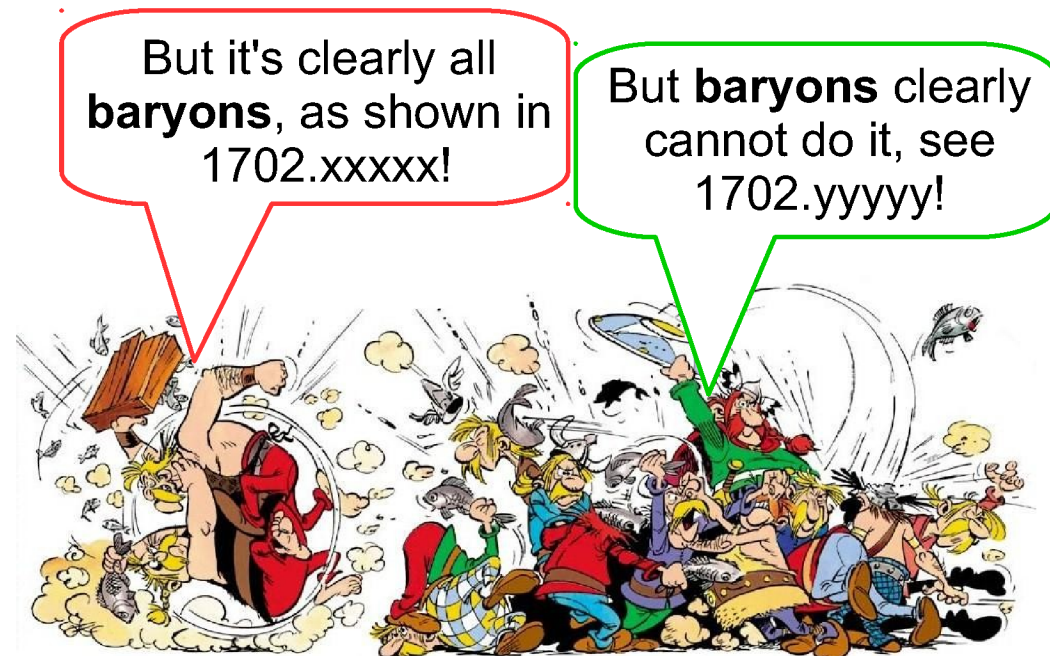
Spergel & Steinhard: astro-ph/9909386
Arsen, Bringmann, Pfrommer, 1205.5809

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Motivation: Particle physics

- Dark sector often assumed to be simple, mainly because we don't know much...
- Large self-interactions are natural in models with a more complex dark sector (e.g. with a new gauge group)

- Strongly interacting DM

Carlson, Machacek, Hall (1992)
Kusenko, Steinhardt: astro-ph/0106008

- New light mediator in the dark sector

Feng, Kaplinghat, Yu: arXiv:0905.3039
Buckley & Fox: arXiv:0911.3898
Loeb & Weiner: arXiv:1011.6374

- Bonus: We can potentially study the dark sector even if DM has highly suppressed couplings to Standard Model particles.

How large a cross section?

- To be observable on astrophysical scales, self-interaction cross sections have to be large, typically

$$\sigma / m_\chi \sim 1 \text{ cm}^2/\text{g} \sim 2 \text{ barns}/\text{GeV}$$

- The nucleon nucleon scattering cross section ~ 20 barns at low energies
- The typical cross section of a WIMP is 20 orders of magnitude smaller!

- **Potential impact:** Evidence for DM self-interactions on astrophysical scales would rule out most popular models for DM, such as supersymmetric WIMPs, gravitinos, axions...

Constraints on self-interactions

- Various astrophysical observations give constraints on SIDM:

- Bullet cluster Randall et al 0704.0261



- Subhalo evaporation rate

Gnedin, Ostriker: astro-ph/0010436

- Halo ellipticity

Miralda-Escude (2002)

- Core density in clusters and dwarfs

Yoshida et al.: astro-ph/0006134

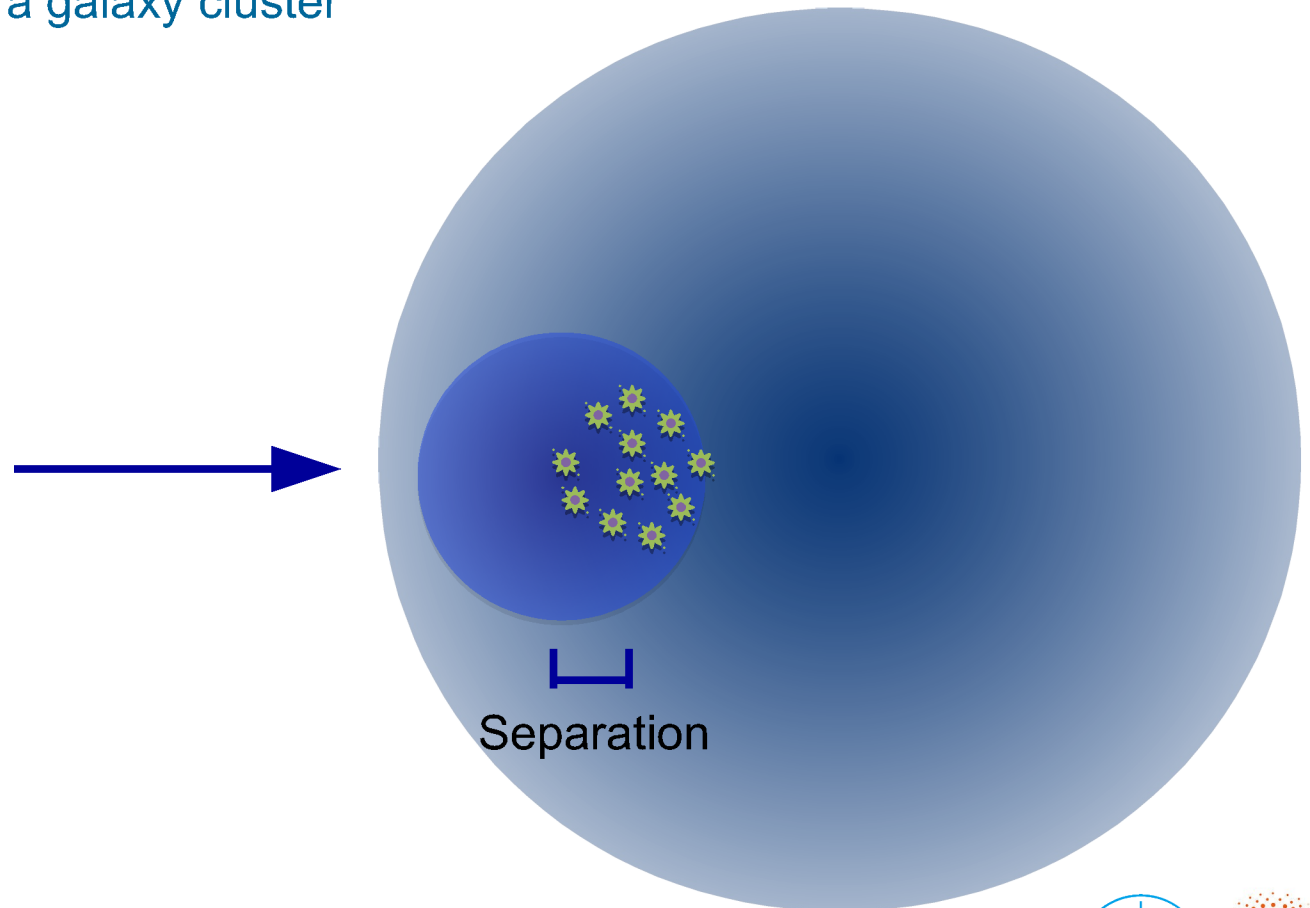
Dave et al.: astro-ph/0006218

- SIDM probed at different velocities in different systems

→ a handle on the velocity dependence of the self scattering cross section!

A smoking gun observable

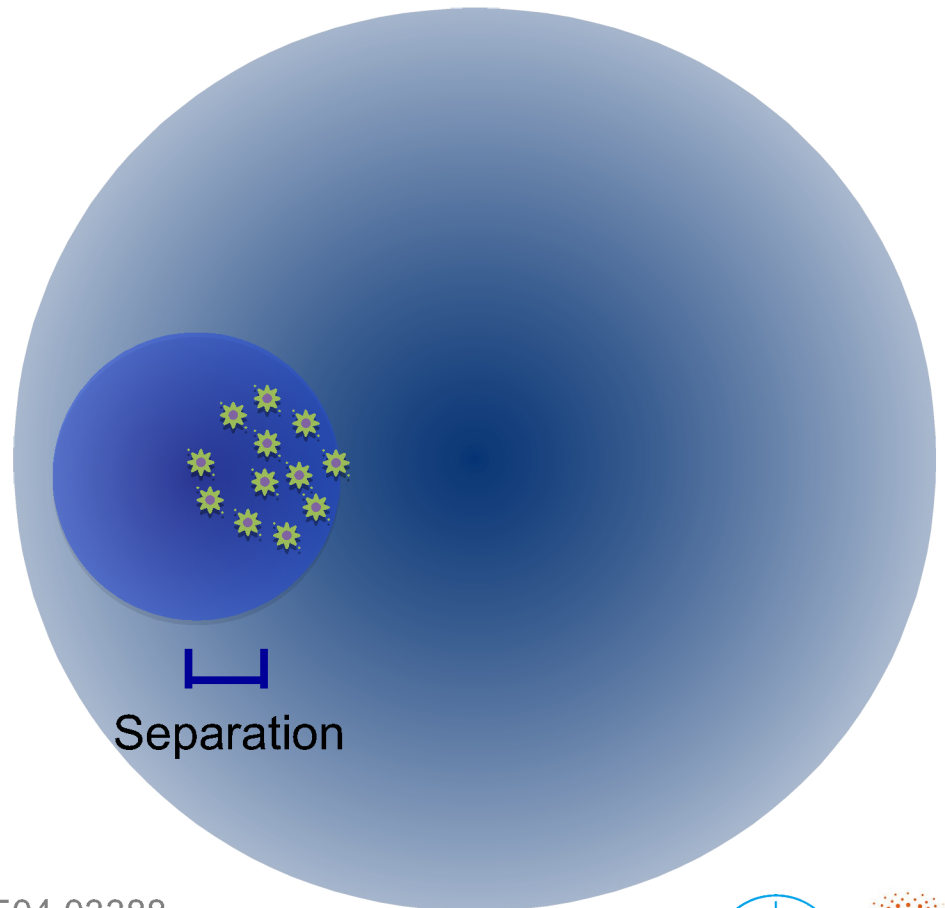
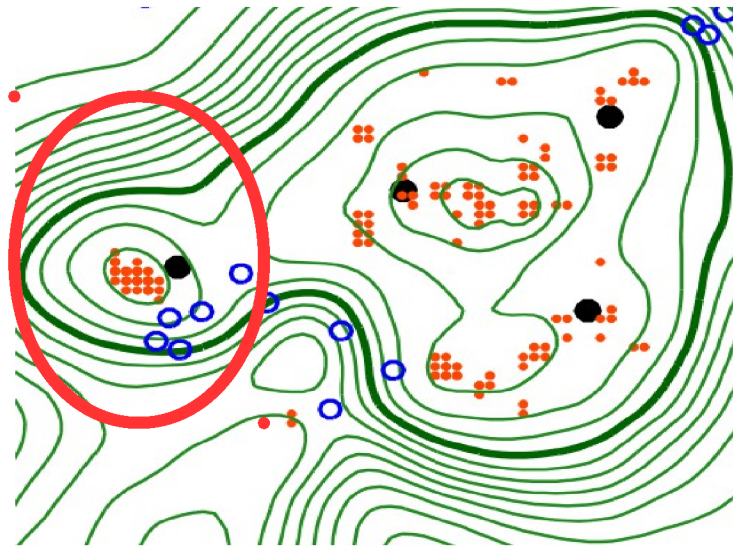
- Smoking gun signal? Separation between dark matter halo and stars of a galaxy falling into a galaxy cluster



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Observed offset: $1.62 \pm 0.48 \text{ kpc}$



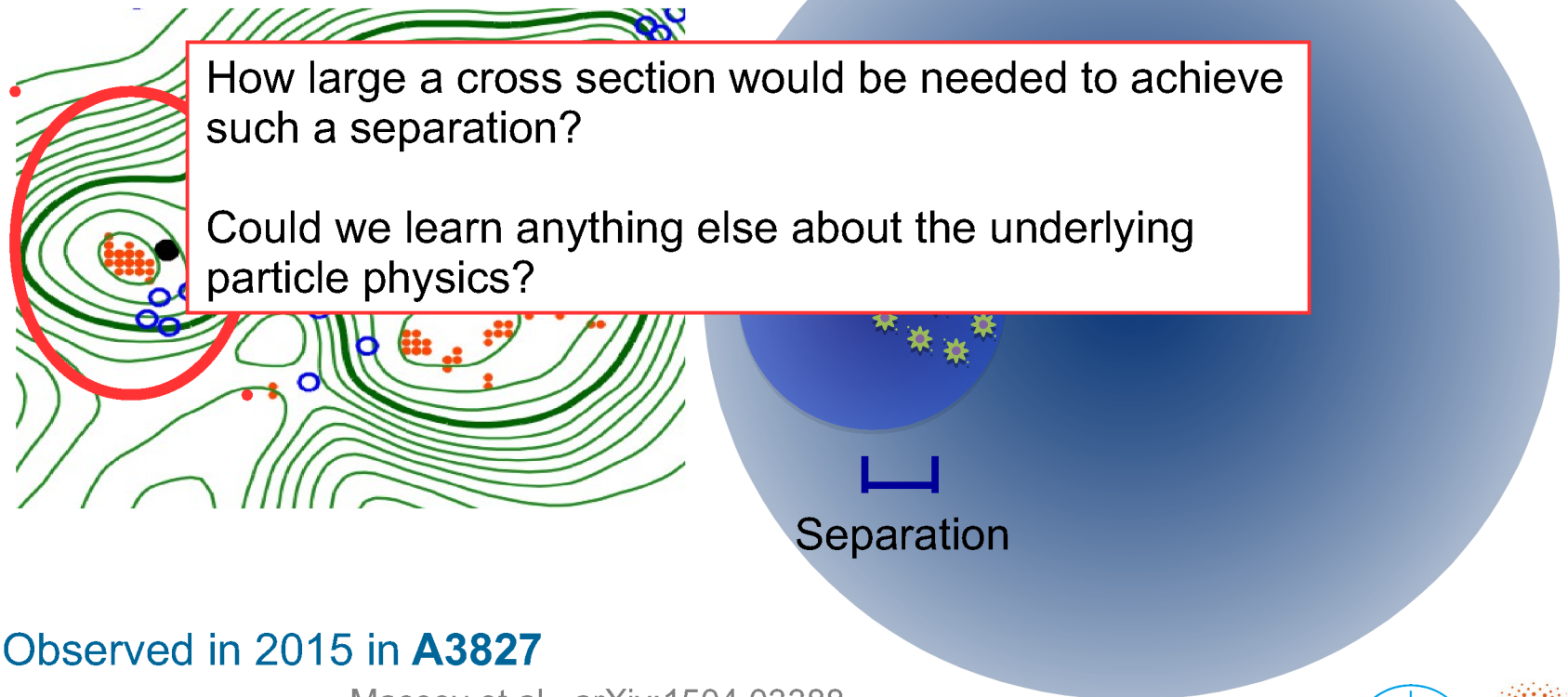
- Observed in 2015 in **A3827**

Massey et al., arXiv:1504.03388

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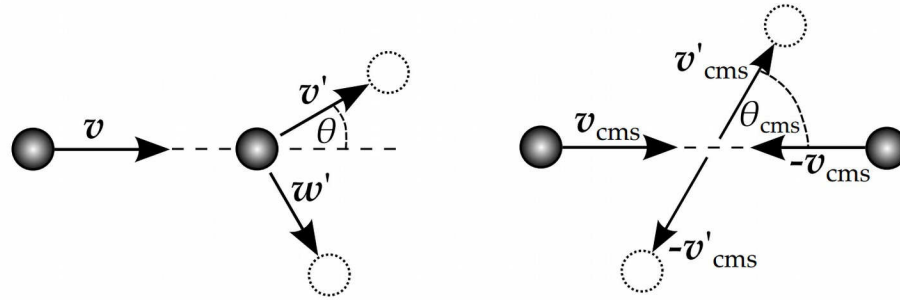
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Frequent vs. rare scatters



The momentum transfer in a collision of two DM particles is completely fixed by the scattering angle. The effective momentum transfer is given by

$$\sigma_T = 2\pi \int_{-1}^1 \frac{d\sigma}{d\Omega} (1 - |\cos \theta|) d \cos \theta$$

This is the quantity typically studied

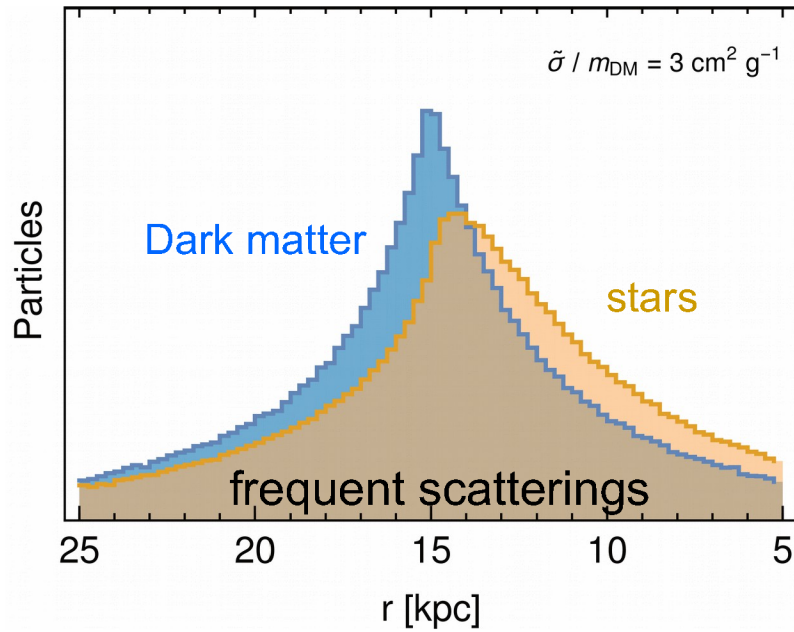
However, this is not all that matters...

Kahlhoefer et al, 1308.3419

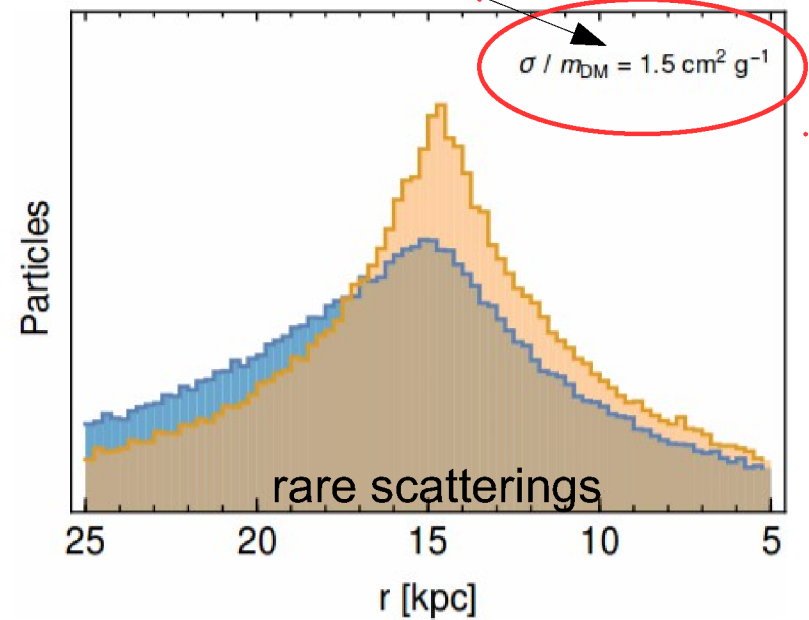
Can be obtained with **rare scatters and large momentum transfer** (e.g. isotropic scattering) or **frequent scatters with small momentum transfer** (e.g. long range interactions)

Infalling galaxy in A3827

Kahlhoefer et al, 1504.06576



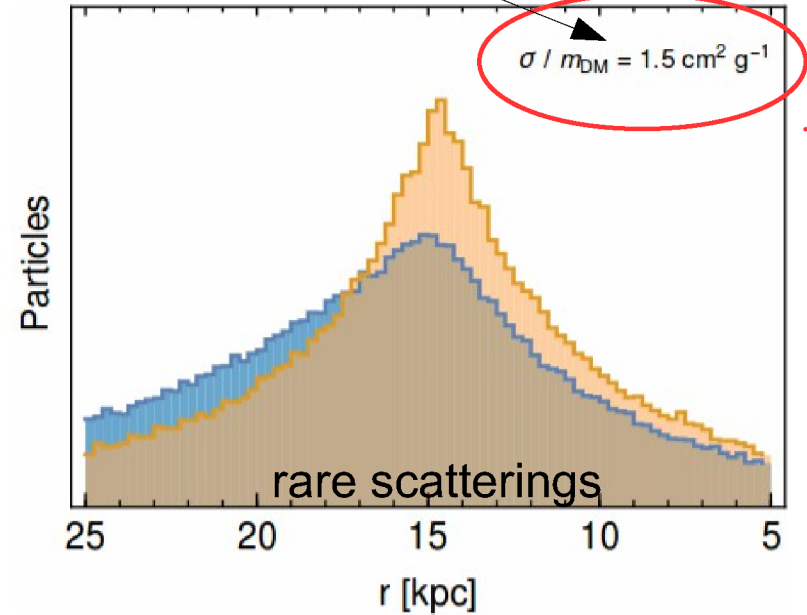
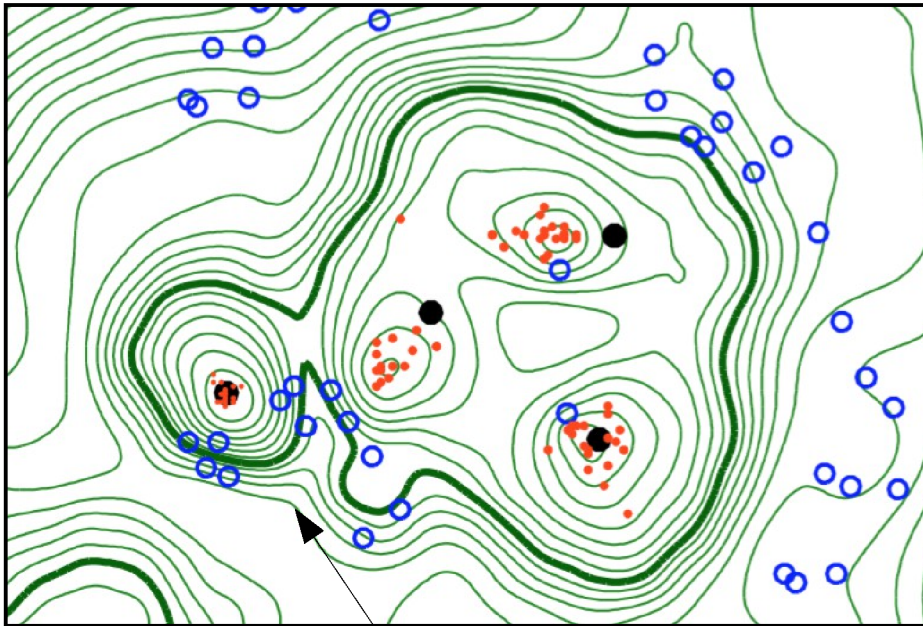
A3827: In (some) tension with upper bounds



Infalling galaxy in A3827

R Massey, talk at SIDM17

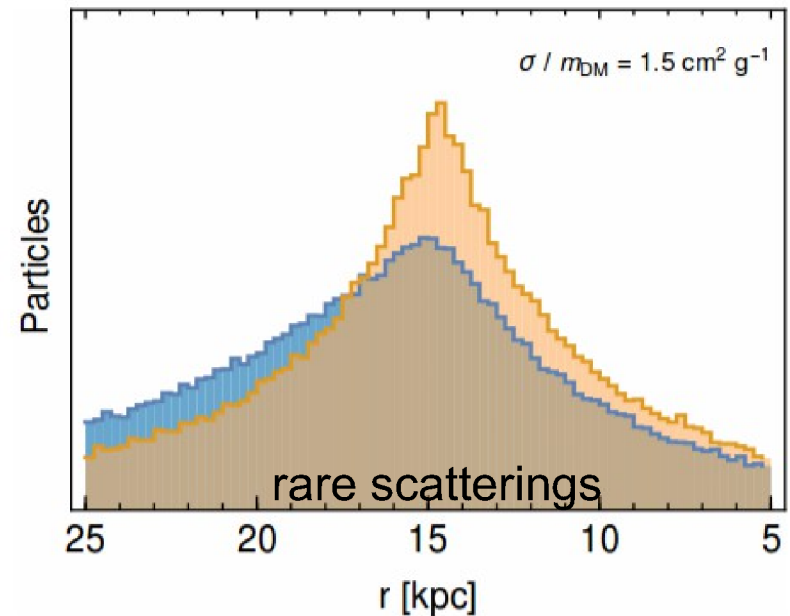
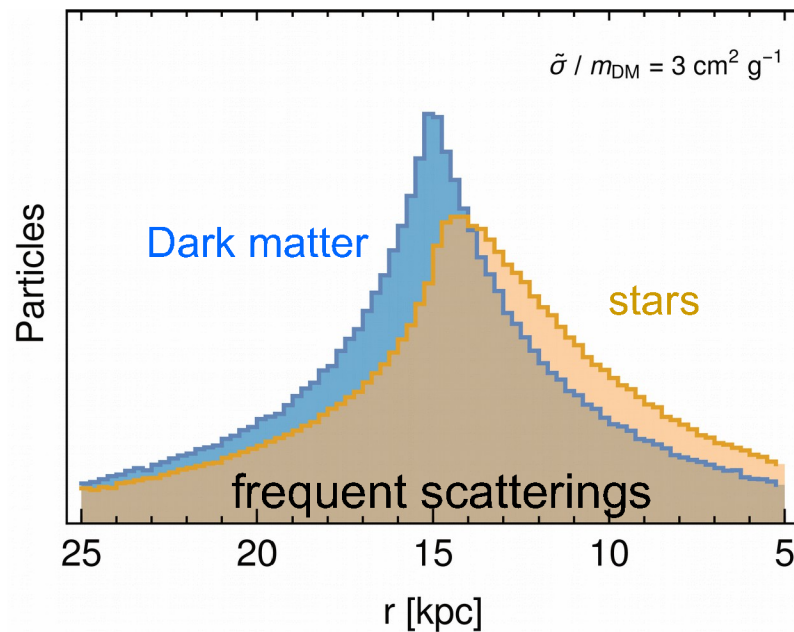
A3827: In (some) tension with upper bounds



Reanalysis from 2017 – offset gone :-('

More generally: Distinguishing different types of SIDM

Kahlhoefer et al, 1504.06576



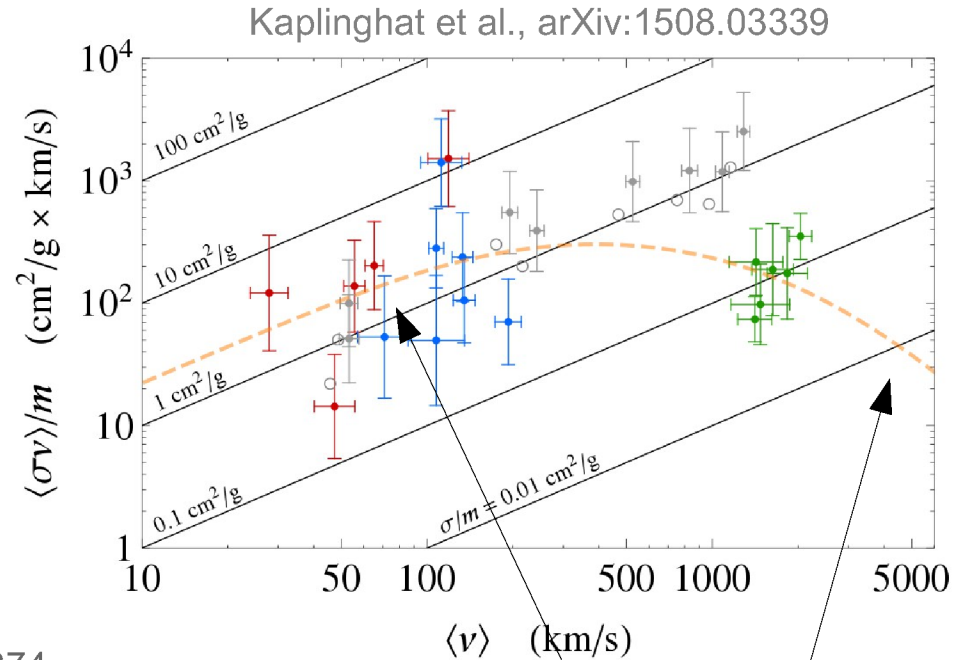
- **Effective drag force:** the DM subhalo retains its shape, while the distribution of stars are both shifted and deformed.
- **Contact interactions:** the DM subhalo is deformed due to the scattered DM particles leaving the subhalo in the backward direction.
- Potentially distinguishable (but very tough)!

Velocity dependent self-interactions

- Idea: Relate core size of different systems to SIDM cross section
- DM self-interactions seem to depend on the typical relative velocity of DM particles.
- Simplest realisation
→ light mediator!

Loeb & Weiner: arXiv:1011.6374

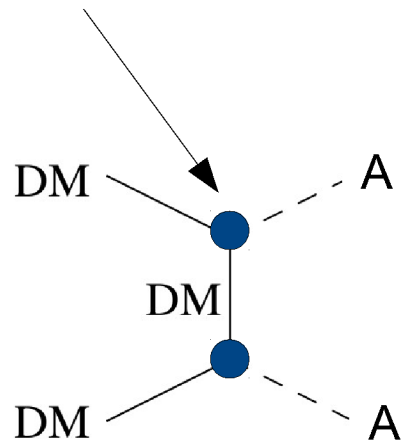
- Consider a mediator with mass $m_{\text{med}} \sim m_{\text{DM}} v_{\text{DM}}$:
 - Scattering for small momentum transfer ($q < m_{\text{med}}$) proportional to $1/m_{\text{med}}^4$
 - Scattering for large momentum transfer ($q > m_{\text{med}}$) proportional to $1/q^4$



A new light mediator

- > The relic abundance is typically set by annihilations into pairs of mediators (so-called dark sector freeze-out):

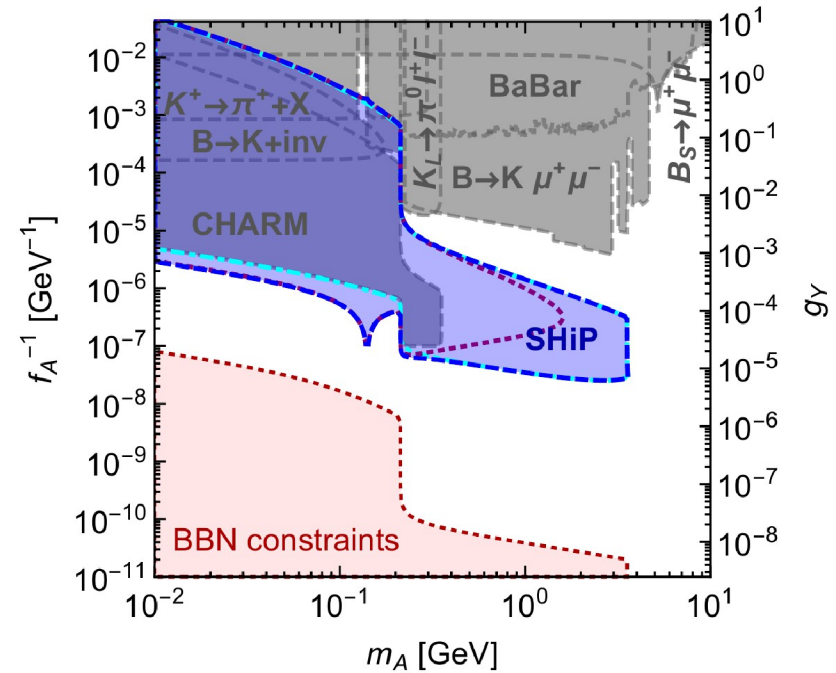
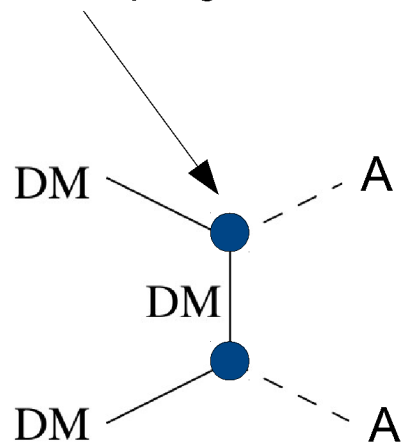
Fix dark sector coupling via relic abundance



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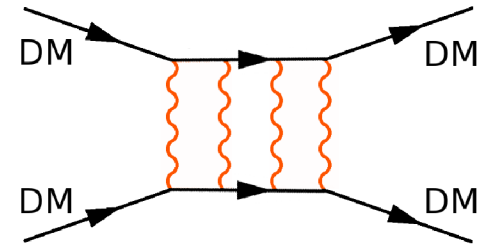
Fix dark sector coupling via relic abundance



- To avoid overclosing the Universe, the mediator should ultimately decay, so its couplings to SM states cannot be arbitrarily small

Enhancement of DM self-interactions

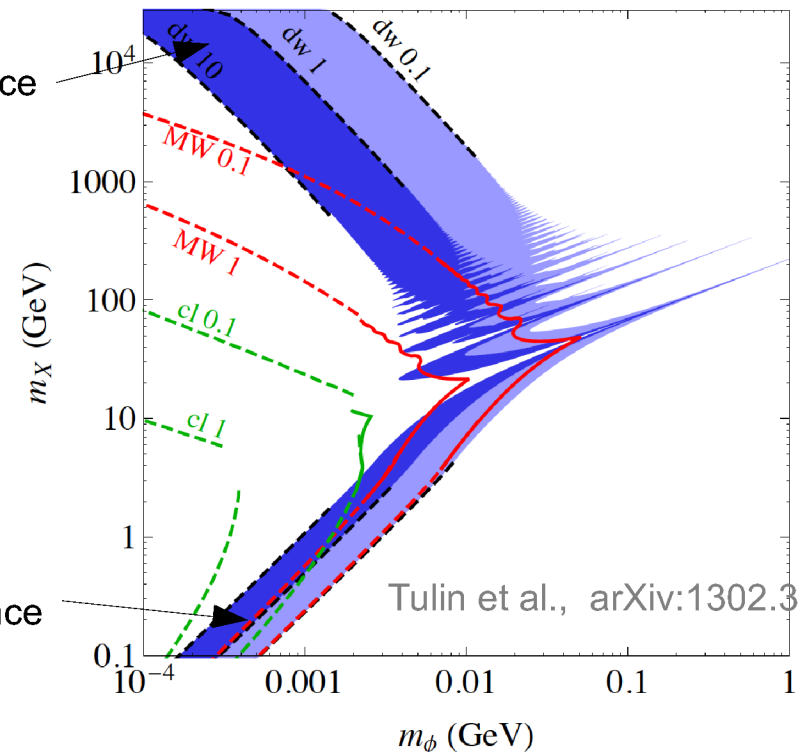
- DM self-interactions are enhanced also by non-perturbative effects due to multiple mediator exchange.
- Scalar and vector mediators particularly interesting



Dark matter with relic density (s -wave)

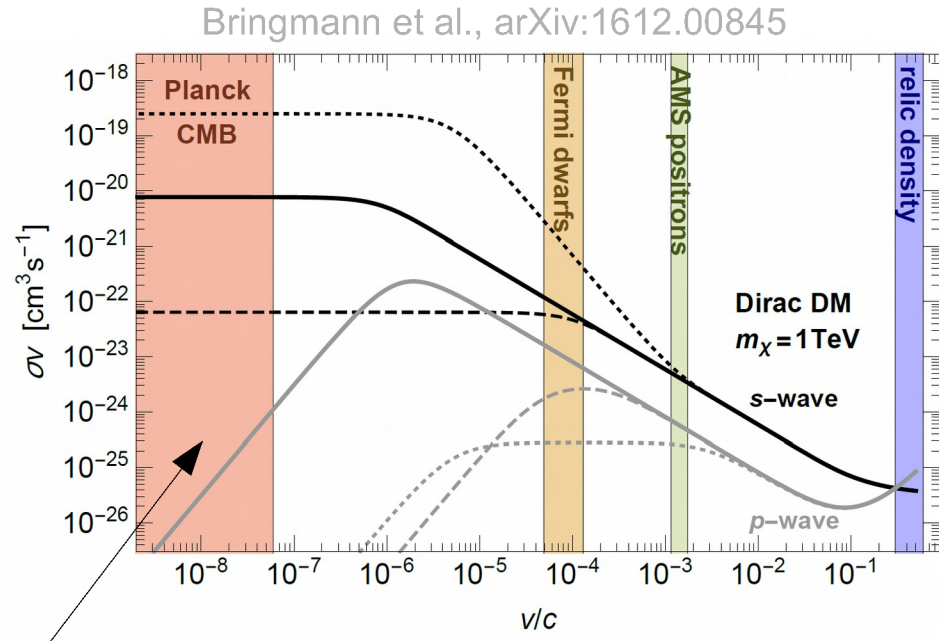
strong velocity dependence

weak velocity dependence



Enhancement of DM annihilations

- Significant non-perturbative corrections to the tree-level annihilation rate (Sommerfeld enhancement).
- Effects small during freeze-out, but increase with decreasing DM velocity.

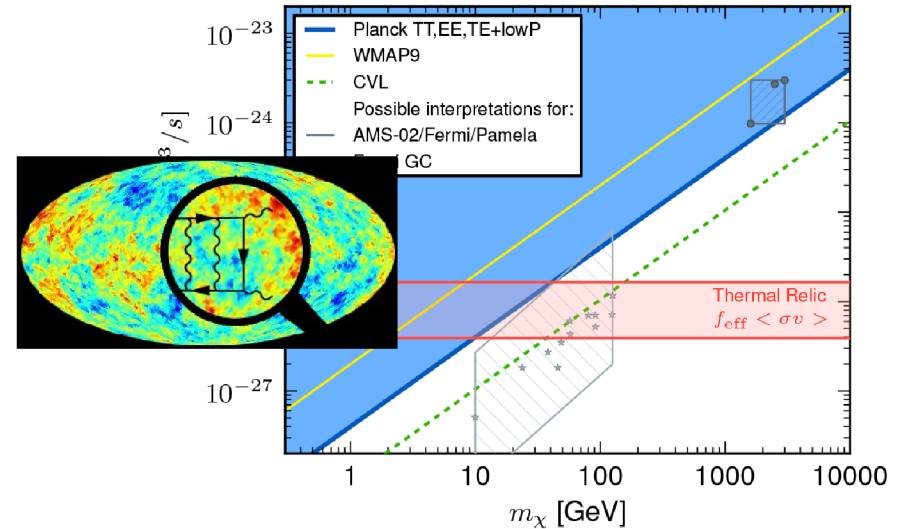


During recombination
dark matter particles
move at walking speed.

Constraints on DM self-interactions

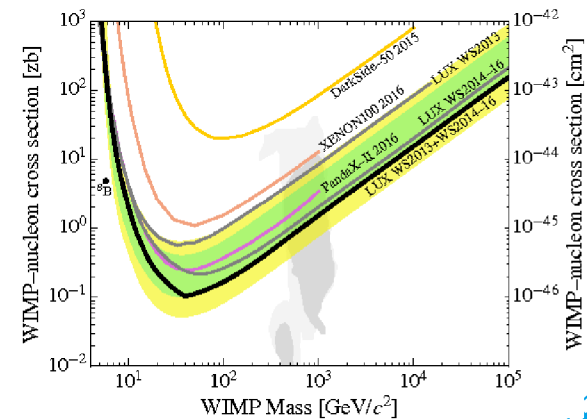
- DM annihilations during recombination, followed by mediator decays into SM particles, inject energetic electrons and photons into the plasma.

→ very strong reionisation bounds from the CMB for s-wave annihilation



- DM-nucleon scattering cross section also strongly enhanced for light mediators

→ see talk by Felix



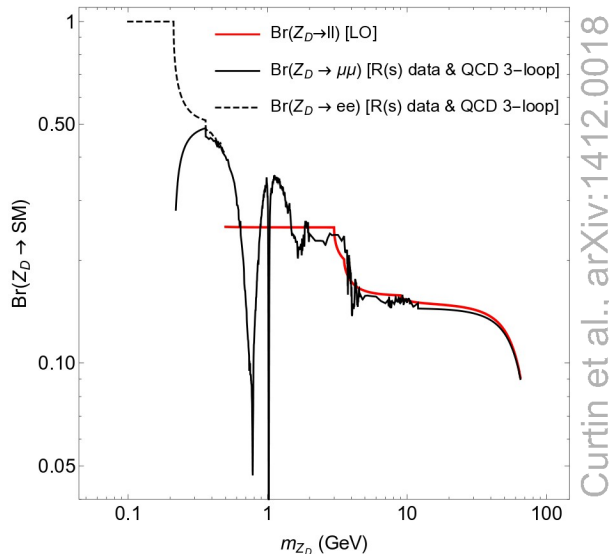
Vector mediators

- Example: A new gauge boson from a spontaneously broken U(1)' gauge group that mixes with the neutral gauge bosons of the Standard Model.

$$\mathcal{L} \supset -g_\chi^V \phi^\mu \bar{\chi} \gamma_\mu \chi - \frac{1}{2} \sin \epsilon B_{\mu\nu} \phi^{\mu\nu} - \delta m^2 \phi^\mu Z_\mu$$

Kinetic mixing:
Mediator obtains photon-like couplings

Mass mixing:
Mediator obtains Z-like couplings



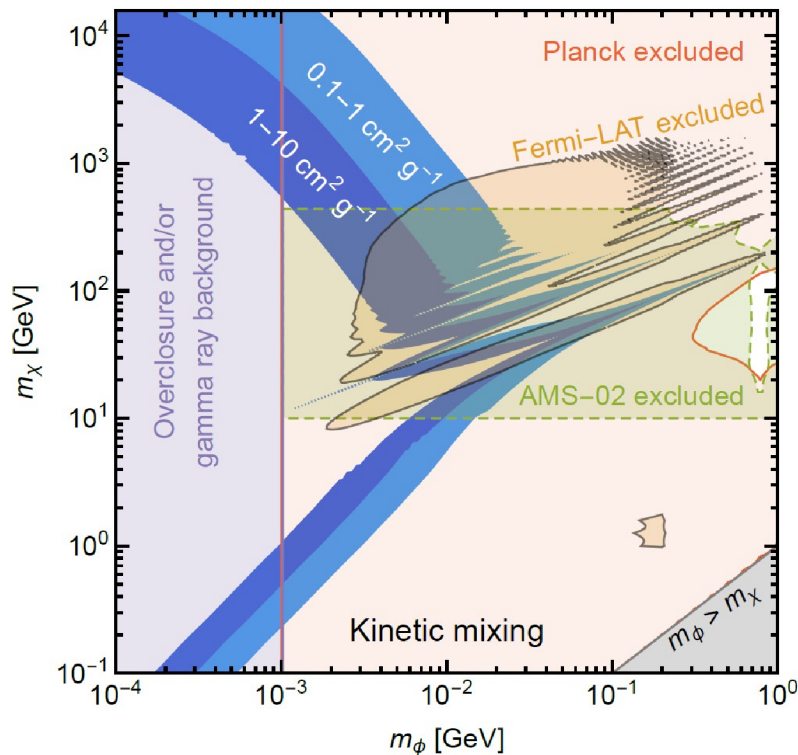
➤ Main difference:

- A gauge boson with kinetic mixing is effectively stable below the electron threshold.
- Mass mixing induces sizable decay rates into neutrinos

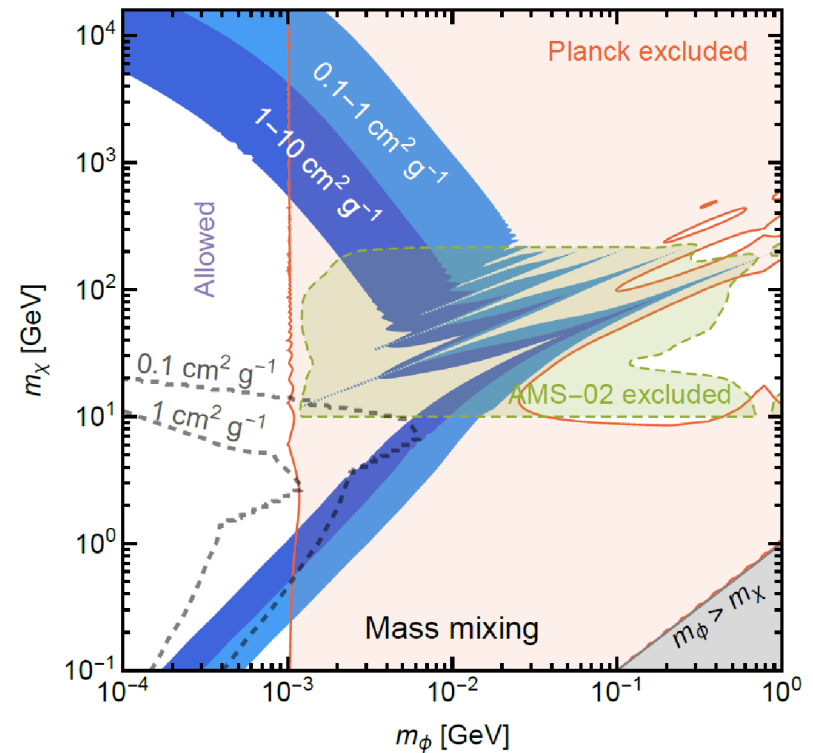
Constraints on vector mediators

- For vector mediators, DM annihilation proceeds via s-wave:
 - Large Sommerfeld enhancement for small velocities
 - g_x fixed by relic density – essentially independent of coupling to SM

Bringmann et al., arXiv:1612.00845

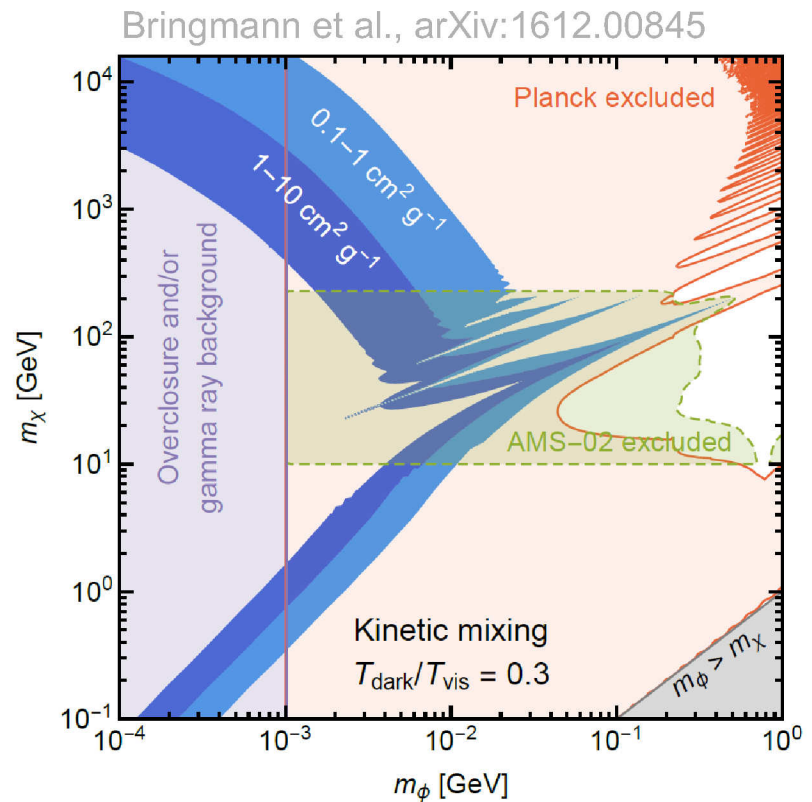


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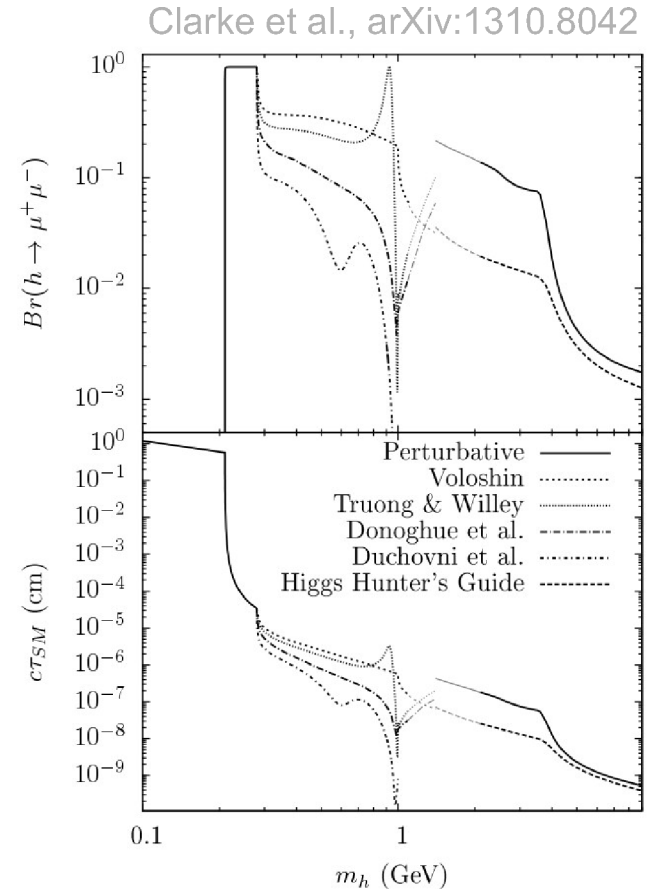
Constraints on vector mediators

- Only assumption: The two sectors have the same temperature during freeze out.
- But even for different temperatures in the two sectors there are very strong constraints.



Scalar mediators

- Example: A real scalar singlet that obtains a vacuum expectation value and mixes with the SM Higgs boson.
- This mixing induces Yukawa-like couplings to SM fermions consistent with minimal flavour violation:
$$\mathcal{L} = \mathcal{L}_{\text{SM}} - \frac{g_y m_f}{v} \phi \bar{f} f - \frac{1}{2} \kappa \phi \bar{\chi} \chi$$
- Branching ratios in the GeV region are difficult to calculate due to hadronic resonances
- Below the pion threshold the leptonic and photonic decay modes are well understood.



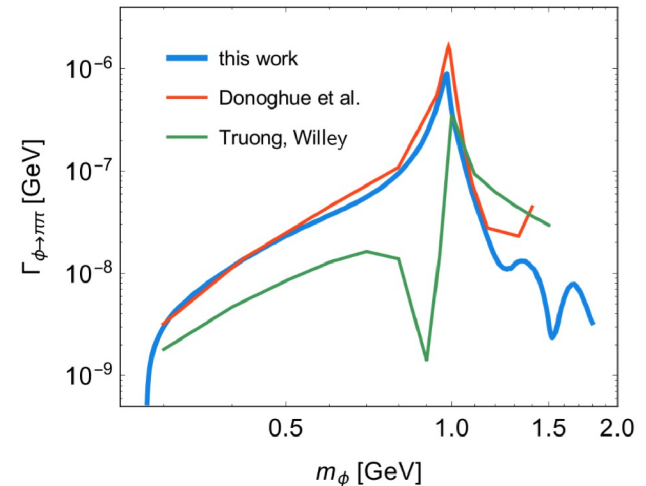
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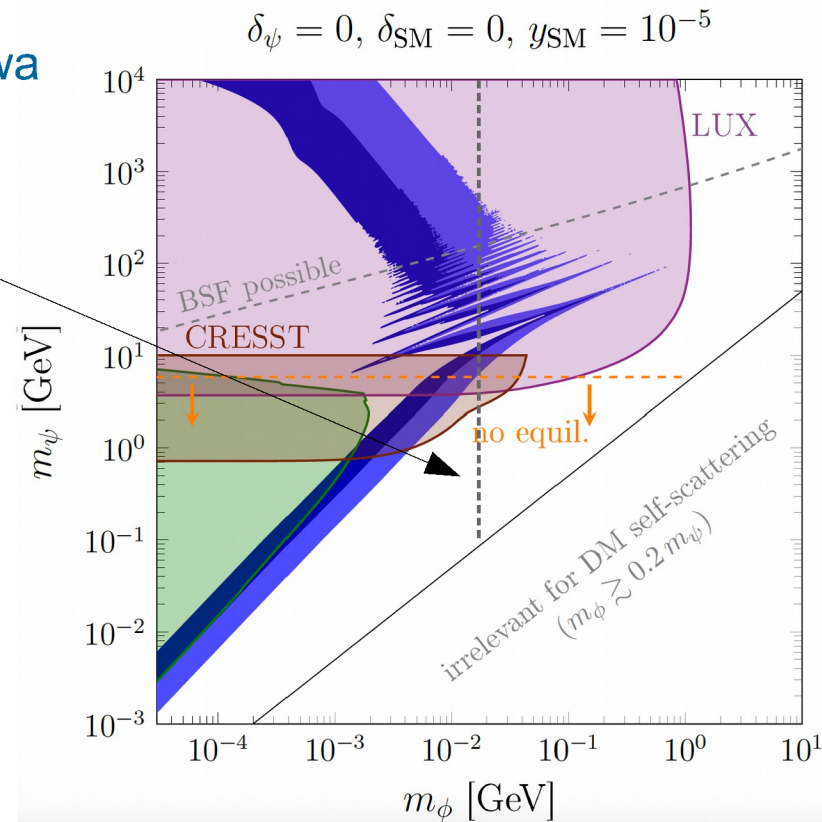
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M Winkler at Planck17



Constraints on scalar mediators

- For fermionic DM and scalar mediators annihilation proceeds via p-wave
- No constraints from indirect detection or the CMB.
- Direct detection constraints are very strong for scalar mediators.
- Lifetime rather long due to Yukawa suppression
- Naive BBN bound: $\tau < 1$ s
- Only velocity independent scattering allowed (if at all)



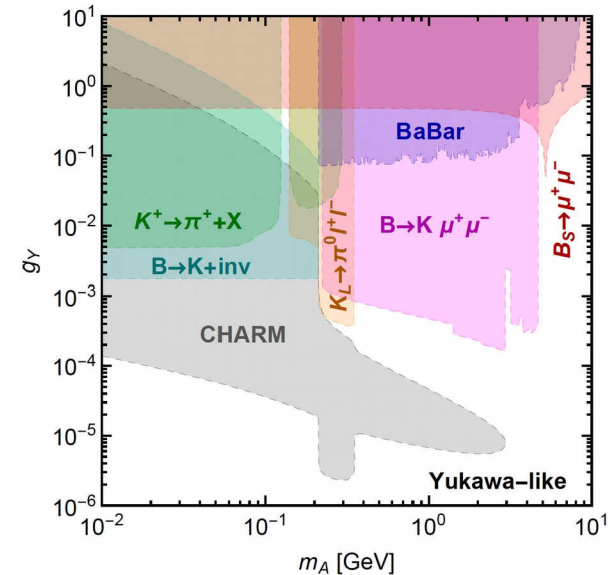
1704.02149

Pseudoscalar mediators

$$\mathcal{L}_{\text{DM}} = i g_\chi A \bar{\chi} \gamma^5 \chi$$

$$\mathcal{L}_{\text{SM}}^{(Y)} = i g_Y \sum_{f=q,\ell} \frac{\sqrt{2} m_f}{v} A \bar{f} \gamma^5 f$$

- In the non-relativistic limit, scattering via the exchange of pseudoscalar mediators is strongly suppressed by powers of the momentum transfer.
- Direct detection constraints are therefore effectively absent
- The same effect suppresses DM self-scattering
- Strongest bounds come from direct searches for light pseudoscalars.

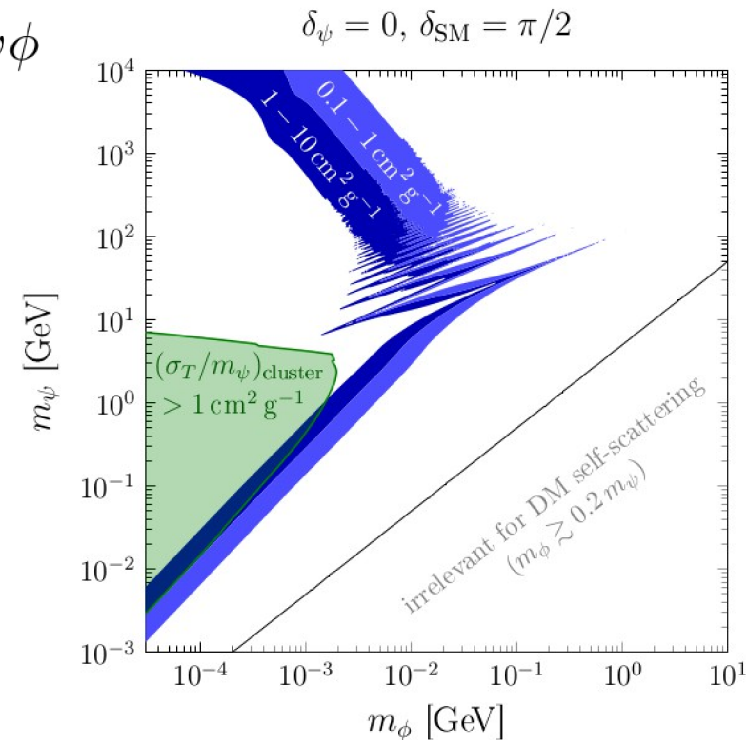


Dolan et al., arXiv:1412.5174

Idea: A mixed mediator (CP violation)

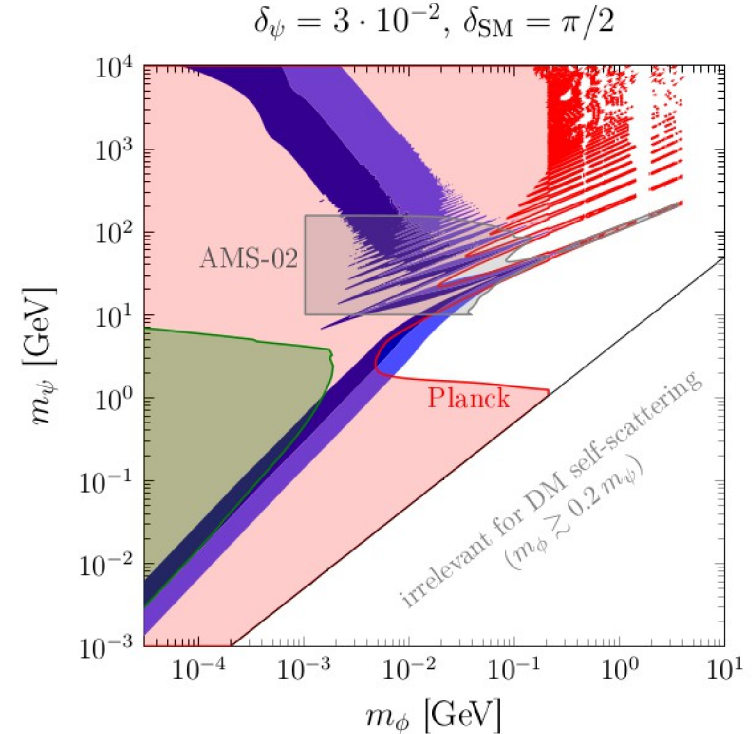
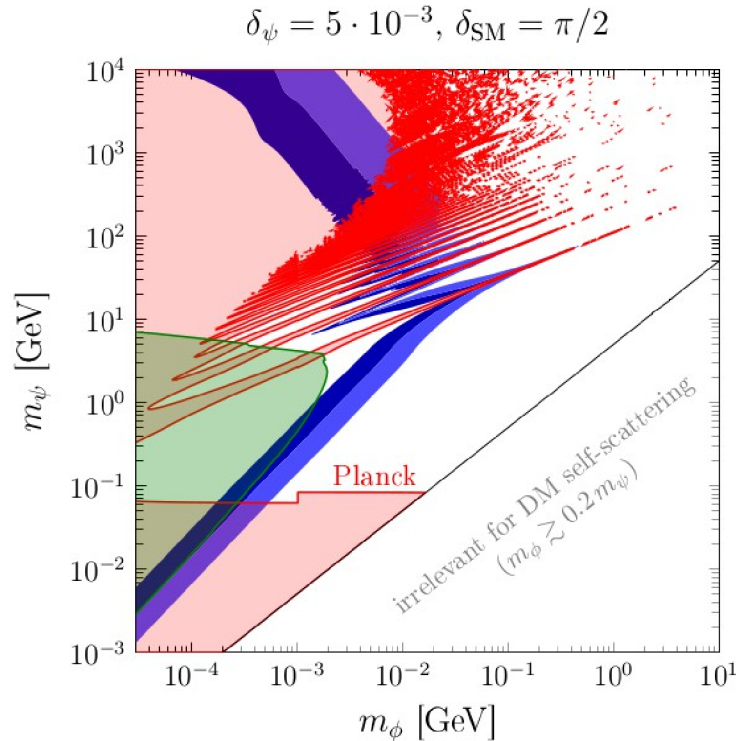
$$\mathcal{L}_{\text{DM}} \supset y_\psi \cos \delta_\psi \bar{\psi}\psi\phi + y_\psi \sin \delta_\psi i\bar{\psi}\gamma^5\psi\phi$$

- For $\delta_\psi \sim 0$ (like a scalar) DM self-interactions can be large.
- For $\delta_{\text{SM}} \sim \pi/2$ (like a pseudoscalar) direct detection constraints are strongly suppressed.
- Large allowed parameter space!
- Constraints on the CP-violating phase δ_{SM} (e.g. from electron EDMs) can be satisfied even for very light mediators as long as y_{SM} is sufficiently small ($y_{\text{SM}} \ll 10^{-2}$).



The return of CMB constraints

- Central problem: The fact that annihilation can only proceed via p-wave was a consequence of CP conservation.
- As soon as δ_ψ is not exactly zero, s-wave annihilation is again possible and will receive large Sommerfeld enhancement.



Future directions for light mediators

- There are a number of other ways to evade the various constraints
 - Inert decays of the mediator, for example into (sterile) neutrinos → **Torsten!**
 - No thermalization (DM production via the freeze-in mechanism)
Bernal et al., arXiv:1510.08063
 - Suppressed couplings to quarks (to evade direct detection constraints)
 - Small mass splitting (inelastic scattering)
Blennow et al., 1612.06681
- Nevertheless, constraints from BBN, direct detection and the CMB are very generic and will generally be relevant to any model of DM interacting via a new light mediator.
- Exciting phenomenology and interesting model-building challenges!

Summary

- Self interacting dark matter could solve some problems of the collisionless cold dark matter paradigm and can arise naturally in more complex dark sectors
- Orthogonal handle on properties of DM: We can potentially study the dark sector even if DM has highly suppressed couplings to Standard Model particles.
- Can potentially distinguish effective drag forces (from frequent self-interactions) and rare self-interactions
- Also could infer the velocity dependence of the cross section.
- The simplest possibilities (scalar or vector mediator coupling to fermionic dark matter with no additional new states) are in strong tension with direct and indirect detection experiments.
- One simple way out is spontaneous CP violation in the dark sector
- Huge possible impact, ruling out WIMPs, axions, gravitinos,...

Thank you!