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Jets in Inclusive e^+e^- and Leptoproduction

by

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Jets In Inclusive e^+e^- And Leptoproduction

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Abstract

The assumption of jets with bounded p_T leads to the following consequences:

- a) In e^+e^- annihilation the coefficient of the $\cos^2\theta$ term (α) of single particle inclusive distributions exhibits a unique dependence on the observed particle momentum. This dependence provides a measure of $\langle p_T^2 \rangle$ in a jet.
- b) In two particle inclusive annihilation the average of the squared relative p_T is determined by the same parameter and by the momenta of the two particles.
- c) The observation that in the current fragmentation region of leptoproduction the p_T distribution of fast hadrons is broader than that of slow ones is explained.

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1. Introduction

A basic ingredient of the parton model is the presence of a transverse momentum cut-off ¹⁾. This cut-off is assumed to apply to the distribution of partons in a hadron, and to the distribution of hadrons "radiated" by a parton. It is essential to the explanation of scaling phenomena.

Tests of the cut-off itself are scarce. A sharp cut-off leads to the prediction that in deep inelastic processes with spin 1/2 partons, σ_L/σ_T behaves as $1/q^2$ (for fixed $\omega = -2p \cdot q/q^2$), and to the vanishing (for large q^2) of azimuthal asymmetries of hadrons produced in leptonproduction ²⁾. It also predicts bounded $\langle p_T^2 \rangle$ for the produced hadrons around the current-target axis. And, of course, the cut-off leads to the prediction of jets in e^+e^- annihilation. ³⁾

We discuss here some straightforward consequences of the existence of a transverse momentum cut-off. In e^+e^- annihilation into one hadron plus anything the hadron angular distribution becomes, as is well known, $1 + \cos^2\theta$ for large momentum hadrons (assuming spin 1/2 partons). At low momenta the distribution should be isotropic. We show that the transition between the two extremes is controlled by the mean squared transverse momentum of hadrons with respect to the jet axis. The same is true of deviations from scaling at intermediate momenta. In two particle inclusive e^+e^- annihilation the relative $\langle p_T^2 \rangle$ of hadrons coming out in opposite hemispheres is also related to $\langle p_T^2 \rangle$ of hadrons relative to a jet axis. Similarly, the transverse momenta of hadrons produced in the forward region of current + hadron \rightarrow hadron + X are related to the $\langle p_T^2 \rangle$ of e^+e^- annihilation. As a consequence, we find a broadening of the

distribution of current fragments as x_F increases towards 1. All these features may serve as tests of the cut-off assumption originally introduced in order to obtain Bjorken scaling.

2. Consequences of the cut-off

The parton model predicts a jet structure for hadronic e^+e^- annihilation events. Searches for jets at low energies ($\sqrt{Q^2} \leq 4.8$ GeV)⁴⁾ have not been conclusive. Higher energy data ($\sqrt{Q^2} = 6.2$ and 7.4 GeV)⁵⁾ indicate jet structure, consistent with a parton model involving spin 1/2 constituents. In the following we assume a jet structure and explore the (mostly kinematical) consequences for e^+e^- annihilation and inclusive lepton production. Caveats are collected at the end of the section in order to avoid mutilating the otherwise simple discussion.

2a. Single Particle Inclusive e^+e^- Annihilation

In a jet the distribution of hadron momenta perpendicular to the axis is sharply cut off. In the parton model this axis is defined by the original parton anti-parton direction. Large momentum hadrons should closely follow the jet axis and exhibit its angular distribution. On the other hand, low momentum hadrons do not know which way the parton went (or know nothing about partons) and should be distributed isotropically.⁶⁾

Assuming annihilation through a single photon the jet axis angular distribution is ($\alpha_j = \alpha_{jet}(Q^2)$)

$$\frac{d\sigma}{d\Omega_{jet}} \propto 1 + \alpha_j \cos^2 \theta_j + \alpha_j p^2 \sin^2 \theta_j \cos 2\varphi_j \quad (1)$$

P is the e^- or e^+ polarization perpendicular to the e^+e^- orbit plane;

θ_j and φ_j are the polar and azimuthal angles of the jet relative to the e^+e^- axis and the plane of the e^+e^- ring (we assume zero crossing angle between the beams). In general, $-1 \leq \alpha_j \leq 1$, with $\alpha_j = 1 - O(1/Q^2)$ (-1) for spin $1/2$ (0) partons.

A priori, the single particle inclusive distribution relative to

the jet axis may depend on Q^2 , $x = 2p/\sqrt{Q^2}$ and $p_T = p \sin \tilde{\theta}$.

Denote it by $f(Q^2, x, p_T)$ (In the parton model this is the fragmentation function $D_q^h(x, p_T)$). Here $\tilde{\theta}$ is the angle between the particle momentum p and the jet axis. Consequently,

$$Q^2 \frac{d\sigma}{d^3p/E} \propto \int \frac{d\sigma_{\text{jet}}}{d\Omega_{\text{jet}}} \cdot f(Q^2, x, p_T) d\Omega_{\text{jet}} \quad (2)$$

With the help of Fig. 1 we find

$$\left. \begin{aligned} Q^2 \frac{d\sigma}{d^3p/E} \propto (I_1 + \frac{1}{2} \alpha_j I_2) [1 + \alpha(Q^2, p) \cos^2 \theta + \alpha(Q^2, p) p^2 \sin^2 \theta \cos 2\varphi] \\ \alpha = \alpha_j \frac{1 - 3/2 \cdot I_2/I_1}{1 + 1/2 \cdot \alpha_j I_2/I_1} \end{aligned} \right\} \quad (3)$$

where

$$\left. \begin{aligned} I_1 &= \int d\cos \tilde{\theta} f(Q^2, x, p_T) = \frac{1}{2p^2} \int \frac{dp_T^2}{\sqrt{1 - p_T^2/p^2}} f(Q^2, x, p_T) \\ I_2 &= \int d\cos \tilde{\theta} \sin^2 \tilde{\theta} f(Q^2, x, p_T) = \\ &= \frac{1}{2p^2} \int \frac{dp_T^2}{\sqrt{1 - p_T^2/p^2}} \cdot \frac{p_T^2}{p^2} f(Q^2, x, p_T) \end{aligned} \right\} \quad (4)$$

In general, α is a function of the particle momentum p .

For large p ,

$$\left. \begin{aligned} I_2 / I_1 &= \frac{\langle p_T^2 \rangle}{p^2} + O\left(\left(\frac{\langle p_T^2 \rangle}{p^2}\right)^2\right) \\ \langle p_T^2 \rangle &= \frac{\int p_T^2 f(Q^2, x, p_T) dp_T^2}{\int f(Q^2, x, p_T) dp_T^2} \end{aligned} \right\} \quad (5)$$

independent of the detailed form of f . Then,

$$\alpha \cong \alpha_j \left(1 - \frac{\alpha_j + 3}{2} \frac{\langle p_T^2 \rangle}{p^2}\right) \quad (6)$$

$\langle p_T^2 \rangle$ may depend on Q^2 and x through the function $f(Q^2, x, p_T)$. This dependence is probably weak. If f factorizes into a function of Q^2, x times a function of p_T there is no Q^2 and x dependence in $\langle p_T^2 \rangle$. From now on we ignore such a dependence.

In the high energy limit, with all spin 1/2 partons, $\alpha_j \rightarrow 1$. We therefore predict that asymptotically

$$\alpha \cong 1 - 2 \langle p_T^2 \rangle / p^2 \quad (7)$$

is a function of p alone. Once the existence of jets and the momentum dependence of α are established, eq. (7) permits a model independent determination of $\langle p_T^2 \rangle$, the mean squared transverse momentum of hadrons relative to the jet axis.

Asymptotically, the parton model predicts a constant $R = \sigma_{had}/\sigma_{\mu\mu}$, $Q^2 \frac{d\sigma}{dx}$ a function of x alone, and $\alpha = 1$ (or $\sigma_L/\sigma_T = \frac{1-\alpha}{1+\alpha} = 0$).

The last two properties are related. Let us perform the angle integration

in eq. (3), set $f(Q^2, x, p_T) = f(x) \cdot g(p_T)$ and expand the result in powers of p^{-2} . We find for $\alpha_j = 1$ and $p^2 \gg \langle p_T^2 \rangle$:

$$\begin{aligned} Q^2 x \frac{d\sigma}{dx} &\propto x f(x) \left(1 + \frac{1}{2} \frac{\langle p_T^2 \rangle}{p^2} + \dots \right) \\ &= x f(x) \left(1 + \frac{1}{4} (1 - \alpha) + \dots \right) \end{aligned} \quad (8)$$

Thus, $\alpha \neq 1$ in some x range implies that scaling must be violated there even if scaling is assumed at the jet level ⁶⁾ (as we do in eq. (8)).

We have remarked that $\alpha(p)$ is independent of the details of $f(Q^2, x, p_T)$ for large p . This is no longer true of eq. (8). Suppose that the correct scaling variable at the jet level is not x but rather the commonly used

$x_{||} = 2p_{||}/\sqrt{Q^2} = x \sin \theta$. Denote the parton fragmentation function by $\tilde{f}(x_{||}, p_T)$. For large p , $\alpha(p)$ coincides with eqs. (6-7) to $O(1/p^4)$. However, eq. (8) is replaced by

$$Q^2 x \frac{d\sigma}{dx} \propto x \tilde{f}(x) \left(1 + \frac{1}{2} \frac{\langle p_T^2 \rangle}{p^2} - \frac{1}{2} x \frac{\tilde{f}'(x)}{\tilde{f}(x)} \cdot \frac{\langle p_T^2 \rangle}{p^2} + \dots \right) \quad (9)$$

Note that as long as $\tilde{f}(x)$ is a decreasing function of x , the scaling limit is approached from above in either case. The deviations from scaling depend, however, on the choice of scaling variable at the jet level. The choice of $x_{||}$ as the scaling variable for the fragmentation function clearly

leads to difficulties as $x \rightarrow 1$, since there the last term in eq. (9) behaves as $(1-x)^{-1}$ (for $\tilde{f}(x) \propto (1-x)^n$). This indicates that $x_{||}$ may be the wrong variable, at least for large x . Choice of $x_{||}$ does not reflect the fact that for large x one remains at a fixed distance from the kinematical boundary as $\tilde{\theta}$ varies. When $\tilde{\theta}$ increases, so does p_T . This tends to push $\tilde{f}(x_{||}, p_T)$ downwards. However, at the same time, since the observed fixed quantity is x , $x_{||} = x \cos \tilde{\theta}$ decreases, which tends to push $\tilde{f}(x_{||}, p_T)$ upwards. It is this which leads to the large scaling violation for x near 1 in eq. (9). Obviously the correct choice of variable is a dynamical question which we cannot answer here.

Until now we have ignored the effect on $\langle p_T^2 \rangle$ and approach to scaling due to the presence of different types of particles. For example, an increasing Kaon fraction at large x would affect $\langle p_T^2 \rangle$. However, one can in principle establish $\langle p_T^2 \rangle$ for each species as we have described, and we regard this as a detail. Finally, we have ignored the effects arising from the existence of different parton species. As long as α_j is the same for all species, none of our conclusions are affected. In this case $\langle p_T^2 \rangle$ also include an average over several parton fragmentation functions (not just one $f(x, p_T)$), weighted by parton charges. For large p we still have $\alpha(p) \rightarrow \alpha_j$. If, on the other hand, we include partons with different spins, things change. For example, with spin 0, 1/2 partons one has

$$\alpha_j = \frac{\sum Q_i (\frac{1}{2})^2 - \frac{1}{2} \sum Q_i (0)^2}{\sum Q_i (\frac{1}{2})^2 + \frac{1}{2} \sum Q_i (0)^2} \quad (10)$$

Since $\alpha(p)$ for a particle is an average over different fragmentation functions, it no longer approaches α_j as p becomes large (except for the improbable case that the fragmentation of partons into hadrons does not depend on the parton spin).

If some of the partons have larger masses than others, this also affects our conclusions. For example, if the observed increase in R around $\sqrt{Q^2} \cong 4$ GeV is due to a threshold associated with new parton types, then $\alpha(p)$ could be a different function of p below and well above this threshold. The approach to scaling of $Q^2 \frac{d\sigma}{dx}$ is also affected. The details depend on the fragmentation functions of the new heavy partons into stable hadrons. In the transition region one expects two contributions to α . One (light partons) has $\alpha_j \cong 1$ and the other (heavy new partons) has $\alpha_j^{new} \cong (1 - m_p^2/Q^2)/(1 + m_p^2/Q^2)$. The latter is small near the new particle threshold ($Q^2 \sim 4m_p^2$). Even for this reason alone large breaking of scaling is expected near new thresholds.

2b. Two Particle Distributions in e^+e^-

We now consider p_T correlations in $e^+e^- \rightarrow h_1 + h_2 + X$, with h_1 and h_2 in opposite hemispheres (relative angle close to 180°) and x_1, x_2 not too small ($x_i = 2p_i/\sqrt{Q^2}$). We may then assume that they come from two opposite jets, and are emitted independently. Each of them has a mean $\langle p_T^2 \rangle$ with respect to its jet ($\langle p_T^2 \rangle_{1/j}$ and $\langle p_T^2 \rangle_{2/j}$) and a mean relative squared transverse momentum $\langle p_T^2 \rangle_{2/1}$. The latter can be measured. With the aid of fig. (2) we find

$$\langle p_T^2 \rangle_{2/1} = \langle p_T^2 \rangle_{2/j} + \frac{p_2^2}{p_1^2} \langle p_T^2 \rangle_{1/j} - \frac{3}{2} \frac{\langle p_T^2 \rangle_{1/j} \langle p_T^2 \rangle_{2/j}}{p_1^2} \quad (11)$$

For finite x_1, x_2 , under the cut-off assumption we can ignore the last term in eq. (11). If the two observed particles are charge conjugates ($\pi^+\pi^-$, K^+K^- , $p\bar{p}$ etc.) we have after averaging over parton types

$$\langle p_T^2 \rangle_{2/1} = \langle p_T^2 \rangle \left(1 + \frac{x_2^2}{x_1^2} \right), \quad (12)$$

with the same $\langle p_T^2 \rangle$ as for the single particle case. Eq. (12) is valid only for $p_i^2 \gg \langle p_T^2 \rangle_{i/jet}$ ($i=1,2$). It can be used without having to experimentally define a jet axis. It also indicates that in order to use particle no. 1 for the approximate definition of a jet axis, x_1 must be close to 1 ($x_1 > .5$, say). Otherwise $\langle p_T^2 \rangle_{2/1}$ may not be as small as $\langle p_T^2 \rangle_{2/j}$.

An immediate consequence of the assumed sharp cut-off in transverse momenta of hadrons relative to a jet axis is the absence of azimuthal asymmetry in $e^+e^- \rightarrow h_1 + h_2 + X$ ⁷⁾. In principle using p_1 as an axis, the cross section could depend on the azimuthal angle defined by p_2 around this axis. Such a dependence is predicted to disappear when Q^2 increases (for fixed x_1, x_2). The proof is essentially the same as in inclusive electroproduction ²⁾. This prediction is a genuine test of the p_T -cut-off assumption with spin 1/2 partons, since the more common prediction of $\sigma_L/\sigma_T \rightarrow 0$ can be easily obtained in other models.

2c. The Parton Fragmentation Region in Leptoproduction

Consider now the p_T distribution of hadrons in the parton fragmentation region of electro- or neutrino-production. It is customary to view this process in the Breit frame, with the current-target direction as z-axis.

After absorbing the current, the target parton has its p_{11} with respect to this axis reversed, while its p_T is unaffected. The final hadron distribution is assumed to be of the form ¹⁾

$$f(p_{11}, p_T) \sim d^q(x, p_T(q/N)) \cdot D_q^h(z, p_T(h/q)) \quad (13)$$

which must be summed over (quarks) partons and integrated over internal variables. Here $x = -q^2/2 p_N \cdot q$ and $z = 2 p_h \cdot q/q^2$. Averaging again over quark types and applying the same arguments as before (see Fig. 3) we find (neglecting $O(1/q^2)$ terms)

$$\langle p_T^2 \rangle_{h/(8-N)} \cong \langle p_T^2 \rangle_{h/q} + z^2 \langle p_T^2 \rangle_{q/N} \quad (14)$$

This predicts a broadening of the p_T distribution for large z . Practically, when z is not close to 0 ($z > \sim 2$, say) and q^2 is not too small ($\sqrt{-q^2}$ larger than mass of observed particle) one may replace z by the usual Feynman scaling variable x_F . However due to arguments similar to those presented in section 2a. (in discussing X versus X_{11}) replacing z by x_F will have an effect on $\langle p_T^2 \rangle_{h/(8-N)}$, since for $x_F \rightarrow 1$ the latter has to vanish.

2d. Comparison with Data

In the parton model ¹⁾ the same parton fragmentation functions $D_q^h(z, p_T)$ appear both in e^+e^- annihilation and in lepto-production. Some support for this can be found in existing data. For example, in $\mu^- p \rightarrow \mu^- + h + X$ at FNAL ⁸⁾

$\sigma_{tot} x_F \frac{d\sigma}{dx_F}$ can be approximately described by an exponential, e^{-ax_F} with $a \cong 3.4-4$. In e^+e^- annihilation, over the range $3 \leq \sqrt{Q^2} \leq 7.4$ GeV ²⁵⁾,

$Q^2 x \frac{d\sigma}{dx}$ is roughly consistent with the same fall-off for $.3 \lesssim x \lesssim .8$.

This rough agreement encourages us to proceed and discuss relations

between p_T distributions in the two types of processes. Estimating

$\langle p_T^2 \rangle_{h/q}$ from inclusive electroproduction in the parton fragmentation region we obtain a predicted curve for $\alpha(p)$ in e^+e^- annihilation.

In section 2c. we have found that the p_T distribution of hadrons, produced in the current fragmentation region of leptonproduction, should broaden with their x_F . Such broadening has indeed been found in previous electro-

production data ⁹⁾, and recently, in the FNAL muon-production data ⁸⁾. The

information available at present is not sufficient for checking the details of our prediction (namely, rise with x_F^2 , see eq. (14)), but is sufficient

for our purposes here. In the FNAL data ⁸⁾ $\langle p_T^2 \rangle_{h/(x-N)}$ obtains the value .17-.21 GeV^2 for $.05 \leq x_F \leq .4$ and .26-.42 for $.4 \leq x_F \leq .85$. The two values

quoted for each x_F range arise from two different parametrizations of the data, and indicate errors involved. Using eq. (14) we see that the $.05 \leq x_F \leq .4$

region can give a reasonable estimate for $\langle p_T^2 \rangle_{h/q}$ (since there $\langle x_F^2 \rangle$ is small). We choose $\langle p_T^2 \rangle_{h/q} = .2$ as a representative value.

We now proceed to the calculation of $\alpha(p)$ in e^+e^- annihilation. In eq. (3)

we set $\alpha_j = 1$, and assume $f(x, p_T) = f(x)g(p_T)$. For $g(p_T)$ we try two forms: $e^{-B p_T^2}$ and $e^{-b p_T}$ (both with $\langle p_T^2 \rangle_{h/q} = .2 \text{ GeV}^2$). The

results are shown in Fig. 4, where the solid line corresponds to $e^{-B p_T^2}$ and the dashed line - to $e^{-b p_T}$. Notice that the model dependence is not

more than a few percent for $p \gg 1 \text{ GeV}$. Moreover, the approximation

$\alpha(p) \cong 1 - 2 \langle p_T^2 \rangle_{h/q} / p^2$ is also good to a few percent for $p \gg 1 \text{ GeV}$.

The differences at low p ($p^2 \cong \langle p_T^2 \rangle_{h/q}$) are due to the different p_T distributions.

For the sake of completeness let us mention that for small p eq. (3) gives

$$\alpha(Q^2, p) \cong \begin{cases} \alpha_j(Q^2) \cdot \frac{3\sqrt{6} \pi}{32(\alpha_j+3)} \cdot \frac{p}{\sqrt{\langle p_T^2 \rangle_{h/q}}} & (e^{-b p_T}) \\ \alpha_j(Q^2) \frac{2}{5(\alpha_j+3)} \cdot \frac{p^2}{\langle p_T^2 \rangle_{h/q}} & (e^{-B p_T^2}) \end{cases} \quad (15)$$

On Fig. 4 we have added the data for α at $\sqrt{Q^2} = 7.4 \text{ GeV}^5$. The agreement is good but not very significant. After all, the model is not expected to apply to low momentum hadrons. And in the region where we expect the model to be valid ($p \gg 1 \text{ GeV}$) the errors in the data are large enough to exclude any clear cut conclusions.

3. Remarks and Conclusions

In this paper we have explored some consequences of the existence of jets, or of a transverse momentum cut-off in parton model language. We conclude with a few remarks.

1. If jets exist one can obtain the parameters α_j and $\langle p_T^2 \rangle_{h/\text{jet}}$ from inclusive experiments without having to find jets event-by-event. The same parameter $\langle p_T^2 \rangle_{h/\text{jet}}$ also appears in inclusive electroproduction in the current fragmentation region.

2. The observation that $\alpha(p) \rightarrow 1$ for large p in e^+e^- annihilation does not prove that jets exist. A strong two-particle correlation of the sort we have discussed (see section 2b.) with a bounded $\langle p_T^2 \rangle_{2/1}$ is a definite hint that jets exist in the subset of events with at least one fast particle ($x_1 > \sim 0.5$, say). One should keep in mind that present data do not definitely prove the existence of jets.

3. The non-scaling effect of $\alpha(p) \neq 1$ is related to the deviation from scaling in $Q^2 \frac{d\sigma}{dx}$, though in a model dependent fashion. This occurs even if (Feynman) scaling is assumed at the jet level. Thus this represents a sort of minimal scaling violation.

4. Under plausible simplifying assumptions α turns out to depend on the particle momentum p . It therefore seems useful to plot α versus p for different Q^2 values rather than versus x .

5. The comparison between e^+e^- and electroproduction data should be viewed with caution, since e^+e^- physics exhibits an apparent threshold behaviour around $\sqrt{Q^2} \cong 4$ GeV, while there is as yet no evidence for such a dramatic behaviour in deep inelastic reactions.

6. The jet picture is unreliable for low momentum particles. Their distributions are probably determined by low energy hadron dynamics and not by the jet picture. Even in the latter $f(Q^2, x, p_T)$ is not expected to scale at very small x . Moreover, for low momentum hadrons one has to include interference effects arising from an overlap of different jet axes in the production amplitude. For events with high momentum particles (i.e. a jet axis in each

event) one can ignore this interference as we have done. The qualitative behaviour of the simple model is probably near the truth also for slow particles.

The parton model is not the only source of jet structure in e^+e^- annihilation. Resonance production models can also lead to jets. Models in which the photon decays into one light meson recoiling against a heavy resonance lead to a jet picture at intermediate Q^2 . At high energies the jet either broadens or remains narrow depending on the average spin of the heavy resonance ¹⁰⁾. Models in which the photon decays into two heavy states, which then decay similarly, can also have a two jet structure at intermediate energies. However, at high energies each jet should dissolve into sub-jets. The number of the latter increases with energy ¹¹⁾. In view of this one should keep an open mind about possible surprises at very high Q^2 .

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Figure Captions

Fig. 1 Geometry of $e^+e^- \rightarrow h + \chi$ in jets.

Fig. 2 Relative p_T geometry in $e^+e^- \rightarrow h_1 + h_2 + \chi$

Fig. 3 p_T geometry for parton fragmentation region in
leptoproduction
a) before interaction
b) after interaction.

Fig. 4 Plot of $\alpha(p)$ for e^+e^- annihilation.

Predictions: solid line - $e^{-B p_T^2}$; dashed line - $e^{-b p_T}$.
Data taken from ref. 5).

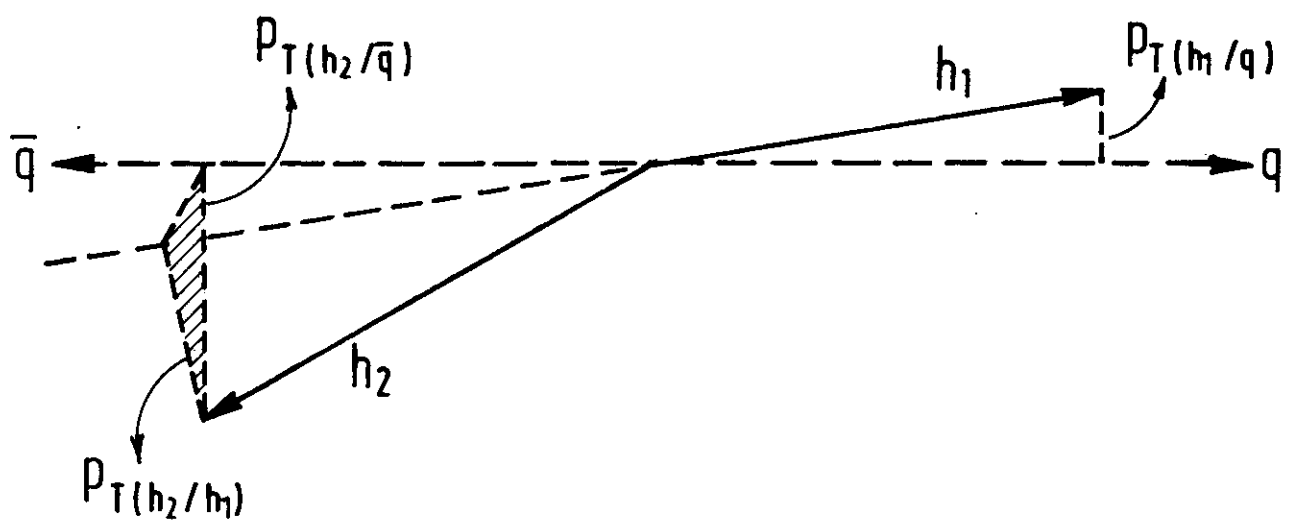


Fig.2

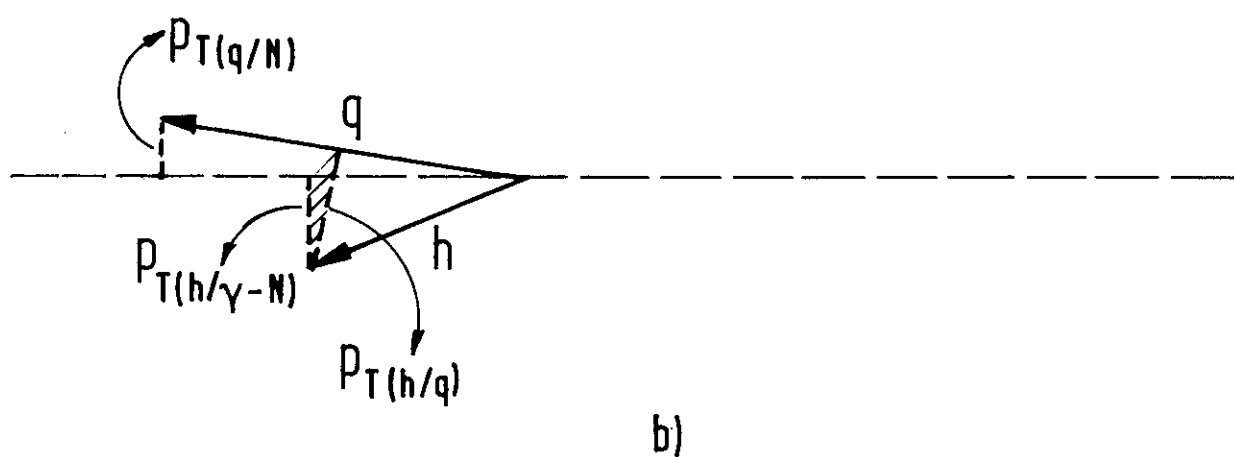
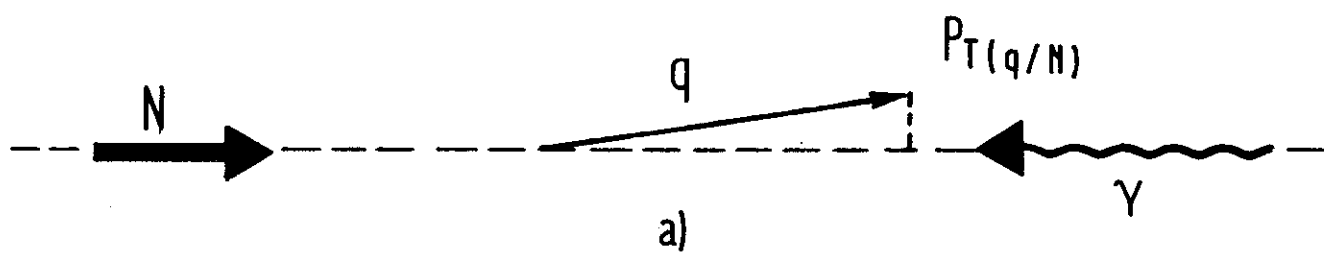


Fig.3

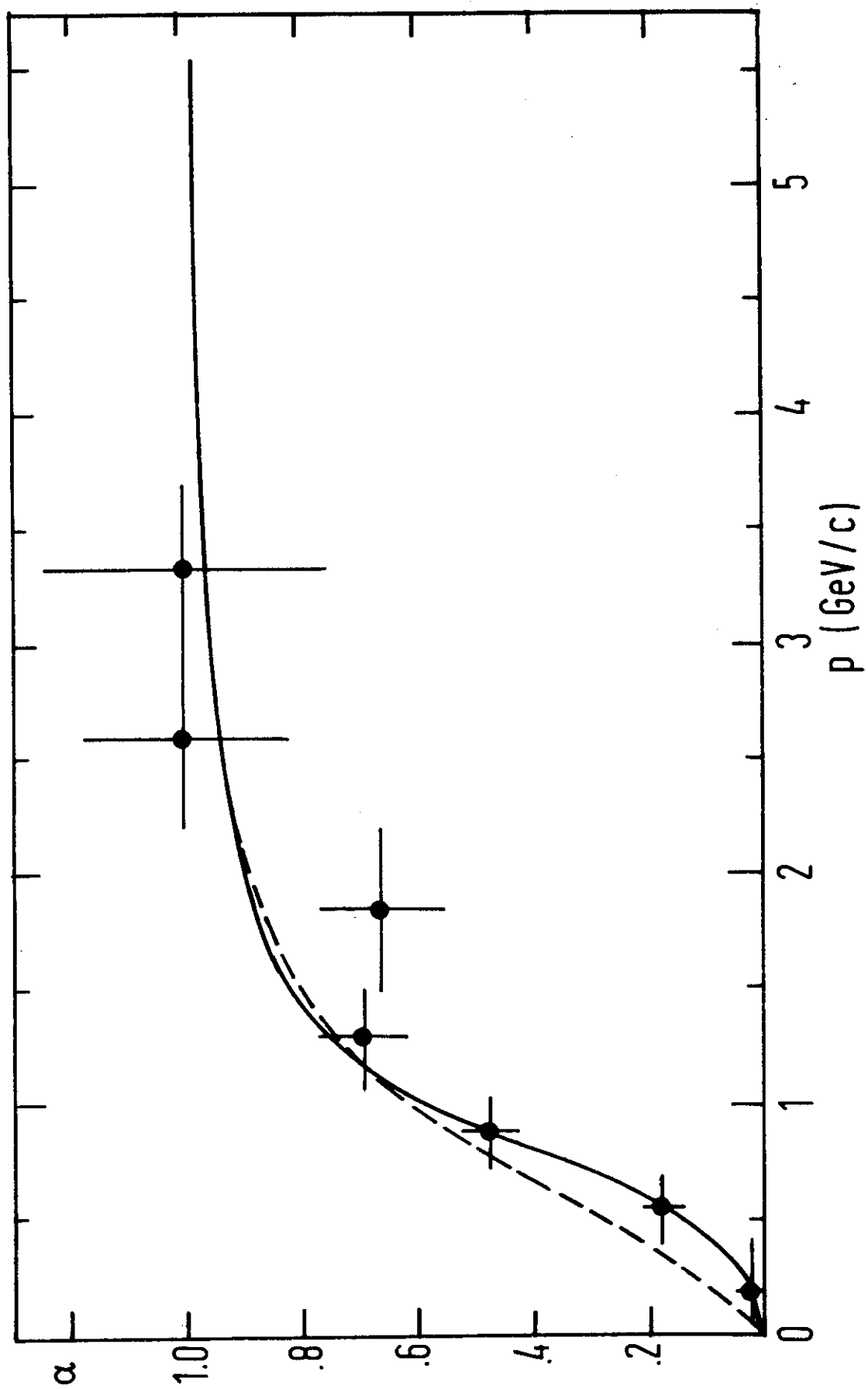


Fig.4