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#### Abstract

New data of the electroexcitation cross section on protons and deuterons in the resonance region are compared with the results in the deep inelastic region for four-momentum transfers  $q^2 \le 1.5 \; (\text{GeV/c})^2$ . The Bloom-Gilman sum-rule is shown to hold for  $q^2 \ge 1.2 \; (\text{GeV/c})^2$ , while the Rittenberg-Rubinstein sum rule is saturated for  $q^2 \ge 0.4 \; (\text{GeV/c})^2$ . It is shown that the sum rules do not saturate in a local way.

### I. Introduction

A systematic investigation of the electroexcitation cross section on protons and deuterons in the resonance region for four-momentum-transfers  $q^2 \le 1.5 (\text{GeV/c})^2$  has been performed by the Karlsruhe-DESY collaboration<sup>1</sup>. Figs. 1 and 2 show the results of these experiments in a compressed representation.

The results of these measurements have been used to derive properties of the dominant nucleon resonances<sup>2</sup>. Another important aspect of these data is their connection to the deep inelastic electron scattering.

The relation between the deep inelastic and the resonance cross section has been discussed by various authors  $^{3-6}$  and has been checked for the electroexcitation on the proton  $^{3,7,8}$ . In the present paper we want to investigate the validity of the sum rules in the region of small four-momentum transfers  $(q^2 \le 1.5 (\text{GeV/c})^2)$  in the case of proton and deuteron targets.

#### II. Sum Rules

In the case of constant four-momentum transfer Bloom and  $Gilman^3$  derived the sum rule

$$\int_{0}^{\nu_{\text{max}}} \{\nu W_{2}(q^{2}, ) - F_{2}(\omega^{*})\} d\nu = 0$$
 (1)

assuming that the structure function  $\nu W_2$  shows scaling behaviour in the deep inelastic region and that the forward scat-

tering amplitude for virtual photons obeys a superconvergence relation.  $F_2(\omega')$  is the scaling function in the deep inelastic region as determined by the SLAC-MIT group<sup>9,10</sup>.  $W_2$  is the structure function in the resonance region, which can be derived from the twofold differential cross section:

$$\frac{d^2\sigma}{d\Omega dE} = \sigma_M \{W_2(q^2, v) + 2 tg^2 \theta/2 W_1(q^2, v)\}$$
 (2)

 $\sigma_{M}$  = Mott cross section  $W_{1}, W_{2}$  = structure functions  $q^{2}$  = four momentum transfer  $\theta$  = electron scattering angle

ν = energy loss of the electron during the scattering process

The structure functions W<sub>1</sub>, W<sub>2</sub> are related to the absorption cross section of virtual photons  $\sigma_t$ ,  $\sigma_\ell$  according to

$$\frac{W_1}{W_2} = \frac{1 + \frac{v^2}{q^2}}{1 + \frac{\sigma_\ell}{\sigma_t}}$$
(3)

We assume, in accordance with existing data 11,12

$$\frac{\sigma_{\ell}}{\sigma_{t}} = 0.18 \tag{4}$$

and calculate  $W_2$  from the measured cross section (2) with the help of (3) and (4).

Rittenberg and Rubinstein  $^4$  generalised the sum rule (1) by postulating a vector sum rule which allows to give a connection between deep inelastic data and resonance cross sections along any line in the  $q^2-\nu$  plane kinematically accessible

$$\int_{V_1}^{V_2} \{vW_2(q^2, v) - F_2(\omega^*)\} dv = 0$$
 (5)

A further ingredient of all sum rules is the choice of the scaling variable. The Bjorken Variable

$$\omega = \frac{2M\nu}{q^2} \tag{6}$$

is prefered by theoretical arguments in the limit

$$v \rightarrow \infty$$
,  $q^2 \rightarrow \infty$ ,  $\omega = finite$ 

while in the kinematical region accessible to experiments scaling behaviour is observed in an extended interval if one plots the data as a function of  $\bar{j}$ 

$$\omega' = \frac{2Mv + M^2}{q^2} \tag{7}$$

or of4,6

$$\omega_{\overline{W}} = \frac{2Mv + a^2}{q^2 + b^2} \tag{8}$$

where  $a^2$  and  $b^2$  have been determined from fits  $^4,5,6$  as

$$a^2 = 1.43 \left(\frac{\text{GeV}}{c}\right)^2$$

$$b^2 = 0.42 \left(\frac{\text{GeV}}{c}\right)^2$$

From light cone arguments 13 the variable

$$\omega_{\rm L} = \frac{M}{|\vec{q}| - \nu} \tag{9}$$

is derived.

In the present paper the scaling variables (6) - (9) have been used to investigate the region of validity of finite energy sum rules for the inelastic electron scattering on proton and deuteron targets. Since  $W_2(q^2, v) = O(q^2)$  because of gauge invariance, the zero has been cancelled by investigating the structure function  $^{4-6}$ 

$$\frac{\omega}{\omega_{\rm W}} v_{\rm W2}$$
 (10)

The sum rule then reads:

$$\int_{0}^{v_{\text{max}}} \frac{\omega}{\omega_{W}} vW_{2}(q^{2}, v) dv = \int_{0}^{v_{\text{max}}} F_{2}(\omega_{W}) dv$$
 (11)

#### III. Results and Discussion

We have investigated the validity of the sum rule for different constant values of the four momentum transfer. The structure function  $W_2$  is derived from the measured cross section with the help of formulas (2) - (4) and interpolated along lines of constant invariant mass W by a cubic interpolation formula. The error of this interpolation is estimated to be of the order of less than 4%, while the typical error of the experimental data is 3% to 5%.

In figs. 3 and 4 we have plotted the values of  $\nu W_2$  for hydrogen as determined from our experiment and the structure functions  $F_2(\omega^*)$ ,  $F_2(\omega_L)$  and  $(\omega_W/\omega)F_2(\omega_W)$  derived from the data in the deep inelastic region 10. The results are given for the four momentum transfers  $q^2 = 0.4$   $(\text{GeV/c})^2$  and  $q^2 = 1.4$   $(\text{GeV/c})^2$ . For the high values of the four momentum transfer the structure functions saturate the sum rules, while at  $q^2 = 0.4$   $(\text{GeV/c})^2$  only the sum rule (11) for the structure function (10) is satisfied. The respective results for the deuteron are given in figs. 5 and 6. They show a behaviour analogue to that of the proton data. The light cone variable (9) does not improve the saturation compared to the Bloom-Gilman variable (7).

To demonstrate the saturation of the sum rule quantitatively in fig. 7 the ratio

$$\frac{I_2}{I_1} = \frac{\int_{0}^{v_{\text{max}}} vW_2(q^2, v) dv}{\int_{0}^{v_{\text{max}}} F_2(\omega') dv}$$
(12)

is plotted as a function of the four momentum transfer  $q^2$ . Results are given for two upper limits  $W_{max}$  of the invariant mass which is connected to  $v_{max}$  by

$$W_{\text{max}} = \sqrt{M^2 + 2Mv_{\text{max}} + |q^2|}$$

Taking into account that the systematic errors of both experiments  $^{1,9}$  used in the analysis are of the order of 3% to 4%, from fig. 7 follows that the sum rule saturates for  $q^2 \ge 1.2$   $(GeV/c)^2$ . The behaviour for proton and deuteron data is the same.

Minimizing the ratio  $(I_2/I_1)-1$  in the case of the structure function (10) the parameters  $a^2$  and  $b^2$  have been determined to

$$a^2 = (1.3 \pm 0.07) (GeV/c)^2$$

$$b^2 = (0.4 \pm 0.02) (GeV/c)^2$$
(13)

Within the error limits the results for proton and deuteron targets coincide, they are in good agreement with the results of foregoing analyses 4,5,6.

In fig. 8 the ratio

$$\frac{I_2}{I_1} = \frac{\int_0^{\infty} \frac{\omega}{\omega_W} vW_2(q^2, v) dv}{\int_0^{\max} F_2(\omega_W) dv}$$
(14)

has been plotted as a function of  $q^2$  for an upper integration limit  $W_{\rm max}$  = 1.8 GeV. The parameters in (14) are used for the plot. In the whole  $q^2$ -region covered by the present experiment (fig. 1 and 2) the sum rule is in good agreement with the proton and deuteron data, while differences are observed for the smaller value of the integration constant  $W_{\rm max}$  = 1.3 GeV. From this follows that the sum rule saturates only if the contribution of all resonances is taken into account. Hence local duality  $^{3}$ ,  $^{4}$  describes only in an approximate way the data in the resonance region.

In conclusion we have shown that the Bloom-Gilman sum rule holds for  $q^2 \ge 1.2 \, (\text{GeV/c})^2$  while the Rittenberg-Rubinstein sum rule holds for all four-momenta investigated for proton

and deuteron targets. Local duality describes the data only approximately, a result which was obtained <sup>14</sup> in electron <sup>12</sup>C scattering too.

#### Acknowledgement

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#### FIGURE CAPTIONS

- Fig. 1: Lines of constant  $vW_2$  in the  $v-q^2$  plane for protons. Data were taken along the straight lines of constant scattering angle.
- Fig. 2: Same as fig. 1 for deuterons.
- Fig. 3:  $vW_2$  of hydrogen as a function of v for  $q^2 = 0.4$   $(\text{GeV/c})^2$ . For comparison the scaling function in the deep inelastic region is plotted for the variable  $w_1$ , the light cone variable  $w_L$  and the variable  $w_W$ .
- Fig. 4: Same as fig. 3 for  $q^2 = 1.4 (GeV/c)^2$ .
- Fig. 5:  $vW_2$  of deuterium as a function of v for  $q^2 = 0.4$   $(GeV/c)^2$ . For comparison the scaling function in the deep inelastic region is plotted for the variable w', the light cone variable  $w_I$ , and the variable  $w_W$ .
- Fig. 6: Same as fig. 5 for  $q^2 = 1.4 (GeV/c)^2$ .
- Fig. 7: Ratio (12) as a function of q<sup>2</sup> for two different values of the upper integration limit. Values for protons and deuterons are plotted.
- Fig. 8: Ratio (13) as a function of q<sup>2</sup> for two different values of the upper integration limit. Results for protons and deuterons are plotted.

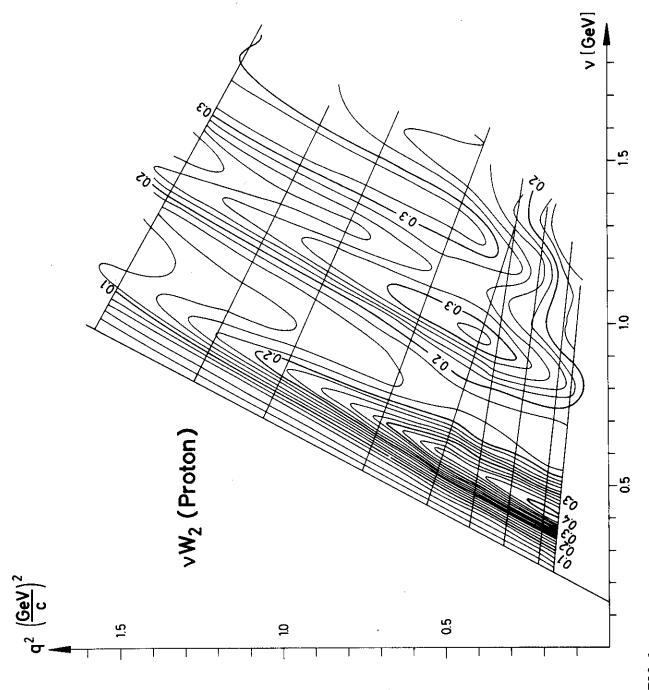
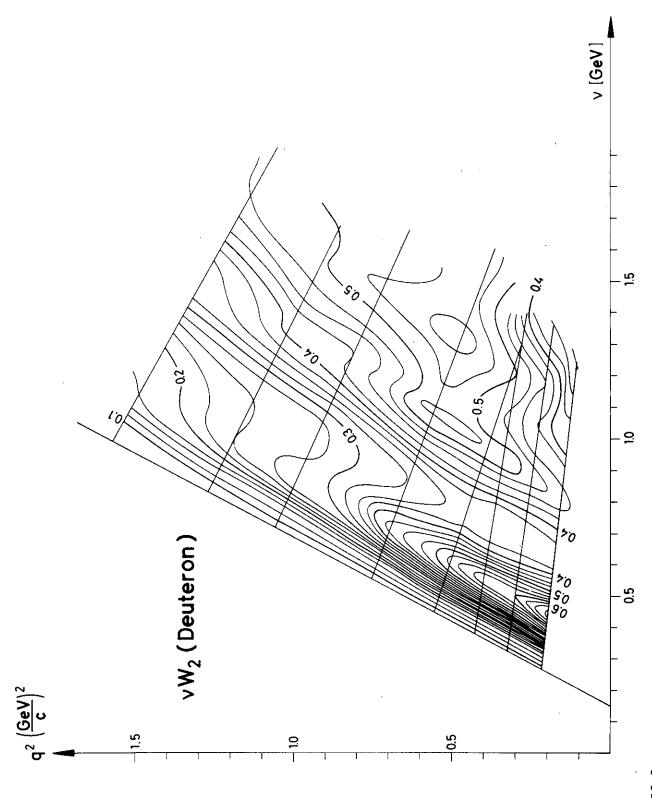
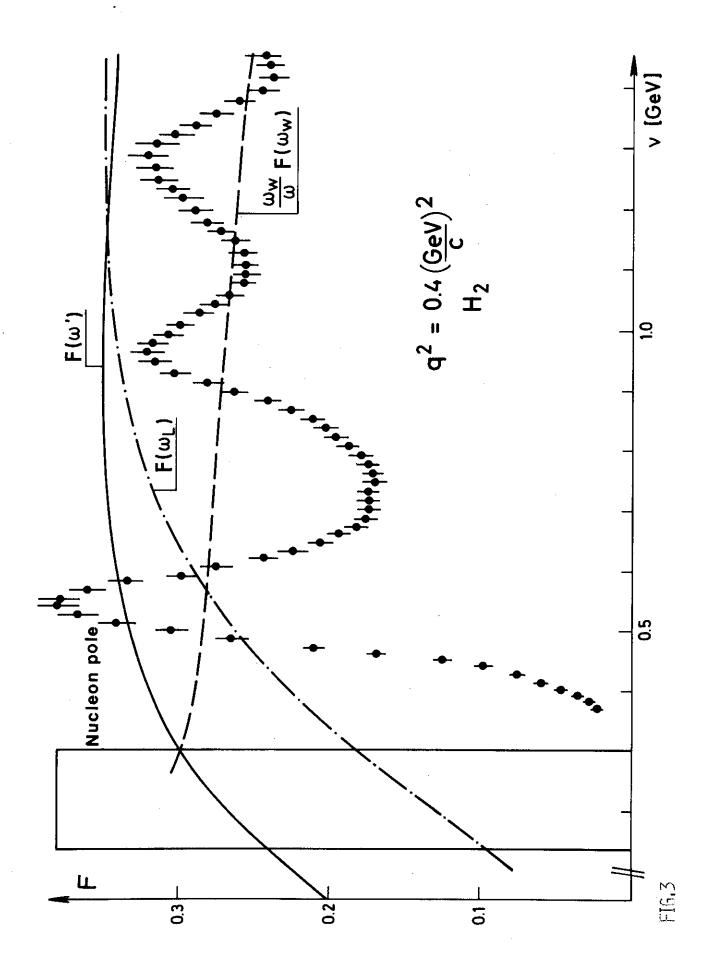
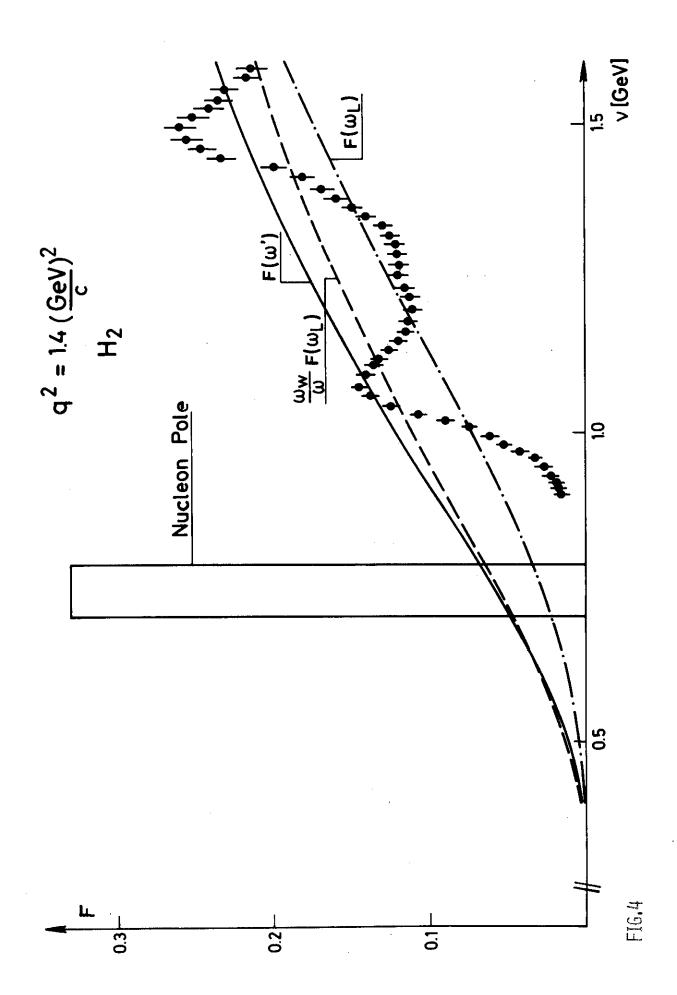


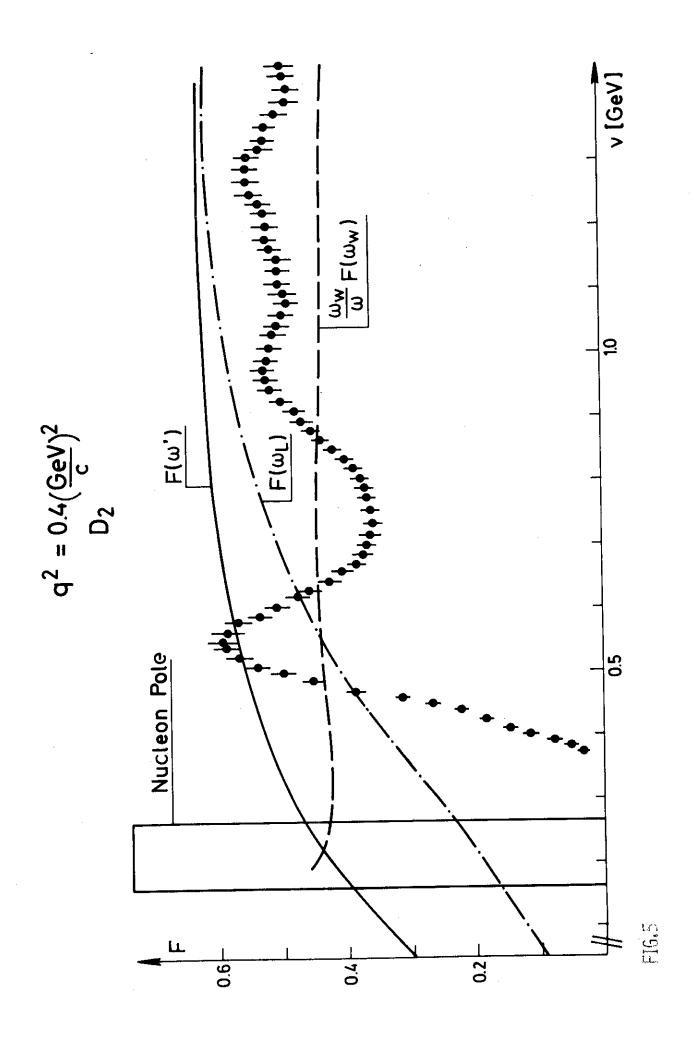
FIG.1



FIG,2







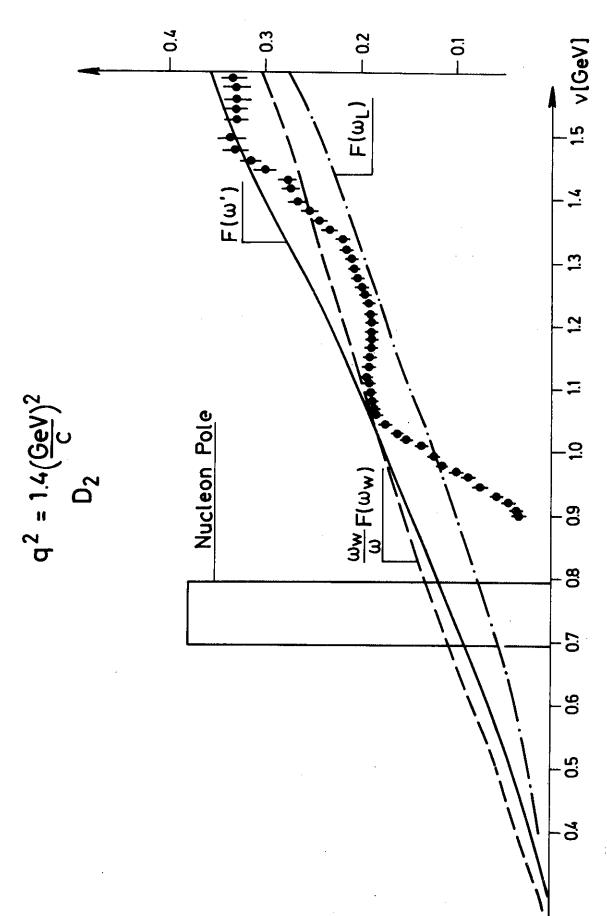
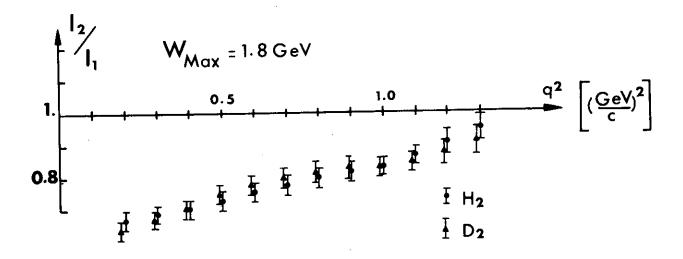
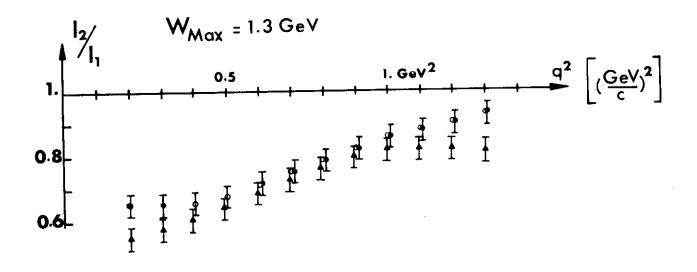


FIG.6

## BLOOM - GILMAN SUM - RULE





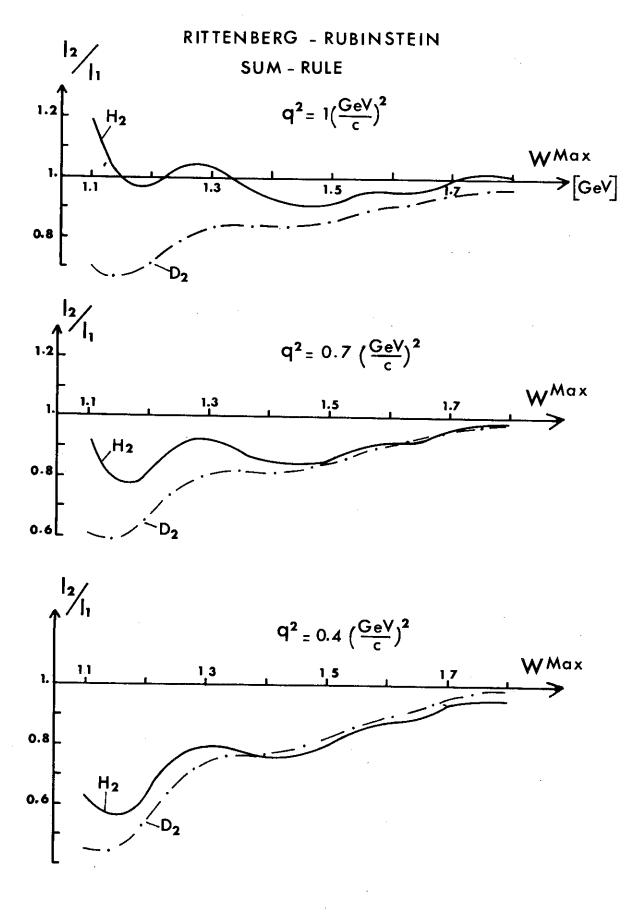


FIG.8