

Polarimetry at the ILC

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Introduction

Polarization Measurement Using Collision Data

- Combination of Cross Section Measurements

- Frequency and Accuracy of the Helicity Reversal

Improvement by Constraints from Polarimeter Measurement

Conclusion and Outlook

Advantages of Polarized Beams

▶ International Linear Collider (ILC)

- ▶ e^-e^+ collider with polarized beams of $|80\%|$ and $|30\% - 60\%|$, respectively
- ▶ Selectable polarization sign $\rightarrow$ choice of spin configuration

▶ Advantages:

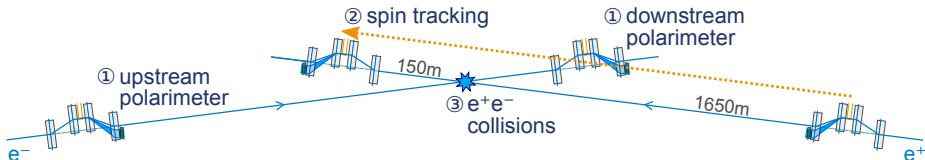
- ▶ Sensitive to new observables (e.g. left-right-asymmetry)
- ▶ Reduction of background processes and simultaneously increase of signal processes
- ▶ Deep insights into the chiral structure of the weak-interaction for known and unknown particle

All event rates depend linearly on the polarization!

$\Rightarrow$ Has to be known as precisely as the luminosity!

$\Rightarrow$ Requirement for permille-level precision

ILC Polarimetry Concept



1. Measurement of the time-resolved beam polarization before and after the e^-e^+ IP

► Via laser-Compton polarimeter

Ref.: Jenny List, Annika Vauth, and Benedikt Vormwald:

A Quartz Cherenkov Detector for Compton-Polarimetry at Future e^+e^- Colliders (<https://bib-pubdb1.desy.de/record/221054>)

A Calibration System for Compton Polarimetry at e^+e^- Colliders (<https://bib-pubdb1.desy.de/record/289025>)

2. Extrapolating the beam polarization to the e^-e^+ IP

► Via Spin Tracking

Ref.: Moritz Beckmann, Jenny List, Annika Vauth, and Benedikt Vormwald:

Spin transport and polarimetry in the beam delivery system of the international linear collider

(<http://iopscience.iop.org/article/10.1088/1748-0221/9/07/P07003/pdf>)

3. Determination of the luminosity-weighted averaged polarization from collision data

► Calculating the polarization from known standard model processes

⇒ Discussed in the following

Determination of the Polarization from Collision Data

Goal:

General strategy for the polarization determination which yields the best precision per measurement time

► Previous Work:

- Using the information from W -pair production

Ref.: Theses Ivan Marchesini
(<http://pubdb.xfel.eu/record/94888>)

- Using the information from single W , γ , Z events

Ref.: Talk Graham W. Wilson
(<https://agenda.linearcollider.org/event/5468/contributions/24027/>)

► Current Work:

- Combining all relevant processes, including all uncertainties and their correlations
- Compensating for a non-perfect helicity reversal
- Including constraints from the polarimeter measurement



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The New Unified Approach

χ^2 -Method:

- ▶ Combining all suitable processes

$$\chi^2 = \sum_{\text{process}} (\vec{\sigma}_{\text{data}} - \vec{\sigma}_{\text{theory}})^T \Xi^{-1} (\vec{\sigma}_{\text{data}} - \vec{\sigma}_{\text{theory}})$$

- ▶ Considering all statistical and systematical uncertainties

$$\vec{\sigma} := (\sigma_{-+} \quad \sigma_{+-} \quad \sigma_{--} \quad \sigma_{++})^T$$

$$\Xi := \Xi_N + \Xi_B + \Xi_\varepsilon + \Xi_{\mathcal{L}};$$

- ▶ Using a full covariance Matrix (Ξ)

$$(\Xi_\varepsilon)_{ij} = \text{corr}(\vec{\sigma}_i^\varepsilon, \vec{\sigma}_j^\varepsilon) \frac{\partial \vec{\sigma}_i}{\partial \varepsilon_i} \frac{\partial \vec{\sigma}_j}{\partial \varepsilon_j} \Delta \varepsilon_i \Delta \varepsilon_j$$

Compensation non-perfect helicity reversal: Using 4 independent parameters

$$\underbrace{P_{e^-}^- = -80\%}_{\text{"left"-handed } e^- \text{-beam}}$$

$$\underbrace{P_{e^-}^+ = 80\%}_{\text{"right"-handed } e^- \text{-beam}}$$

$$\underbrace{P_{e^+}^- = -30\%}_{\text{"left"-handed } e^+ \text{-beam}}$$

$$\underbrace{P_{e^+}^+ = 30\%}_{\text{"right"-handed } e^+ \text{-beam}}$$

Alternative parametrization: Average Polarization and deviation

$$P_{e^\pm}^- = -|P_{e^\pm}| + \frac{1}{2}\delta_{e^\pm}$$

$$P_{e^\pm}^+ = |P_{e^\pm}| + \frac{1}{2}\delta_{e^\pm}$$

Theoretical Limit of the Statistical Precision

Currently implemented processes:

Process	Channel
single $W^\pm$	$e\nu l\nu, e\nu q\bar{q}$
WW	$q\bar{q}q\bar{q}, q\bar{q}l\nu, l\nu l\nu$
ZZ	$q\bar{q}q\bar{q}, q\bar{q}ll, llll$
$ZZWW$ Mix	$q\bar{q}q\bar{q}, l\nu l\nu$
Z	$q\bar{q}, ll$

- ▶ Same processes as for physics analysis (DBD)
 - Classification
 - Cross section
- ▶ Any combination of processes can be used
- ▶ Further Process can easily added

Consider best case scenario using σ_{tot} :

- ▶ Assumption of a perfect 4π detector
- ▶ No background
- ▶ No systematic uncertainties
- ▶ Using all implemented processes

Statistical precision H-20: $\Delta P/P [\%]$

E	500	350	250	500	250
$\mathcal{L}$	500	200	500	3500	1500
P_{e-}^-	0.2	0.3	0.1	0.08	0.09
P_{e-}^+	0.05	0.06	0.03	0.02	0.02
P_{e+}^-	0.1	0.1	0.06	0.04	0.04
P_{e+}^+	0.2	0.3	0.1	0.08	0.08

Comparison to Previous Analyses (Statistical Uncertainty Only)

E	500	250
$\mathcal{L}$	3500	1500
P_{e-}^-	0.08	0.09
P_{e-}^+	0.02	0.02
P_{e+}^-	0.04	0.04
P_{e+}^+	0.08	0.08

Single boson:

- ▶ $\mathcal{L} = 2000 \text{ fb}^{-1}$, $E = 500 \text{ GeV}$
- ▶ No background estimation
- ▶ Fiducial cross section cuts
- ▶ Limitation on δ : $\Delta\delta < 10^{-3}$

$$P_{e-} : 0.085\% \quad \delta_{e-} : 0.12\%$$

$$P_{e+} : 0.22\% \quad \delta_{e+} : 0.32\%$$

E	500	350	250
$\mathcal{L}$	500	200	500
P_{e-}^-	0.2	0.3	0.1
P_{e-}^+	0.05	0.06	0.03
P_{e+}^-	0.1	0.1	0.06
P_{e+}^+	0.2	0.3	0.1

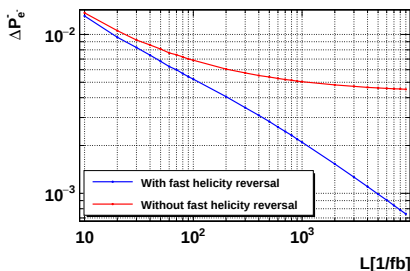
W-pairs:

- ▶ $\mathcal{L} = 500 \text{ fb}^{-1}$, $E = 500 \text{ GeV}$
- ▶ Full background estimation
- ▶ Differential cross section (angular fit)
- ▶ Only using 2 free parameters

$$P_{e-} : 0.08\% \quad P_{e+} : 0.34\%$$

Systematic Uncertainties and their Correlations

Systematic quantity		related to:
Integrated luminosity	$\mathcal{L}$	accelerator
Selection efficiency	ε	detector
Background estimate	B	theory



Remark:

A non-perfect helicity reversal has close to no influence on the precision due to compensation of the unified approach

► Uncertainties influenced by

- Detector calibration and alignment
- Machine performance
- B assumed constant and small
- ⇒ $\Delta\mathcal{L}$, $\Delta\varepsilon$ are time dependent

► Correlations:

- Data sets taken concurrently
- Generate correlations
- ⇒ Lead to cancellation of systematic uncertainties

⇒ Fast helicity reversal

- Fast switch between $\sigma_{\pm\pm}$ measurements e.g. train-by-train
- ⇒ Faster than changes in calibrations, alignments, etc.

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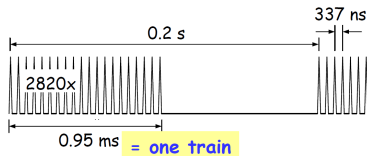
Improvement by Constraints from Polarimeter Measurement

Conclusion and Outlook



Fast Helicity Reversal

ILC Bunch Structure

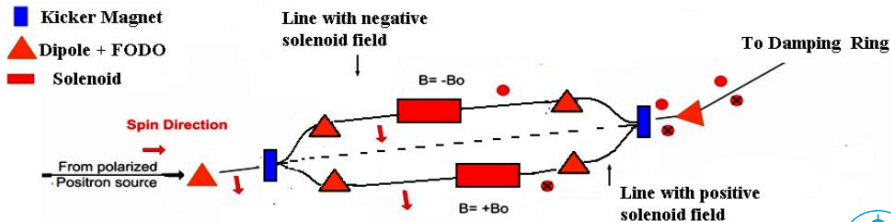


► Frequency:

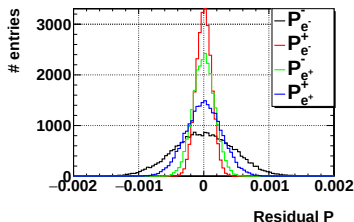
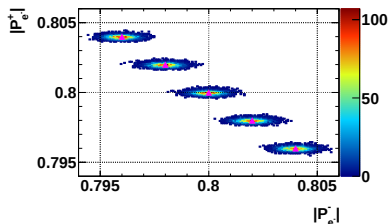
- bunch-by-bunch:
switch every few bunches
- train-by-train:
switch between two trains

► Accuracy:

- Non-perfect is realistic
- Particularly for positron beam
→ two beam lines



Testing for a Non-Perfect Helicity Reversal



► Variation in the absolute polarization

- Toy Measurement for 5 different polarization discrepancies for both beams
- Nominal initial polarizations:
 $|P_{e-}| = 80\%$, $|P_{e+}| = 30\%$
- Statistical uncertainties only

► χ^2 -Fit:

- Correct determination of the 4 polarization values
- No noticeable changes in the uncertainties

⇒ Non-Perfect Helicity Reversal:

- ⇒ No noticeable impact on polarization precision using total cross sections
- ⇒ In addition:
consider polarimeter information

Introduction

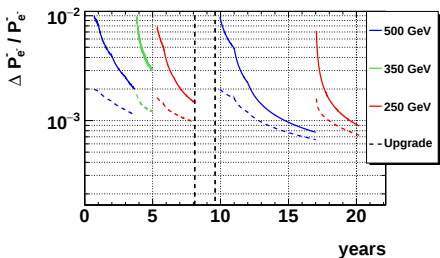
Polarization Measurement Using Collision Data

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Consider Constraints from the Polarimeter Measurement



Simplified approach: (as a first step)

- ▶ Neglect spin transport
- ▶ Using $\Delta P/P = 0.25\%$:
- ▶ Gaussian distribution
 - ▶ Mean: $|P_{e-}| = 80\%, |P_{e+}| = 30\%$
 - ▶ Width: ΔP

Implementation:

$$\chi^2_{+} = \sum_P \left[\frac{(P_{e\pm}^{\pm} - \mathcal{P}_{e\pm}^{\pm})^2}{\Delta \mathcal{P}^2} \right]$$

- ▶ $P_{e\pm}^{\pm}$: 4 fitted parameters
- ▶ $\mathcal{P}_{e\pm}^{\pm}$: Polarimeter measurement
- ▶ $\Delta \mathcal{P}$: Polarimeter uncertainty

E	500	350	250	500	250
$\mathcal{L}$	500	200	500	3500	1500
Without Constraint					
P_{e-}^{-}	0.2	0.3	0.1	0.08	0.09
With Constraint					
P_{e-}^{-}	0.1	0.1	0.1	0.07	0.07

Prospective Implementations of Polarimeter Constraints

► Consideration of the upstream polarimeter:

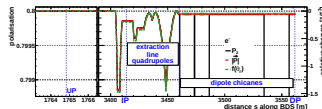
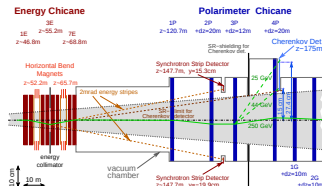
- Using the information of both polarimeters
- Compensation of misalignments in the BDS (Spin tracking)
- Compensation for beam collision effects

► Time-dependence of the beam polarization:

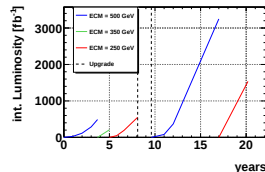
- Currently, there is always the assumption of a time-independent beam polarization
- e.g. 7 years run → not realistic scenario
- Correction for potential time-dependencies

⇒ Implementation in the unified approach:

- ⇒ Straight forward



H-20



Outlook

Considering systematic quantities for each process

- ▶ Determination of the selection efficiency ε and background estimation B
- ▶ Determination of the systematic uncertainties: ΔB , $\Delta\varepsilon$, $\Delta\mathcal{L}$
- ▶ Determination of realistic correlation factors

Implementing differential cross sections within the χ^2 -method

- ▶ Using the angular information of a process to further improve the precision
- ▶ Consider a well separation from possible BSM effects



Conclusion

- ▶ **Polarization provides a deep insight in the chiral structure of the standard model and beyond**
 - ⇒ A permille-level precision of the luminosity-weighted average polarization at the IP is required
- ▶ **New unified approach combining all suitable cross sections and the polarimeter measurement**

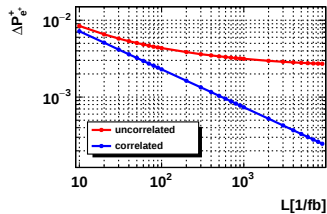
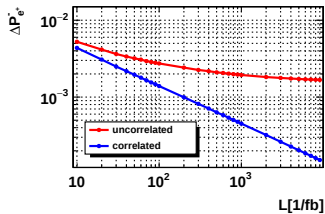
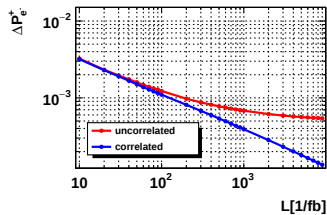
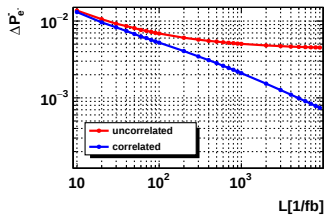
$$\chi^2 = \sum_{\text{process}} (\vec{\sigma}_{\text{data}} - \vec{\sigma}_{\text{theory}})^T \Xi^{-1} (\vec{\sigma}_{\text{data}} - \vec{\sigma}_{\text{theory}}) + \sum_P \left[\frac{(P_{e^\pm}^\pm - \mathcal{P}_{e^\pm}^\pm)^2}{\Delta \mathcal{P}^2} \right]$$

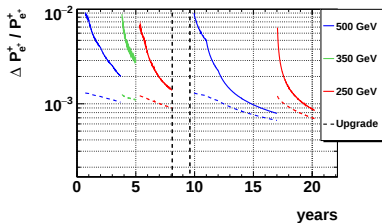
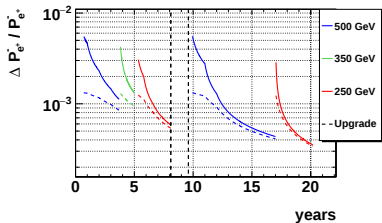
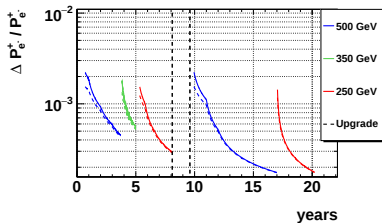
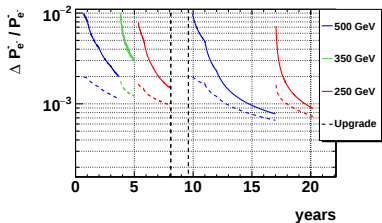
- ⇒ Statistical precision of a permille-level is achievable
 - ⇒ Impact of time-dependent systematic uncertainties can be reduced due to a fast helicity reversal
 - ⇒ Non-perfect helicity reversal has no impact on the statistical precision
- ▶ **Further improvement due to polarimeter constraints**
 - **particular for low integrated luminosity**



Backup Slides



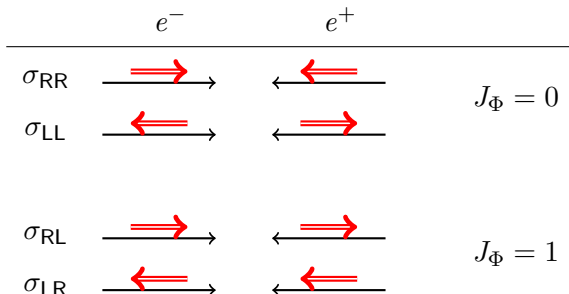




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$\mathcal{L}$	500	200	500	3500	1500
Without Constraint					
P_{e-}^-	0.2	0.3	0.1	0.08	0.09
P_{e-}^+	0.05	0.06	0.03	0.02	0.02
P_{e+}^-	0.1	0.1	0.06	0.04	0.04
P_{e+}^+	0.2	0.3	0.1	0.08	0.08
With Constraint					
P_{e-}^-	0.1	0.1	0.1	0.07	0.07
P_{e-}^+	0.04	0.05	0.03	0.02	0.02
P_{e+}^-	0.09	0.09	0.05	0.04	0.03
P_{e+}^+	0.1	0.1	0.09	0.07	0.07

Polarization at a e^-e^+ Collider

- ▶ Helicity is the projection of the spin vector on the direction of motion
- ▶ In case of massless particles, helicity is equal to chirality
- ▶ If $E_{\text{kin}} \gg E_0 \longrightarrow m_e \approx 0$



- ▶ For a bunch of particles the polarization is defined as:

$$P := \frac{N_R - N_L}{N_R + N_L}$$

Laser-Compton Polarimeters

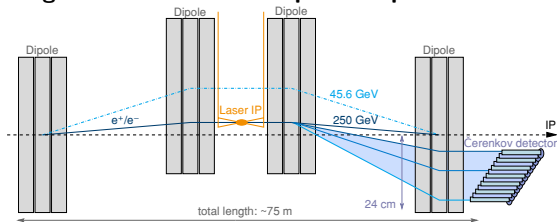
Spin Tracking

Collision Data



Laser-Compton Polarimeters

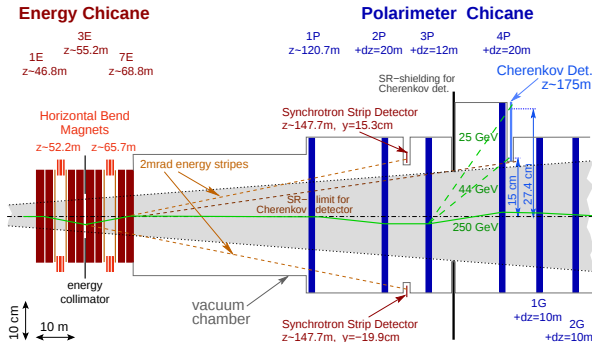
Magnetic chicane of the upstream polarimeters



- ▶ Compton scattering of the beam with a polarized Laser
- ▶ $\mathcal{O}(10^3)$ particles per bunch ($2 \cdot 10^{10}$) are scattered
- ▶ Magnetic chicane: energy spectrum
⇒ spatial distribution

- ▶ Energy spectrum measurement:
⇒ Counting the scattered particles at different positions
- ▶ Design of the magnetic Chicane:
 - ▶ Laser-bunch interaction point moves with beam energy
→ position of the Compton edge stays the same
 - ▶ Orbit of the non-scattered particles is unaffected by the magnetic chicane

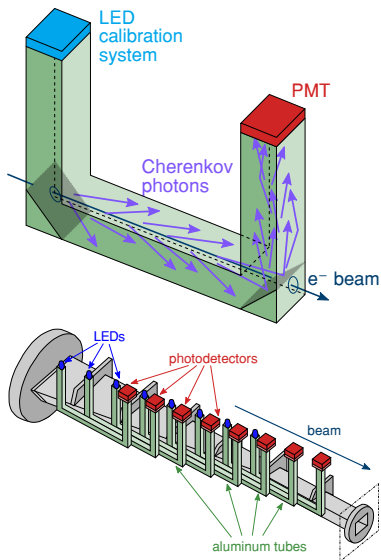
Downstream Polarimeter



Difference to Upstream Polarimeter due to a large disturbed beam

- ▶ Stronger banding of the beam after γ -IP
- ▶ 2 additional magnets to restore the beam orbit
- ▶ Measuring one bunch per train

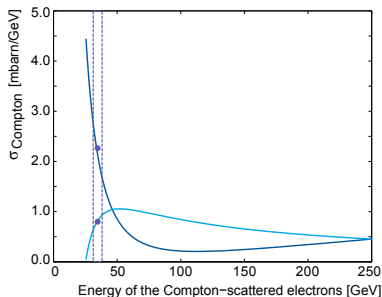
Cherenkov Detectors: Basic Concept



- ▶ U-shape channels filled with gas:
e.g. perfluorobutane
- ▶ Concept
 - ▶ Scattered particles propagate through the bottom
 - ▶ Produced Cherenkov light is reflected to one end of the channel
 - ▶ Light measurement with photomultiplier tube (PMT)
- ▶ At the other end: LED for PMT calibration
- ▶ Sampling of the energy distribution
→ Number of Cherenkov detector
- ▶ Energy resolution
→ Thickness of a Cherenkov detector
- ▶ Quartz Cherenkov detector concept:
Ref.: Theses Annika Vauth

<http://bib-pubdb1.desy.de/record/171400>

Differential Compton Cross Section



Energy dependence:

$$\frac{d\sigma_C}{dy_C} = \frac{2\pi r_e^2}{x_C} (a_C + \lambda \mathcal{P} \cdot b_C); \quad y_C := 1 - \frac{E'}{E}$$

e^- Polarization: $\mathcal{P}$; Laser Polarization: λ

DarkBlue: $\lambda \mathcal{P} = +1$

Cyan: $\lambda \mathcal{P} = -1$

Calculating $\mathcal{P}_i$ of the i -th channel with asymmetry A_i , analysing power Π_i

$$A_i := \frac{N_i^- - N_i^+}{N_i^- + N_i^+}; \quad \Pi_i = \frac{\mathcal{I}_i^- - \mathcal{I}_i^+}{\mathcal{I}_i^- + \mathcal{I}_i^+}; \quad \mathcal{I}_i^\pm := \int_{E_i - \Delta/2}^{E_i + \Delta/2} \frac{d\sigma_C}{dy_C} \Big|_{\lambda \mathcal{P} = \pm 1} dy_C$$

$N^\pm := \#e_{\text{Compton}}$ for $\lambda \mathcal{P} = \pm 1$; E_i : energy of i -th channel; Δ : energy width

$$\Rightarrow \lambda \mathcal{P}_i = \frac{A_i}{\Pi_i} \quad \Rightarrow \quad \mathcal{P} = \langle \mathcal{P}_i \rangle$$

Compton Scattering Cross Section: Formulary

$$\frac{d\sigma}{dy_C} = \frac{2\pi r_e^2}{x_C} (a_C + \lambda \mathcal{P} \cdot b_C)$$

$$y_C := 1 - \frac{E'_\gamma}{E}; \quad x_C := \frac{4EE_\gamma}{m_e^2} \cos^2\left(\frac{\vartheta_0}{2}\right)$$

$$r_C := \frac{y_C}{x_C(1 - y_C)}$$

$$a_C := (1 - y_C)^{-1} + 1 - y_C - 4r_C(1 - r_C)$$

$$b_C := r_C x_C (1 - 2r_C)(2 - y_C)$$

E, E_γ : e^-, γ energy before Compton scattering

E', E'_γ : e^-, γ energy after Compton scattering

m_e, r_e : mass, classical radius of e^-

ϑ_0 : crossing angle between e^-, γ

$\mathcal{P}$: longitudinal polarization of e^-

λ : circular polarization of γ_{Laser}

Characteristic Point:

$$E'_{\text{crossover}} = \frac{E}{1 + x_C/2},$$

$$E'_{\text{ComptonEdge}} = E'_{\text{min}} = \frac{E}{1 + x_C}$$



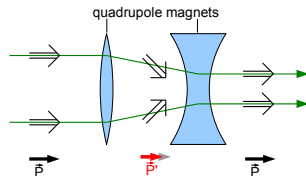
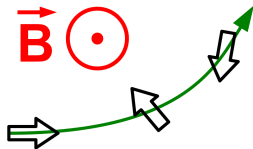
Laser-Compton Polarimeters

Spin Tracking

Collision Data



Spin Precession



- ▶ Polarimeters are 1.65 km and 150 m away from IP
 - Particles propagate through magnets
 - Magnets influence the spin, as well
 - Described by Thomas precession

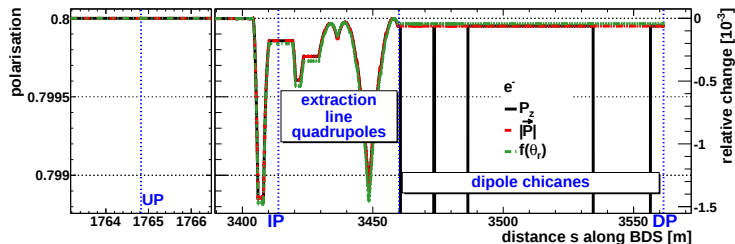
- ▶ if $\vec{B}_{\parallel} = \vec{E} = 0$:

$$\frac{d}{dt} \vec{S} = -\frac{q}{m\gamma} \left((1 + a\gamma) \vec{B}_{\perp} \right) \times \vec{S}$$

- ▶ Effects from focusing and defocusing can cancel
- ▶ For a series of quadrupole magnets $\mathcal{P}$ described by the angular divergence θ_r

$$f(\theta_r) = |\vec{\mathcal{P}}|_{\max} \cdot \cos((1 + a\gamma) \cdot \theta_r)$$

Spin Tracking



Further causes of longitudinal beam polarization change:

- ▶ *Bremsstrahlung*:
Deceleration by passing through matter → negligible for colliders
- ▶ *Beamstrahlung*:
Deflection by the em-field of the oncoming bunch during collision
- ▶ *Synchrotron radiation*:
Deflection by the em-field of accelerator magnets

Systematic Polarization Uncertainty

contribution	uncertainty [10^{-3}]
Beam and polarization alignment at polarimeters and IP ($\Delta\vartheta_{\text{bunch}} = 50 \mu\text{rad}$, $\Delta\vartheta_{\text{pol}} = 25 \text{ mrad}$)	0.72
Variation in beam parameters (10 % in the emittances)	0.03
Bunch rotation to compensate the beam crossing angle	< 0.01
Longitudinal precession in detector magnets	0.01
Emission of synchrotron radiation	0.005
Misalignments (10μ) without collision effects	0.43
Total (quadratic sum)	0.85
Collision effects in absence of misalignments	< 2.2

[Ref.:] Thesis Moritz Beckmann (<http://bib-pubdb1.desy.de/record/155874>)



Laser-Compton Polarimeters

Spin Tracking

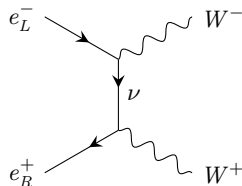
Collision Data



Concept

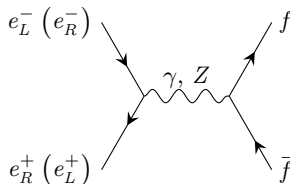
Example Processes:

W-pair production:



$$\sigma_{LL} = \sigma_{RR} = \sigma_{RL} = 0$$

s-channel spin-1 particle:



$$\sigma_{LL} = \sigma_{RR} = 0$$

- ▶ Calculation of the P from polarized σ measurement of well known SM-process
 - Using the information of their chiral structure
 - ▶ Requirement to consider a process:
 - ▶ Theoretical very well known
 - Reduction of theoretical uncertainties
 - ▶ High absolute cross section (high rate)
 - Minimizing the statistical error
 - ▶ Large left-right-asymmetry
 - Minimizing the influence of systematic uncertainties
 - ▶ Well separable from possible BSM-effects
 - ▶ Feature of the ILC:
 - Using 4 different polarization configuration (→ signs of the polarizations)
- ⇒ Task: Providing the absolute scale calibration

Special Case: The Modified Blondel Scheme (MBS)

► Constraints for the Modified Blondel Scheme:

- Process must fulfill: $\sigma_{LL} \equiv \sigma_{RR} \equiv 0$
- Perfect helicity reversal: $+|P| \longleftrightarrow -|P| \Rightarrow |P| \equiv \text{const.}$

► Unique solution:

4 possible cross section measurements: $\sigma_{-+}, \sigma_{+-}, \sigma_{--}, \sigma_{++}$

Maximal 4 unknown quantities: $\sigma_{LR}, \sigma_{RL}, |P_{e-}|, |P_{e+}|$

► Solve for $|P_{e\mp}|$:

$$\sigma_{\pm\pm} = \frac{(1 \pm |P_{e-}|)}{2} \frac{(1 \mp |P_{e+}|)}{2} \cdot \sigma_{RL} + \frac{(1 \mp |P_{e-}|)}{2} \frac{(1 \pm |P_{e+}|)}{2} \cdot \sigma_{LR}$$

► Modified Blondel-Scheme:

$$|P_{e\mp}| = \sqrt{\frac{(\sigma_{-+} + \sigma_{+-} - \sigma_{--} - \sigma_{++})(\pm\sigma_{-+} \mp \sigma_{+-} + \sigma_{--} - \sigma_{++})}{(\sigma_{-+} + \sigma_{+-} + \sigma_{--} + \sigma_{++})(\pm\sigma_{-+} \mp \sigma_{+-} - \sigma_{--} + \sigma_{++})}}$$

► Uncertainties are calculated via analytic error propagation

The Unified Approach: χ^2 -Method

- ▶ Desire for a more general approach:
 - ▶ Consider any process with a polarization dependence + using several processes at once
 - ▶ Compensate non-perfect helicity reversal: $+ |P^R| \longleftrightarrow - |P^L|$
- ▶ Consider a χ^2 -Method: Using all 4 chiral cross sections

$$\chi^2 = \sum_{\text{process}} \left\{ \sum_{\pm\pm} \left[\frac{(\sigma^{\text{data}} - \sigma^{\text{theory}})^2}{\Delta\sigma^2} \right] \right\}$$

- ▶ Compensate non-perfect helicity reversal: 4 free parameters

$$\underbrace{P_L^- = -80\%}_{\text{left-handed } e^- \text{-beam}}$$

$$\underbrace{P_R^- = 80\%}_{\text{right-handed } e^- \text{-beam}}$$

$$\underbrace{P_L^+ = -30\%}_{\text{left-handed } e^+ \text{-beam}}$$

$$\underbrace{P_R^+ = 30\%}_{\text{right-handed } e^+ \text{-beam}}$$

- ▶ Error determination via toy experiments

Polarized Cross Section

- Theoretical polarized cross section:

$$\sigma(P_{e-}, P_{e+}) = \frac{(1-P_{e-})}{2} \frac{(1-P_{e+})}{2} \cdot \sigma_{LL} + \frac{(1+P_{e-})}{2} \frac{(1+P_{e+})}{2} \cdot \sigma_{RR} \\ + \frac{(1-P_{e-})}{2} \frac{(1+P_{e+})}{2} \cdot \sigma_{LR} + \frac{(1+P_{e-})}{2} \frac{(1-P_{e+})}{2} \cdot \sigma_{RL}$$

- Measured polarized cross section:

$$\sigma(P_{e-}, P_{e+}) = \frac{N}{\varepsilon \cdot \mathcal{L}} = \frac{D - \langle B \rangle}{\varepsilon \cdot \mathcal{L}};$$

Statistic quantity: selected data D , number of events N

Systematic quantity: background B , selection efficiency ε ,
integrated luminosity $\mathcal{L}$

- Cross section of the 4 polarization configurations

$$\sigma_{--} := \sigma(-|P_{e-}|, -|P_{e+}|)$$

$$\sigma_{++} := \sigma(+|P_{e-}|, +|P_{e+}|)$$

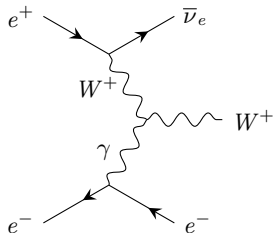
$$\sigma_{-+} := \sigma(-|P_{e-}|, +|P_{e+}|)$$

$$\sigma_{+-} := \sigma(+|P_{e-}|, -|P_{e+}|)$$

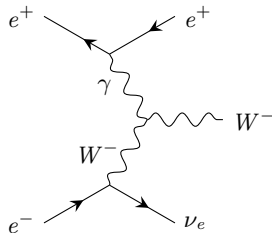


Previous Single $W^\pm$, Z , γ Study: Leading Diagrams

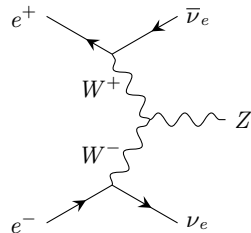
Single W^+



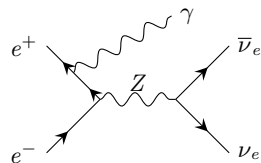
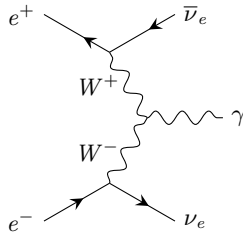
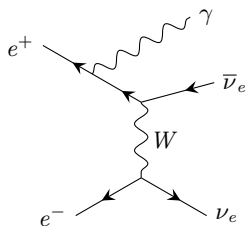
Single W^-



Single Z



Single γ



Comparison to the Previous W-Pair Study

Study by Ivan Marchesini:

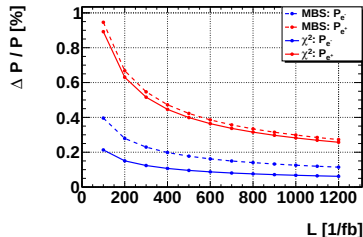
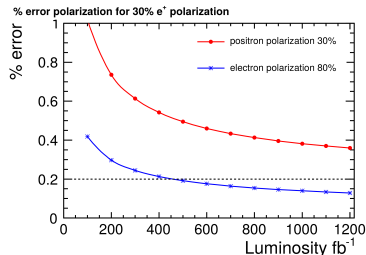
- ▶ Using $e^-e^+ \rightarrow W^+W^- \rightarrow q\bar{q}l\nu$
- ▶ Statistical uncertainties only
- ▶ Consider equal absolute polarizations (MBS)
- ▶ Including full background study

Adjustment of the current study:

- ▶ Limited to $e^-e^+ \rightarrow W^+W^- \rightarrow q\bar{q}l\nu$
- ▶ Forced equal absolute polarizations ($|P^L| \equiv |P^R|$)
- ▶ Including same background estimation and selection efficiency

Comparison:

- ⇒ χ^2 -method yields better precision under same conditions than the MBS



Comparison to Previous Single $W^\pm, \gamma, Z$ Study

Study by Graham W. Wilson

- Using 4 Processes simultaneously:

$$e^- e^+ \rightarrow \nu \bar{\nu} \gamma; \quad e^- e^+ \rightarrow \nu \bar{\nu} Z$$

$$e^- e^+ \rightarrow e^+ \nu W^- \rightarrow e^+ \nu \mu^- \bar{\nu}$$

$$e^- e^+ \rightarrow e^- \bar{\nu} W^+ \rightarrow e^- \bar{\nu} \mu^+ \nu$$

- Consider equal absolute polarizations
2 Parameters: P_{e^-}, P_{e^+}
- Consider deviations: 4 Parameters

$$P_{e^\pm}^L = -|P_{e^\pm}| + \frac{1}{2}\delta_\pm$$

$$P_{e^\pm}^R = |P_{e^\pm}| + \frac{1}{2}\delta_\pm$$

Comparison to Current analysis

- Differences:

Previous: Constraint on δ : $\Delta\delta < 10^{-3}$

Current: direct fit of $P_{e^\pm}^{L,R}$

- Very similar precision even without additional constraint on δ

parameters		$\Delta P/P, \mathcal{L} = 2\text{ab}^{-1}$	
#	P	Previous	Current
2	P_{e^-}	0.07%	0.051%
	P_{e^+}	0.22%	0.21%
4	P_{e^-}	0.085%	0.088%
	δ_{e^-}	0.12%	0.19%
	P_{e^+}	0.22%	0.23%
	δ_{e^+}	0.32%	0.56%

$\mathcal{L}$ equally distributed between $\sigma_{\pm\pm}$

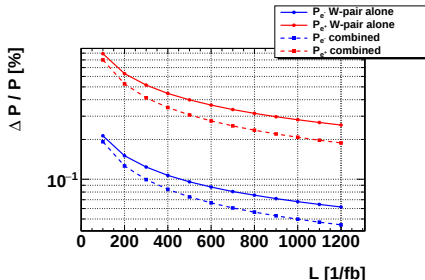
Statistical precision only



Combining W-Pair + Single W, Z, γ

Combined vs. W-Pairs alone

- ▶ W-Pair yields only enough information for 2 parameter fit P_{e-}, P_{e+}
 - ▶ Large improvement
→ due to additional processes
 - ▶ Combined: fit of 4 parameters is possible $P_{e-}^L, P_{e-}^R, P_{e+}^L, P_{e+}^R$
- ⇒ Compensation for a non-perfect helicity reversal



$$\Delta P/P, \mathcal{L} = 2\text{ab}^{-1}$$

	single W, Z, γ	Combined
P_{e-}	0.088%	0.079%
δ_{e-}	0.19%	0.18%
P_{e+}	0.23%	0.16%
δ_{e+}	0.56%	0.51%

Combined vs. Single Boson

- ▶ The 4 processes Single $W^{\pm}$, Single Z , Single γ yields a large analysis power
- ▶ Combined precision dominated by single boson processes

Consider Correlated Uncertainty

Implementing correlated uncertainty:

$$\chi^2 = \sum_{\text{process}} \sum_{i \in \pm\pm} \frac{(\sigma_i^{\text{data}} - \sigma_i^{\text{theory}})^2}{\Delta\sigma_i^2} \longrightarrow \sum_{\text{process}} (\vec{\sigma}_{\text{data}} - \vec{\sigma}_{\text{theory}})^T \Xi^{-1} (\vec{\sigma}_{\text{data}} - \vec{\sigma}_{\text{theory}})$$

$$\vec{\sigma} := (\sigma_{-+} \quad \sigma_{+-} \quad \sigma_{--} \quad \sigma_{++})^T$$

$$\Xi := \Xi_N + \Xi_B + \Xi_\varepsilon + \Xi_{\mathcal{L}}; \quad \text{e.g. } (\Xi_\varepsilon)_{ij} = \text{corr}(\vec{\sigma}_i^\varepsilon, \vec{\sigma}_j^\varepsilon) \frac{\partial \vec{\sigma}_i}{\partial \varepsilon_i} \frac{\partial \vec{\sigma}_j}{\partial \varepsilon_j} \Delta\varepsilon_i \Delta\varepsilon_j$$

Occurrence of correlated uncertainties:

- ▶ Fast switch between $\sigma_{\pm\pm}$
- ▶ Faster than change in e.g. $\delta\mathcal{L}$
- $\Delta\sigma_{\pm\pm}(\Delta\mathcal{L})$ becomes correlated
- ⇒ $\text{corr}(\vec{\sigma}_i^{\mathcal{L}}, \vec{\sigma}_j^{\mathcal{L}}) \neq 0 \quad \forall i \neq j$

Consider disadvantageous situation:

- ▶ $\varepsilon = 0.6$
- ▶ $\Delta\varepsilon/\varepsilon = 0.01$
- ▶ $\Delta\mathcal{L}/\mathcal{L} = 0.001$
- Studying the impact of correlations

Outlook

▶ Open issues

- ▶ Implementing fiducial cuts for all processes → correct description of all systematics
- ▶ Including a complete background analyses

▶ Further Improvement

- ▶ Consider also differential cross sections
- ▶ Study the possibility to use fiducial and differential cross sections simultaneously

