Search for $D^0$ decays to invisible final states at Belle

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Abstract

We report the result from the first search for $D^0$ decays to invisible final states. The analysis is performed on a data sample of 924 fb$^{-1}$ collected at and near the $\Upsilon(4S)$ and $\Upsilon(5S)$ resonances with the Belle detector at the KEKB asymmetric-energy $e^+e^-$ collider. The absolute branching fraction is determined using an inclusive $D^0$ sample, obtained by fully reconstructing the rest of the particle system including the other charmed particle. No significant signal yield is observed and an upper limit of $9.4 \times 10^{-5}$ is set on the branching fraction of $D^0$ to invisible final states at 90% confidence level.

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In the Standard Model (SM), heavy (D or B) meson decay to $\nu\bar{\nu}$ is helicity suppressed [1] with an expected branching fraction of $\mathcal{B}(D^0 \to \nu\bar{\nu}) = 1.1 \times 10^{-30}$ [2], which is beyond the reach of current collider experiments. The branching fraction may be enhanced by non-SM mechanisms such as the decay of D and B mesons to dark matter (DM) final states with and without an additional light meson in the final states, as estimated in Ref. [1]. With several DM candidates [3, 4], the branching fraction of $D^0$ to invisible final states could be enhanced to as large as $\mathcal{O}(10^{-15})$.

Recent DM searches are mainly based on the direct detection of the nuclear recoil signal due to DM interaction [5, 6]; or $\gamma$-ray, $e^+e^-$ and $p\bar{p}$ production due to DM annihilation [7, 8]. At an $e^+e^-$ “flavor factory,” in which two heavy-flavor particles are produced in flavor-conjugate states, the indirect detection of DM candidates is performed as follows. One of the D or B mesons is fully reconstructed, and then energy-momentum conservation is used to search for the decay of the other D or B meson into an invisible final state.

In Belle, there are many $e^+e^- \to c\bar{c}$ continuum events, in which a few hundred million $D$ mesons are produced. We use the charm tagger method to select an inclusive $D^0$ sample, which permits the identification of $D^0$ decays involving invisible particles [9–12]: the process $e^+e^- \to c\bar{c} \to D^{(*)}_{\text{tag}} X_{\text{frag}} D^{*-}_{\text{sig}}$ with $D^{*-}_{\text{sig}} \to D^0_{\text{sig}} \pi^-_{s}$ is reconstructed except for $D^0_{\text{sig}}$, as illustrated in Fig. 1. Here, $D^{(*)}_{\text{tag}}$ represents a charmed particle used as a tag: $D^{(*)0}, D^{(*)+}, D_s^{(*)+}, \text{or } \Lambda^+_s$. Since the center-of-mass (c.m.) energy of KEKB is above the open charm threshold, a fragmentation system ($X_{\text{frag}}$) with a few light unflavored mesons may also be produced. The $\pi^-_{s}$ denotes a charged pion from $D^{*-}_{\text{sig}}$ decay.

This search for $D^0 \to$ invisible decay with the charm tagger method at B factories provides a powerful way to search for DM: any clear signal would be an indication for new physics. Measurements of $B^0$ decays to invisible final states with both hadronic and semileptonic B tagging methods are already reported by both Belle and BaBar [13, 14].

We use the data sample of 924 fb$^{-1}$ collected at or near the $\Upsilon(4S)$ and $\Upsilon(5S)$ resonances with the Belle detector [15] at the KEKB asymmetric-energy $e^+e^-$ collider [16]. The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF) and an electromagnetic calorimeter (ECL) comprised of CsI(Tl) crystals located inside a superconducting solenoid that provides a 1.5 T magnetic field. An iron flux-return yoke
located outside the solenoid is instrumented to detect $K^0_L$ mesons and to identify muons. The detector is described in detail elsewhere [15].

The data set used in this analysis was collected with two different inner-detector configurations. About 156 fb$^{-1}$ were collected with a beam pipe of radius 2 cm and with 3 layers of SVD, while the rest of the data set was collected with a beam pipe of radius 1.5 cm and 4 layers of SVD [17]. Large Monte Carlo (MC) samples for signal and several backgrounds are generated with EvtGen [18] and simulated with GEANT3 [19] with the configurations of the Belle detector. These samples are used to obtain expected distributions of various physical quantities for signal and background, to optimize the selection criteria, and to determine the signal selection efficiency.

![Diagram](image)

**FIG. 1:** An illustration of the charm tagger method.

We use the knowledge of the $e^+e^-$ four-momentum to identify a $D^0$ that escaped detection by fully reconstructing the remainder of the event (whether this $D^0$ decays visibly or not). The four types of $D_{\text{tag}}$ are reconstructed using 23 decay modes. ($D_{\text{tag}}^a$ candidates are described later.) The decay modes and the corresponding requirements on the $D_{\text{tag}}$ momentum in the c.m. frame ($p^*$) are listed in Table I; these requirements were optimized in Ref. [11].

The selection criteria for the final-state charged particles in $D_{\text{tag}}$ are based on information obtained from the tracking systems (SVD and CDC) and the hadron identification systems (CDC, ACC, and TOF). These particles are required to have an impact parameter within $\pm 0.5$ cm of the interaction point (IP) in the transverse plane, and within $\pm 1.5$ cm along the positron beam direction. The likelihood values of each track for different particle types, $L_p$, $L_K$, and $L_\pi$, are determined from the information provided by the hadron-identification.
TABLE I: $D_{\text{tag}}$ decay modes and corresponding requirements on the $D_{\text{tag}}$ momentum in the c.m. frame ($p^*$).

<table>
<thead>
<tr>
<th>$D^0$ decay</th>
<th>$p^*$ (GeV/c)</th>
<th>$D^+$ decay</th>
<th>$p^*$ (GeV/c)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$K^-\pi^+$</td>
<td>&gt; 2.3</td>
<td>$K^-\pi^+\pi^+$</td>
<td>&gt; 2.3</td>
</tr>
<tr>
<td>$K^-\pi^+\pi^0$</td>
<td>&gt; 2.5</td>
<td>$K^-\pi^+\pi^0\pi^+$</td>
<td>&gt; 2.5</td>
</tr>
<tr>
<td>$K^-\pi^-\pi^+$</td>
<td>&gt; 2.3</td>
<td>$K^0_S\pi^+$</td>
<td>&gt; 2.3</td>
</tr>
<tr>
<td>$K^-\pi^-\pi^+\pi^0$</td>
<td>&gt; 2.5</td>
<td>$K^0_S\pi^+\pi^0\pi^+$</td>
<td>&gt; 2.4</td>
</tr>
<tr>
<td>$K^0_S\pi^+\pi^-$</td>
<td>&gt; 2.3</td>
<td>$K^0_S\pi^+\pi^-\pi^0$</td>
<td>&gt; 2.4</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>$D_s^+$ decay</th>
<th>$p^*$ (GeV/c)</th>
<th>$D_s^+$ decay</th>
<th>$p^*$ (GeV/c)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$pK^-\pi^+$</td>
<td>&gt; 2.3</td>
<td>$K^+K^-\pi^+$</td>
<td>&gt; 2.3</td>
</tr>
<tr>
<td>$pK^-\pi^+\pi^0$</td>
<td>&gt; 2.5</td>
<td>$K^0_SK^+$</td>
<td>&gt; 2.3</td>
</tr>
<tr>
<td>$pK^0_S^+$</td>
<td>&gt; 2.3</td>
<td>$K^0_SK^0_S\pi^+$</td>
<td>&gt; 2.3</td>
</tr>
<tr>
<td>$\Lambda\pi^+$</td>
<td>&gt; 2.3</td>
<td>$K^+K^-\pi^+\pi^0$</td>
<td>&gt; 2.5</td>
</tr>
<tr>
<td>$\Lambda\pi^+\pi^0$</td>
<td>&gt; 2.5</td>
<td>$K^0_SK^-\pi^+\pi^+$</td>
<td>&gt; 2.4</td>
</tr>
<tr>
<td>$\Lambda\pi^+\pi^-$</td>
<td>&gt; 2.3</td>
<td>$K^0_SK^-\pi^-\pi^0$</td>
<td>&gt; 2.4</td>
</tr>
</tbody>
</table>

system. The track is identified as a proton if $L_K/(L_K + L_p) < 0.9$ and $L_\pi/(L_\pi + L_p) < 0.9$, as a pion if $L_K/(L_K + L_\pi) < 0.9$, and as a kaon if $L_K/(L_K + L_\pi) > 0.1$. The efficiencies are about 99% for identifying each type of charged hadron.

Photons are reconstructed from the energy clusters in the ECL that are not associated with charged tracks. A $\pi^0$ is reconstructed from two photon candidates by requiring the di-photon invariant mass ($M_{\gamma\gamma}$) to be between 0.115 and 0.150 GeV/$c^2$ (with an efficiency of 89%). The energy of each photon candidate is required to be greater than 50 MeV and a mass-constrained fit is performed on the reconstructed $\pi^0$ candidate. For the $D_{\text{tag}}$ channels with more than two tracks, a $K^0_S$ and two tracks, or a $\Lambda$ in the final states, the photons are required to have an energy greater than 100 MeV in the ECL endcaps.
\(K_S^0 (\Lambda)\) candidates are reconstructed in the \(\pi^+\pi^- (p\pi^-)\) mode and are required to have invariant \(M_{\pi^+\pi^-} (M_{p\pi^-})\) between 0.468 and 0.508 GeV/c\(^2\) (1.111 and 1.121 GeV/c\(^2\)), leading to an efficiency of about 64\% (47\%). A successful vertex fit is also required \((\chi^2 < 100\) for \(\Lambda\)). \(K_L^0\) candidates are reconstructed from the clusters in KLM that are not associated with charged tracks.

\(D_{\text{tag}}\) candidates are required to have an invariant mass within \(\pm 3\sigma\) of the nominal mass [20] (where \(\sigma\) is the resolution of measurement) and be successfully fit to a common vertex with a mass constraint.

\(D_{\text{tag}}^*\) candidates are reconstructed via five decay modes: \(D^{*+} \rightarrow D^0\pi^+, D^{*+} \rightarrow D^+\pi^0, D^{*0} \rightarrow D^0\pi^0, D^{*0} \rightarrow D^0\gamma,\) and \(D_{s\pi}^{*+} \rightarrow D_s^+\gamma\). The \(\gamma\) candidate used in \(D^{*0}\) or \(D_{s\pi}^{*+}\) reconstructions is required to have an energy greater than 0.12 GeV and is paired with all other photons in the event to ensure that it is not from a \(\pi^0\) decay: if \(M_{\gamma\gamma}\) is within \(\pm 10\) MeV/c\(^2\) of the nominal \(\pi^0\) mass and the energy asymmetry \(\left|\left((E_{\gamma_1} - E_{\gamma_2})/(E_{\gamma_1} + E_{\gamma_2})\right)\right|\) is less than 0.5, the \(D^{*0}\) or \(D_{s\pi}^{*+}\) candidate is rejected. The mass difference between the \(D_{\text{tag}}^*\) and \(D_{\text{tag}}\) is required to be within \(\pm 3\sigma\) of the nominal \(D_{(s)} - D_{(s)}\) mass difference [20]. The \(\pi^+\) from the \(D_{\text{tag}}^*\) decay is refitted to the \(D_{\text{tag}}\) vertex.

The \(X_{\text{frag}}\) system is reconstructed from the remaining particles with up to three pions, including at most one \(\pi^0\): nothing, \(\pi^+, \pi^0, \pi^+\pi^0, \pi^+\pi^-, \pi^+\pi^-\pi^+,\) and \(\pi^+\pi^-\pi^0\). If \(D_{\text{tag}}\) is \(\Lambda^+_c\), a \(\bar{p}\) is included in \(X_{\text{frag}}\) for baryonic number conservation. If \(D_{\text{tag}}\) is \(D_{s\pi}^+\), a kaon is included in \(X_{\text{frag}}\) for strangeness conservation. If \(D_{\text{tag}}\) is \(D^0\) or \(D^+\), \(X_{\text{frag}}\) modes with an additional \(K^+K^-\) pair are also considered. The \(X_{\text{frag}}\) modes are listed in Table II. The charge of \(D_{\text{tag}}^* X_{\text{frag}}\) is required to be +1 [2]. For each combination of \(D_{\text{tag}}^* X_{\text{frag}}\), the missing mass recoiling against \(D_{\text{tag}}^* X_{\text{frag}}\), \(M_{\text{miss}}(D_{\text{tag}}^* X_{\text{frag}})\), is required to be between 1.86 and 2.16 GeV/c\(^2\) to select a \(\overline{D}_{\text{sig}}\) candidate. At this stage, all candidates satisfying the selection criteria are retained.

For each \(D_{\text{tag}}^* X_{\text{frag}}\) candidate satisfying the above \(M_{\text{miss}}(D_{\text{tag}}^* X_{\text{frag}})\) requirement, the remaining tracks not associated with \(D_{\text{tag}}^* X_{\text{frag}}\) are examined for a \(\pi^-\) candidate. For each such candidate, the missing momentum recoiling against the \(D_{\text{tag}}^* X_{\text{frag}} \pi^-\) system in the c.m. frame is calculated and required to be greater than 2.0 GeV/c. The missing mass for the \(D_{\text{tag}}^* X_{\text{frag}} \pi^-\) system \(M_{D^0}\) is subsequently calculated from a fit in which \(M_{\text{miss}}(D_{\text{tag}}^* X_{\text{frag}})\) is constrained to the nominal \(D^+\) mass \((m_{D^+})\) [20] (to improve the resolution). If more than one \(\overline{D}_{\text{sig}}^0\) candidate is found in an event, we first choose the one with the smallest \(\chi^2\),
which is obtained from the fit with \( M_{\text{miss}}(D_{\text{tag}}^{(*)}X_{\text{frag}}) \) constrained to \( m_{D^{*+}} \). If still more than one candidate is found (with multiple \( \pi_s \)’s), we choose the one with the largest opening angle between \( D_{\text{sig}}^0 \) and \( D_{\text{tag}}^{(*)} \) in the c.m. frame. Multiple candidates are found in 56.6% of the data with an average multiplicity of inclusive \( D^0 \) candidates of 2.7, which is consistent with MC simulation.

**TABLE II: \( X_{\text{frag}} \) system for \( D_{\text{tag}}^{(*)} \).**

<table>
<thead>
<tr>
<th>( D^{(*)}+ )</th>
<th>( D^{(*)}0 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>nothing(( K^+K^- ))</td>
<td>( \pi^+(K^+K^-) )</td>
</tr>
<tr>
<td>( \pi^0(K^+K^-) )</td>
<td>( \pi^+\pi^0(K^+K^-) )</td>
</tr>
<tr>
<td>( \pi^+\pi^-(K^+K^-) )</td>
<td>( \pi^+\pi^-\pi^+(K^+K^-) )</td>
</tr>
<tr>
<td>( \pi^+\pi^-\pi^0(K^+K^-) )</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>( \Lambda_c^+ )</th>
<th>( D_{s}^{(*)+} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \pi^+\bar{p} )</td>
<td>( K^0_S, \pi^0K^0_S )</td>
</tr>
<tr>
<td>( \pi^+\pi^0\bar{p} )</td>
<td>( \pi^+K^-, \pi^+\pi^0K^- )</td>
</tr>
<tr>
<td>( \pi^+\pi^-\pi^+\bar{p} )</td>
<td>( \pi^+\pi^-K^0_S, \pi^+\pi^-\pi^0K^0_S )</td>
</tr>
<tr>
<td></td>
<td>( \pi^+\pi^-\pi^+K^- )</td>
</tr>
</tbody>
</table>

The inclusive \( D^0 \) yield is extracted from a one-dimensional extended unbinned maximum likelihood fit, with the likelihood defined as

\[
L = e^{-\sum_j N_j} \frac{N!}{\prod_{i=1}^{N} (\sum_j N_j P_j(M_{D^0}^i))},
\]

where \( N \) is the total number of candidates, \( N_j \) is the number of events in component \( j \), \( M_{D^0}^i \) is \( m_{D^0} \) value of the \( i \)-th candidate, and \( P_j \) represents the corresponding one-dimensional probability density function (PDF). There are two components in the fit: inclusive \( D^0 \) signal, modelled with combination of two Gaussian functions and a bifurcated Gaussian function with common means, and the background, modelled with an ARGUS function [21]. The free parameters in the fit are the yields of the two components and all the shape parameters.
except for the end-point of the ARGUS function, which is fixed by MC simulation. The fit is shown in Fig. 2, and we obtain $694667^{+1494}_{-1563}$ inclusive $D^0$ decays.

![Fig. 2: $M_{D^0}$ distribution of the inclusive $D^0$ sample. The points with error bars are data; the solid line is the fit result; the blue dotted line is background, and the red area is the inclusive $D^0$ signal.](image)

Candidates for invisible $D^0$ decays are identified by requiring no remaining final-state particles associated with $D^0_{\text{sig}}$. More precisely, events from the inclusive $D^0_{\text{sig}}$ sample with remaining charged tracks, $\pi^0$, $K^0_L$, $K^0_S$, or $\Lambda$ are vetoed. In addition to $M_{D^0}$, the residual energy in the ECL, denoted as $E_{\text{ECL}}$, is also used to extract the $D^0 \rightarrow$ invisible signal. $E_{\text{ECL}}$ is defined as the sum of the energies of the ECL clusters that are not associated with the particles of the $D^0_{\text{tag}}X_{\text{frag}}\pi^-_s$ system. In order to suppress the beam background, cluster energies are required to be above ECL-region-dependent thresholds: 50 MeV for $32.2^\circ < \theta < 128.7^\circ$, 100 MeV for $\theta < 32.2^\circ$, and 150 MeV for $\theta > 128.7^\circ$.

We consider two backgrounds for the $D^0 \rightarrow$ invisible signal: the $D^0$ background from the $e^+e^- \rightarrow c\bar{c}$ process in which correctly-tagged $D^0$ peak in $M_{D^0}$ (e.g. $D^0 \rightarrow K^0\pi^0$); and the non-$D^0$ background from $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$), $\Upsilon(4S)$, and $\Upsilon(5S)$ decays. The signal yield is extracted from a two-dimensional extended unbinned maximum likelihood fit, with the likelihood defined as

$$L = \frac{e^{-\sum_j N_j}}{N!} \prod_{i=1}^{N} \left( \sum_j N_j P_j(M_{D^0}, E_{\text{ECL}}^i) \right),$$

(2)

where $P_j$ represents the corresponding two-dimensional PDF, and $E_{\text{ECL}}^i$ is the $E_{\text{ECL}}$ value.
of the $i$-th candidate. The $P_j$ functions are products of $M_{D^0}$ PDFs and $E_{ECL}$ PDFs since correlations between $M_{D^0}$ and $E_{ECL}$ are found to be small. There are three components in the fit: signal, $D^0$ background, and non-$D^0$ background. The PDFs in $E_{ECL}$ are histograms obtained from MC simulation. The $D^0$ and non-$D^0$ background PDFs in $E_{ECL}$ have a small peaking structure near $E_{ECL} = 0$ GeV, and the corresponding systematic effects are described below. The signal PDF in $M_{D^0}$ is fixed as the one obtained by the fit to the $M_{D^0}$ distribution of the inclusive $D^0$ sample. The $D^0$ background PDFs in $M_{D^0}$ is parameterized with the sum of three Gaussian functions. The non-$D^0$ background PDF in $M_{D^0}$ is an ARGUS function. The free parameters in the fit are the yields of the three components, the $D^0$ background PDF shape parameters, and the non-$D^0$ background PDF shape parameters except for the end-point of the ARGUS function.

The projections of the fit are shown in Fig. 3. The fitted signal yield of $D^0 \rightarrow$ invisible is $-6.3^{+22.5}_{-21.0}$, which is consistent with zero.

![Graphs showing fit results for $D^0$ decays to invisible final states. The top panel shows the $M_{D^0}$ distribution for $E_{ECL} < 0.5$ GeV and the bottom one shows $E_{ECL}$ for $M_{D^0} > 1.86$ GeV/c^2. The points with error bars are data; the solid line is the fit result; the blue dotted line is $D^0$ background; the green dashed line is non-$D^0$ background, and the red area is the signal of $D^0$ decaying to invisible final states.](image)

FIG. 3: Fit results of $D^0$ decays to invisible final states. The top panel shows the $M_{D^0}$ distribution for $E_{ECL} < 0.5$ GeV and the bottom one shows $E_{ECL}$ for $M_{D^0} > 1.86$ GeV/c^2. The points with error bars are data; the solid line is the fit result; the blue dotted line is $D^0$ background; the green dashed line is non-$D^0$ background, and the red area is the signal of $D^0$ decaying to invisible final states.

The branching fraction is calculated using

$$B = \frac{N_{\text{sig}}}{\epsilon \times N_{D^0}^{\text{incl}}},$$

(3)
where $N_{\text{sig}}$, $N_{D^0}^{\text{incl}}$, and $\epsilon$ are the fitted signal yield of $D^0 \rightarrow$ invisible decays, the number of inclusive $D^0$ mesons, and the efficiency of reconstructing $D^0 \rightarrow$ invisible decays within the inclusive $D^0$ sample, respectively. We calibrate the reconstruction efficiency, estimated using the MC simulation by including in $\epsilon$ a factor $C_{\text{veto}} = 1.1$ due to the corrections associated with the vetoes on remaining final state particles in the reconstruction of $\overline{D}^0_{\text{sig}}$. The $C_{\text{veto}}$ value is obtained from a study with $D^0 \rightarrow K^-\pi^+$ control sample described below. The calibrated reconstruction efficiency for the signal is $(62.4^{+3.2}_{-3.1})\%$.

As a check, we repeat the entire analysis with the $D^0 \rightarrow K^-\pi^+$ control sample. After $D^0 \rightarrow K^-\pi^+$ candidates are reconstructed from tracks associated with $\overline{D}^0_{\text{sig}}$ and $M_{K^-\pi^+}$ is required to be between 1.80 and 1.92 GeV/$c^2$, exactly the same selection criteria as for the $D^0 \rightarrow$ invisible analysis are applied, excluding $K^-$ and $\pi^+$ from $\overline{D}^0_{\text{sig}}$. The projections of the fit to his control sample are shown in Fig. 4. The efficiency of reconstructing $D^0 \rightarrow K^-\pi^+$ is 29.0%. With a signal yield of $7842^{+116}_{-117}$, we obtain $\mathcal{B}(D^0 \rightarrow K^-\pi^+) = (3.89 \pm 0.06\text{(stat.)})\%$, which is consistent with the world average of $(3.93 \pm 0.04)\%$ [20].

![Fit results of $D^0 \rightarrow K^-\pi^+$](image)

FIG. 4: Fit results of $D^0 \rightarrow K^-\pi^+$. The top panel shows the $M_{D^0}$ distribution for $E_{ECL} < 0.5$ GeV and the bottom one shows $E_{ECL}$ for $M_{D^0} > 1.86$ GeV/$c^2$. The points with error bars are data; the solid line is the fit result; the blue dotted line is $D^0$ background; the green dashed line is non-$D^0$ background, and the red area is the $D^0 \rightarrow K^-\pi^+$ signal.

Sources of various systematic uncertainties on the branching fraction calculation are shown in Table III. The uncertainties associated with $\epsilon$ and $N_{D^0}^{\text{incl}}$ are quoted as percentages, while the uncertainties associated with signal yield extraction are quoted as event

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yields. The uncertainty due to the yield of inclusive signal $D^0$ mesons includes the statistical and systematic uncertainties. The latter includes uncertainties due to signal $D^0$ PDF and background PDF modeling, and these are obtained by the variation of the measured yield using different shape functions in the $D^0 \to K^-\pi^+$ fit and the fit to the inclusive $D^0$ mass spectrum, respectively. The calibration factors for the MC reconstruction efficiency due to vetoes ($C_{\text{veto}}$) and the associated systematic uncertainty are obtained by comparing the data ($\epsilon_{\text{data}}$) and MC veto efficiency ($\epsilon_{\text{MC}}$) using the $D^0 \to K^-\pi^+$ control sample. In addition, the ratios $\epsilon_{\text{data}}/\epsilon_{\text{MC}}$ with different $D_{\text{tag}}^{(s)}/X_{\text{frag}}$ reconstruction modes are studied and are found to be consistent with each other within $\pm 1\sigma$ of their statistical uncertainty; the variation is included in the systematic uncertainty. The statistical uncertainty of the MC sample in the efficiency estimation is also included.

The uncertainty due to a possible yield bias is estimated by an MC ensemble test with an assumed branching fraction of zero. The uncertainties due to the shape-fixed PDF in the fit are obtained from the signal yield change when varying the PDF shape. For the signal PDF in $E_{\text{ECL}}$, the histogram PDF is varied by the data-MC difference in the $E_{\text{ECL}}$ distribution of the $D^0 \to K^-\pi^+$ control sample. For the $D^0$ background PDF in $E_{\text{ECL}}$, we vary the first-bin content of the histograms by $\pm 1\sigma$ of the branching fraction of the $D^0$ decay modes, where $\sigma$ denotes the measurement error on the branching fraction. For the non-$D^0$ background PDF in $E_{\text{ECL}}$, we find that the MC can describe data well in the region $M_{D^0} < 1.855 \text{ GeV}/c^2$, and the histogram PDF is also varied by the data-MC difference in the $E_{\text{ECL}}$ distribution in this region. For the signal PDF in $M_{D^0}$, we vary the shape parameters by $\pm 1\sigma$, where $\sigma$ denotes standard deviation of the shape parameters obtained by the fit on $M_{D^0}$ distribution of the inclusive $D^0$ sample. For the non-$D^0$ background PDF in $M_{D^0}$, we float the end-point in the fit and the signal yield variation is found to be negligible.

Since the observed yield for $D^0 \to \text{invisible}$ is not significant, we calculate a 90% confidence level Bayesian upper limit on the branching fraction ($B_{UL}$) [22]. The upper limit is obtained by integrating the likelihood function:

$$\int_0^{B_{UL}} L(B) dB = 0.9 \int_0^1 L(B) dB,$$

where $L(B)$ denotes the likelihood value. The systematic uncertainties are taken into account.
TABLE III: Summary of the systematic uncertainties on the branching fraction.

<table>
<thead>
<tr>
<th>Source</th>
<th>in %</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N^\text{incl.}_{D^0}$</td>
<td>$\pm 0.2,\text{(stat.)} \pm 3.6,\text{(syst.)}$</td>
</tr>
<tr>
<td>$C_{\text{veto}}$</td>
<td>$+4.7/ -4.6$</td>
</tr>
<tr>
<td>MC statistics</td>
<td>$\pm 1.9$</td>
</tr>
<tr>
<td>Total</td>
<td>$+6.2/ -6.1$</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Source</th>
<th>in events</th>
</tr>
</thead>
<tbody>
<tr>
<td>Yield bias</td>
<td>$-0.5$</td>
</tr>
<tr>
<td>Signal PDF in $E_{ECL}$</td>
<td>$+2.3$</td>
</tr>
<tr>
<td>$D^0$ background PDF in $E_{ECL}$</td>
<td>$+2.5/ -2.6$</td>
</tr>
<tr>
<td>Non-$D^0$ background PDF in $E_{ECL}$</td>
<td>$-13.7$</td>
</tr>
<tr>
<td>Signal PDF in $M_{D^0}$</td>
<td>$+0.2/ -0.4$</td>
</tr>
<tr>
<td>Non-$D^0$ background PDF in $M_{D^0}$</td>
<td>negligible</td>
</tr>
<tr>
<td>Total</td>
<td>$+3.4/ -14.0$</td>
</tr>
</tbody>
</table>

by replacing $\mathcal{L}(B)$ with a smeared likelihood function:

$$
\mathcal{L}_{\text{smear}}(B) = \int_{0}^{1} \mathcal{L}(B') e^{\frac{(B - B')^2}{2\Delta B^2}} dB',
$$

(5)

where $\Delta B$ is the total systematic uncertainty on $B'$. We thus determine the upper limit on the branching fraction of $D^0 \rightarrow$ invisible to be $9.4 \times 10^{-5}$ at the 90% confidence level.

In conclusion, we have performed the first search for $D^0$ decays into invisible final states with the charm tagger method by using a data sample of 924 fb$^{-1}$ collected by Belle. No significant signal yield is found and we set an upper limit on the branching fraction of $9.4 \times 10^{-5}$ at the 90% confidence level for the $D^0 \rightarrow$ invisible decay. Further improvement in this measurement may be possible in the near future with other $e^+e^-$ collider experiments such as BESIII and Belle II.

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[2] Throughout this paper, inclusion of charge-conjugate decay modes is always implied.


[22] As we use a Bayesian method, this is formally a “credibility level”. However, we use “confidence level” here following common convention.