



Interferometric phase detection at x-ray energies via Fano resonance control

K. P. Heeg,¹ C. Ott,¹ D. Schumacher,² H.-C. Wille,² R. Röhlberger,² T. Pfeifer,¹ and J. Evers¹

¹Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, D-69117 Heidelberg, Germany

²Deutsches Elektronen-Synchrotron DESY, Notkestrasse 85, 22607 Hamburg, Germany

(Received 6 November 2014; published 18 May 2015)

Modern x-ray light sources promise access to structure and dynamics of matter in largely unexplored spectral regions. However, the desired information is encoded in the light intensity and phase, whereas detectors register only the intensity. This phase problem is ubiquitous in crystallography and imaging and impedes the exploration of quantum effects at x-ray energies. Here, we demonstrate phase-sensitive measurements characterizing the quantum state of a nuclear two-level system at hard x-ray energies. The nuclei are initially prepared in a superposition state. Subsequently, the relative phase of this superposition is interferometrically reconstructed from the emitted x rays. Our results form a first step towards x-ray quantum state tomography and provide new avenues for structure determination and precision metrology via x-ray Fano interference.

DOI: 10.1103/PhysRevLett.114.207401

PACS numbers: 78.70.Ck, 03.65.Wj, 07.60.Ly, 32.70.Jz

The phase of electromagnetic fields is the key to interferometry. This technique of superimposing electromagnetic waves is an important method with applications across all the natural sciences [1]. But standard detectors for optical or higher-frequency fields are sensitive to the field intensity only, masking the phase required for many applications [2]. In x-ray science, prominent examples are crystallography [3] and coherent imaging [4]. In the latter, photons are elastically scattered off of an object to characterize it. Although the relation between the scattered light and the original object is well known, the lack of phase information prevents a straightforward reconstruction of the original object [5]. Next to structure determination, the reconstruction of quantum states also requires phase-sensitive measurements [6,7]. This quantum state tomography has been successfully demonstrated at optical frequencies [8], but remains an open challenge in the x-ray domain [9]. However, in the past years, a tremendous boost in activities related to x-ray quantum optics has been witnessed, fueled by the advent of novel light sources [10]. Next to the interaction of x rays with innershell electrons [11–13], in particular, targeting nuclear resonances has proven a promising approach in this direction [14–18].

In this work, we demonstrate phase-sensitive measurements on an archetype quantum mechanical two-level system (TLS) at hard x-ray frequencies, represented by such a nuclear resonance of a Mössbauer isotope. The TLS is realized in a large ensemble of identical nuclei, operated in such a way that the incident x rays couple the ground state to a single collective excited state [19]. The phase sensitivity is gained by a cavity-based x-ray interferometer with the TLS in one of its arms. Tuning the phase of the non-TLS path enables us to determine the phase of the light emitted by the TLS via the intensity at one of the output

ports of the interferometer. The x-ray pulse is nearly instantaneous on the time scale of the nuclei and prepares the TLS in an initial coherent superposition of its two states. After this, we determine the phase of the light emitted by the TLS, which allows us to characterize the initial state prepared by the x-ray pulse.

The state of the TLS is described by its density matrix, and the phase reconstructed here can be identified with the phase of the off-diagonal density matrix elements. Our measurement therefore forms an important step towards the full tomography of the TLS quantum state, which is a crucial tool for the exploration of quantum effects at x-ray energies. The interferometric measurement technique combined with the precise mapping of the spectroscopic line shape of the TLS in turn provide new avenues for structure determination and precision metrology.

The experimental scheme and setup are illustrated in Fig. 1. A nanometer-sized thin-film structure of materials with an alternating index of refraction is used to form an x-ray cavity. The guiding layer of the cavity contains a sheet of ⁵⁷Fe nuclei with a Mössbauer resonance at 14.4 keV, which is used to form the TLS. X-ray light impinges on this structure in grazing incidence at angle θ , and we record the spectrum of the reflected light. In this setting, we interpret the cavity as an interferometer, comprising two pathways that contribute to the x-ray reflectance as depicted in Fig. 1. The first path ($r_C e^{i\phi_C}$) consists of light reflected by the cavity alone. In the second path ($r_N e^{i\phi_N}$), the x rays interact with the near-resonant TLS. Both channels include possible multiple reflections in the cavity. The total recorded reflectance arises from the interference between the two paths, governed by their relative phase. As we will show, the phase ϕ_C depends on the incidence angle θ , and thus can be externally controlled.

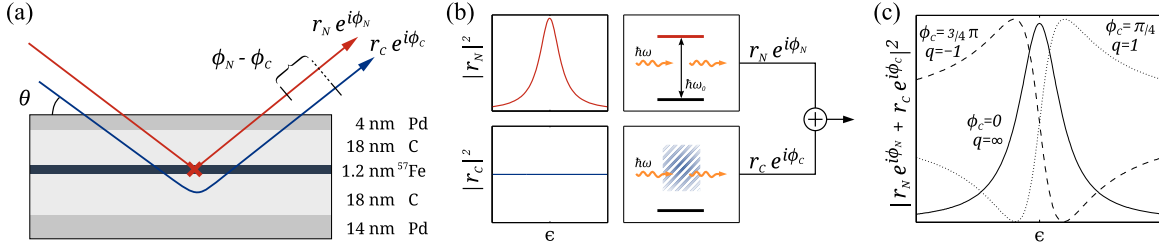


FIG. 1 (color online). Schematic setup of the x-ray interferometer and origin of the Fano interference. (a) X-ray light is reflected by a thin-film cavity under a grazing angle θ . The Pd layers act as cavity mirrors and C as the guiding layer. The phases of the reflection by the empty cavity ($r_C e^{i\phi_C}$, blue line) and from the embedded ^{57}Fe nuclei in the center ($r_N e^{i\phi_N}$, red line) can be controlled via the incidence angle θ and the energy ϵ , respectively. (b) The empty-cavity reflection forms a broad spectral continuum, whereas the isolated “bound state” nuclear response r_N has a Lorentzian shape. (c) The interference of these two paths leads to asymmetric line shapes controlled by the phase ϕ_C , which we observe experimentally.

We have experimentally explored this phase control at the Dynamics Beam line P01 of the PETRA III synchrotron radiation source (DESY, Hamburg). We employed nuclear resonant scattering, where a short broadband incident pulse excites the nuclei, and subsequently the delayed scattered photons are detected. The cavity is formed by a Pd(4 nm)/C(36 nm)/Pd(14 nm) (top to bottom) layer system with the Pd layers acting as the mirrors and the C as the guiding layer. A 1.2-nm-thick active layer of ^{57}Fe was placed in the center of the carbon layer. Far-off-resonant background photons are suppressed using a high-resolution monochromator for the incident light. To record the spectrum of the scattered light, we use a spectrally narrow resonant absorber foil (consisting of a 6- μm -thick stainless steel foil enriched to 95% in ^{57}Fe), which we scan in energy across the nuclear resonance with the help of a Doppler drive [14]. Further, the secondary nuclear scattering in this foil and the corresponding delay merge both interferometer pathways in the time domain (see Supplemental Material [20]), and we collect the interference signal in a time window 40–190 ns after excitation. The Mössbauer nucleus ^{57}Fe features a transition at $\hbar\omega_0 = 14.4$ keV with a line width $\hbar\gamma = 4.7$ neV. Since the incident x-ray pulse in the 10–100 ps range is much shorter than the natural nuclear lifetime of 141 ns, and since we record the light emitted from the nuclei starting a few tens of nanoseconds after excitation by the x-ray pulse, the preparation of the TLS state in the low-excitation regime and the measurement of the subsequently emitted light can be approximated as independent processes.

Measured emission spectra are shown in Fig. 2 for selected incidence angles θ around $\theta = \theta_{\min} = 0.1388^\circ$, where the cavity reflectance assumes a deep minimum at frequencies far off the nuclear resonance. Spectra covering a wider range of angles are summarized in the Supplemental Material [20]. The narrow spikes visible in all panels are artifacts of the data acquisition system and have been excluded from the data analysis (see Ref. [20]). Clearly, the incidence angle acts as a knob to control the spectral response from a Lorentzian shape for $\theta = \theta_{\min}$ to

strongly asymmetric line shapes, demonstrating the interferometric nature of our setup.

To interpret these results, we follow a recently developed quantum-optical framework for the description of nuclei in x-ray waveguides and obtain at critical coupling [21] for the experimentally observed reflectance

$$|R|^2 = \left| \sqrt{\sigma_0} e^{i\phi_C} + \frac{\gamma_{\text{SR}}}{\Gamma} \frac{1}{\epsilon + i} \right|^2. \quad (1)$$

Here, the first term corresponds to the interferometer path due to the cavity alone, with empty-cavity response $\sigma_0 = 1/(1 + \kappa^2/\Delta_C^2)$, with cavity loss rate κ , and Δ_C is the detuning between cavity eigenmode frequency and the frequency of the probing x-ray field. The second path is represented by a complex-valued Lorentzian bound state amplitude typical of a TLS in the second term. The dimensionless energy $\epsilon = (\omega - \omega_0 - \Delta_{\text{LS}})/(\Gamma/2)$ is modified by cooperative phenomena [19]: The Lorentzian is not centered on the nuclear resonance at ω_0 , but slightly shifted by Δ_{LS} due to a collective Lamb shift (LS) [14]. Moreover, its width Γ is superradiantly (SR) broadened from the natural line width $\hbar\gamma = 4.7$ neV of ^{57}Fe to $\Gamma = \gamma + \gamma_{\text{SR}}$. These cooperative modifications to the resonance position and width are given by $\Delta_{\text{LS}} = -(2/3)|g|^2 N \Delta_C / (\kappa^2 + \Delta_C^2)$ and $\gamma_{\text{SR}} = (4/3)|g|^2 N \kappa / (\kappa^2 + \Delta_C^2)$, respectively [21]. Here, g is the cavity-nucleus coupling constant and N the number of nuclei.

The experimentally observed line shapes can then be understood by noting that the TLS response features the narrow spectral width typical of Mössbauer resonances, whereas the cavity modes have orders of magnitude higher spectral width and therefore act as continuum channels. The interference of a narrow bound state with a continuum is known to give rise to asymmetric Fano resonances [22–24]. Note that asymmetric line shapes for nuclear resonances have previously been predicted or observed [25–30], though not interpreted as Fano resonances. However, they are also well known at hard x-ray energies [31,32]. Relating the phase ϕ_C and the Fano q parameter as

$\phi_C = -\arg(q - i)$ [33], we can indeed rewrite Eq. (1) as a Fano profile:

$$|R|^2 = \frac{|\epsilon + q|^2}{1 + \epsilon^2} \sigma_0, \quad q = \frac{\gamma_{SR}}{\Gamma} \frac{\kappa}{\Delta_C} + i \frac{\gamma}{\Gamma}. \quad (2)$$

We find that q has an imaginary component, which corresponds to an incoherent loss channel [34], caused by spontaneous emission and internal conversion. However, in the strongly superradiant case ($\Gamma \gg \gamma$) the loss channels are rendered ineffective on the accelerated time scale and can be neglected. Then, $q \approx \kappa/\Delta_C$, and $|R|^2 \approx (\epsilon + q)^2 / [(1 + \epsilon^2)(1 + q^2)]$, such that $0 \leq |R|^2 \leq 1$. In particular, in this limit, the present system forms an ideal implementation of the original Fano model. In contrast, in the opposite limit $\Gamma \approx \gamma$, we find $|R|^2 \approx \sigma_0$ without any spectral signatures. It is therefore the collectively enhanced decay rate that enables the Fano implementation with full visibility of the reflectance modulation despite the low Q factor of the cavity. Close to the cavity resonance at $\Delta_C = 0$, one can linearize $\Delta_C \approx \delta_C(\theta - \theta_{\min})$, where $\theta_{\min}$ is the incidence angle with vanishing reflectance of the cavity alone. Thus, the incidence angle θ can be used to control Δ_C , and thereby q and the interferometer phase ϕ_C .

For a quantitative analysis of the experimental data, we fitted a generic Fano line shape to the experimentally recorded spectra. Each fit was repeated multiple times with randomly modified initial parameters to avoid bias, and the respective results are indistinguishable within their error bars. This procedure enables us to determine the superradiant decay width Γ , the cooperative Lamb shift Δ_{LS} , as well as the Fano q parameter as a function of the incidence angle θ independent of our theoretical model. As can be seen from Fig 2, we found good quantitative agreement of model and data. Using the so-obtained superradiant enhancement γ_{SR} and the cooperative Lamb shift Δ_{LS} , we normalized the experimental spectra to the dimensionless energy ϵ for further analysis (see Supplemental Material [20] for other recorded spectra).

A full state tomography requires a measurement of the TLS density matrix [6]. Because of a lack of intensity calibration, we can determine the off-diagonal density matrix elements up to a global scaling factor in the present experiment. The x-ray photons are coherently scattered, preserving their energy. Selecting all detection events of a particular photon energy ϵ therefore provides access to a large number of identically prepared TLS states. Repeated measurements on the light emitted by identically prepared TLS states then enables us to determine the characteristics of the off-diagonal density matrix element ρ_{eg} . Up to a global scaling factor,

$$\rho_{eg} \sim \sigma_{eg}(\epsilon) e^{i\phi_N}, \quad (3)$$

where $\sigma_{eg}(\epsilon)$ contains the spectral shape and ϕ_N is the phase of the density matrix element. The shape is directly

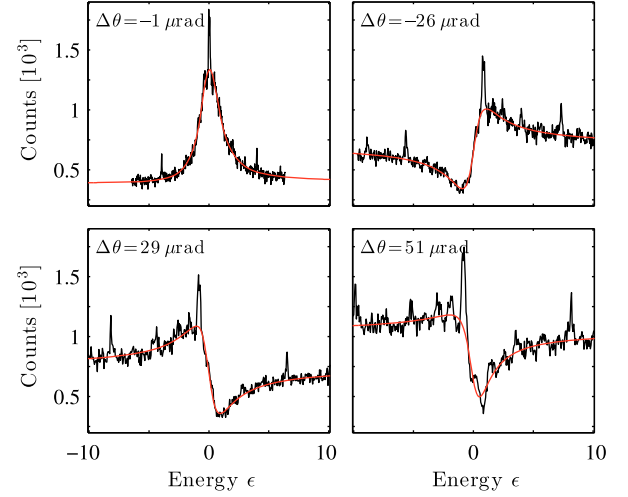


FIG. 2 (color online). Fano line shape control with nuclei. The different panels show the reflected intensity measured at different relative incidence angles $\Delta\theta = \theta - \theta_{\min}$ with uncertainty $\pm 3 \mu\text{rad}$. Experimental data are shown without baseline subtraction. Therefore, the intensities in the different panels cannot be directly compared.

obtained from the pure nuclear spectrum shown in the top left-hand panel of Fig. 2, where the empty-cavity response vanishes at $\theta = \theta_{\min}$. Further, our interferometric measurements provide a handle to determine the desired phase of the off-diagonal density matrix elements, since ρ_{eg} is directly proportional to the light amplitude emitted by the TLS (see Supplemental Material [20]). Hence, the TLS phase can be identified with the phase ϕ_N of the off-diagonal density matrix elements.

For the reconstruction of the phase of the nuclear contribution, i.e., the phase of the TLS, we employed a general ansatz for the reflectance

$$|R(\Delta\theta, \epsilon)|^2 \sim |r_C(\Delta\theta) e^{i\phi_C} + r_N(\epsilon) e^{i\phi_N}|^2, \quad (4)$$

without assumptions on the shape of the nuclear response r_N except that it only depends on ϵ and that it vanishes at large detunings $r_N(\epsilon \rightarrow \pm\infty) = 0$. To extract the nuclear phase ϕ_N , we define the experimentally accessible quantity

$$\begin{aligned} \xi(\Delta\theta, \epsilon) &= \frac{|R(\Delta\theta, \epsilon)|^2 - |R(0, \epsilon)|^2 - |R(\Delta\theta, \pm\infty)|^2}{2|R(0, \epsilon)||R(\Delta\theta, \pm\infty)|} \\ &= \cos(\phi_N - \phi_C). \end{aligned} \quad (5)$$

As the relation between the incidence angle and the cavity phase $\phi_C(\Delta\theta) = -\arg[q(\Delta\theta) - i]$ is known from the quantum-optical model, the phase of the nuclear contribution ϕ_N can then be determined as a function of ϵ via Eq. (5) by fitting the cosine to the measured ξ for all available $\Delta\theta$ values. The global offset to the phase $\phi_N(\epsilon)$ is fixed by the definition of the cavity phase ϕ_C . To evaluate $\xi(\Delta\theta, \epsilon)$ from the data without referring to the line shape to be

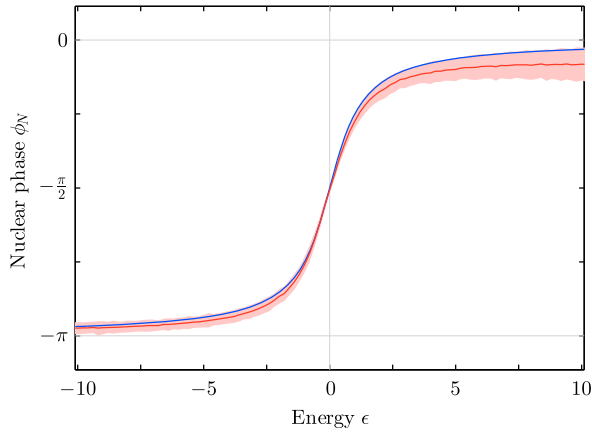


FIG. 3 (color online). Nuclear phase reconstructed from the experimental data. The red line shows the phase obtained via Eq. (5) as a function of the scaled energy ϵ . Error ranges are depicted in light red shading. The theoretically expected phase of the Lorentzian typical for a TLS is shown in blue.

reconstructed, we fitted a general rational function $R_{\text{rat}} = (a_0 + a_1\epsilon + a_2\epsilon^2)/(b_0 + b_1\epsilon + b_2\epsilon^2)$ to the data, normalized it to $0 \leq R_{\text{rat}} \leq 1$, and evaluated it at the according values for $\Delta\theta$ and ϵ . Since the angle $\Delta\theta = 0$ was not measured, we obtained $|R(0, \epsilon)|$ from the mean of the results for $\Delta\theta = \pm 1 \mu\text{rad}$.

The results of this phase retrieval are shown in Fig. 3. It can be seen that the reconstructed phase of the off-diagonal density matrix element agrees well to the expected Lorentzian shape as a function of the dimensionless energy ϵ , in particular, close to the resonance energy. The main cause of the discrepancy with respect to the expected phase at large ϵ can be traced back to an uncertainty of $|R(0, \epsilon)|$ in the denominator of Eq. (5). Here, the measured values are tiny and already small absolute deviations result in large relative errors.

The phase-sensitive interferometric measurement of the optical response of a TLS demonstrated here opens a number of promising research directions. On the one hand, the combination of the techniques developed here with measurements of the magnitude of the density matrix elements, either via detecting light intensity or conversion electrons [35], could lead to the development of complete quantum state tomography at x-ray energies. Importantly, the method demonstrated here does not depend on the Lorentzian line shape, but can be used to reconstruct the phase of arbitrary nuclear line shapes. Therefore, also more advanced setups, e.g., involving multiple magnetic hyperfine states with selectively coupled resonances, can be addressed [15,16]. On the other hand, the nuclear resonances are of primary significance in precision spectroscopy and metrology at x-ray frequencies due to their narrow linewidth [36,37]. Using our approach, tiny phase changes can be extracted from the measured data with high precision, assisted by the discovery of the mechanism

behind the asymmetric line shapes. Conversely, the interferometric phase can be used to manipulate light-matter interactions, as demonstrated by the Fano line shape control which enables us to continuously adjust between Lorentz and Fano line shapes in the x-ray optical response. The high sensitivity of the Fano line shape on the arrangement of scatterers allows for a multitude of applications ranging from structure determination with unprecedented accuracy to precision stabilization of interferometers. Furthermore, Fano interferences are ubiquitous features in light-matter interaction, and our phase control concept provides access to such large application potential of Fano processes in the x-ray region [38,39]. These concepts can also be generalized towards active and dynamical control of spectroscopic line shapes [33], further fueling the emerging field of x-ray quantum optics.

We are grateful to T. Guryeva for support during sample preparation and to F. U. Dill and K. Schlage for setting up beam line instrumentation. K. P. H acknowledges funding by the German National Academic Foundation. T. P. acknowledges support from the MPRG program of the Max-Planck-Gesellschaft (MPG).

- [1] P. Hariharan, *Basics of Interferometry* (Academic Press, Amsterdam, 2006).
- [2] A. Zavatta and M. Bellini, *Nat. Photonics* **6**, 350 (2012).
- [3] H. N. Chapman *et al.*, *Nature (London)* **470**, 73 (2011).
- [4] A. Barty, J. Küpper, and H. N. Chapman, *Annu. Rev. Phys. Chem.* **64**, 415 (2013).
- [5] G. L. Taylor, *Acta Crystallogr. Sect. D* **66**, 325 (2010).
- [6] G. M. D'Ariano, M. G. A. Paris, and M. F. Sacchi, *Adv. Imaging Electron Phys.* **128**, 205 (2003).
- [7] K. Vogel and H. Risken, *Phys. Rev. A* **40**, 2847 (1989).
- [8] D. T. Smithey, M. Beck, M. G. Raymer, and A. Faridani, *Phys. Rev. Lett.* **70**, 1244 (1993).
- [9] P. Thibault and A. Menzel, *Nature (London)* **494**, 68 (2013).
- [10] B. W. Adams, C. Buth, S. M. Cavaletto, J. Evers, Z. Harman, C. H. Keitel, A. Palfy, A. Picon, R. Röhlberger, Y. Rostovtsev, and K. Tamasaku, *J. Mod. Opt.* **60**, 2 (2013).
- [11] N. Rohringer, D. Ryan, R. A. London, M. Purvis, F. Albert, J. Dunn, J. D. Bozek, C. Bostedt, A. Graf, R. Hill, S. P. Hau-Riege, and J. J. Rocca, *Nature (London)* **481**, 488 (2012).
- [12] T. E. Glover, D. M. Fritz, M. Cammarata, T. K. Allison, S. Coh, J. M. Feldkamp, H. Lemke, D. Zhu, Y. Feng, R. N. Coffee, M. Fuchs, S. Ghimire, J. Chen, S. Shwartz, D. A. Reis, S. E. Harris, and J. B. Hastings, *Nature (London)* **488**, 603 (2012).
- [13] M. Beye, S. Schreck, F. Sorgenfrei, C. Trabant, N. Pontius, C. Schüßler-Langeheine, W. Wurth, and A. Föhlisch, *Nature (London)* **501**, 191 (2013).
- [14] R. Röhlberger, K. Schlage, B. Sahoo, S. Couet, and R. Rüffer, *Science* **328**, 1248 (2010).
- [15] R. Röhlberger, H.-C. Wille, K. Schlage, and B. Sahoo, *Nature (London)* **482**, 199 (2012).
- [16] K. P. Heeg, H.-C. Wille, K. Schlage, T. Guryeva, D. Schumacher, I. Uschmann, K. S. Schulze, B. Marx,

- T. Kämpfer, G. G. Paulus, R. Röhlberger, and J. Evers, *Phys. Rev. Lett.* **111**, 073601 (2013).
- [17] F. Vagizov, V. Antonov, Y. V. Radeonychev, R. N. Shakhmuratov, and O. Kocharovskaya, *Nature (London)* **508**, 80 (2014).
- [18] K. P. Heeg, J. Haber, D. Schumacher, L. Bocklage, H.-C. Wille, K. S. Schulze, R. Loetzsch, I. Uschmann, G. G. Paulus, R. Ruffer, R. Röhlberger, and J. Evers, *Phys. Rev. Lett.* **114**, 203601 (2015).
- [19] J. Hannon and G. Trammell, *Hyperfine Interact.* **123/124**, 127 (1999).
- [20] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevLett.114.207401> for details on the measurement method, experimentally recorded spectra for other incidence angles, and details on the theoretical modeling.
- [21] K. P. Heeg and J. Evers, *Phys. Rev. A* **88**, 043828 (2013).
- [22] H. Beutler, *Z. Phys. A* **93**, 177 (1935).
- [23] U. Fano, *Nuovo Cimento* **12**, 154 (1935).
- [24] U. Fano, *Phys. Rev.* **124**, 1866 (1961).
- [25] P. J. Black and P. B. Moon, *Nature (London)* **188**, 481 (1960).
- [26] S. Bernstein and E. C. Campbell, *Phys. Rev.* **132**, 1625 (1963).
- [27] F. Parak, R. L. Mössbauer, U. Biebl, H. Formanek, and W. Hoppe, *Z. Phys.* **244**, 456 (1971).
- [28] G. Smirnov, *Hyperfine Interact.* **27**, 203 (1986).
- [29] R. Röhlberger, E. Gerdau, E. Lüken, H. Rüter, J. Metge, and O. Leupold, *Z. Phys. B* **92**, 489 (1993).
- [30] Y. V. Shvyd'ko and G. V. Smirnov, *J. Phys. Condens. Matter* **1**, 10563 (1989).
- [31] K. Tamasaku and T. Ishikawa, *Phys. Rev. Lett.* **98**, 244801 (2007).
- [32] K. Tamasaku, K. Sawada, and T. Ishikawa, *Phys. Rev. Lett.* **103**, 254801 (2009).
- [33] C. Ott, A. Kaldun, P. Raith, K. Meyer, M. Laux, J. Evers, C. H. Keitel, C. H. Greene, and T. Pfeifer, *Science* **340**, 716 (2013).
- [34] A. Bärnthaler, S. Rotter, F. Libisch, J. Burgdörfer, S. Gehler, U. Kuhl, and H.-J. Stöckmann, *Phys. Rev. Lett.* **105**, 056801 (2010).
- [35] W. Sturhahn, K. W. Quast, T. S. Toellner, E. E. Alp, J. Metge, and E. Gerdau, *Phys. Rev. B* **53**, 171 (1996).
- [36] R. V. Pound and G. A. Rebka, *Phys. Rev. Lett.* **3**, 439 (1959).
- [37] W. Potzel, C. Schäfer, M. Steiner, H. Karzel, W. Schiessl, M. Peter, G. Kalvius, T. Katila, E. Ikonen, P. Helistö, J. Hietaniemi, and K. Riski, *Hyperfine Interact.* **72**, 195 (1992).
- [38] B. Lukyanchuk, N. I. Zheludev, S. A. Maier, N. J. Halas, P. Nordlander, H. Giessen, and C. T. Chong, *Nat. Mater.* **9**, 707 (2010).
- [39] A. E. Miroshnichenko, S. Flach, and Y. S. Kivshar, *Rev. Mod. Phys.* **82**, 2257 (2010).