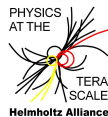


Beyond the Standard Model in WHIZARD

Jürgen R. Reuter

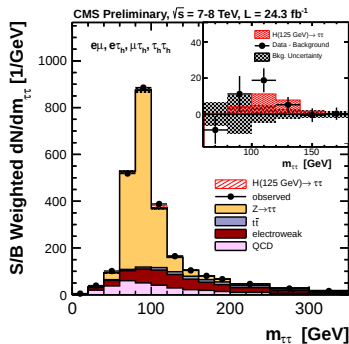
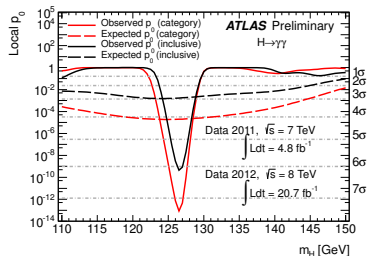
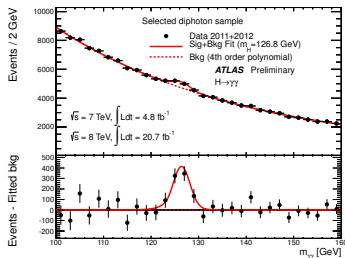
DESY Hamburg



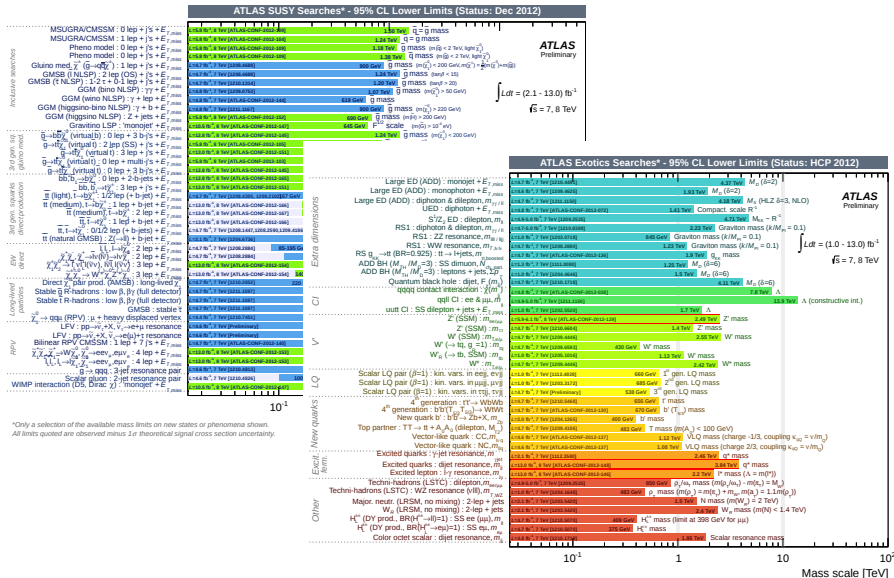
2nd WHIZARD Forum, Würzburg, March 17, 2015

Standard Model Triumph:

► 2012: Discovery of a Higgs boson

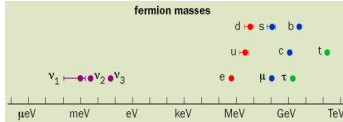


No evidence beyond SM... and what now?

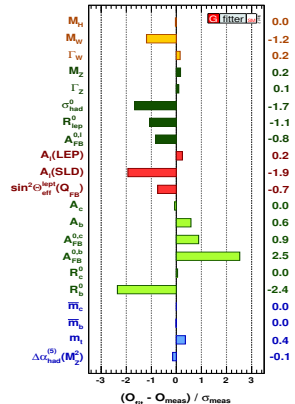
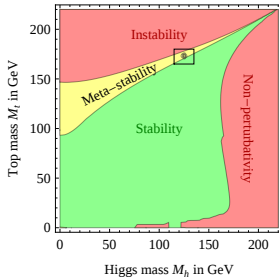


Doubts on the Standardmodel

- describes microcosm (too good?)
- 28 free parameters



- Higgs ?, form of Higgs potential ?



Hierarchy Problem

chiral symmetry: $\delta m_f \propto v \ln(\Lambda^2/v^2)$

no symmetry for quantum corrections to Higgs mass

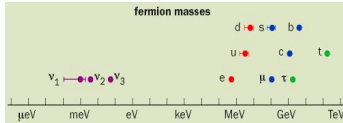
$$\delta M_H^2 \propto \Lambda^2 \sim M_{\text{Planck}}^2 = (10^{19})^2 \text{ GeV}^2$$

[illegible]

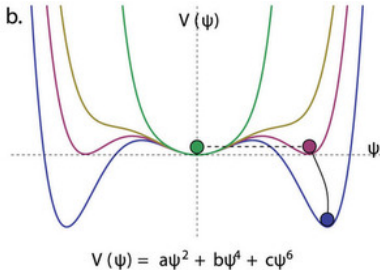
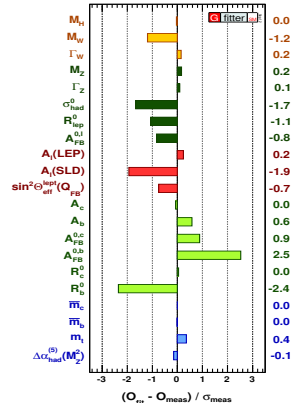
1000000000000000000000000000000000) GeV²

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- describes microcosm (too good?)
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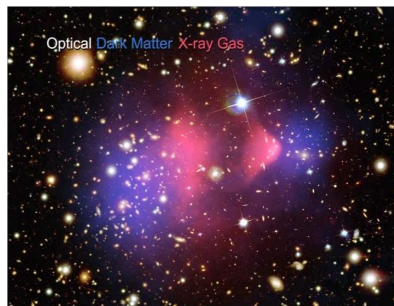
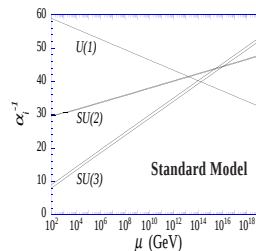
$$\delta M_H^2 \propto \Lambda^2 \sim M_{\text{Planck}}^2 = (10^{19})^2 \text{ GeV}^2$$

$$(125 \text{ GeV})^2 = (1000000000000000000000000000000020000 -$$

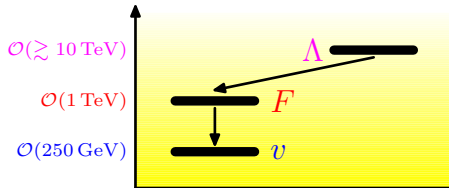
10000000000000000000000000000000000) GeV²

Open Questions

- Unification of all forces (?)
- Baryon asymmetry $\Delta N_B - \Delta N_{\bar{B}} \sim 10^{-9}$
missing CP violation
- Flavor: three generations (?)
- Tiny neutrino masses: $m_\nu \sim \frac{v^2}{M}$
- Dark Matter:
 - ▶ stable
 - ▶ weakly interacting
 - ▶ $m_{DM} \sim 100 \text{ GeV}$
- Quantum theory of gravitation
- Cosmic inflation
- Dark Energy



Characteristics and Spectra

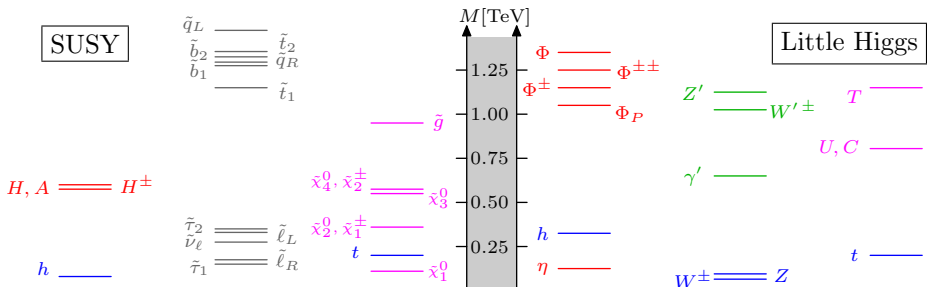


Scale Λ : “hidden sector”,
symmetry breaking

Scale F : new particles

Scale v : h , W/Z , $\ell^\pm$, ...

Terascale: new particles to stabilize the hierarchy



Search for new Particles (LHC)

Decay products of heavy particles

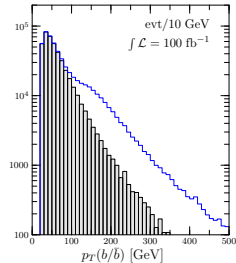
- ▶ high- p_T Jets
- ▶ (many) hard leptons

Production of colored particles

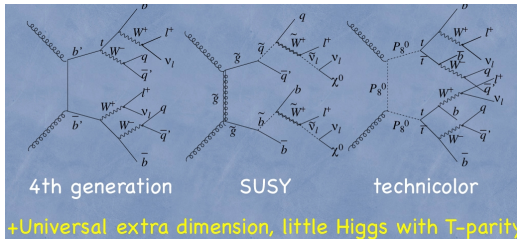
Weakly interacting particles only in decays

Dark Matter $\Leftrightarrow$ **discrete parity** (R, T, KK)

- ▶ only pairs of new particles $\Rightarrow$ high energies, long decay chains
- ▶ Dark Matter $\Rightarrow$ missing energy ($\cancel{E}_T$)



Different Models/Decay Chains — identical signatures



Search for new Particles (LHC)

Decay products of heavy particles

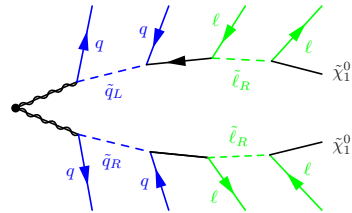
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Production of colored particles

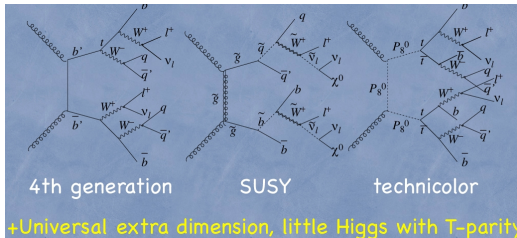
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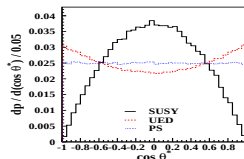
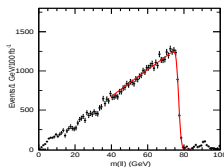
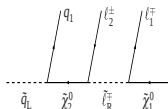


Different Models/Decay Chains — identical signatures



Model Discrimination

- **Mass of new particles:** endpoints/edges of decay spectra



- **Spin of new particles:** angular correlations, (charge) asymmetries ...

- Modellbestimmung: **Measurements of coupling constants**

⇒ Precise prediction for signals and backgrounds

- Fiducial volumes: consider almost arbitrary cuts
- Exclusive/[inclusive] many-body final states: $2 \rightarrow 4$ to $2 \rightarrow 10$
- Quantum corrections: real and virtual corrections

WHIZARD in a Nutshell – Release 2.2

WHIZARD is a universal event generator for elementary processes at colliders:

- ▶ e^+e^- : LEP and TESLA/NLC $\Rightarrow$ ILC, CLIC, FCC-ee ...
- ▶ pp : Tevatron $\Rightarrow$ LHC, HL/E-LHC, VLHC, FCC, XXX ...

It contains

1. **O'Mega**: **Optimized automatic matrix elements** for arbitrary elementary processes, supports SM and many BSM extensions
2. **Phase-space** parameterization module (**very efficient PS**)
3. **VAMP**: **Generic adaptive Monte Carlo integration and (unweighted) event generation**
4. **CIRCE1/2**: Lepton/[photon] collider beam spectra
5. Intrinsic support or external interfaces for: Feynman rules, beam properties, cascade decays, shower, hadronization, analysis, event file formats, etc., etc.
6. Free-format steering language **SINDARIN**

WHIZARD 2 – Installation and Run

- ▶ Download WHIZARD from <http://www.hepforge.org/archive/whizard/whizard-2.2.2.tar.gz> and unpack it
- ▶ WHIZARD intended to be centrally installed on a system, e.g. in `/usr/local` (or locally on user account)
- ▶ Create build directory and `configure`
External programs (LHAPDF, StdHEP, HepMC, LCIO, FastJet) might need flags
- ▶ `make, make install`
- ▶ Create SINDARIN steering file (in any working directory)
- ▶ Run `whizard` (in working directory)
- ▶ **Supported event formats:** HepMC, LCIO, StdHEP, LHEF, LHA, div. ASCII formats

```

WHIZARD self tests:
make check-am
make check-TESTS
PASS: expressions.run
PASS: beams.run
PASS: cputime.run
PASS: state_matrices.run
PASS: interactions.run
PASS: beam_structures.run
PASS: models.run
[.....]
PASS: phs_forests.run
PASS: rng_base.run
PASS: selectors.run
PASS: phs_wood.run
PASS: mci_vamp.run
PASS: particle_specifiers.run
PASS: prclib_stacks.run
PASS: slha_interface.run
PASS: subevt_expr.run
PASS: process_stacks.run
PASS: cascades.run
PASS: processes.run
PASS: decays.run
XFAIL: hgg_colors.run
PASS: events.run
PASS: eio_base.run
PASS: rt_data.run
PASS: dispatch.run
PASS: process_configurations.run
PASS: event_weights_1.run
PASS: integrations.run
PASS: simulations.run
PASS: process_libraries.run
PASS: compilations.run
PASS: prclib_interfaces.run
PASS: commands.run
PASS: errors.run
PASS: helicity.run
PASS: qedtest_1.run
PASS: beam_setup_1.run
PASS: reweight_1.run
PASS: colors.run
PASS: lhef_1.run
PASS: alphas.run
PASS: smtest_1.run
PASS: hepmc.run
PASS: restrictions.run
PASS: pdf_builtin.run
PASS: stdhep_1.run
PASS: static_1.run

=====
Testsuite summary for WHIZARD 2.2.5
=====
# TOTAL: 270
# PASS: 265
# SKIP: 2
# XFAIL: 3
# FAIL: 0
# XPASS: 0
# ERROR: 0
=====

```

Implemented Physics Content/Classification

► Hard Matrix Elements

- Multiplicities, technical details, performance
- Particles, Lorentz structures and interactions
- Color structures
- Flavor structures
- Higher-order matrix elements (cf. Christian Weiss' talk yesterday)
- Special features: non-standard stuff
- Supported models

► Structured beams (cf. Thorsten Ohl's talk on Wednesday)

- Structure functions for lepton and hadron colliders/beam spectra
- Beam radiation/beamstrahlung
- Multiple interactions/underlying event
- "Full" events/hadronization etc.

► Analysis setup

- Cuts, event formats, data analyses, interfacing....

Structured Beams

► Hadron Colliders structured beams

- LHAPDF interface (v. 4/5 and 6)
- Most prominent PDFs directly included (e.g. CT10, MMHT2014 etc.)
-
- ISR and FSR (two different own implementations, interface to PYTHIA6) (cf. Talk Bijan Chokoufé)
- Matching matrix elements/showers (cf. Talk Bijan Chokoufé)
- Underlying event/multiple interactions [not validated]

► Lepton Colliders structured beams

- ISR (implemented: Skrzypek/Jadach, Kuraev/Fadin, incl. p_T distributions)
- arbitrarily polarized beams (density matrices)
- Beamstrahlung (CIRCE1 module)
- Correlated beam spectra / [photon collider spectra] (CIRCE2 module)
- external beam spectra can be read in (files/generating code)
- FSR/exclusive ISR (QED shower) not (yet) implemented

► Hadronic events/hadronic decays

- through PYTHIA6 interface (or HERWIG/Sherpa/PYTHIA8 externally)

Hard matrix elements: particle types

Possible particle types

- ▶ Spin 0 particles
- ▶ Spin 1/2 fermions (Majorana and Dirac)
Fermi statistics for both fermion-number conserving and violating cases
- ▶ Spin 1 particles
 - ▶ massive and massless
 - ▶ Unitarity and Feynman gauge
 - ▶ arbitrary R_ξ gauges
- ▶ Spin 3/2 particles (Majorana only, gravitinos)
- ▶ Spin 2 particles (massless and massive, gravitons)
- ▶ Dynamic particles vs. pure insertions
- ▶ Unphysical particles for Ward- and Slavnov-Taylor identities

Gravitinos in WHIZARD

JRR, 2001

```
*** Checking polarization vectorspinors: ***
p.ueps ( 2)= 0: passed at      86%
p.ueps ( 1)= 0: passed at      86%
.....
*** Checking the irreducibility condition: ***
g.ueps ( 2): passed at      95%
.....
g.ueps (-2): passed at      95%
g.veps ( 2): passed at      95%
.....
g.veps (-2): passed at      95%
*** Testing vectorspinor normalization ***
ueps( 2).ueps( 2)= -2m: passed at  100%
ueps( 1).ueps( 1)= -2m: passed at  100%
.....
*** Majorana properties of gravitino vertices: ***
f_sgr      + gr_sf      = 0: passed at      84%
slr_grf     + slr_fgr     = 0: passed at      88%
.....
v2lr_fgr   + v2lr_grf   = 0: passed at      77% [expected  0.000E+00, got  0.633E-12]
*** Testing the gravitino propagator: ***
Transversality:
p.pr.test: passed at      66% [expected  0.000E+00, got  0.437E-10]
p.pr.ueps ( 2): passed at      86%
.....
p.pr.veps (-2): passed at      79% [expected  0.000E+00, got  0.342E-12]
Irreducibility:
g.pr.test: passed at      78% [expected  0.000E+00, got  0.471E-12]
g.pr.ueps ( 2): passed at      92%
```

Gravitons in WHIZARD

Ohl, 2000

```
*** Checking polarisation tensors: ***
```

```
e2( 2).e2( 2)=1: passed at 100%
```

```
e2( 2).e2(-2)=0: passed at 100%
```

```
....
```

```
e2( 0).e2( 2)=0: passed at 100%
```

```
e2( 0).e2( 1)=0: passed at 94%
```

```
....
```

```
|p.e2( 2)| =0: passed at 96%
```

```
|e2( 2).p|=0: passed at 96%
```

```
|p.e2(-2)| =0: passed at 96%
```

```
|e2(-2).p|=0: passed at 96%
```

```
|p.e2( 1)| =0: passed at 88%
```

```
|e2( 1).p|=0: passed at 88%
```

```
|p.e2( 0)| =0: passed at 84%
```

```
|e2( 0).p|=0: passed at 84%
```

```
|p.e2(-1)| =0: passed at 88%
```

```
|e2(-1).p|=0: passed at 88%
```

```
*** Checking the graviton propagator:
```

```
p.pr.e(-2): passed at 90%
```

```
p.pr.e(-1): passed at 82%
```

```
p.pr.e(0): passed at 82%
```

```
p.pr.e(1): passed at 82%
```

```
p.pr.e(2): passed at 90%
```

```
p.pr.ttest: passed at 74% [expected 0.000E+00, got 0.210E-11]
```

Hard matrix elements: Lorentz structures

Hard-coded set of Lorentz structures

- Purely scalar couplings:

$$\phi^3, \quad \phi^4$$

- Scalar couplings to vectors:

$$gV^\mu\phi_1\overleftrightarrow{\partial}_\mu\phi_2, \quad \phi V^2, \quad \phi^2V^2, \quad \frac{1}{2}\phi F_{1,\mu\nu}F_2^{\mu\nu}, \quad \frac{1}{2}\phi F_{1,\mu\nu}\tilde{F}_2^{\mu\nu}, \quad \phi(i\partial_\mu V_1^\nu)(i\partial_\nu V_2^\mu)$$

- Pure vector couplings:

$$F_{\mu\nu}F^{\mu\nu}, \quad V_1^\mu((i\partial_\nu V_2^\rho)\overleftrightarrow{\partial}_\mu(i\partial_\rho V_3^\nu)), \quad gF_1^{\mu\nu}F_{2,\nu\rho}F_{3,\mu}^\rho, \\ g/2 \cdot \epsilon^{\mu\nu\lambda\tau}F_{1,\mu\nu}F_{2,\tau\rho}F_{3,\lambda}^\rho$$

- Fermionic couplings to scalars:

$$g_S\bar{\psi}_1 S\psi_2, \quad g_P\bar{\psi}_1 P\gamma_5\psi_2, \quad \bar{\psi}_1\phi(g_S + g_P\gamma_5)\psi_2, \quad g_L\bar{\psi}_1\phi(1 - \gamma_5)\psi_2, \\ g_R\bar{\psi}_1\phi(1 + \gamma_5)\psi_2, \quad g_L\bar{\psi}_1\phi(1 - \gamma_5)\psi_2 + g_R\bar{\psi}_1\phi(1 + \gamma_5)\psi_2$$

- Fermionic couplings to vectors:

$$g_V\bar{\psi}_1 V\psi_2, \quad g_A\bar{\psi}_1\gamma_5 V\psi_2, \quad \bar{\psi}_1 V(g_V - g_A\gamma_5)\psi_2, \quad g_L\bar{\psi}_1 V(1 - \gamma_5)\psi_2, \\ g_R\bar{\psi}_1 V(1 + \gamma_5)\psi_2, \quad g_L\bar{\psi}_1 V(1 - \gamma_5)\psi_2 + g_R\bar{\psi}_1 V(1 + \gamma_5)\psi_2$$

- ▶ Fermionic couplings in SUSY Ward identities (not listed here)
- ▶ Fermionic couplings to tensors:

$$g_T T_{\mu\nu} \bar{\psi}_1 [\gamma^\mu, \gamma^\nu] \psi_2$$

- ▶ Tensor couplings to vectors:

$$T^{\mu\nu} (V_{1,\mu} V_{2,\nu} + V_{1,\nu} V_{2,\mu}), \quad T^{\alpha\beta} (V_1^\mu i \overleftrightarrow{\partial}_\alpha i \overleftrightarrow{\partial}_\beta V_{2,\mu}, \\ T^{\alpha\beta} (V_1^\mu i \overleftrightarrow{\partial}_\beta (i \partial_\mu V_{2,\alpha}) + V_1^\mu i \overleftrightarrow{\partial}_\alpha (i \partial_\mu V_{2,\beta})), \quad T^{\alpha\beta} ((i \partial^\mu V_1^\nu) i \overleftrightarrow{\partial}_\alpha i \overleftrightarrow{\partial}_\beta (i \partial_\nu V_{2,\mu}))$$

- ▶ Gravitino couplings:

$$\bar{\psi} \gamma^\mu S \psi_\mu, \quad \bar{\psi} \gamma^\mu \not{k}_S S \psi_\mu, \quad \bar{\psi} \gamma^\mu \gamma^5 P \not{k}_P \psi_\mu, \quad \bar{\psi} \gamma^5 \gamma^\mu [\not{k}_V, V] \psi_\mu \text{ etc.}$$

growing number of dim. 6/dim. 8 operators: HEFT, aTGC, aQGC, anom. top couplings, ...

- ▶ Fermionic couplings in SUSY Ward identities (not listed here)
- ▶ Fermionic couplings to tensors:

$$g_T T_{\mu\nu} \bar{\psi}_1 [\gamma^\mu, \gamma^\nu] \psi_2$$

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growing number of dim. 6/dim. 8 operators: HEFT, aTGC, aQGC, anom. top couplings, ...

- ▶ Completely general Lorentz structures:

foreseen for next major release, incl. UFO interface, v2.3.0



Hard matrix elements: Color structures

Possible Color structures

- ▶ In principle all $SU(N)$ gauge theories supported, but specialize to $N = 3$
- ▶ Color flow formalism
Stelzer/Willenbrock, 2003; Kilian/Ohl/JRR/Specki, 2011
- ▶ Fundamental representations: $\mathbf{3}, \bar{\mathbf{3}}$
- ▶ Adjoint representation: $\mathbf{8}$
- ▶ Covers all interactions e.g. in SUSY and extra dimensions
- ▶ **in preparation:** generalized color structures with representations $\mathbf{6}, \bar{\mathbf{6}}, \mathbf{10}, \bar{\mathbf{10}}$ as well as $\epsilon_{ijk}\phi_i\phi_j\phi_k$ couplings

Phase Space Setup

Heuristic algorithm tries to classify phase-space structure based on a few fundamental rules

WHIZARD phase space channels

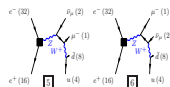
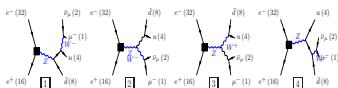
March 15, 2007

Process: $cc10$ ($e^-e^+ \rightarrow \mu^- \bar{\nu}_\mu u \bar{d}$)

Color code: resonance, t-channel, radiation, infrared, collinear, external/off-shell

Grove 1

Multiplicity: 1
Resonances: 2
Log-enhanced: 0
t-channel: 0



Grove 2

Multiplicity: 2
Resonances: 2
Log-enhanced: 1
t-channel: 1



Grove 3

Multiplicity: 2
Resonances: 2
Log-enhanced: 0
t-channel: 0



WHIZARD phase space channels

March 16, 2007

Process: $q\bar{q}t\bar{d}cc$ ($u\bar{u} \rightarrow b\bar{b}W^+W^-$)

Color code: resonance, t-channel, radiation, infrared, collinear, external/off-shell

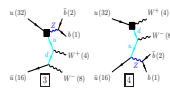
Grove 1

Multiplicity: 2
Resonances: 2
Log-enhanced: 0
t-channel: 0



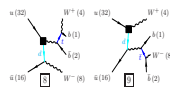
Grove 3

Multiplicity: 3
Resonances: 1
Log-enhanced: 2
t-channel: 2



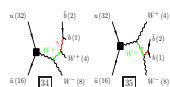
Grove 6

Multiplicity: 3
Resonances: 1
Log-enhanced: 1
t-channel: 1



Grove 19

Multiplicity: 4
Resonances: 0
Log-enhanced: 2
t-channel: 0



WHIZARD – Overview over Physics Models

MODEL TYPE	with CKM matrix	trivial CKM
QED with e, μ, τ, γ	—	QED
QCD with d, u, s, c, b, t, g	—	QCD
Standard Model	SM_CKM	SM
SM with anomalous gauge coupl.	SM_ac_CKM	SM_ac
SM with anomalous top coupl.	SMtop_CKM	SMtop
SM for e^+e^- top threshold	—	SM.tt.threshold
SM with anom. Higgs coupl.	—	SM.rx / NoH
SM ext. for VV scattering	—	SSC / SSC2/ AltH
SM with Z'	—	Zprime
2HDM	2HDM_CKM	2HDM
MSSM	MSSM_CKM	MSSM
MSSM with gravitinos	—	MSSM_Grav
NMSSM	NMSSM_CKM	NMSSM
extended SUSY models	—	PS/E/SSM
Littlest Higgs	—	Littlest
Littlest Higgs with ungauged $U(1)$	—	Littlest_Eta
Littlest Higgs with T parity	—	Littlest_Tpar
Simplest Little Higgs (anomaly-free/univ.)	—	Simplest[univ]
3-site model	—	Threshsl
UED	—	UED
SM with gravitino and photino	—	GravTest
Augmentable SM template	—	Template

new models easily: FeynRules interface [Christensen/Duhr/Fuks/JRR/Speckner, 1010.3251](#)

Claude Duhr's talk

Interface to SARAH in the SUSY Toolbox [Staub, 0909.2863; Ohl/Porod/Speckner/Staub, 1109.5147](#)

Lukas Mitzka' talk

WHIZARD – Overview over Physics Models

MODEL TYPE	with CKM matrix	trivial CKM
QED with e, μ, τ, γ	—	QED
QCD with d, u, s, c, b, t, g	—	QCD
Standard Model	SM_CKM	SM
SM with anomalous gauge coupl.	SM_ac_CKM	SM_ac
SM with anomalous top coupl.	SMtop_CKM	SMtop
SM for e^+e^- top threshold	—	SM.tt.threshold
SM with anom. Higgs coupl.	—	SM.rx / NoH
SM ext. for VV scattering	—	SSC / SSC2/ AltH
SM with Z'	—	Zprime
2HDM	2HDM_CKM	2HDM
MSSM	MSSM_CKM	MSSM
MSSM with gravitinos	—	MSSM_Grav
NMSSM	NMSSM_CKM	NMSSM
extended SUSY models	—	PS/E/SSM
Littlest Higgs	—	Littlest
Littlest Higgs with ungauged $U(1)$	—	Littlest_Eta
Littlest Higgs with T parity	—	Littlest_Tpar
Simplest Little Higgs (anomaly-free/univ.)	—	Simplest[univ]
3-site model	—	Threshsl
UED	—	UED
SM with gravitino and photino	—	GravTest
Augmentable SM template	—	Template

cf. Marco Sekulla's talk

new models easily: FeynRules interface [Christensen/Duhr/Fuks/JRR/Speckner, 1010.3251](#)

Claude Duhr's talk

Interface to SARAH in the SUSY Toolbox [Staub, 0909.2863; Ohl/Porod/Speckner/Staub, 1109.5147](#)

Lukas Mitzka' talk

The Phantom Menace – Checking new models

- ▶ E.g. MSSM
- ▶ 5318 couplings (with Goldstone/4-point)
- ▶ negative neutralino matrices: explicit factor of i
- ▶ Fully implemented, fully tested and fully functional
- ▶ Model `MSSM`
- ▶ Recommended usage: SUSY Les Houches Accord (SLHA)

```
read_slha ("spsxx")  
?slha_read_decays = true/false
```

**What about tests?
Have we checked?**



- ▶ Unitarity Checks $2 \rightarrow 2, 2 \rightarrow 3$
- ▶ Ward-/Slavnov-Taylor identities for gauge symmetries and SUSY

Comparison of Automated Tools for Perturbative Interactions in SuperSymmetry

cf. http://projects.hepforge.org/whizard/susy_comparison.html

		$\tau^+ \tau^- \rightarrow X$					
Process	status	Madgraph/Helas		Whizard/O'Mega		Sherpa/A'Megic	
		0.5 TeV	2 TeV	0.5 TeV	2 TeV	0.5 TeV	2 TeV
$\tilde{\tau}_1 \tilde{\tau}_1^*$	●	257.57(7)	79.63(4)	257.32(1)	79.636(4)	257.30(1)	79.638(4)
$\tilde{\tau}_2 \tilde{\tau}_2^*$	●	46.55(1)	66.86(2)	46.368(2)	66.862(3)	46.372(2)	66.862(3)
$\tilde{\tau}_1 \tilde{\tau}_2^*$	●	95.50(3)	19.00(1)	94.637(3)	19.0015(8)	94.645(5)	19.000(1)
$\tilde{\nu}_\tau \tilde{\nu}_\tau^*$	●	502.26(7)	272.01(8)	502.27(2)	272.01(1)	502.30(3)	272.01(1)
$\tilde{\chi}_1^0 \tilde{\chi}_1^0$	●	249.94(2)	26.431(1)	249.954(9)	26.431(1)	249.96(1)	26.431(1)
$\tilde{\chi}_0^0 \tilde{\chi}_0^0$	●	69.967(3)	9.8940(3)	69.969(2)	9.8940(4)	69.968(3)	9.8937(5)
$\tilde{\chi}_1^0 \tilde{\chi}_2^0$	●	17.0387(3)	0.7913(1)	17.0394(1)	0.79136(2)	17.040(1)	0.79137(5)
$\tilde{\chi}_1^0 \tilde{\chi}_3^0$	●	7.01378(4)	1.50743(3)	7.01414(6)	1.5075(5)	7.0141(4)	1.50740(8)
$\tilde{\chi}_1^0 \tilde{\chi}_4^0$	●	82.351(7)	18.887(1)	82.353(3)	18.8879(9)	82.357(4)	18.8896(1)
$\tilde{\chi}_2^0 \tilde{\chi}_2^0$	●	—	1.7588(1)	—	1.75884(5)	—	1.7588(1)
$\tilde{\chi}_2^0 \tilde{\chi}_3^0$	●	—	2.96384(7)	—	2.9640(1)	—	2.9639(1)
$\tilde{\chi}_2^0 \tilde{\chi}_4^0$	●	—	0.046995(4)	—	0.0469966(9)	—	0.046999(2)
$\tilde{\chi}_3^0 \tilde{\chi}_3^0$	●	—	8.5852(4)	—	8.55857(3)	—	8.5856(4)
$\tilde{\chi}_4^0 \tilde{\chi}_4^0$	●	—	0.26438(2)	—	0.264389(5)	—	0.26437(1)
$\tilde{\chi}_1^+ \tilde{\chi}_1^-$	●	185.09(3)	45.15(1)	185.093(6)	45.147(2)	185.10(1)	45.151(2)
$\tilde{\chi}_2^+ \tilde{\chi}_2^-$	●	—	26.515(1)	—	26.5162(6)	—	26.515(1)
$\tilde{\chi}_1^+ \tilde{\chi}_2^-$	●	—	4.2127(4)	—	4.21267(9)	—	4.2125(2)
$h^0 h^0$	●	0.3533827(3)	0.0001242(2)	0.35339(2)	0.00012422(3)	0.35340(2)	0.000124218(6)
$h^0 H^0$	●	—	0.005167(4)	—	0.0051669(3)	—	0.0051671(3)
$H^0 H^0$	●	—	0.07931(3)	—	0.079301(6)	—	0.079311(4)
$A^0 A^0$	●	—	0.07975(3)	—	0.079758(6)	—	0.079744(4)
$Z h^0$	●	59.591(3)	3.1803(8)	59.589(3)	3.1802(1)	59.602(3)	3.1829(2)
$Z H^0$	●	2.8316(3)	4.671(5)	2.83169(9)	4.6706(3)	2.8318(1)	4.6706(2)
$Z A^0$	●	2.9915(4)	4.682(5)	2.99162(9)	4.6821(3)	2.9917(2)	4.6817(2)
$A^0 h^0$	●	—	0.005143(4)	—	0.0051434(3)	—	0.0051440(3)
$A^0 H^0$	●	—	1.4880(2)	—	1.48793(9)	—	1.48802(8)
$H^+ H^-$	●	—	5.2344(6)	—	5.2344(2)	—	5.2345(3)

Comparison for the N²SM

Braum, Fuks, JRR, 2010

Process	MG-FR	CH-FR	WO-ST	Comparison
CAU+CAU>Znu, nu-CAU	1.48897 × 10 ⁻⁴	1.48892 × 10 ⁻⁴	1.48908 × 10 ⁻⁴	$\delta = 0.0000272$
CAU+CAU>Znu, nu-CAU	7.52098 × 10 ⁻⁵	7.5179 × 10 ⁻⁵	7.59266 × 10 ⁻⁵	$\delta = 0.889717$
CAU+CAU>Znu, nu-CAU	4.49207 × 10 ⁻⁵	4.48924 × 10 ⁻⁵	4.48006 × 10 ⁻⁵	$\delta = 0.0893631$
CAU+CAU>Znu, nu-CAU	9.7555 × 10 ⁻⁶	9.7535 × 10 ⁻⁶	9.76318 × 10 ⁻⁶	$\delta = 0.0032106$
CAU+CAU>Znu, nu-CAU	5.35941 × 10 ⁻⁶	5.35924 × 10 ⁻⁶	5.36016 × 10 ⁻⁶	$\delta = 0.0181235$
CAU+CAU>Znu, nu-CAU	7.12912 × 10 ⁻⁷	7.1289 × 10 ⁻⁷	7.12873 × 10 ⁻⁷	$\delta = 0.167014$
CAU+CAU>Znu, nu-CAU	7.11532 × 10 ⁻⁸	7.1158 × 10 ⁻⁸	7.10877 × 10 ⁻⁸	$\delta = 0.0984331$
CAU+CAU>Znu, nu-CAU	3.61339 × 10 ⁻⁹	3.6133 × 10 ⁻⁹	3.61477 × 10 ⁻⁹	$\delta = 0.015598$
CAU+CAU>Znu, nu-CAU	3.10409 × 10 ⁻¹⁰	3.1039 × 10 ⁻¹⁰	3.1032 × 10 ⁻¹⁰	$\delta = 0.0000093$
CAU+CAU>Znu, nu-CAU	1.90467 × 10 ⁻¹¹	1.9152 × 10 ⁻¹¹	1.91931 × 10 ⁻¹¹	$\delta = 0.777633$
CAU+CAU>Znu, nu-CAU	1.02967 × 10 ⁻¹²	1.03135 × 10 ⁻¹²	1.03164 × 10 ⁻¹²	$\delta = 0.191235$
CAU+CAU>Znu, nu-CAU	4.8171 × 10 ⁻¹⁴	4.8169 × 10 ⁻¹⁴	4.81646 × 10 ⁻¹⁴	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	1.05047 × 10 ⁻¹⁵	1.0504 × 10 ⁻¹⁵	1.04972 × 10 ⁻¹⁵	$\delta = 0.0713687$
CAU+CAU>Znu, nu-CAU	1.17192 × 10 ⁻¹⁶	1.17192 × 10 ⁻¹⁶	1.17143 × 10 ⁻¹⁶	$\delta = 0.0487576$
CAU+CAU>Znu, nu-CAU	1.17209 × 10 ⁻¹⁷	1.17209 × 10 ⁻¹⁷	1.17107 × 10 ⁻¹⁷	$\delta = 0.0079197$
CAU+CAU>Znu, nu-CAU	1.50518 × 10 ⁻¹⁸	1.50518 × 10 ⁻¹⁸	1.50487 × 10 ⁻¹⁸	$\delta = 0.031815$
CAU+CAU>Znu, nu-CAU	1.41851 × 10 ⁻¹⁹	1.4178 × 10 ⁻¹⁹	1.41078 × 10 ⁻¹⁹	$\delta = 0.0669563$
CAU+CAU>Znu, nu-CAU	1.39313 × 10 ⁻²⁰	1.39225 × 10 ⁻²⁰	1.39136 × 10 ⁻²⁰	$\delta = 0.112937$
CAU+CAU>Znu, nu-CAU	1.3723 × 10 ⁻²¹	1.3713 × 10 ⁻²¹	1.36946 × 10 ⁻²¹	$\delta = 0.178773$
CAU+CAU>Znu, nu-CAU	7.66119 × 10 ⁻²²	7.6632 × 10 ⁻²²	7.66407 × 10 ⁻²²	$\delta = 0.0376056$
CAU+CAU>Znu, nu-CAU	4.83808 × 10 ⁻²³	4.8377 × 10 ⁻²³	4.83538 × 10 ⁻²³	$\delta = 0.0557661$
CAU+CAU>Znu, nu-CAU	4.83161 × 10 ⁻²⁴	4.8377 × 10 ⁻²⁴	4.84208 × 10 ⁻²⁴	$\delta = 0.0966177$
CAU+CAU>Znu, nu-CAU	1.07724 × 10 ⁻²⁵	1.0791 × 10 ⁻²⁵	1.07879 × 10 ⁻²⁵	$\delta = 0.04135$
CAU+CAU>Znu, nu-CAU	1.63913 × 10 ⁻²⁶	1.6397 × 10 ⁻²⁶	1.63781 × 10 ⁻²⁶	$\delta = 0.115289$
CAU+CAU>Znu, nu-CAU	1.07887 × 10 ⁻²⁷	1.07891 × 10 ⁻²⁷	1.07862 × 10 ⁻²⁷	$\delta = 0.0441113$
CAU+CAU>Znu, nu-CAU	1.63962 × 10 ⁻²⁸	1.6397 × 10 ⁻²⁸	1.64002 × 10 ⁻²⁸	$\delta = 0.0249076$
CAU+CAU>Znu, nu-CAU	1.20597 × 10 ⁻²⁹	1.2063 × 10 ⁻²⁹	1.20707 × 10 ⁻²⁹	$\delta = 0.0912099$
CAU+CAU>Znu, nu-CAU	9.48274 × 10 ⁻³⁰	9.48274 × 10 ⁻³⁰	9.48274 × 10 ⁻³⁰	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	2.78463 × 10 ⁻³¹	2.7848 × 10 ⁻³¹	2.78524 × 10 ⁻³¹	$\delta = 0.0218196$
CAU+CAU>Znu, nu-CAU	1.1076 × 10 ⁻³²	1.1077 × 10 ⁻³²	1.10663 × 10 ⁻³²	$\delta = 0.0927793$
CAU+CAU>Znu, nu-CAU	1.10735 × 10 ⁻³³	1.1077 × 10 ⁻³³	1.10896 × 10 ⁻³³	$\delta = 0.144713$
CAU+CAU>Znu, nu-CAU	4.50337 × 10 ⁻³⁴	4.5034 × 10 ⁻³⁴	4.49875 × 10 ⁻³⁴	$\delta = 0.103213$
CAU+CAU>Znu, nu-CAU	2.69738 × 10 ⁻³⁵	2.697 × 10 ⁻³⁵	2.69575 × 10 ⁻³⁵	$\delta = 0.060399$
CAU+CAU>Znu, nu-CAU	3.7641 × 10 ⁻³⁶	3.7641 × 10 ⁻³⁶	3.76402 × 10 ⁻³⁶	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	2.69745 × 10 ⁻³⁷	2.6974 × 10 ⁻³⁷	2.69754 × 10 ⁻³⁷	$\delta = 0.1919164$
CAU+CAU>Znu, nu-CAU	2.69745 × 10 ⁻³⁸	2.6974 × 10 ⁻³⁸	2.69754 × 10 ⁻³⁸	$\delta = 0.121324$
CAU+CAU>Znu, nu-CAU	4.46003 × 10 ⁻³⁹	4.4579 × 10 ⁻³⁹	4.45895 × 10 ⁻³⁹	$\delta = 0.0479212$
CAU+CAU>Znu, nu-CAU	6.00416 × 10 ⁻⁴⁰	6.00416 × 10 ⁻⁴⁰	6.0032 × 10 ⁻⁴⁰	$\delta = 0.1000000$
CAU+CAU>Znu, nu-CAU	1.21893 × 10 ⁻⁴¹	1.21893 × 10 ⁻⁴¹	1.21746 × 10 ⁻⁴¹	$\delta = 0.117813$
CAU+CAU>Znu, nu-CAU	8.67964 × 10 ⁻⁴²	8.67924 × 10 ⁻⁴²	8.68336 × 10 ⁻⁴²	$\delta = 0.0939997$
CAU+CAU>Znu, nu-CAU	3.86644 × 10 ⁻⁴³	3.86646 × 10 ⁻⁴³	3.86804 × 10 ⁻⁴³	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	9.62043 × 10 ⁻⁴⁴	9.6198 × 10 ⁻⁴⁴	9.63712 × 10 ⁻⁴⁴	$\delta = 0.179837$
CAU+CAU>Znu, nu-CAU	9.2264 × 10 ⁻⁴⁵	9.2259 × 10 ⁻⁴⁵	9.2133 × 10 ⁻⁴⁵	$\delta = 0.076501$
CAU+CAU>Znu, nu-CAU	3.10364 × 10 ⁻⁴⁶	3.10364 × 10 ⁻⁴⁶	3.10364 × 10 ⁻⁴⁶	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	3.71434 × 10 ⁻⁴⁷	3.7123 × 10 ⁻⁴⁷	3.70949 × 10 ⁻⁴⁷	$\delta = 0.1307$
CAU+CAU>Znu, nu-CAU	3.11845 × 10 ⁻⁴⁸	3.11823 × 10 ⁻⁴⁸	3.11982 × 10 ⁻⁴⁸	$\delta = 0.052071$
CAU+CAU>Znu, nu-CAU	1.22726 × 10 ⁻⁴⁹	1.22726 × 10 ⁻⁴⁹	1.22626 × 10 ⁻⁴⁹	$\delta = 0.0072319$
CAU+CAU>Znu, nu-CAU	6.13979 × 10 ⁻⁵⁰	6.1388 × 10 ⁻⁵⁰	6.13801 × 10 ⁻⁵⁰	$\delta = 0.0649458$
CAU+CAU>Znu, nu-CAU	1.58793 × 10 ⁻⁵¹	1.58662 × 10 ⁻⁵¹	1.58717 × 10 ⁻⁵¹	$\delta = 0.0712317$
CAU+CAU>Znu, nu-CAU	1.60964 × 10 ⁻⁵²	1.60964 × 10 ⁻⁵²	1.60964 × 10 ⁻⁵²	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	1.30224 × 10 ⁻⁵³	1.30227 × 10 ⁻⁵³	1.30388 × 10 ⁻⁵³	$\delta = 0.125935$
CAU+CAU>Znu, nu-CAU	8.49209 × 10 ⁻⁵⁴	8.4901 × 10 ⁻⁵⁴	8.4772 × 10 ⁻⁵⁴	$\delta = 0.228377$
CAU+CAU>Znu, nu-CAU	4.58133 × 10 ⁻⁵⁵	4.58133 × 10 ⁻⁵⁵	4.58095 × 10 ⁻⁵⁵	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	2.63941 × 10 ⁻⁵⁶	2.64222 × 10 ⁻⁵⁶	2.64605 × 10 ⁻⁵⁶	$\delta = 0.105543$
CAU+CAU>Znu, nu-CAU	4.92753 × 10 ⁻⁵⁷	4.9314 × 10 ⁻⁵⁷	4.92995 × 10 ⁻⁵⁷	$\delta = 0.0784249$
CAU+CAU>Znu, nu-CAU	2.16262 × 10 ⁻⁵⁸	2.1626 × 10 ⁻⁵⁸	2.16185 × 10 ⁻⁵⁸	$\delta = 0.039671$
CAU+CAU>Znu, nu-CAU	7.80572 × 10 ⁻⁵⁹	7.80572 × 10 ⁻⁵⁹	7.80465 × 10 ⁻⁵⁹	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	5.13735 × 10 ⁻⁶⁰	5.1379 × 10 ⁻⁶⁰	5.12057 × 10 ⁻⁶⁰	$\delta = 0.0629371$
CAU+CAU>Znu, nu-CAU	9.84532 × 10 ⁻⁶¹	9.8445 × 10 ⁻⁶¹	9.82302 × 10 ⁻⁶¹	$\delta = 0.226659$
CAU+CAU>Znu, nu-CAU	2.37901 × 10 ⁻⁶²	2.37901 × 10 ⁻⁶²	2.37864 × 10 ⁻⁶²	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	2.38658 × 10 ⁻⁶³	2.38658 × 10 ⁻⁶³	2.39651 × 10 ⁻⁶³	$\delta = 0.478646$
CAU+CAU>Znu, nu-CAU	1.07849 × 10 ⁻⁶⁴	1.07877 × 10 ⁻⁶⁴	1.07962 × 10 ⁻⁶⁴	$\delta = 0.105076$
CAU+CAU>Znu, nu-CAU	1.48776 × 10 ⁻⁶⁵	1.48809 × 10 ⁻⁶⁵	1.48668 × 10 ⁻⁶⁵	$\delta = 0.149764$
CAU+CAU>Znu, nu-CAU	4.85736 × 10 ⁻⁶⁶	4.8605 × 10 ⁻⁶⁶	4.86451 × 10 ⁻⁶⁶	$\delta = 0.762018$
CAU+CAU>Znu, nu-CAU	1.04814 × 10 ⁻⁶⁷	1.0476 × 10 ⁻⁶⁷	1.04791 × 10 ⁻⁶⁷	$\delta = 0.0519548$
CAU+CAU>Znu, nu-CAU	6.71339 × 10 ⁻⁶⁸	6.71339 × 10 ⁻⁶⁸	6.71339 × 10 ⁻⁶⁸	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	9.0489 × 10 ⁻⁶⁹	9.0461 × 10 ⁻⁶⁹	9.03717 × 10 ⁻⁶⁹	$\delta = 0.12971$
CAU+CAU>Znu, nu-CAU	3.63906 × 10 ⁻⁷⁰	3.6363 × 10 ⁻⁷⁰	3.66445 × 10 ⁻⁷⁰	$\delta = 0.080459$
CAU+CAU>Znu, nu-CAU	4.79074 × 10 ⁻⁷¹	4.79074 × 10 ⁻⁷¹	4.79074 × 10 ⁻⁷¹	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	6.01345 × 10 ⁻⁷²	6.01345 × 10 ⁻⁷²	6.0137 × 10 ⁻⁷²	$\delta = 0.00999268$
CAU+CAU>Znu, nu-CAU	2.81408 × 10 ⁻⁷³	2.8139 × 10 ⁻⁷³	2.82663 × 10 ⁻⁷³	$\delta = 0.416466$
CAU+CAU>Znu, nu-CAU	2.24843 × 10 ⁻⁷⁴	2.24843 × 10 ⁻⁷⁴	2.24843 × 10 ⁻⁷⁴	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	2.24843 × 10 ⁻⁷⁵	2.24843 × 10 ⁻⁷⁵	2.24843 × 10 ⁻⁷⁵	$\delta = 0.0000000$
CAU+CAU>Znu, nu-CAU	2.03826 × 10 ⁻⁷⁶	2.03826 × 10 ⁻⁷⁶	2.03557 × 10 ⁻⁷⁶	$\delta = 0.103037$
CAU+CAU>Znu, nu-CAU	7.32275 × 10 ⁻⁷⁷	7.3228 × 10 ⁻⁷⁷	7.3236 × 10 ⁻⁷⁷	$\delta = 0.0133547$
Process	MG-FR	CH-FR	WO-ST	Comparison
W->Z,b,t	7.11557 × 10 ⁻¹	7.0989 × 10 ⁻¹	7.11436 × 10 ⁻¹	$\delta = 0.234537$
W->Z,Z,W	3.01819 × 10 ²	3.0264 × 10 ²	3.0193 × 10 ²	$\delta = 0.271739$
W->Z,a,W	7.4661 × 10 ³	7.4604 × 10 ³	7.43748 × 10 ³	$\delta = 0.384101$
W->Zs14,sv1	2.36706 × 10 ⁻³	2.369 × 10 ⁻³	2.37235 × 10 ⁻³	$\delta = 0.223033$
W->Zs15,sv2	2.40865 × 10 ⁻³	2.4109 × 10 ⁻³	2.41163 × 10 ⁻³	$\delta = 0.123994$
W->Zs11,sv3	1.16665 × 10 ⁻³	1.1695 × 10 ⁻³	1.17192 × 10 ⁻³	$\delta = 0.45102$
W->Zs16,sv3	1.2085 × 10 ⁻³	1.2067 × 10 ⁻³	1.20652 × 10 ⁻³	$\delta = 0.164307$
W->Zsd1,su3	3.51869 × 10 ⁻³	3.5133 × 10 ⁻³	3.51169 × 10 ⁻³	$\delta = 0.199274$
W->Zsd4,su2	3.51372 × 10 ⁻³	3.5133 × 10 ⁻³	3.51307 × 10 ⁻³	$\delta = 0.0186828$
W->Zsd1,su6	1.14587 × 10 ⁻²	1.1447 × 10 ⁻²	1.14423 × 10 ⁻²	$\delta = 0.143534$
W->Zsd6,su6	2.3412 × 10 ⁻²	2.3479 × 10 ⁻²	2.34716 × 10 ⁻²	$\delta = 0.285674$
W->Zsd1,su6	1.79614 × 10 ⁻²	1.79532 × 10 ⁻²	1.79362 × 10 ⁻²	$\delta = 0.140162$
W->Zsd6,su1	1.27978 × 10 ⁻²	1.2783 × 10 ⁻²	1.27793 × 10 ⁻²	$\delta = 0.144221$
W->Zn1,x1	5.58187 × 10 ⁻³	5.5834 × 10 ⁻³	5.5787 × 10 ⁻³	$\delta = 0.0842243$
W->Zn2,x1	2.58653 × 10 ⁻²	2.5885 × 10 ⁻²	2.59104 × 10 ⁻²	$\delta = 0.174$
W->Zn3,x1	1.87516 × 10 ⁻¹	1.8743 × 10 ⁻¹	1.87014 × 10 ⁻¹	$\delta = 0.267929$
W->Zn4,x1	5.29225 × 10 ⁻²	5.2915 × 10 ⁻²	5.28743 × 10 ⁻²	$\delta = 0.091285$
W->Zn5,x1	8.68647 × 10 ⁻²	8.6797 × 10 ⁻²	8.68217 × 10 ⁻²	$\delta = 0.0779207$
W->Zn1,x2	4.25162 × 10 ⁻³	4.2539 × 10 ⁻³	4.25377 × 10 ⁻³	$\delta = 0.0535405$
W->Zn2,x2	1.86172 × 10 ⁻²	1.8623 × 10 ⁻²	1.86507 × 10 ⁻²	$\delta = 0.179804$
W->Zn3,x2	5.08905 × 10 ⁻²	5.0974 × 10 ⁻²	5.10002 × 10 ⁻²	$\delta = 0.215293$
W->Zn4,x2	3.87418 × 10 ⁻²	3.8743 × 10 ⁻²	3.87516 × 10 ⁻²	$\delta = 0.0253781$
W->Zn5,x2	2.30577 × 10 ⁻²	2.3033 × 10 ⁻²	2.3038 × 10 ⁻²	$\delta = 0.107112$
W->Zh01,H	3.06927 × 10 ⁻⁶	3.069 × 10 ⁻⁶	3.07074 × 10 ⁻⁶	$\delta = 0.0566669$
W->Zh02,H	1.20593 × 10 ⁻⁴	1.2061 × 10 ⁻⁴	1.20462 × 10 ⁻⁴	$\delta = 0.122403$
W->Zh03,H	2.1414 × 10 ⁻³	2.1392 × 10 ⁻³	2.13929 × 10 ⁻³	$\delta = 0.102916$
W->ZA01,H	2.71579 × 10 ⁻⁴	2.7161 × 10 ⁻⁴	2.71278 × 10 ⁻⁴	$\delta = 0.122268$
W->ZA02,H	1.28349 × 10 ⁻³	1.2827 × 10 ⁻³	1.28247 × 10 ⁻³	$\delta = 0.0795463$
W->ZW,h01	7.94029 × 10 ¹	7.9468 × 10 ¹	7.93492 × 10 ¹	$\delta = 0.149577$
W->ZW,h02	1.70391	1.7037	1.7087	$\delta = 0.293178$
W->ZW,h03	3.98499 × 10 ⁻⁵	3.9924 × 10 ⁻⁵	4.00474 × 10 ⁻⁵	$\delta = 0.494346$
W->ZW,A01	6.99895 × 10 ⁻⁸	6.985 × 10 ⁻⁸	7.00424 × 10 ⁻⁸	$\delta = 0.275123$
W->ZW,A02	1.36107 × 10 ⁻⁵	1.361 × 10 ⁻⁵	1.36221 × 10 ⁻⁵	$\delta = 0.0886822$
W->Z,H	1.40065 × 10 ⁻⁵	1.4004 × 10 ⁻⁵	1.39963 × 10 ⁻⁵	$\delta = 0.07301$

Resonances in VV scattering

→ Marco Sekulla's talk

Model-independent description for LHC, respect weak isospin ($\rho \approx 0$):

	$J = 0$	$J = 1$	$J = 2$
$I = 0$	σ^0 (Higgs singlet?)	ω^0 (γ'/Z' ?)	a^0 (Graviton ?)
$I = 1$	$\pi^\pm, \pi^0$ (2HDM ?)	$\rho^\pm, \rho^0$ (W'/Z' ?)	$t^\pm, t^0$
$I = 2$	$\phi^{\pm\pm}, \phi^\pm, \phi^0$ (Higgs triplet ?)	—	$f^{\pm\pm}, f^\pm, f^0$

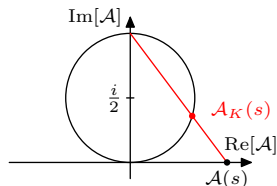
K-Matrix unitarization

$$\mathcal{A}_K(s) = \mathcal{A}(s)/(1 - i\mathcal{A}(s))$$

- ▶ Low-energy theorem (LET): $\frac{s}{v^2}$
- ▶ K-matrix ampl.: $|\mathcal{A}(s)|^2 \xrightarrow{s \rightarrow \infty} 1$
- ▶ Poles $\pm iv$: M_0, Γ large

Alboreanu/Kilian/JRR, 0806.4145

Kilian/Ohl/JRR/Sekulla, 1408.6207



- ▶ Unitarization in each spin-isospin eigen-channel
- ▶ breaks “vertex crossing invariance”
- ▶ Explicit “time arrow” in WHIZARD

Example: LHC SUSY cascade decays, Input File

```
model = MSSM

process dec_su_q = su1 => u, neu2
process dec_neu_sl2 = neu2 => SE12, e1

process susyproc = u,U => SU1, su1
process fullproc = u, U => SU1, u, e1, SE12

compile

?slha_read_decays = true
read_slha("spslap_decays.slha")

integrate (dec_su_q, dec_neu_sl2) { iterations = 1:1000 }

\textcolor{blue}{sqrts} = 14000
\textcolor{blue}{beams} = p, p => lhpdf

integrate (susyproc) { iterations = 5:10000, 2:10000 }
integrate (fullproc)

n_events = 10000

unstable su1 (dec_su_q) { <polarization_option> }

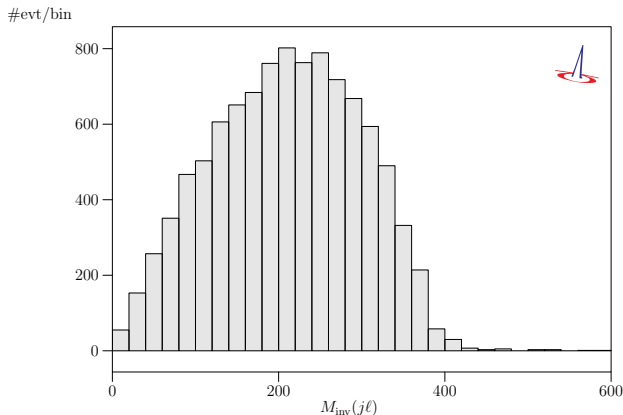
simulate (fullproc) {
  $sample = "casc_dec_full"
  analysis =
    record inv_mass1_full (eval M / 1 GeV [combine[u,e1]])
```

Example: LHC SUSY cascade decays

$$p + p \rightarrow \tilde{u}^* + \tilde{u} \rightarrow \tilde{u}^* + u + \tilde{e}^+ + e^-$$

► Full process:

```
integrate (fullproc)
```

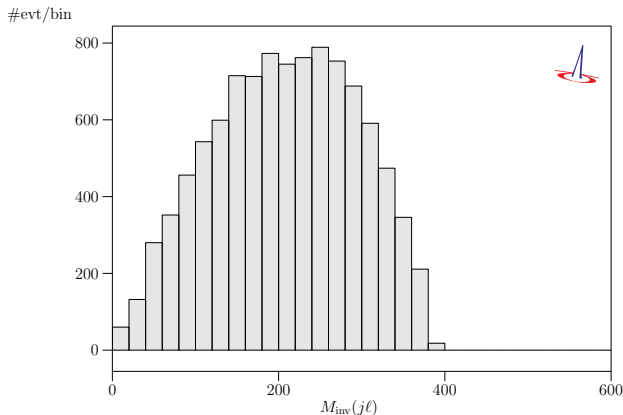


Example: LHC SUSY cascade decays

$$p + p \rightarrow \tilde{u}^* + \tilde{u} \rightarrow \tilde{u}^* + u + \tilde{e}^+ + e^-$$

► **Factorized process w/ full spin correlations:**

```
unstable su1 (dec_su_q)
```

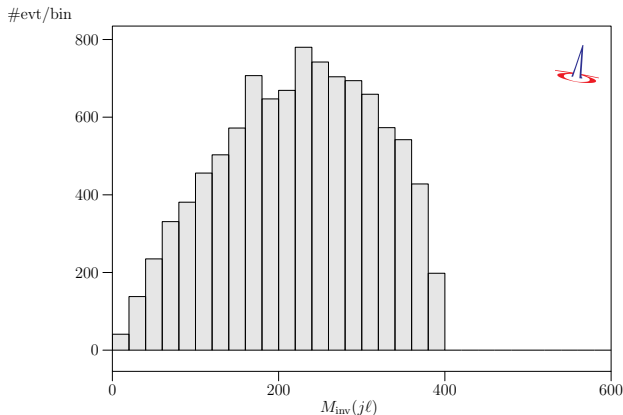


Example: LHC SUSY cascade decays

$$p + p \rightarrow \tilde{u}^* + \tilde{u} \rightarrow \tilde{u}^* + u + \tilde{e}^+ + e^-$$

► Factorized process w/ classical spin correlations:

```
unstable su1 (dec_su_q) { ?diagonal_decay = true }
```

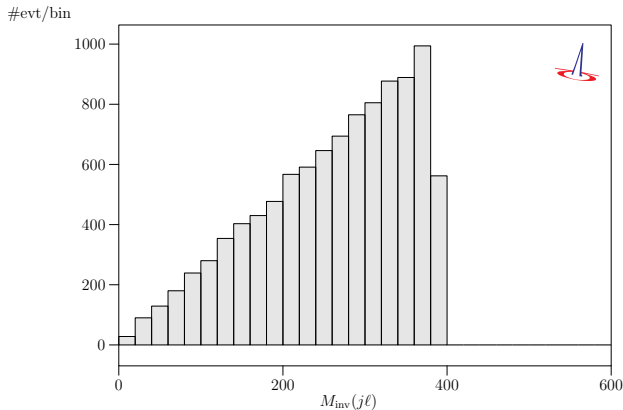


Example: LHC SUSY cascade decays

$$p + p \rightarrow \tilde{u}^* + \tilde{u} \rightarrow \tilde{u}^* + u + \tilde{e}^+ + e^-$$

► Factorized process w/ no spin correlations:

```
unstable sul (dec_su_q) { ?isotropic_decay = true }
```



New/Upcoming Features in 2.2/2.3

► New features in production version 2.2

- Complete Reweighting of Event Samples (incl. LHEF 2013) ✓
- Process containers: inclusive production samples (e.g. SUSY) ✓ `process`
`inclusive = e1, E1 => (Z, h) + (Z, H) + (A, H)`
- Automatic generation of **decays**, depending on the model ✓
- Simplified models for **electroweak vector bosons** (w/ light Higgs) ✓
- Decay chains with different options for spin correlations:
`unstable "W+" (Wud)`
`unstable "W+" (Wud) { ?diagonal_decay = true }`
`unstable "W+" (Wud) { ?isotropic_decay = true }`
- Projection on polarized intermediate states:
`unstable "W+" (Wud) { decay_helicity = -1 }`

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► Features in preparation: 2.3 – 2.4

- BSM: **general Lorentz structures** in matrix-element generator (O'Mega)
- New syntax/features decays and chains (steering unstable particles):
`process higgsstr = e1, E1 => (Z => e2, E2), (H => b, bbar)`

Summary and Outlook

- ▶ **WHIZARD 2** for LC & LHC physics **and beyond**
- ▶ A lot of focus lately on NLO and QCD
- ▶ **Covers the whole SM, and most possible paths beyond (BSM)**
- ▶ **We try to be prepared for discoveries...**
- ▶ **Immense internal technical improvements**
- ▶ Continuous improvement
 - WHIZARD 2.2 $\Rightarrow$ release series
 - WHIZARD 2.3-2.4 $\Rightarrow$ General Lorentz structures
 - WHIZARD 3 $\Rightarrow$ NLO (QCD)



Tell us about your model!

`whizard@desy.de`

Where do we go? ... the standard way ...?



Where do we go? ... the way beyond ...?



We'll be there ...

We'll be there ...

բարձր մաշտակութեան և ելոյնով:



BACKUP SLIDES:

O'Mega: Optimal matrix elements

Ohl/JRR, 2001



- Replace forest of tree diagrams by
Directed Acyclical Graph (DAG) of the algebraic expression (including color).

$$ab(ab + c) =$$

$$=$$

O'Mega: Optimal matrix elements

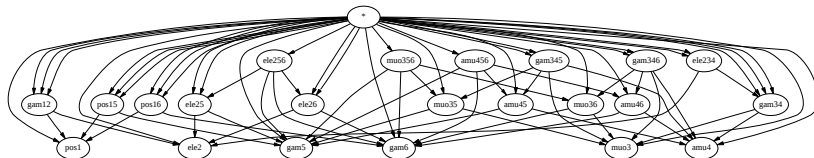
Ohl/JRR, 2001



- Replace forest of tree diagrams by
Directed Acyclical Graph (DAG) of the algebraic expression (including **color**).

$$ab(ab + c) = \begin{array}{c} \text{Diagram 1: A tree with root node having two children. The left child has two children labeled 'a' and 'b'. The right child has two children, one labeled 'a' and one labeled 'b', which then merge into a node labeled 'c' via a '+' operation. There are 'x' marks on the edges from the root to its children and from the root's left child to its children.} \end{array} = \begin{array}{c} \text{Diagram 2: A tree with root node having two children. The left child has two children labeled 'a' and 'b'. The right child has two children, one labeled 'a' and one labeled 'b', which then merge into a node labeled 'c' via a '+' operation. There are 'x' marks on the edges from the root to its children and from the root's left child to its children.} \end{array}$$

- Example: $e^+e^- \rightarrow \mu^+\mu^-\gamma\gamma$



O'Mega: Optimal matrix elements

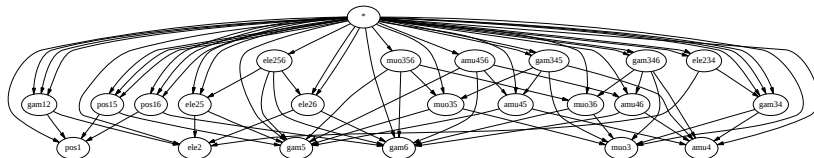
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- ▶ Example: $e^+e^- \rightarrow \mu^+\mu^-\gamma\gamma$



- ▶ Unification of model setup: only one binary (2.3.0)

O'Mega: Optimal matrix elements

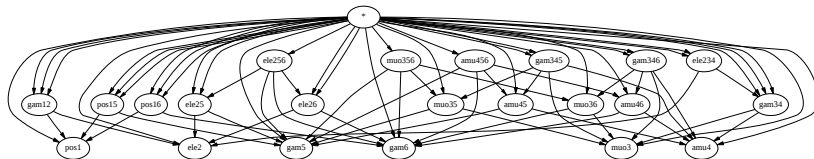
Ohl/JRR, 2001



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- ▶ Example: $e^+e^- \rightarrow \mu^+\mu^-\gamma\gamma$



- ▶ Unification of model setup: only one binary (2.3.0)
- ▶ Specification of order of strong or EW coupling (2.3.x/2.4)

O'Mega: Optimal matrix elements

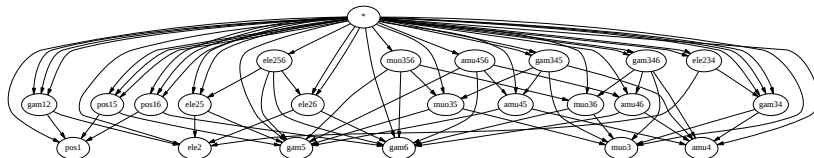
Ohl/JRR, 2001



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$$ab(ab + c) = \begin{array}{c} \text{Diagram 1: A tree with root node having two children. The left child has two children labeled 'a' and 'b'. The right child has two children, one labeled 'c' and the other is a node with two children labeled 'a' and 'b'. All internal nodes have a cross above them.} \\ \\ \text{Diagram 2: A tree with root node having two children. The left child has two children labeled 'a' and 'b'. The right child has two children, one labeled 'c' and the other is a node with two children labeled 'a' and 'b'. All internal nodes have a cross above them.} \end{array} = \begin{array}{c} \text{Diagram 3: A tree with root node having two children. The left child has two children labeled 'a' and 'b'. The right child has two children, one labeled 'c' and the other is a node with two children labeled 'a' and 'b'. All internal nodes have a cross above them.} \end{array}$$

- Example: $e^+e^- \rightarrow \mu^+\mu^-\gamma\gamma$



- Unification of model setup: only one binary (2.3.0)
- Specification of order of strong or EW coupling (2.3.x/2.4)
- Teaser: new algorithm for generating loop diagrams (3.0 ?)

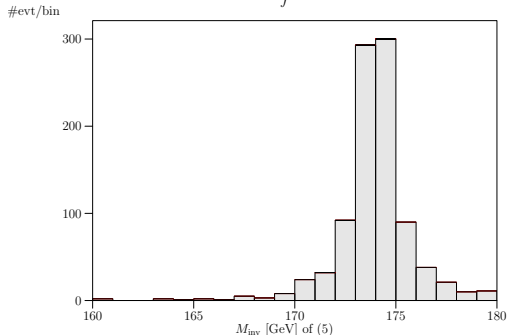
WHIZARD histograms

WHIZARD data analysis

March 16, 2007

Process: qqttdec ($u\bar{u} \rightarrow b\bar{b}W^+W^-$)

$$\sqrt{s} = 500.0 \text{ GeV} \quad \int \mathcal{L} = 0.2754 \times 10^{-01} \text{ fb}^{-1}$$



$\sigma_{\text{tot}} = 36305. \pm 310. \text{ fb} \quad [\pm 0.85 \%]$
 $n_{\text{evt, tot}} = 1000$
 $\sigma_{\text{cut}} = 36305. \pm 0.115 \times 10^{+04} \text{ fb} \quad [\pm 3.16 \%]$
 $n_{\text{evt, cut}} = 1000 \quad [100.00 \%]$

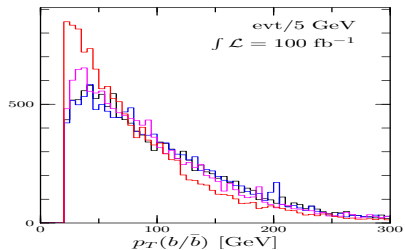
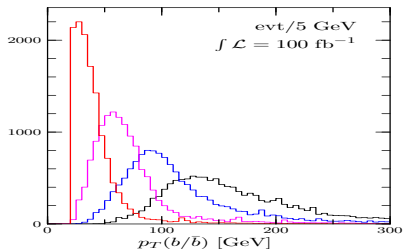
New completely general cut syntax in WHIZARD 2.0.0 (analysis.dat)

```

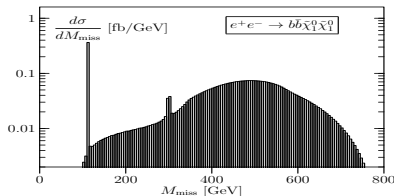
process default
cut all E of visible (any) > 10
cut all M of visible (any), visible (any) > 10
cut all Q of incoming particle (any), visible (any) < -10
histogram max_val(PT of jet) within 50 400 nbin 35

```

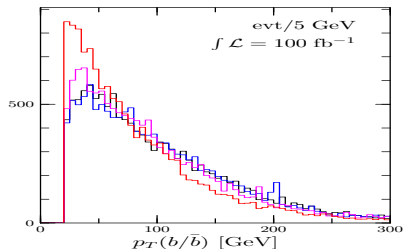
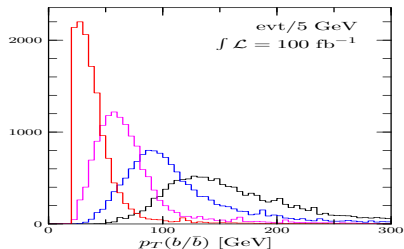
► First MSSM multijet combinatorics studies (2005):



► Beamstrahlung/ISR effects in $e + e^-$ (BSM) physics:



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► Beamstrahlung/ISR effects in e^+e^- (BSM) physics:

