

DESY 14-139

August 2014

Inflation with Fayet-Iliopoulos Terms

Clemens Wieck, Martin Wolfgang Winkler

Deutsches Elektronen-Synchrotron DESY, 22607 Hamburg, Germany

Abstract

Two of the most attractive realizations of inflation in supergravity are based upon the presence of a constant Fayet-Iliopoulos (FI) term. In D-term hybrid inflation it is the FI term itself which sets the energy scale of inflation. Alternatively, the breaking of a $U(1)$ symmetry induced by the FI term can dynamically generate the quadratic potential of chaotic inflation. The purpose of this note is to study the possible UV embedding of these schemes in terms of the ‘field-dependent FI term’ related to a string modulus field which is stabilized by a non-perturbative superpotential. We find that in settings where the FI term drives inflation, gauge invariance prevents a decoupling of the modulus from the inflationary dynamics. The resulting inflation models generically contain additional dynamical degrees of freedom compared to D-term hybrid inflation. However, the dynamical realization of chaotic inflation can be obtained in complete analogy to the case of a constant FI term. We present a simple string-inspired toy model of this type.

Contents

1	Introduction	2
2	FI Terms in Supergravity and String Theory	4
2.1	Constant FI Terms	4
2.2	Field-Dependent FI Terms	5
3	Inflation with Constant FI Terms	6
3.1	D-Term Hybrid Inflation	7
3.2	Chaotic Inflation	7
4	Field-Dependent FI Terms and Modulus Stabilization	9
5	D-Term Inflation from Field-Dependent FI Terms	11
6	F-Term Inflation from Field-Dependent FI Terms	14
6.1	Modulus Stabilization	14
6.2	Chaotic Inflation	15
7	Conclusion	17

1 Introduction

Inflation is a promising paradigm to explain the initial conditions of the universe. In particular, hybrid inflation scenarios driven by F-terms [1, 2] or D-terms [3, 4] have been studied extensively in the literature and provide intriguing links to UV-complete theories like string theory. In D-term hybrid inflation (DHI) the vacuum energy is determined by a constant Fayet-Iliopoulos (FI) term associated with a $U(1)$ gauge symmetry. Inflation proceeds in a false vacuum state where the slope of the inflaton potential is generated by quantum corrections. When the inflaton reaches a critical value the $U(1)$ symmetry is spontaneously broken and inflation ends in a waterfall phase transition.

On the other hand, implementations of chaotic inflation [5] in supergravity have gained new traction in the literature since the possible discovery of primordial gravitational waves by the BICEP2 experiment [6]. While the signal is currently being analyzed regarding a possible foreground contamination (see, for example, [7]), the tensor-to-scalar ratio inferred by the BICEP2 collaboration is in good agreement with the value predicted by chaotic inflation with a quadratic potential.

Recently it was noted that DHI may contain a regime of chaotic inflation [8]. Specifically, if the critical value of the inflaton is super-Planckian a phase of chaotic inflation may follow

after the $U(1)$ phase transition. We show explicitly that DHI in the waterfall regime is identical to the standard realization of chaotic inflation in supergravity discussed in [9, 10]. The role of the “stabilizer field” invoked in [9, 10] is played by one of the waterfall fields. The non-minimal Kähler potential of the stabilizer, which is required to decouple it from inflation, is explained by a $U(1)$ gauge interaction and can be obtained by integrating out the vector supermultiplet of the broken symmetry.

With regard to a possible UV embedding of these inflation models, it was noted in [11–13] that constant FI terms in supergravity are potentially troubled. However, supergravity models in which the arguments of [11–13] do not apply have been studied in [14–16]. Given this ongoing discussion in the literature, we are particularly interested in ‘field-dependent FI terms’¹ generated in the presence of a (pseudo-)anomalous $U(1)$ symmetry, in the following denoted by $U(1)_A$. The appearance of such D-terms was first discussed in the context of the Green-Schwarz mechanism [17] in heterotic string theory in [18]. There it was argued that the dilaton, whose axionic part cancels the anomalies associated with $U(1)_A$, acquires a D-term which bears resemblance to an FI term if the dilaton is assumed to be stabilized. Similar D-terms arise in certain compactifications of type IIB string theory, where the role of the dilaton is played by a Kähler modulus (see, for example, the discussion in [19]). However, it was soon realized that modulus or dilaton stabilization is a subtle issue in the presence of the field-dependent FI term [20]. Gauge invariance of the modulus superpotential poses severe restrictions on possible setups [19, 21–23]. In particular, it has been shown that invoking non-perturbative superpotential terms for the Kähler modulus or dilaton requires the inclusion of additional fields charged under $U(1)_A$. Otherwise, the respective field can not be stabilized in a gauge-invariant way. This can be achieved, for example, by including a gauge sector with chiral matter which undergoes gaugino condensation [24, 25].

We wish to clarify whether a field-dependent FI term can play the role of an effective constant which drives inflation.² In the case of DHI we discuss a series of obstacles which prevent possible setups from resembling the simple controllable model introduced in [3, 4]. Taking stabilization of all additional fields into account, it turns out that in all feasible setups of modulus stabilization with non-perturbative superpotentials the modulus never decouples from the dynamics of inflation, rendering much more complicated multi-field inflation models. We remark, however, that in cases where the modulus which generates the FI term does not appear in the superpotential some of our arguments may be avoided. This can be realized, for example, in the Large Volume Scenario, cf. the discussion in [27].

In the case of inflation in the chaotic regime of DHI, on the other hand, a separation of

¹Notice that this terminology is somewhat misleading. The ‘field-dependent FI term’ is the D-term of a modulus field which transforms non-linearly under a $U(1)$ symmetry. Thus, it is quite different in nature from the constant gauge-invariant term introduced by Fayet and Iliopoulos.

²For alternative and recent attempts to reconcile inflation with field-dependent FI terms, see [26–30].

the modulus from the inflaton dynamics seems possible in all moduli stabilization schemes. We provide an example in which the effective theory, after integrating out the modulus and the heavy $U(1)$ vector supermultiplet supersymmetrically, is identical to single-field chaotic inflation.

2 FI Terms in Supergravity and String Theory

In order to introduce the basic notions for the following discussion, let us briefly review both constant FI terms and field-dependent FI terms related to an anomalous $U(1)$ symmetry.

2.1 Constant FI Terms

In a supergravity theory with $U(1)$ gauge interactions the Lagrangian is determined by the choice of superpotential W , Kähler potential K , gauge kinetic function f , and Killing vectors η^α specifying the gauge transformation properties of chiral superfields ϕ_α . The superpotential and Kähler potential enter the Lagrangian in the combination $K + \log |W|^2$, which must be gauge-invariant. The gauge kinetic function transforms trivially under the $U(1)$ up to a possible shift required for anomaly cancellation. It determines the gauge coupling as $g^2 = (\text{Re } f)^{-1}$. In case the $U(1)$ symmetry is linearly realized, chiral superfields ϕ_α transform as

$$\phi_\alpha \rightarrow e^{iq_\alpha \epsilon} \phi_\alpha, \quad (2.1)$$

where ϵ is a chiral superfield gauge transformation parameter and q_α denotes the charge of ϕ_α . This corresponds to the choice of Killing vector $\eta^\alpha = iq_\alpha \phi_\alpha$. The transformation of the $U(1)$ vector superfield $\mathcal{V}$ can be written as

$$\mathcal{V} \rightarrow \mathcal{V} - \frac{i}{2}(\epsilon - \bar{\epsilon}). \quad (2.2)$$

The scalar potential may contain an F-term and a D-term piece, i.e., $V = V_F + V_D$ with

$$V_F = e^K \left(K^{\alpha\bar{\alpha}} D_\alpha W D_{\bar{\alpha}} \bar{W} - 3|W|^2 \right), \quad (2.3)$$

$$V_D = \frac{1}{2\text{Re } f} D^2. \quad (2.4)$$

The D -terms associated with the $U(1)$ can be expressed as

$$D = -i\eta^\alpha K_\alpha - \underbrace{i \frac{W_\alpha}{W} \eta^\alpha}_{\equiv \xi}. \quad (2.5)$$

Notice that, by gauge invariance, W may transform with a constant phase denoted by ξ . This is precisely the constant FI term introduced in [31].

2.2 Field-Dependent FI Terms

The consistency of constant FI terms from the perspective of string theory and quantum gravity is an issue of vital discussion in the literature. In [11–13] it was pointed out that a constant FI term in supergravity may be inconsistent when coupled to quantum gravity, while possible counter-examples have been studied in [14–16]. Whatever the outcome of this discussion, so far there are no known four-dimensional effective theories derived from string theory which contain constant FI terms. String theory, however, provides an elegant mechanism which generates field-dependent FI terms which, from the viewpoint of cosmology, may play a similar role as their constant counterparts.

Depending on the full gauge group and chiral spectrum of the theory under consideration, a $U(1)$ symmetry like the one in Section 2.1 can have several gauge anomalies, in which case we denote it by $U(1)_A$. These manifest as divergences of the gauge current J , i.e.,

$$\partial_\mu J^\mu \propto c_1 A_{G^2-U(1)_A} \text{tr } \mathcal{F}_{\mu\nu} \tilde{\mathcal{F}}^{\mu\nu} + c_2 A_{U(1)_A^3} F_{\mu\nu} \tilde{F}^{\mu\nu} + c_3 A_{\text{grav}^2-U(1)_A} \text{tr } R_{\mu\nu} \tilde{R}^{\mu\nu}, \quad (2.6)$$

where $\mathcal{F}$, F , and R denote the field strengths of a non-Abelian gauge group piece G , $U(1)_A$, and the Riemann tensor, respectively. The prefactors c_i depend on the underlying string construction, while the anomaly coefficients A are given by

$$A_{G^2-U(1)_A} = \sum_f q_f \ell(\mathbf{R}_f), \quad A_{U(1)_A^3} = \sum_\alpha q_\alpha^3, \quad A_{\text{grav}^2-U(1)_A} = \sum_\alpha q_\alpha. \quad (2.7)$$

The first sum runs over all chiral fermions transforming in the representation $\mathbf{R}$ of G and $\ell(\mathbf{R})$ denotes the quadratic index of $\mathbf{R}$. The sums in the second and third expression run over all chiral fermions.

For the theory to be consistent, all anomalies must be canceled by the four-dimensional variant of the Green-Schwarz mechanism [17]. This means there must be at least one axion which shifts under $U(1)_A$, and this shift cancels all anomalies via its coupling to the field strengths. Motivated by compactifications of type IIB string theory, we take the axion to be the imaginary part of a Kähler modulus ρ and assume all other moduli to be stabilized by fluxes [32]. Note that the discussion proceeds analogously in heterotic string theory with the dilaton playing the role of the Kähler modulus. The transformation of ρ under $U(1)_A$ reads

$$\rho \rightarrow \rho - i\delta_{\text{GS}}\epsilon, \quad (2.8)$$

which corresponds to the Killing vector $\eta^\rho = -i\delta_{\text{GS}}$. In what follows we consider the case $G = SU(N_c)$ and N_f quark pairs transforming as (N_c, q) and $(\bar{N}_c, \tilde{q})$ under $SU(N_c) \times U(1)_A$, respectively. Cancellation of the pure $U(1)_A^3$ and the mixed $SU(N_c) \times U(1)_A^2$ anomaly then implies [19]

$$\delta_{\text{GS}} = \frac{1}{6\pi\kappa} \sum_\alpha q_\alpha^3 = \frac{1}{4\pi\tilde{\kappa}} N_f (q + \tilde{q}), \quad (2.9)$$

where the first sum again runs over all chiral fermions. We do not impose additional constraints on δ_{GS} related to the cancellation of the gauge-gravity anomaly, as in type IIB orientifold compactifications the coupling of the axion to the Riemann tensor is model-dependent. The coefficients κ and $\tilde{\kappa}$ which enter the above equation are $\mathcal{O}(1)$ constants which appear in the gauge kinetic functions, i.e.,

$$f = \frac{\kappa}{2\pi}\rho, \quad \tilde{f} = \frac{\tilde{\kappa}}{2\pi}\rho, \quad (2.10)$$

for $U(1)_A$ and $SU(N_c)$, respectively. The $U(1)_A$ gauge coupling is given by

$$g^2 = \frac{1}{\text{Re } f} = \frac{4\pi}{\kappa(\rho + \bar{\rho})}, \quad (2.11)$$

and similarly for the gauge coupling of the $SU(N_c)$. In the following we choose a normalization which coincides with the one used in the work of KKLT [33], i.e., $\kappa = \tilde{\kappa} = \frac{1}{2}$.

Since ρ transforms non-trivially under $U(1)_A$, the familiar no-scale Kähler potential must be modified accordingly,

$$K = -3 \log(\rho + \bar{\rho}) \quad \longrightarrow \quad K = -3 \log(\rho + \bar{\rho} - 2\delta_{\text{GS}}\mathcal{V}). \quad (2.12)$$

Allowing for the presence of additional chiral fields ϕ_α which transform linearly under $U(1)_A$, the D-term potential reads

$$V_D = \frac{4\pi}{\rho + \bar{\rho}} \left(\sum_\alpha q_\alpha K_\alpha \phi_\alpha + \xi_{\text{GS}} \right)^2, \quad (2.13)$$

where we have assumed gauge invariance of W , i.e., the absence of a constant FI term in V_D . The piece

$$\xi_{\text{GS}} \equiv -\delta_{\text{GS}} \partial_\rho K \simeq \frac{3\delta_{\text{GS}}}{\rho + \bar{\rho}}, \quad (2.14)$$

is usually called a field-dependent FI term in the literature.

3 Inflation with Constant FI Terms

Before discussing inflation in models with a field-dependent FI term as in Eq. (2.13), let us first turn to the simpler case of inflation with constant FI terms. The prime example of this kind is D-term hybrid inflation. We first review the well-known embedding of DHI in supergravity before discussing a very interesting and less investigated situation: DHI can contain a phase of chaotic inflation with a quadratic potential after the waterfall transition.

3.1 D-Term Hybrid Inflation

DHI in supergravity can be described by the superpotential

$$W = \lambda \varphi \phi_+ \phi_- , \quad (3.1)$$

and Kähler potential

$$K = |\phi_+|^2 + |\phi_-|^2 - \frac{(\varphi - \bar{\varphi})^2}{2} . \quad (3.2)$$

Here, the real part of φ is identified with the inflaton, protected from supergravity corrections by a shift symmetry of K , and $\phi_{\pm}$ are the waterfall fields responsible for ending inflation. They carry the charges $q_{\pm}$ under a $U(1)$ gauge symmetry. Along the inflationary trajectory $\varphi = \bar{\varphi}$, the F- and D-term potentials read

$$\begin{aligned} V_F &= \lambda^2 e^{|\phi_-|^2} |\phi_-|^2 \varphi^2 , \\ V_D &= \frac{g^2}{2} (q_- |\phi_-|^2 + \xi)^2 , \end{aligned} \quad (3.3)$$

where we have set $\phi_+ = 0$ which corresponds to its minimum during and after inflation. Notice that gauge invariance requires $q_+ + q_- = \xi$. For the moment, we have neglected the dependence of the Kähler potential on the vector superfield of the $U(1)$.

The scalar potential $V = V_F + V_D$ has a supersymmetric Minkowski minimum at $|\phi_-| = \sqrt{\xi/|q_-|}$ and $\varphi = 0$. For large values of the inflaton field, $\varphi > \varphi_c \equiv g\sqrt{|q_-|\xi}/\lambda$, the potential has a plateau where $\phi_- = 0$, and the gauge symmetry is restored. The corresponding potential energy is determined by the FI term,

$$V_0 = \frac{g^2 \xi^2}{2} . \quad (3.4)$$

The Yukawa interaction in the superpotential breaks the shift symmetry in the inflaton direction and lifts the potential at the one-loop level, generating a slope for the inflaton. Standard DHI has a potential problem due to the generation of cosmic strings in the $U(1)$ phase transition. Furthermore, it predicts a scalar spectral index of $n_s > 0.98$ in tension with CMB data [34]. However, minor modifications of the Kähler potential can reconcile the model with observation (see for example [35]).

3.2 Chaotic Inflation

It was realized recently that in DHI inflation not necessarily terminates after the $U(1)$ phase transition [8]. If the critical field value is very large, $\varphi_c \gg 1$, the scalar potential in the waterfall regime may be sufficiently flat for inflation to continue. This type of situation is achieved if the Yukawa coupling λ is suppressed compared to the gauge coupling g . Indeed,

the inflaton potential (3.3) is of the form $m^2\varphi^2$ close to the supersymmetric minimum which suggests the possibility of chaotic inflation.

In order to see that, in the waterfall regime, DHI is indeed identical to the standard realization of chaotic inflation in supergravity, we consider the full Kähler potential including the $U(1)$ vector superfield $\mathcal{V}$,

$$K = \bar{\phi}_+ e^{2q_+ \mathcal{V}} \phi_+ + \bar{\phi}_- e^{2q_- \mathcal{V}} \phi_- - \frac{(\varphi - \bar{\varphi})^2}{2} + 2\xi \mathcal{V}. \quad (3.5)$$

We perform the field redefinitions

$$\phi_+ \rightarrow \left(\frac{\phi_-}{\sqrt{\xi/|q_-|}} \right)^{-\frac{q_+}{|q_-|}} \phi_+, \quad \mathcal{V} \rightarrow \mathcal{V} + \frac{1}{2|q_-|} \log \left(\frac{|\phi_-|^2}{\xi/|q_-|} \right), \quad (3.6)$$

which, after a Kähler transformation, yield

$$W = \lambda \sqrt{\frac{\xi}{|q_-|}} \varphi \phi_+, \quad (3.7)$$

$$K = \bar{\phi}_+ e^{2q_+ \mathcal{V}} \phi_+ + \frac{\xi}{|q_-|} e^{2q_- \mathcal{V}} - \frac{(\varphi - \bar{\varphi})^2}{2} + 2\xi \mathcal{V}. \quad (3.8)$$

Apparently, the field redefinitions in (3.6) correspond to a gauge choice. What we end up with is the superfield version of unitary gauge, as can be seen from the fact that the chiral superfield ϕ_- has disappeared from the spectrum. It has been eaten by the vector superfield $\mathcal{V}$, which became massive in turn. Integrating out $\mathcal{V}$ supersymmetrically by solving its equation of motion, $\partial_{\mathcal{V}} K = 0$, yields

$$\mathcal{V} = -\frac{q_+}{2|q_-|\xi} |\phi_+|^2 + \mathcal{O}(|\phi_+|^4). \quad (3.9)$$

After performing another Kähler transformation we arrive at the effective super- and Kähler potential,

$$W = m \varphi \phi_+ \quad (3.10)$$

$$K = |\phi_+|^2 - \frac{|\phi_+|^4}{\Lambda^2} - \frac{(\varphi - \bar{\varphi})^2}{2}, \quad (3.11)$$

with $m = \lambda \sqrt{\xi/|q_-|} e^{\xi/2|q_-|}$ and $\Lambda^2 = 2|q_-|\xi/q_+^2$.

Notice that Eqs. (3.10) and (3.11) define the standard embedding of chaotic inflation in supergravity [9,10]. Here, ϕ_+ plays the role of the stabilizer field. Note, however, that in [10] the Kähler potential term $|\phi_+|^4/\Lambda^2$ was introduced by hand in order to give a sufficiently large mass, $m_{\phi_+} > H$, to the stabilizer field during inflation. In our case this term arises in the effective theory via the exchange of the heavy $U(1)$ gauge boson.

So far we have worked in the supersymmetric limit, which is valid only in the vicinity of the minimum $\varphi = 0$. However, corrections are suppressed as long as the scale of the $U(1)$

breaking is large compared to the supersymmetry breaking scale, which coincides with the Hubble scale. This becomes evident by considering the full potential. Tracing the minimum of ϕ_- , the inflaton potential for $\varphi < \varphi_c$ takes the form³

$$V = V_0 \left(1 - \frac{V_0}{2g^2\xi^2} \right), \quad (3.12)$$

with $V_0 = \lambda^2\varphi^2\xi$. This implies that, if $\sqrt{g\xi} > M_{\text{GUT}} \sim 0.01$ in Planck units, the last 50-60 e-folds of inflation can occur within the quadratic regime of the potential. The cosmic string problem of DHI is absent in this case since the $U(1)$ symmetry is already broken during inflation.

4 Field-Dependent FI Terms and Modulus Stabilization

The aim of the present note is to investigate whether the simple inflation models discussed in Section 3 can effectively arise in a UV-complete theory like string theory. Therefore, we concentrate on the field-dependent FI terms related to the Green-Schwarz mechanism in the presence of an anomalous $U(1)_A$ symmetry, as introduced in Section 2.2. The field-dependent FI-term from a modulus ρ scales as $(\rho + \bar{\rho})^{-1}$ and the corresponding Lagrangian scales as $(\rho + \bar{\rho})^{-3}$, cf. Eq. (2.13). Thus, if the super- and Kähler potential exhibit no further dependence on ρ it is a runaway direction. Therefore, an appropriate mechanism to stabilize ρ has to be considered.

Naively, we could assume that ρ obtains a large supersymmetric mass $m_\rho \gg \xi_{\text{GS}}$ by some unspecified mechanism so that the field-dependent FI term becomes an effective constant. However, it was argued in [20] that this assumption is inconsistent. The reason is that the vector superfield $\mathcal{V}$ of $U(1)_A$ would receive the same large mass m_ρ via the Stückelberg mechanism. This, however, immediately implies that one can integrate out $\mathcal{V}$ supersymmetrically at the scale m_ρ which excludes the very existence of an FI term in the effective theory. Hence, a more careful treatment of modulus stabilization is required in the presence of the field-dependent FI term.

The standard procedure to stabilize the lightest Kähler modulus ρ is to employ instantonic contributions to the superpotential of the form

$$W = W_0 + \sum_j A_j e^{-a_j \rho}. \quad (4.1)$$

The interplay of one or several such terms with a constant W_0 , stemming from fluxes in the internal manifold [36], or with corrections to the Kähler potential can lead to stable minima for ρ .

³We neglect the small correction to V from the factor e^K .

The coefficients A_j are typically assumed to be constant in the effective theory and may arise from integrating out heavy moduli. However, if ρ contains the Green-Schwarz axion, constant coefficients A_j would result in a violation of $U(1)_A$ gauge invariance. In order to remedy the theory, the A_j must be promoted to functions $A_j(\phi_\alpha)$ of chiral superfields ϕ_α which carry charge under $U(1)_A$. Writing each piece of the superpotential in the form

$$W \supset A(\phi_\alpha) e^{-q_0 \rho / \delta_{\text{GS}}}, \quad (4.2)$$

gauge invariance implies $q[A(\phi_\alpha)] = -q_0$ for the charge of the function A , cf. the transformation (2.8). Superpotential terms as in Eq. (4.2) arise, for example, in intersecting D-brane models where the couplings between matter fields are suppressed by the world-sheet instanton action. Generation of Yukawa couplings of this type has first been treated in [37, 38], for a review see [39]. Alternatively, the ϕ_α can be associated with the mesonic states of a strongly coupled non-Abelian gauge theory. Consider an $SU(N_c)$ gauge theory with one pair of quarks $\{Q, \tilde{Q}\}$ transforming as (N_c, q) and $(\bar{N}_c, \tilde{q})$ under $SU(N_c) \times U(1)_A$, respectively. To ensure that the D-term potentials of these fields do not cancel the modulus-dependent FI term we assume $q + \tilde{q} > 0$. The $SU(N_c)$ undergoes gaugino condensation at a scale

$$\Lambda = e^{-2\pi\rho/(3N_c-1)}. \quad (4.3)$$

At energy scales below Λ the effective theory can be described by the (canonically normalized) mesonic degrees of freedom $M = \sqrt{2Q\tilde{Q}}$. The gauge-invariant superpotential of [24, 25] reads,

$$W = (N_c - 1) \left(\frac{2 e^{-2(q+\tilde{q})\rho/\delta_{\text{GS}}}}{M^2} \right)^{\frac{1}{N_c-1}}, \quad (4.4)$$

after inserting the expression for δ_{GS} in Eq. (2.9). In the case of gaugino condensation the function A in Eq. (4.2) is generically non-analytic. This is important since any field with negative $U(1)_A$ charge⁴ entering A can potentially cancel the FI term through its vacuum expectation value. Only for non-analytic A the inclusion of negatively charged fields is unnecessary.⁵

From the perspective of modulus stabilization the dependence of A on other chiral fields is undesirable: the non-perturbative superpotential of Eq. (4.2) now induces couplings of the modulus to other light degrees of freedom, rather than generating a mass term. Only if the fields ϕ_α themselves are stabilized appropriately an effective modulus mass term may arise.

⁴Notice that exchanging ‘negative charge’ with ‘positive charge’ is merely a choice of convention. Only the sign relative to ξ_{GS} is of importance.

⁵This fact was used in [19] to construct consistent string models with KKLT stabilization and D-term uplift.

5 D-Term Inflation from Field-Dependent FI Terms

Having discussed modulus stabilization, let us analyze whether DHI can proceed with a field-dependent FI term. We are interested in situations where the modulus ρ is stabilized during inflation and does not perturb the dynamics of DHI.⁶ As a starting point, assuming that the superpotential explicitly depends on the charged modulus, we consider

$$W = \lambda\varphi\phi_+\phi_- + W_{\text{mod}}(\rho), \quad (5.1)$$

which entails the superpotential of hybrid inflation and the piece $W_{\text{mod}} = A(\phi_\alpha)e^{-q_0\rho/\delta_{\text{GS}}} + \dots$ responsible for modulus stabilization. In order to promote the instanton contribution to a mass term, stabilization of the fields ϕ_α must be achieved by one of the following mechanisms.

Vector-like mass terms

The presence of gauge anomalies implies charged chiral states in the spectrum. However, as the ϕ_α which enter $A(\phi_\alpha)$ constitute only a subset of the spectrum, they may not contribute to the anomaly, i.e., they could still receive large vector-like masses of the form $m\phi_\alpha\bar{\phi}_\alpha$. In this case, the ϕ_α and the $\bar{\phi}_\alpha$ can be integrated out supersymmetrically yielding $A(\phi_\alpha) = 0$. This would imply that the instanton term disappears in the effective theory below the scale m .⁷

Soft mass terms

Soft masses for the ϕ_α may be generated by non-vanishing F- and D-terms. If the field-dependent FI term is not canceled, gauge-mediated soft masses of the form

$$\mathcal{L}_{\text{soft}}^D = g^2 q_\alpha \xi_{\text{GS}} |\phi_\alpha|^2, \quad (5.2)$$

arise. In addition, depending on the mechanism of modulus stabilization and supersymmetry breaking, gravity-mediated soft terms may appear.⁸ For a minimal choice of the Kähler potential, these are expected to be of the form

$$\mathcal{L}_{\text{soft}}^F = m_{3/2}^2 |\phi_\alpha|^2, \quad (5.3)$$

where $m_{3/2} = e^{K/2}W$ denotes the gravitino mass.

⁶The back-reaction of stabilized Kähler moduli on DHI, in setups where ρ is a gauge singlet, has been previously studied in [40, 41].

⁷This does not hold for non-analytic functions A which arise via gaugino condensation. However, in the case of gaugino condensation vector-like mass terms do not appear because the effective degrees of freedom, the mesons, are already two-particle states.

⁸Notice that the inflaton, protected by a shift symmetry of the Kähler potential, does not receive a soft mass term at tree-level.

Mass terms from spontaneous symmetry breaking

Finally, if $U(1)_A$ is broken spontaneously, Yukawa couplings can become effective mass terms. Consider, for example, a mesonic state M with a coupling $\lambda\phi_- M^2$ to the waterfall field. In the true vacuum of the theory ϕ_- cancels the FI term and the meson receives the mass $\lambda\langle\phi_- \rangle$.

From this discussion it is clear that modulus stabilization either requires the spontaneous breaking of $U(1)_A$ or the breaking of supersymmetry. In principle, all ingredients exist within the simple DHI setup of Section 3.1: during inflation supersymmetry is broken by the inflaton sector while the $U(1)$ symmetry is intact. After inflation supersymmetry is restored but the $U(1)$ is spontaneously broken by the vev of ϕ_- . While this may lead to successful stabilization of all fields, the responsible mechanism is clearly different during and after inflation. Therefore, the modulus sector does not decouple from the inflaton dynamics and we are left with an inflation model with several dynamical degrees of freedom. This may happen, for example, in the supersymmetric racetrack scheme studied in [42].

To obtain the simple controllable DHI setup, the same mechanism of modulus stabilization must operate in the entire cosmological history. This requires the inclusion of additional sources of supersymmetry breaking which fix the modulus during and after inflation. A similar conclusion has previously been drawn in [20]. There it was noted that, in a field-dependent realization of DHI, F-terms and D-terms must split their roles in a way that F-terms provide modulus stabilization while D-terms drive inflation. Assuming that the modulus mass is comparable to the gravitino mass, $m_\rho \sim m_{3/2}$, as for example in the setup by KKLT [33], results in the constraint

$$m_{3/2} > g\xi_{\text{GS}}, \quad (5.4)$$

which ensures that the modulus decouples from inflation. In the following, we wish to point out that a series of problems arises even if this constraint is satisfied.

First, no negatively charged fields beyond ϕ_- should be introduced as these fields would receive large tachyonic masses during inflation and tend to cancel the FI term. Therefore, we consider the case of gaugino condensation, where the function A in the instanton term contains only the positively charged mesonic fields, cf. the discussion in Section 4. It turns out that in this setup, condition (5.4) is insufficient to decouple the modulus sector from inflation. This is because during inflation the FI term induces soft masses $m_M \sim g\sqrt{\xi_{\text{GS}}}$ for the meson fields.⁹ These soft masses are enhanced compared to the Hubble scale as they originate from gauge mediation. In order to avoid that the mesons, and as a consequence also the modulus, are shifted by large amounts at the end of inflation, the gauge-mediated masses should be subdominant. This can be achieved by introducing even larger gravity-mediated soft masses $m_M \sim m_{3/2} > g\sqrt{\xi_{\text{GS}}}$. At the same time the waterfall fields must be protected

⁹Without loss of generality we assume $q_M \sim \mathcal{O}(1)$ for the $U(1)_A$ charge of the mesons.

against such large gravity-mediated masses by a specific choice of Kähler potential, otherwise inflation would never end. The origin of this sequestering could lie in a higher-dimensional theory where the dominant source of supersymmetry breaking is localized on a different brane than the waterfall fields [43].

Second, even in this case, another type of problem occurs related to the size of the instanton term. Given that modulus stabilization must proceed via supersymmetry breaking, one expects that

$$F_\rho \sim A(M_\alpha) e^{-a\rho} \sim m_{3/2}, \quad (5.5)$$

as, for example, in KKLT. For the case of a condensing $SU(N_c)$ gauge theory with a single meson M , one finds $A(M) = (N_c - 1)M^{-2/(N_c-1)}$. The meson is then stabilized by the interplay of this instanton term and its mass term, as explained in detail in [21]. Evidently, the instanton term is responsible for a large vev of M , which can be expressed as

$$M \sim \frac{F_\rho}{m_M}. \quad (5.6)$$

Given a meson mass $m_M \sim m_{3/2}$, the minimum lies at $M \sim 1$ in Planck units. Therefore, if the constraint (5.4) holds, the D-term contribution of the meson exceeds the size of the field-dependent FI term. This is inconsistent with having an effective realization of standard DHI.¹⁰

In order to find a possible way out of this apparent predicament, one may invoke schemes of modulus stabilization with $m_\rho \gg m_{3/2}$. An example of this kind may be given by the modulus stabilization via additional Kähler potential terms as proposed, for example, in [44]. But even this is not a full solution to the problem, as stabilization of the mesons still requires a very large gravitino mass and DHI is spoiled by the large displacement of the meson, cf. Eq. (5.6).

To summarize, in models where the field-dependent FI term drives inflation there is always an intimate connection between modulus stabilization and inflation. Generically, the modulus does not decouple from the dynamics of inflation. When trying to obtain the simple controllable scheme of DHI as an effective theory, a series of problems arises. These problems are related to the fact that inflation back-reacts on the modulus stabilization and vice versa. While we have shown that there is no straight-forward realization of DHI with a field-dependent FI-term, we can not exclude that it arises to some approximation by a very delicate engineering of the Kähler potential and the mechanism of modulus stabilization.

In the following section we explore the possibility that inflation proceeds in the waterfall regime of hybrid inflation. In this case the FI term is canceled during inflation and modulus

¹⁰While it may be possible to obtain an approximate version of DHI with an FI term generated by stabilized mesons, the analysis of such schemes is beyond the scope of this work.

stabilization can be achieved via the breaking of $U(1)_A$. As discussed below, the obstacles mentioned above are absent in this case.

6 F-Term Inflation from Field-Dependent FI Terms

In this section we present a string-inspired toy model of inflation with a field-dependent FI term which circumvents the problems discussed in the previous section. Inflation is driven by the F-term of one of the waterfall fields after the waterfall phase transition, as suggested in [8] and reviewed in Section 3.2. The resulting effective theory after integrating out the modulus and the heavy vector supermultiplet is identical to chaotic inflation with a quadratic potential. We first demonstrate our scheme of modulus stabilization and afterward discuss its coupling to inflation.

6.1 Modulus Stabilization

We consider a setup in which the modulus ρ has the gauge-invariant superpotential

$$W = \chi_+ \left(\phi_-^2 e^{-\rho/\delta_{\text{GS}}} - m\phi_- \right), \quad (6.1)$$

where χ_+ and ϕ_- are chiral superfields with $U(1)_A$ charge $+1$ and -1 , respectively. Yukawa couplings suppressed by an instanton action like the one in Eq. (6.1) arise, for example, in intersecting D-brane models, cf. [39]. Modulus stabilization via Yukawa-type interactions has previously been studied in [45]. We assume the no-scale Kähler potential

$$K = -3 \log \left[\rho + \bar{\rho} - 2\delta_{\text{GS}}\mathcal{V} - \bar{\phi}_- e^{-2\mathcal{V}} \phi_- - \bar{\chi}_+ e^{2\mathcal{V}} \chi_+ \right], \quad (6.2)$$

where, as before, $\mathcal{V}$ denotes the $U(1)_A$ vector supermultiplet. We remark that the choice of K in Eq. (6.2) is convenient and well-motivated from a string theory perspective, but the specific form of K does not affect the following discussions.

At the level of global supersymmetry it is clear that minimizing the F-term potential of χ_+ stabilizes ρ at a non-zero vev. To see things more clearly, let us perform the following field redefinitions,

$$\mathcal{V} \rightarrow \mathcal{V} + \log \left(\frac{|\phi_-|}{\sqrt{\delta_{\text{GS}}}} \right), \quad (6.3)$$

$$\rho \rightarrow \rho + \delta_{\text{GS}} \log \left(\frac{\phi_-}{\sqrt{\delta_{\text{GS}}}} \right), \quad (6.4)$$

$$\chi_+ \rightarrow \frac{\sqrt{\delta_{\text{GS}}}}{\phi_-} \chi_+. \quad (6.5)$$

With these redefinitions, ϕ_- is eliminated from the spectrum and we obtain, analogous to Section 3.2, the superfield version of unitary gauge. The Kähler potential in this frame

becomes

$$K = -3 \log [\rho + \bar{\rho} - 2\delta_{\text{GS}}\mathcal{V} - (\delta_{\text{GS}}e^{-2\mathcal{V}} + \bar{\chi}_+e^{2\mathcal{V}}\chi_+)] . \quad (6.6)$$

We can again integrate out $\mathcal{V}$ supersymmetrically by solving its equation of motion and obtain

$$\mathcal{V} = -\frac{|\chi_+|^2}{2\delta_{\text{GS}}} + \mathcal{O}(|\chi_+|^4) , \quad (6.7)$$

at leading order in χ_+ . Using this solution we find for the effective super- and Kähler potential,

$$W = \delta_{\text{GS}} \chi_+ \left(e^{-\rho/\delta_{\text{GS}}} - \frac{m}{\sqrt{\delta_{\text{GS}}}} \right) , \quad (6.8)$$

$$K = -3 \log \left[\rho + \bar{\rho} - \delta_{\text{GS}} - |\chi_+|^2 + \frac{|\chi_+|^4}{2\delta_{\text{GS}}} \right] . \quad (6.9)$$

The effective Lagrangian defined by Eqs. (6.8) and (6.9) has a supersymmetric minimum at

$$\rho_0 \equiv -\delta_{\text{GS}} \log \left(\frac{m}{\sqrt{\delta_{\text{GS}}}} \right) , \quad (6.10)$$

and $\chi_+ = 0$. In the vacuum, the mass of the canonically normalized modulus is given by

$$m_\rho = \frac{m}{3\sqrt{\delta_{\text{GS}}}} = \frac{1}{3} e^{-\frac{3}{2\xi_{\text{GS}}}} , \quad (6.11)$$

which coincides with the mass of χ_+ . The fermionic components of ρ and χ_+ combine into a Dirac fermion. Notice that there is an intricate relation between the size of the effective FI term defined in Eq. (2.14) and the mass of the modulus field. A large supersymmetric mass for the modulus can be achieved by an effective FI term close to the Planck scale, as it naturally appears in string compactifications. As an example, $m_\rho \sim M_{\text{GUT}}$ corresponds to $\xi_{\text{GS}} \sim 0.4$. In this parameter regime it is possible to stabilize ρ at a large vev, $\rho_0 \gg 1$ in Planck units, to guarantee the validity of the supergravity approximation. We remark that, in this discussion, we treat δ_{GS} as a free parameter since additional chiral states may contribute to the anomaly without affecting our discussion.

6.2 Chaotic Inflation

Consider the system defined by the superpotential

$$W = \chi_+ \left(\phi_-^2 e^{-\rho/\delta_{\text{GS}}} - m\phi_- \right) + \lambda\varphi\phi_+\phi_- , \quad (6.12)$$

which is obtained by adding the superpotential of DHI to the modulus sector discussed in Section 6.1, identifying the waterfall field ϕ_- with the field which renders the instanton term gauge-invariant. As in Section 3, φ is protected by a shift symmetry in the Kähler potential and its real part is the inflaton field. The Kähler potential reads

$$K = -3 \log [\rho + \bar{\rho} - |\phi_-|^2 - |\phi_+|^2 - |\chi_+|^2 + (\varphi - \bar{\varphi})^2] . \quad (6.13)$$

Here we implicitly assume that the inflaton is part of the matter sector of a possible string theory embedding. As an example, it could be associated with a Wilson line scalar with the shift symmetry being a consequence of higher-dimensional gauge invariance. A discussion of the generic obstacles of large-field inflation in string theory by means of our toy model is, however, beyond the scope of this paper. For a recent discussion of large-field inflation with Wilson lines, see [46].

Along the lines of Section 3.2 we can absorb ϕ_- into the vector superfield, which we integrate out supersymmetrically to obtain the effective theory for the remaining degrees of freedom. We find the following effective superpotential and Kähler potential,

$$W = \delta_{\text{GS}} \chi_+ \left(e^{-\rho/\delta_{\text{GS}}} - 3m_\rho \right) + \lambda \sqrt{\delta_{\text{GS}}} \varphi \phi_+, \quad (6.14)$$

$$K = -3 \log \left[\rho + \bar{\rho} - \delta_{\text{GS}} - |\phi_+|^2 - |\chi_+|^2 + \frac{(|\phi_+|^2 + |\chi_+|^2)^2}{2\delta_{\text{GS}}} + (\varphi - \bar{\varphi})^2 \right], \quad (6.15)$$

where we have used Eq. (6.11) to express m in terms of the modulus mass. In case ρ is stabilized at a scale far above the Hubble scale during inflation, it decouples from the dynamics and can be integrated out together with χ_+ , see Section 6.1. The resulting effective theory for φ and ϕ_+ can then be described by

$$W = \hat{m} \hat{\varphi} \hat{\phi}_+, \quad K = |\hat{\phi}_+|^2 - \frac{|\hat{\phi}_+|^4}{2\xi_{\text{GS}}} - \frac{(\hat{\varphi} - \bar{\hat{\varphi}})^2}{2}, \quad (6.16)$$

where we have introduced the mass parameter $\hat{m} = \lambda \sqrt{\xi_{\text{GS}}}/3\sqrt{6}$ and the canonically normalized superfields $\hat{\phi}_+ = \phi_+ \sqrt{3/(2\rho_0 - \delta_{\text{GS}})}$ and $\hat{\varphi} = \varphi \sqrt{6/(2\rho_0 - \delta_{\text{GS}})}$. Evidently, by integrating out all heavy degrees of freedom we have obtained the standard realization of chaotic inflation as an effective theory.

However, for finite m_ρ a small correction to the predictions of chaotic inflation arises due to a displacement of the modulus during inflation. Integrating out ρ at its shifted vev induces an inflaton-dependent correction to the scalar potential. The leading-order correction can be found by expanding V around ρ_0 , i.e.,

$$V = \frac{1}{(\rho + \bar{\rho} - \delta_{\text{GS}})^2} \left[\hat{m}^2 \hat{\varphi}^2 (2\rho_0 - \delta_{\text{GS}})^2 + 3m_\rho^2 |\rho - \rho_0|^2 \right], \quad (6.17)$$

where we have set $\hat{\varphi} = \bar{\hat{\varphi}}$ along the inflationary trajectory. Minimizing this expression with respect to ρ gives

$$\rho - \rho_0 = \frac{4\rho_0 - 2\delta_{\text{GS}}}{3m_\rho^2} \hat{m}^2 \hat{\varphi}^2. \quad (6.18)$$

By plugging this result back into Eq. (6.17) we can obtain an effective potential for the inflaton field. The correction can be conveniently expressed as a power series in H/m_ρ along the lines of [47]. Including the leading-order term we obtain

$$V = V_0 \left(1 - \frac{4}{3} \frac{V_0}{m_\rho^2} \right), \quad (6.19)$$

with $V_0 = \hat{m}^2 \hat{\varphi}^2$. Notice that the numerical coefficient of the correction term differs from the result obtained in [47] due to the different choice of Kähler potential. As naively expected, the correction induced by the shift of the modulus completely disappears in the limit where ρ is infinitely heavy. For $m_\rho > H$ the second term in Eq. (6.19) may have a controllable effect on the inflationary observables. The investigation of this effect is, however, beyond the scope of this note.

Notice that modulus stabilization in the effective theory implies constraints on the initial conditions of the system. In particular, inflation can not begin at arbitrarily large field values of $\hat{\varphi}$. To ensure that ρ remains stabilized in the entire cosmological history, the energy density of the universe must never exceed the modulus mass. This is a conceptual subtlety which remains to be addressed in many effective theories of inflation with moduli stabilization.

7 Conclusion

In this note we have pointed out an intimate connection between D-term hybrid inflation and chaotic inflation, related to Fayet-Iliopoulos terms of different origins. DHI driven by a constant FI term proceeds in the regime where a $U(1)$ gauge symmetry is unbroken, whereas chaotic inflation can be the effective theory after the $U(1)$ phase transition. In this picture, the mass of the inflaton is generated by a Yukawa interaction. The stabilizer field required in a supergravity realization of chaotic inflation can be identified with one of the waterfall fields. The non-minimal Kähler potential, which is usually introduced by hand to decouple the stabilizer from inflation, has its origin in a $U(1)$ gauge interaction. We explicitly show that it is obtained by integrating out the heavy vector superfield of the broken $U(1)$.

From a UV perspective constant FI terms pose a potential problem. Therefore, we have investigated the implementation of DHI and the aforementioned chaotic inflation setup with a field-dependent FI term. In the presence of an anomalous $U(1)$ symmetry, the latter is related to a string modulus which contains the Green-Schwarz axion. We studied the question whether a field-dependent FI term can play the role of its constant counterpart in the early universe. We found that in settings where the field-dependent FI term provides the vacuum energy of inflation, there is always a strong interplay between modulus stabilization and inflation. In models where the charged modulus appears in the superpotential, properly accounting for gauge invariance prevents a decoupling of the modulus from the dynamics of inflation. While successful D-term inflation may be obtained, the resulting scheme does not resemble the simple controllable pattern of DHI.

This leads us to consider inflation in the broken phase of the $U(1)$ symmetry. We have shown that the $U(1)$ phase transition, triggered by the field-dependent FI term, can lead to a successful realization of chaotic inflation – analogous to the case of a constant FI term. In this setting the modulus couples to the $U(1)$ breaking field through an instanton-suppressed

Yukawa coupling. After the breaking of the $U(1)$ symmetry a supersymmetric modulus mass term arises whose size is controlled by the field-dependent FI term. With the FI term close to the Planck scale, as expected in realistic string constructions, m_ρ exceeds the Hubble scale of inflation. In this case the back-reaction of the modulus on the inflaton potential is under control.

Eventually, a picture emerges in which string moduli do not participate in supersymmetry breaking. This appears very attractive from a phenomenological perspective as it allows for low-energy supersymmetry breaking without light moduli.

Acknowledgments

We are grateful to Emilian Dudas, Kwang Sik Jeong, Robert Richter, Fabian Rühle, and Alexander Westphal for stimulating discussions, and to Wilfried Buchmüller for helpful comments on the manuscript. This work has been supported by the German Science Foundation (DFG) within the Collaborative Research Center 676 “Particles, Strings and the Early Universe”. The work of CW is supported by a scholarship of the Joachim Herz Stiftung.

References

- [1] E. J. Copeland, A. R. Liddle, D. H. Lyth, E. D. Stewart and D. Wands, Phys. Rev. D **49**, 6410 (1994) [astro-ph/9401011].
- [2] G. R. Dvali, Q. Shafi and R. K. Schaefer, Phys. Rev. Lett. **73**, 1886 (1994) [hep-ph/9406319].
- [3] P. Binetruy and G. R. Dvali, Phys. Lett. B **388**, 241 (1996) [hep-ph/9606342].
- [4] E. Halyo, Phys. Lett. B **387**, 43 (1996) [hep-ph/9606423].
- [5] A. D. Linde, Phys. Lett. B **129**, 177 (1983).
- [6] P. A. R. Ade *et al.* [BICEP2 Collaboration], Phys. Rev. Lett. **112**, 241101 (2014) [arXiv:1403.3985 [astro-ph.CO]].
- [7] R. Flauger, J. C. Hill and D. N. Spergel, JCAP **1408**, 039 (2014) [arXiv:1405.7351 [astro-ph.CO]].
- [8] W. Buchmuller, V. Domcke and K. Schmitz, arXiv:1406.6300 [hep-ph].
- [9] M. Kawasaki, M. Yamaguchi and T. Yanagida, Phys. Rev. Lett. **85**, 3572 (2000) [hep-ph/0004243].
- [10] R. Kallosh and A. Linde, JCAP **1011**, 011 (2010) [arXiv:1008.3375 [hep-th]].

- [11] Z. Komargodski and N. Seiberg, JHEP **0906**, 007 (2009) [arXiv:0904.1159 [hep-th]].
- [12] Z. Komargodski and N. Seiberg, JHEP **1007**, 017 (2010) [arXiv:1002.2228 [hep-th]].
- [13] K. R. Dienes and B. Thomas, Phys. Rev. D **81**, 065023 (2010) [arXiv:0911.0677 [hep-th]].
- [14] N. Seiberg, JHEP **1007**, 070 (2010) [arXiv:1005.0002 [hep-th]].
- [15] J. Distler and E. Sharpe, Phys. Rev. D **83**, 085010 (2011) [arXiv:1008.0419 [hep-th]].
- [16] F. Catino, G. Villadoro and F. Zwirner, JHEP **1201**, 002 (2012) [arXiv:1110.2174 [hep-th]].
- [17] M. B. Green and J. H. Schwarz, Phys. Lett. B **149**, 117 (1984).
- [18] M. Dine, N. Seiberg and E. Witten, Nucl. Phys. B **289**, 589 (1987).
- [19] A. Achucarro, B. de Carlos, J. A. Casas and L. Doplicher, JHEP **0606**, 014 (2006) [hep-th/0601190].
- [20] P. Binetruy, G. Dvali, R. Kallosh and A. Van Proeyen, Class. Quant. Grav. **21**, 3137 (2004) [hep-th/0402046].
- [21] E. Dudas and S. K. Vempati, Nucl. Phys. B **727**, 139 (2005) [hep-th/0506172].
- [22] K. Choi, A. Falkowski, H. P. Nilles and M. Olechowski, Nucl. Phys. B **718**, 113 (2005) [hep-th/0503216].
- [23] G. Villadoro and F. Zwirner, Phys. Rev. Lett. **95**, 231602 (2005) [hep-th/0508167].
- [24] T. R. Taylor, G. Veneziano and S. Yankielowicz, Nucl. Phys. B **218**, 493 (1983).
- [25] I. Affleck, M. Dine and N. Seiberg, Nucl. Phys. B **256**, 557 (1985).
- [26] R. Gwyn, M. Sakellariadou and S. Sypsas, JHEP **1109**, 075 (2011) [arXiv:1105.1784 [hep-th]].
- [27] A. Hebecker, S. C. Kraus, M. Kuntzler, D. Lust and T. Weigand, JHEP **1301**, 095 (2013) [arXiv:1207.2766 [hep-th]].
- [28] T. Li, Z. Li and D. V. Nanopoulos, arXiv:1405.0197 [hep-th].
- [29] T. Li, Z. Li and D. V. Nanopoulos, JHEP **1407**, 052 (2014) [arXiv:1405.1804 [hep-th]].
- [30] T. Li, Z. Li and D. V. Nanopoulos, arXiv:1407.1819 [hep-th].
- [31] P. Fayet and J. Iliopoulos, Phys. Lett. B **51**, 461 (1974).

- [32] S. B. Giddings, S. Kachru and J. Polchinski, Phys. Rev. D **66**, 106006 (2002) [hep-th/0105097].
- [33] S. Kachru, R. Kallosh, A. D. Linde and S. P. Trivedi, Phys. Rev. D **68**, 046005 (2003) [hep-th/0301240].
- [34] P. A. R. Ade *et al.* [Planck Collaboration], arXiv:1303.5082 [astro-ph.CO].
- [35] W. Buchmuller, V. Domcke and K. Schmitz, JCAP **1304**, 019 (2013) [arXiv:1210.4105 [hep-ph]].
- [36] S. Gukov, C. Vafa and E. Witten, Nucl. Phys. B **584**, 69 (2000) [Erratum-ibid. B **608**, 477 (2001)] [hep-th/9906070].
- [37] R. Blumenhagen, M. Cvetič and T. Weigand, Nucl. Phys. B **771**, 113 (2007) [hep-th/0609191].
- [38] L. E. Ibanez and A. M. Uranga, JHEP **0703**, 052 (2007) [hep-th/0609213].
- [39] R. Blumenhagen, M. Cvetič, S. Kachru and T. Weigand, Ann. Rev. Nucl. Part. Sci. **59**, 269 (2009) [arXiv:0902.3251 [hep-th]].
- [40] P. Brax, C. van de Bruck, A. C. Davis, S. C. Davis, R. Jeannerot and M. Postma, JCAP **0701**, 026 (2007) [hep-th/0610195].
- [41] W. Buchmuller, V. Domcke and C. Wieck, Phys. Lett. B **730**, 155 (2014) [arXiv:1309.3122 [hep-th]].
- [42] R. Kallosh and A. D. Linde, JHEP **0412**, 004 (2004) [hep-th/0411011].
- [43] L. Randall and R. Sundrum, Nucl. Phys. B **557**, 79 (1999) [hep-th/9810155].
- [44] N. Arkani-Hamed, M. Dine and S. P. Martin, Phys. Lett. B **431**, 329 (1998) [hep-ph/9803432].
- [45] F. Brummer, R. Kappl, M. Ratz and K. Schmidt-Hoberg, JHEP **1004**, 006 (2010) [arXiv:1003.0084 [hep-th]].
- [46] F. Marchesano, G. Shiu and A. M. Uranga, arXiv:1404.3040 [hep-th].
- [47] W. Buchmuller, C. Wieck and M. W. Winkler, Phys. Lett. B **736**, 237 (2014) [arXiv:1404.2275 [hep-th]].